



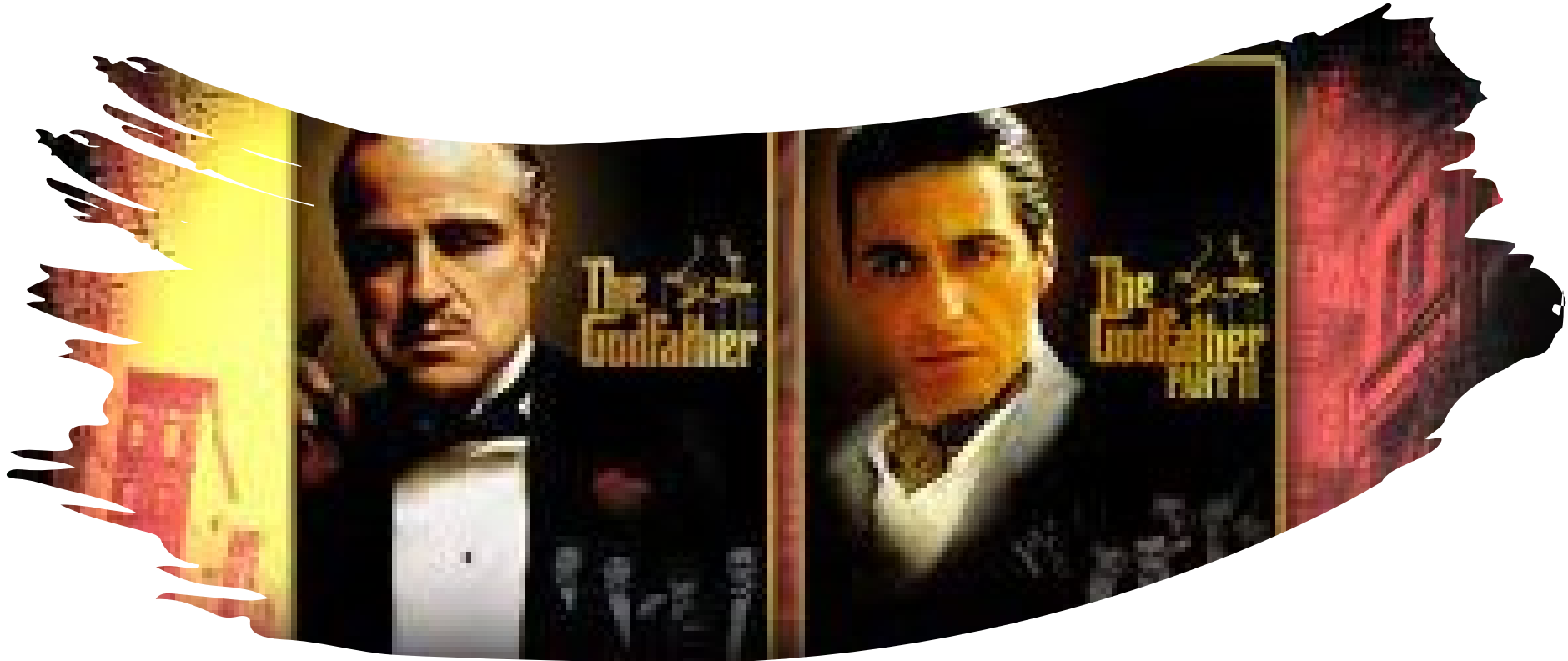
CKM and flavour at Belle II

Jim Libby

Indian Institute of Technology Madras

Outline

- Belle II
- Highlights so far
 - Lepton flavour:
 - tau physics highlights
 - B physics highlights
 - CP violation
 - Tests of lepton-flavour universality
 - Evidence for $B^+ \rightarrow K^+ \nu \nu$
- Prospects

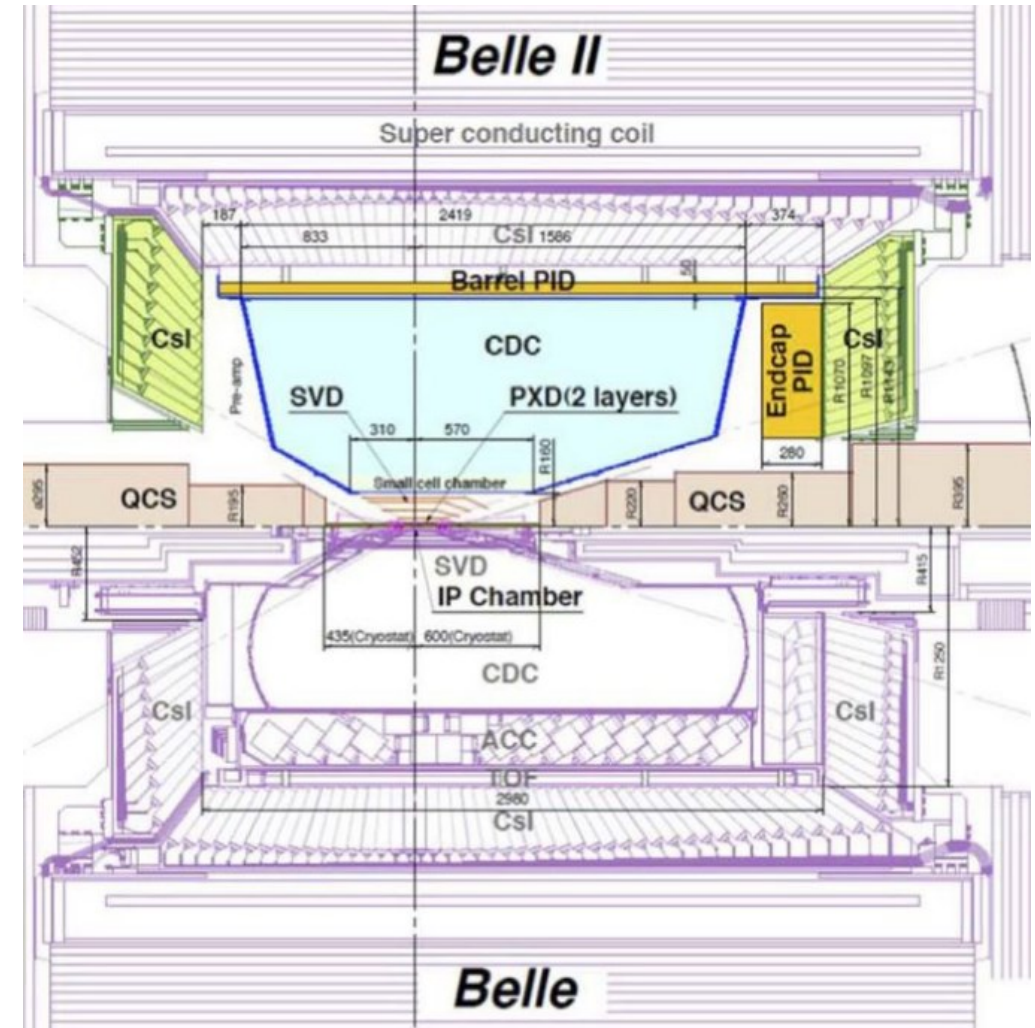


Belle II

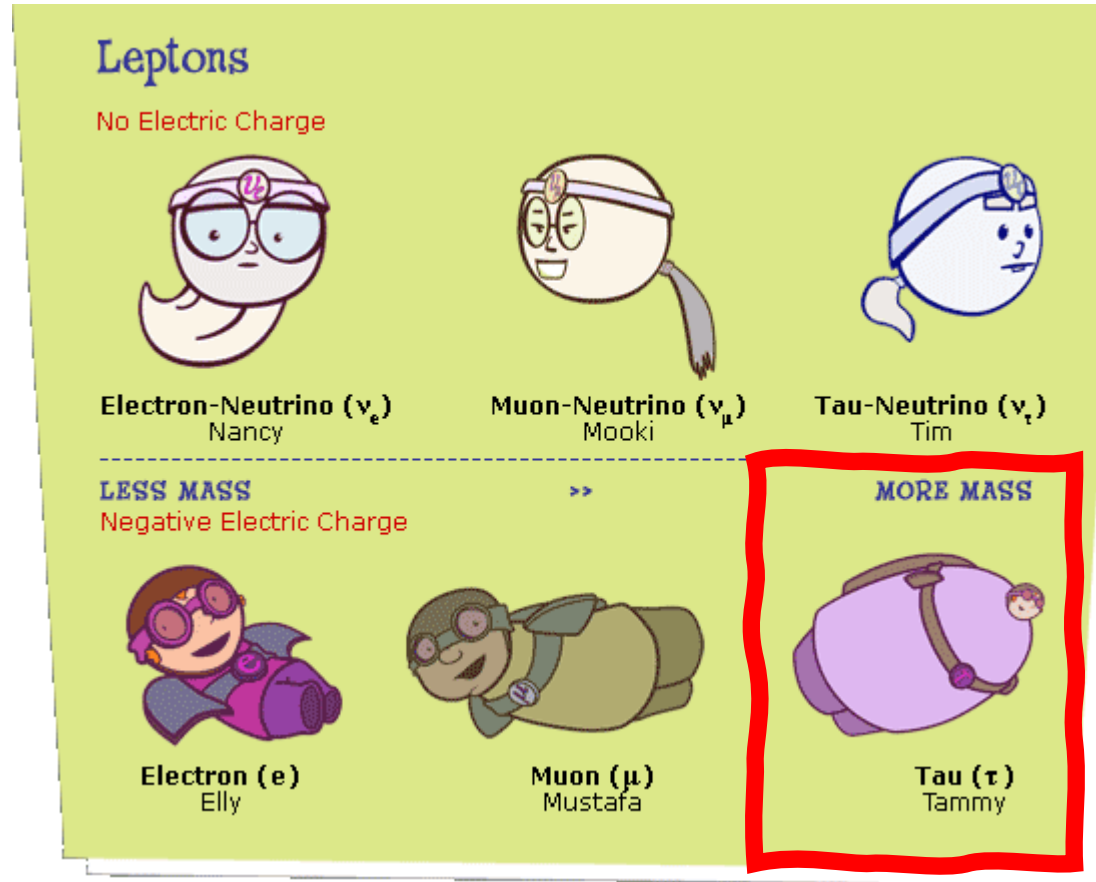
Will the next generation perform as well as the first?

Detectors and data samples

- Belle + BaBar collected $0.71+0.43=1.14 \text{ ab}^{-1}$ $Y(4S)$ samples
 - Many achievements: confirmation of KM mechanism, $b \rightarrow c\tau\nu$, direct CPV in B decay
- SuperKEKB + Belle II@KEK, Tsukuba
 - nanobeam scheme to increase instantaneous luminosity by factor 30 to collect multi- ab^{-1} sample
 - **World record $4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$**
 - Target $6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
 - So far integrated 362 fb^{-1} at $Y(4S)$
 - + 42 fb^{-1} off-resonance to characterize continuum



<https://www.quarked.org/>

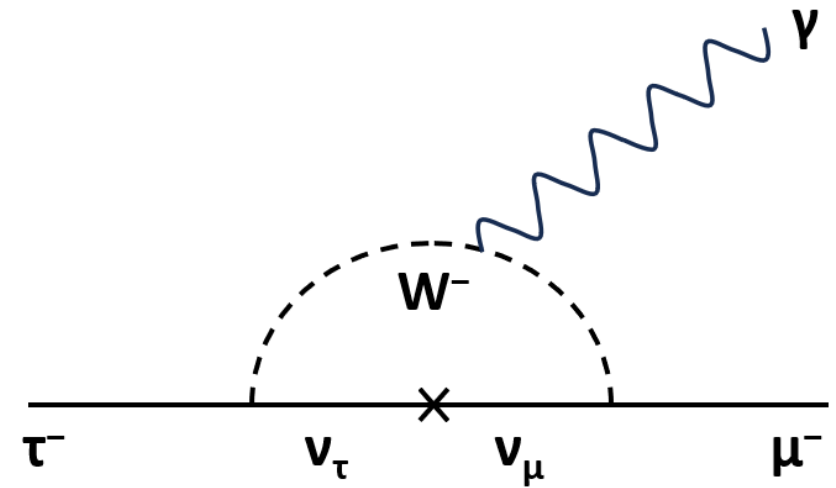
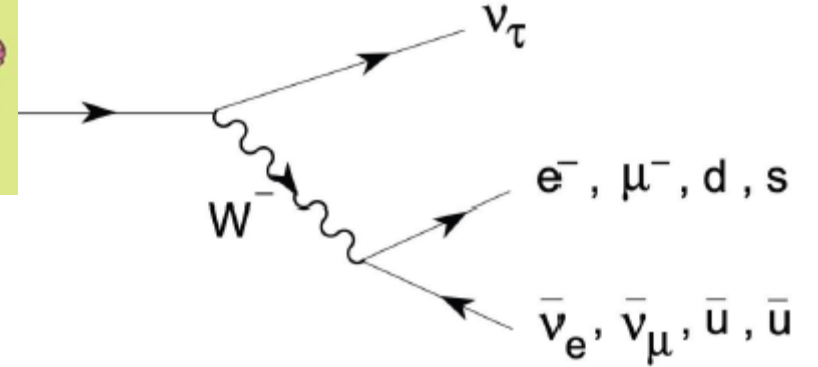


τ physics

Tau physics



- 185 standard model decay modes studied
 - principally hadronic final states
- Unique laboratory to study weak interaction
- Third-generation therefore beyond-SM-sensitivity anticipated
 - Any observation of lepton-flavour violation in $\tau \rightarrow 3\mu$, $\tau \rightarrow \mu\gamma$, $\tau \rightarrow l\phi$ etc **new physics**
 - SM highly suppressed
- Connections to g-2 and lepton universality violation in b decay
- Also, precision measurements of lepton universality in lepton decay, V_{us} , moments, lifetime and **mass**

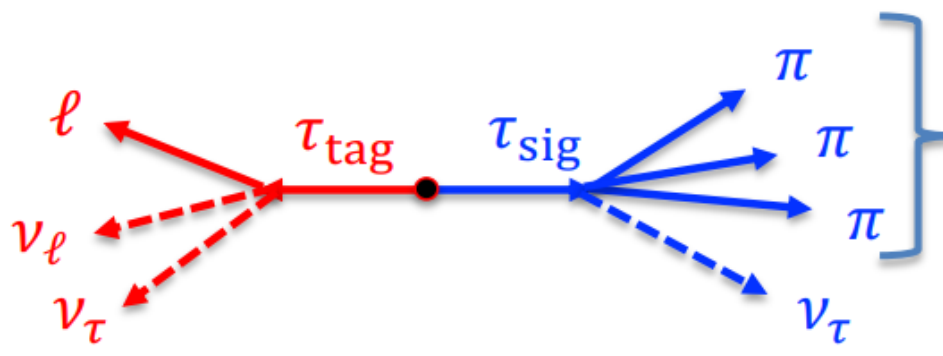


τ mass measurement

- Fundamental parameter of the standard model
 - Important input to lepton-flavour universality tests

$$R_e = \frac{\mathcal{B}[\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau]}{\mathcal{B}[\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu]} \quad \left(\frac{g_\tau}{g_\mu}\right)_e = \sqrt{R_e \frac{\tau_\mu}{\tau_\tau} \frac{m_\mu^3}{m_\tau^3} (1 + \delta_W)(1 + \delta_\gamma)} \quad (\delta\text{s are radiative corrections})$$

- We use the pseudomass variable to determine mass

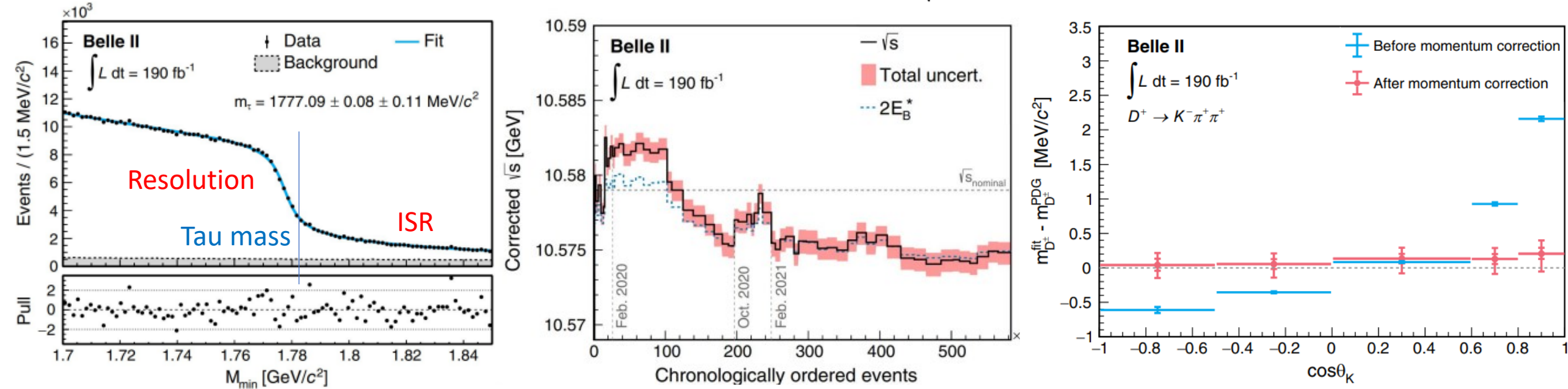


$$M_{\min} = \sqrt{m_{3\pi}^2 + 2(\sqrt{s}/2 - E_{3\pi})(E_{3\pi} - |\vec{p}_{3\pi}|)} \leq m_\tau$$

Fit to the endpoint with empirical function

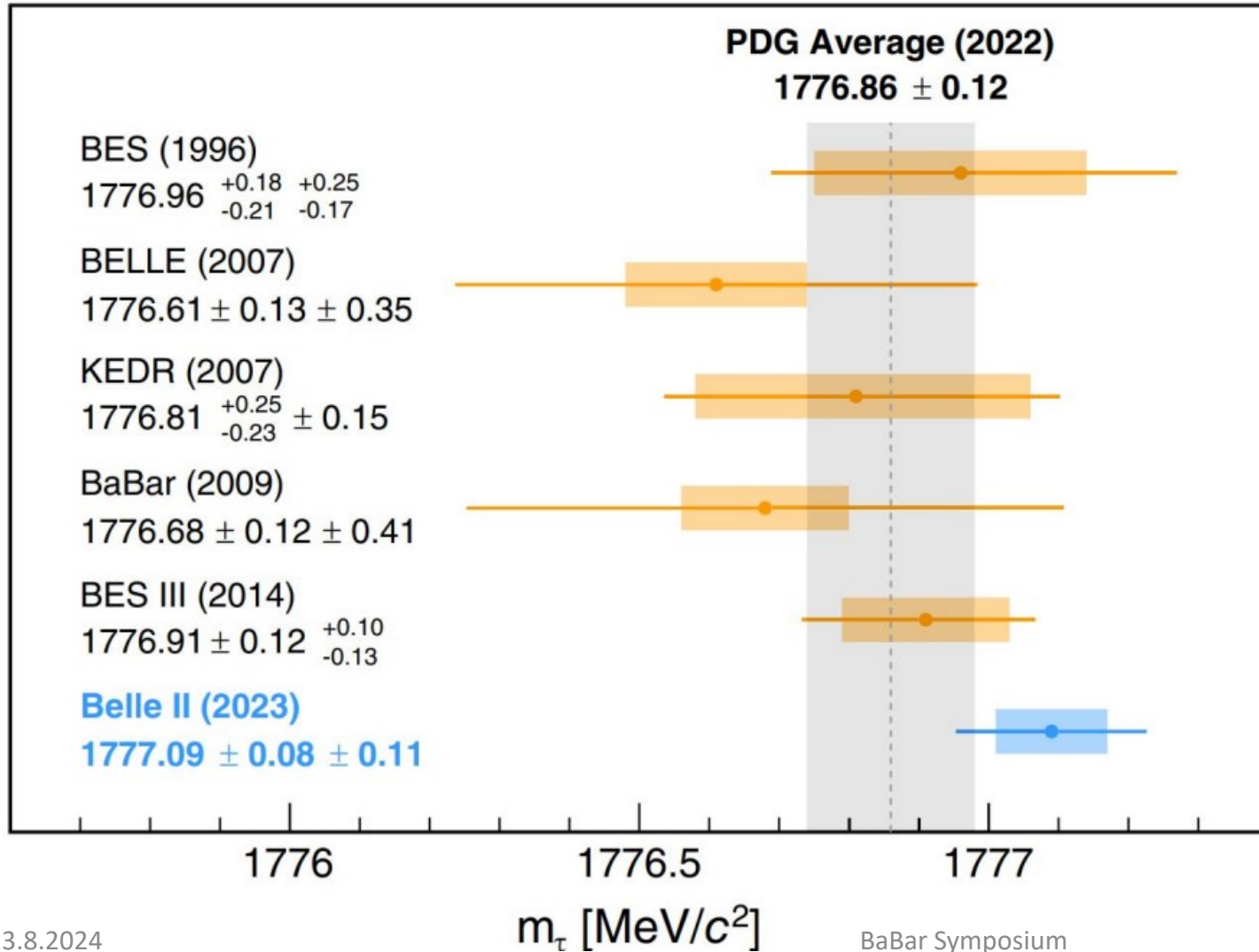
τ mass measurement

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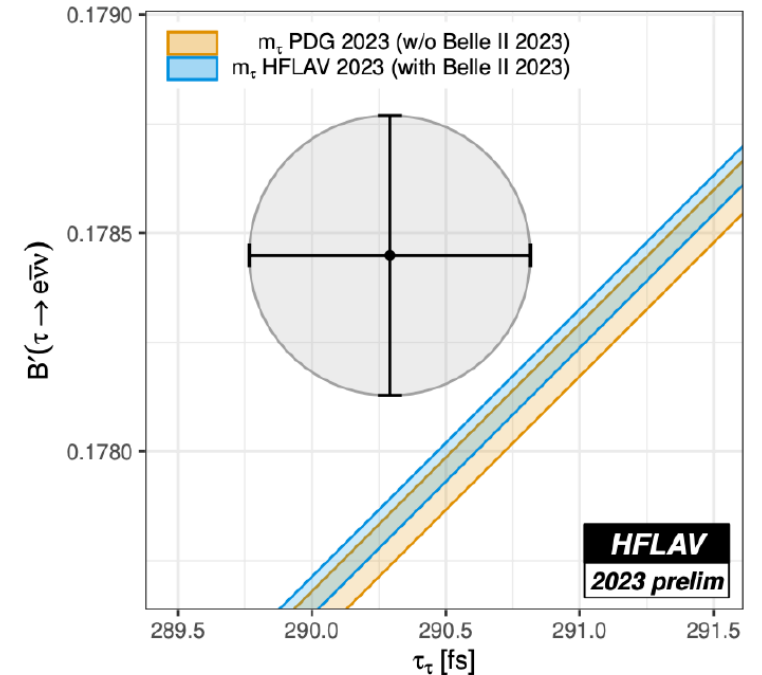
- Fit to distribution with analytic form that accounts for ISR, FSR and resolution
- Knowing the scale key: beam energy (from E_B^*) and momentum (from D mass)

τ mass measurement



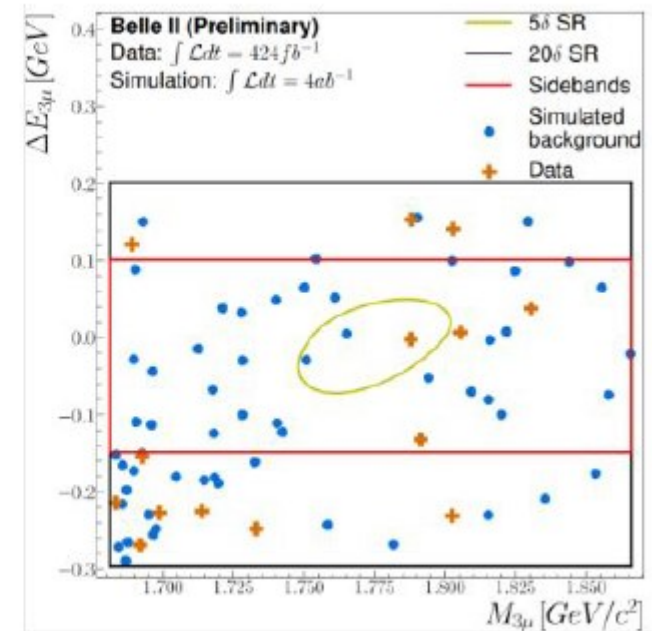
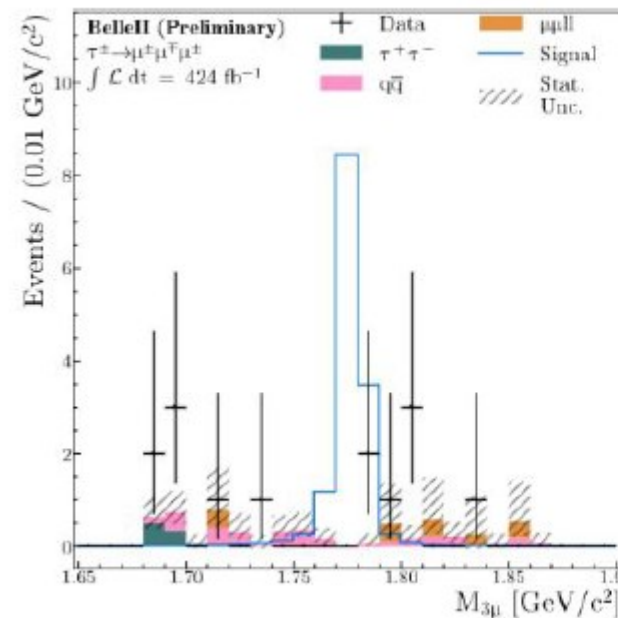
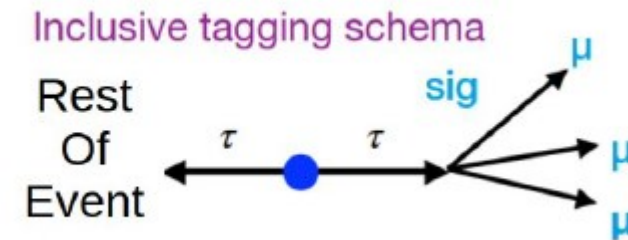
World's most precise measurement to date

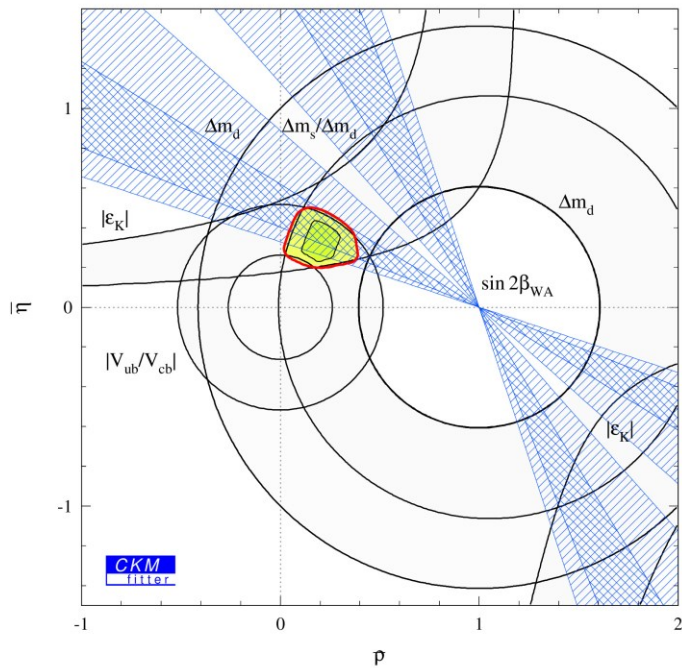
Impact on other precision measurements



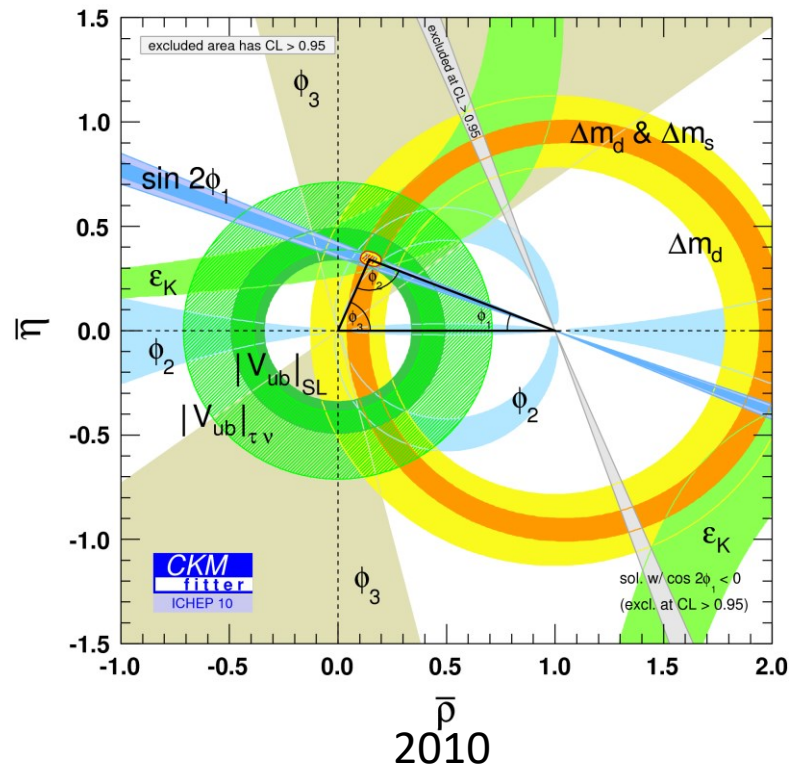
$\tau \rightarrow 3\mu^-$ lepton flavour violation search

- Inclusive tag of the non-signal τ to increase efficiency – multivariate
- Cut ‘n’ count in 2D plane of
 - $M_{3\mu}$ and $\Delta E = E_{3\mu} - E_{\text{beam}}$ (in c.m.)
 - Sideband derived background estimate $0.5^{+1.4}_{-0.5}$ events
- One event observed
- World best limit
 - **BF < 1.9×10^{-8} (90% c.l.)**
- Area of competition
 - [LHCb](#) BF < 4.1×10^{-8} (Run 1 only)
 - [CMS](#) BF < 2.9×10^{-8} (Run 1+2)

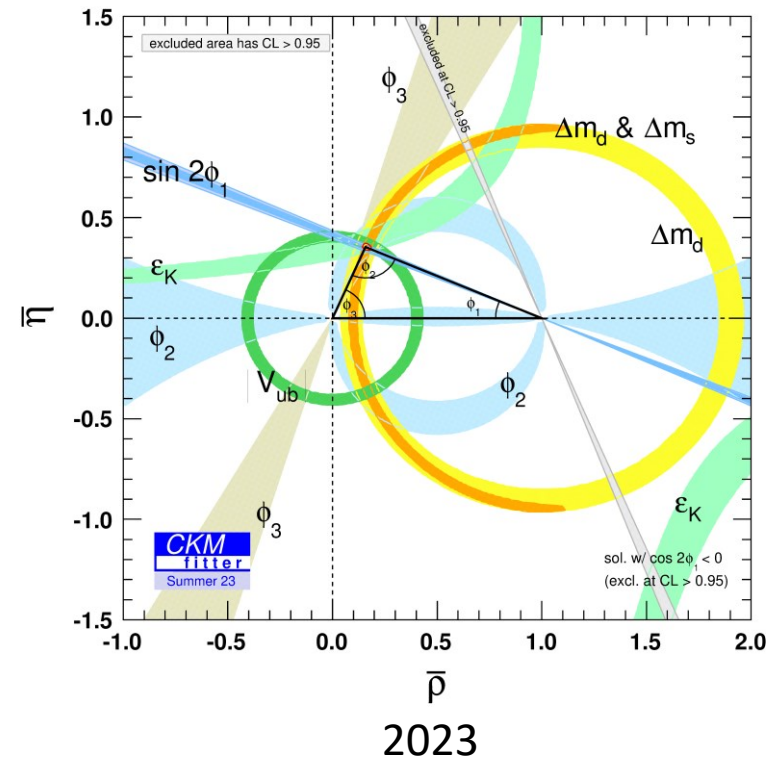




2001



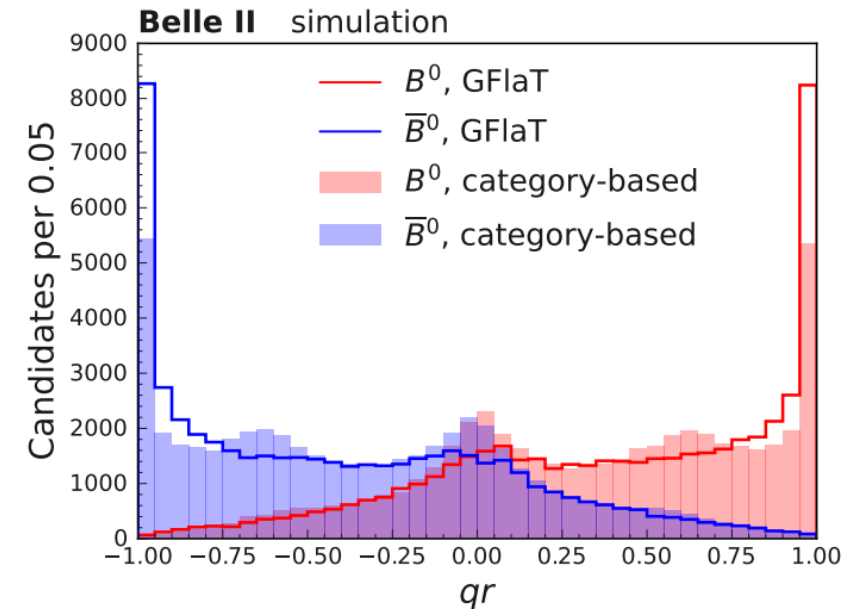
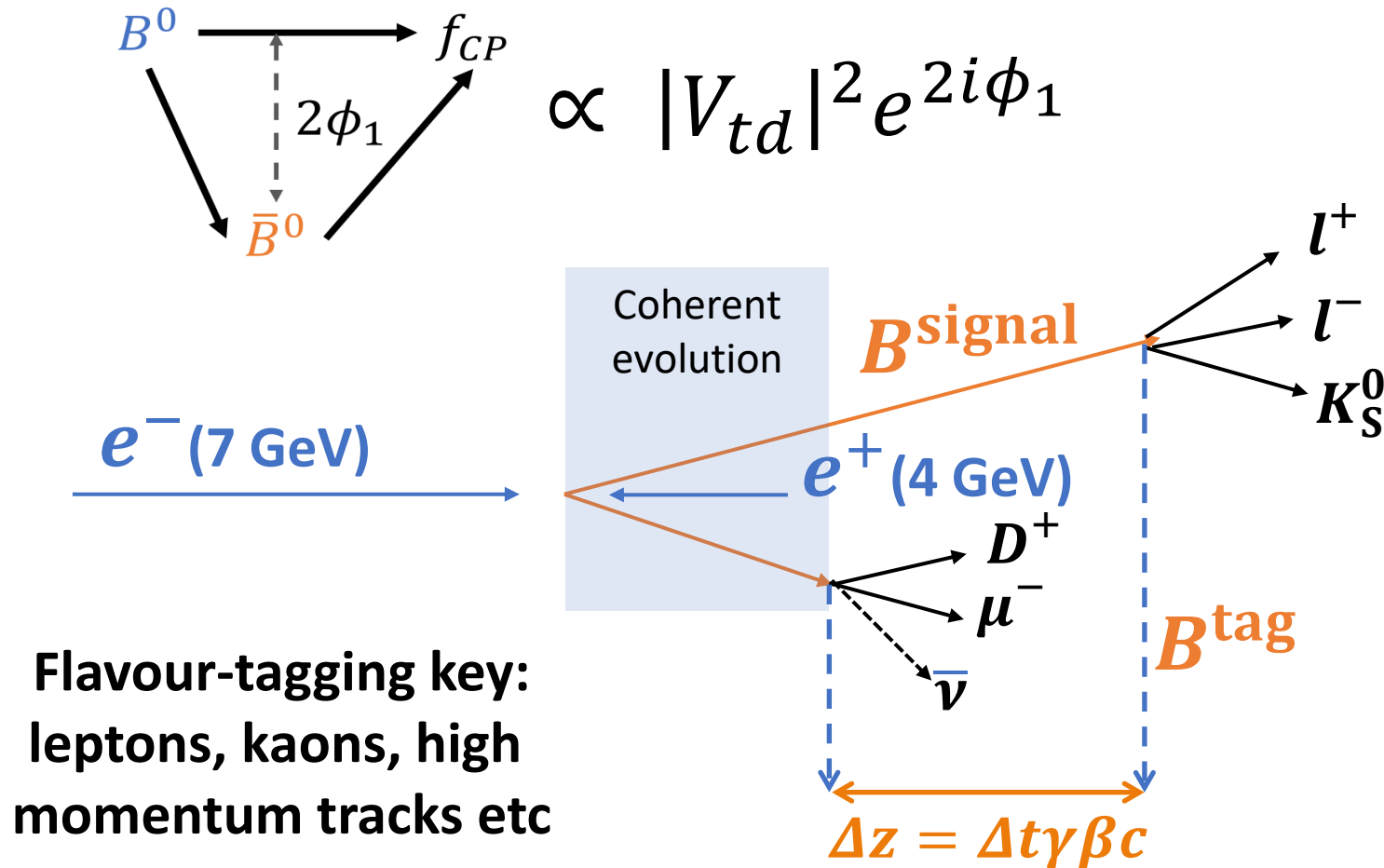
2010



2023

CKM and CP violation

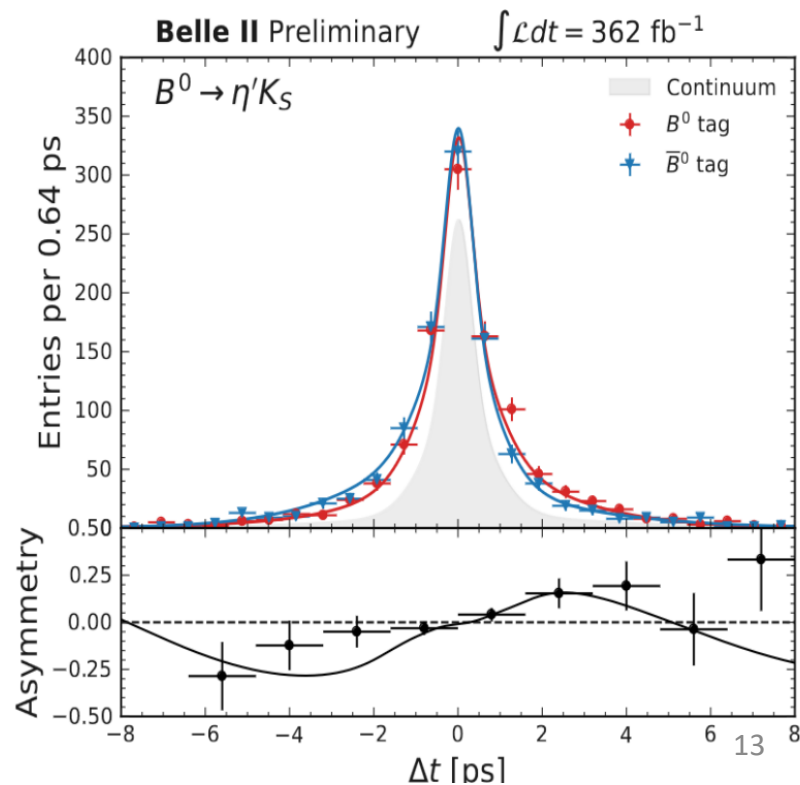
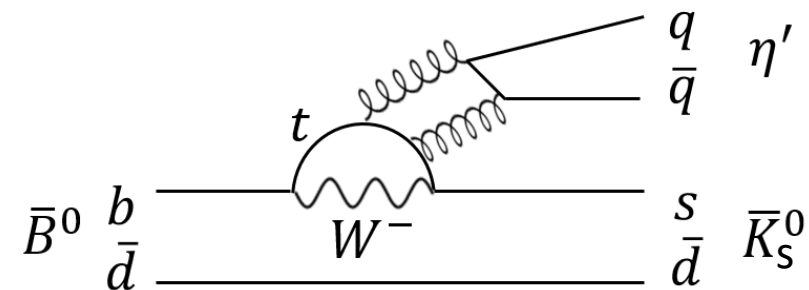
Flavour tagging improvements

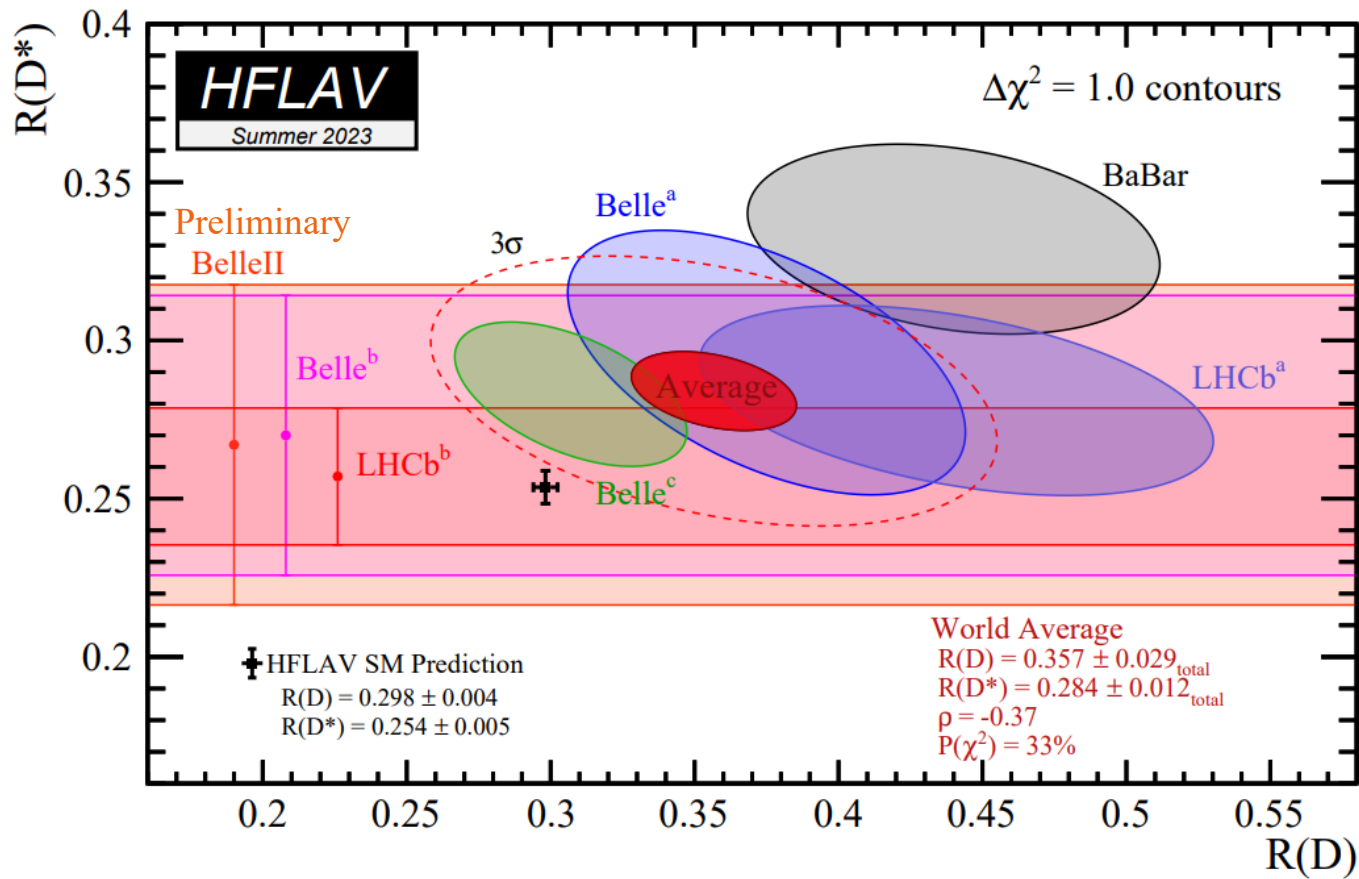


Graph-neural-network approach has improved our tagging by 18%
 $\epsilon(1 - 2\omega) = 37.4\%$

Time-dependent CP violation - $B^0 \rightarrow \eta' K_S^0$

- Decay may also have a BSM phase as it is a gluonic penguin
 - alter the value of ϕ_1 from that measured in $b \rightarrow c\bar{c}s$ transitions such as $B^0 \rightarrow J/\psi K_S^0$
- Reconstructing $\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$ and $\eta' \rightarrow \rho(\pi^+\pi^-)\gamma$ we select 829 ± 35 events in 362 fb^{-1} sample
 - 3D fit to ΔE , m_{BC} and continuum suppression output
- **$\sin 2\phi'_1 = 0.67 \pm 0.10 \pm 0.04$**
- Consistent with current HFLAV average and that from $b \rightarrow c\bar{c}s$ result

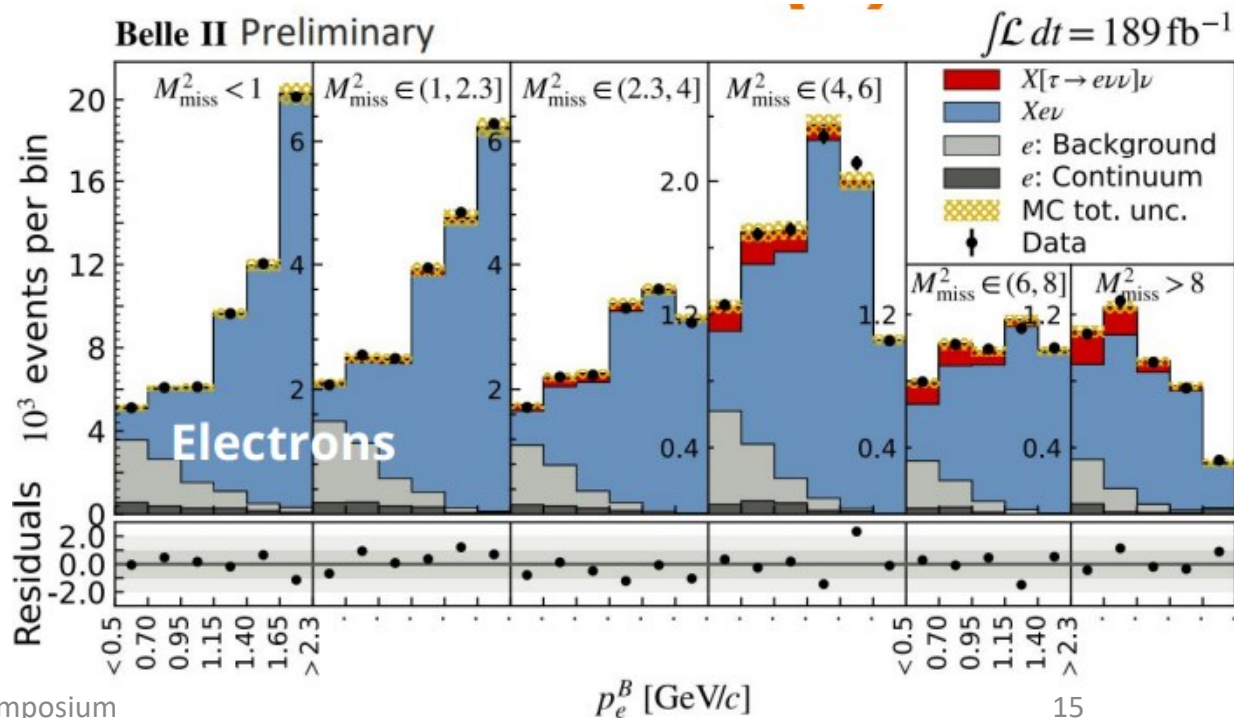
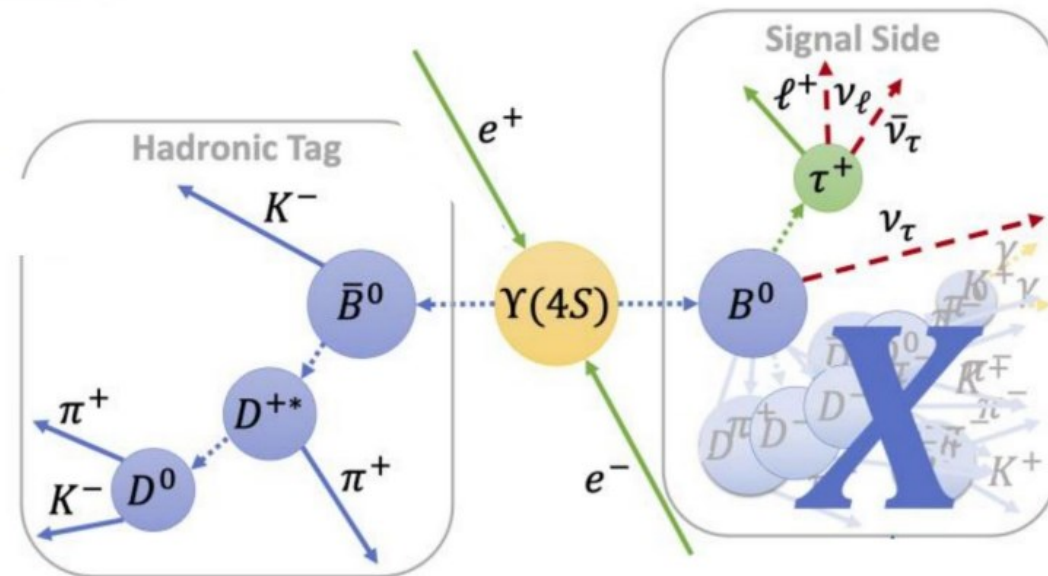




Lepton flavour/universality violation and rare decays

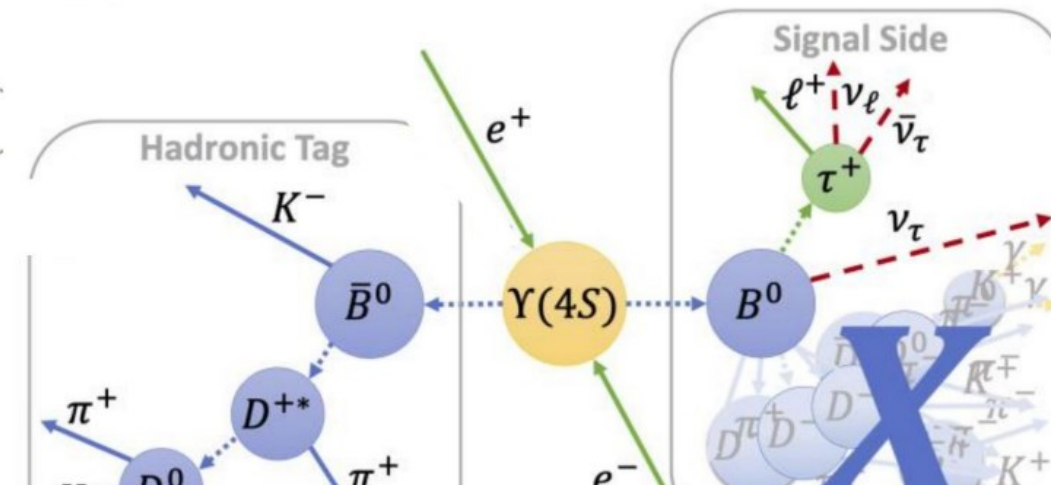
Measurement of $R(X)$

- Inclusive ratio $R(X) = \frac{BF(B \rightarrow X\tau\nu)}{BF(B \rightarrow Xl\nu)}$
 - A complementary alternative to $R(D^{(*)})$
- Hadronic-tagging method with a 189 fb^{-1} Belle II sample
 - Hadronic tag pioneered by BaBar
 - [PRL 92 071802](#)
 - MVA version at Belle II
 - [Comput. Softw. Big Sci. 3 \(2019\) 1, 6](#)
- Use missing-mass squared and lepton momentum to isolate **signal** above $B \rightarrow Xl\nu$ background
- Background templates calibrated to control samples and sidebands



Measurement of $R(X)$

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 - A complementary alternative to $R(D^{(*)})$



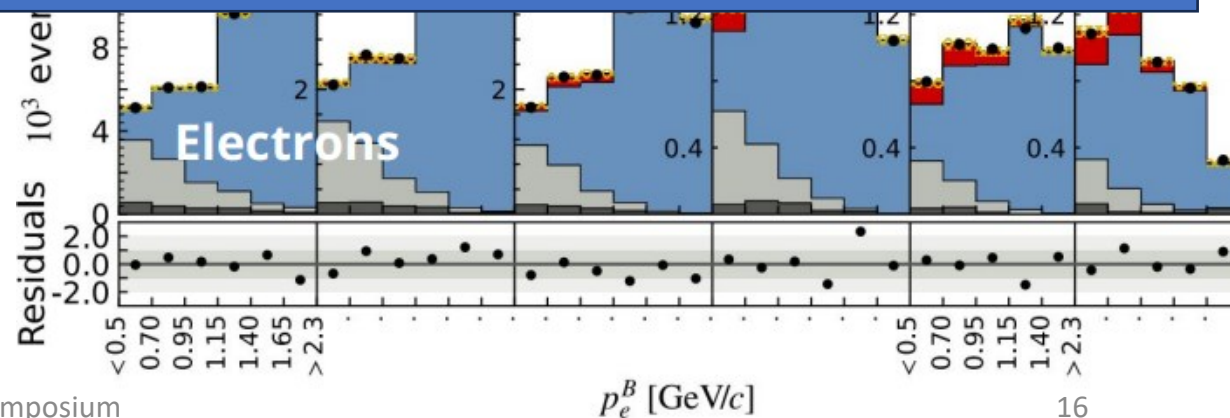
$$R(X) = 0.228 \pm 0.016 \text{ (stat)} \pm 0.036 \text{ (syst)}$$

Systematics dominated by control sample reweighting procedures

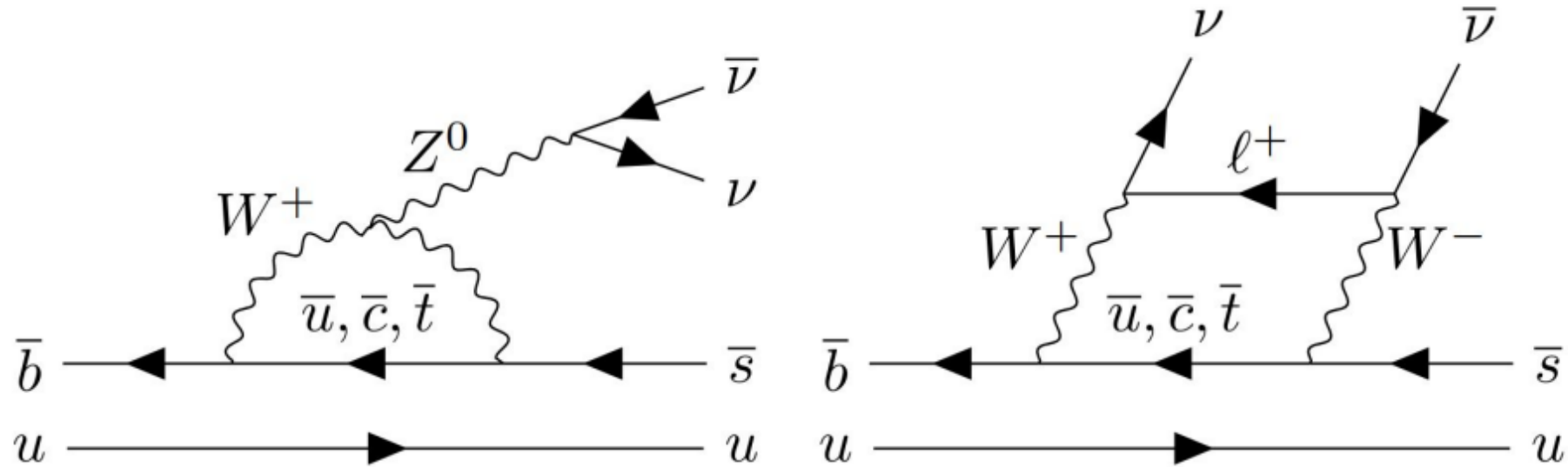
First at B factories

Agrees with SM prediction and the WA $R(D^{(*)})$ values

- Use missing-mass squared and lepton momentum to isolate **signal** above $B \rightarrow Xl\nu$ **background**
- Background templates calibrated to control samples and sidebands



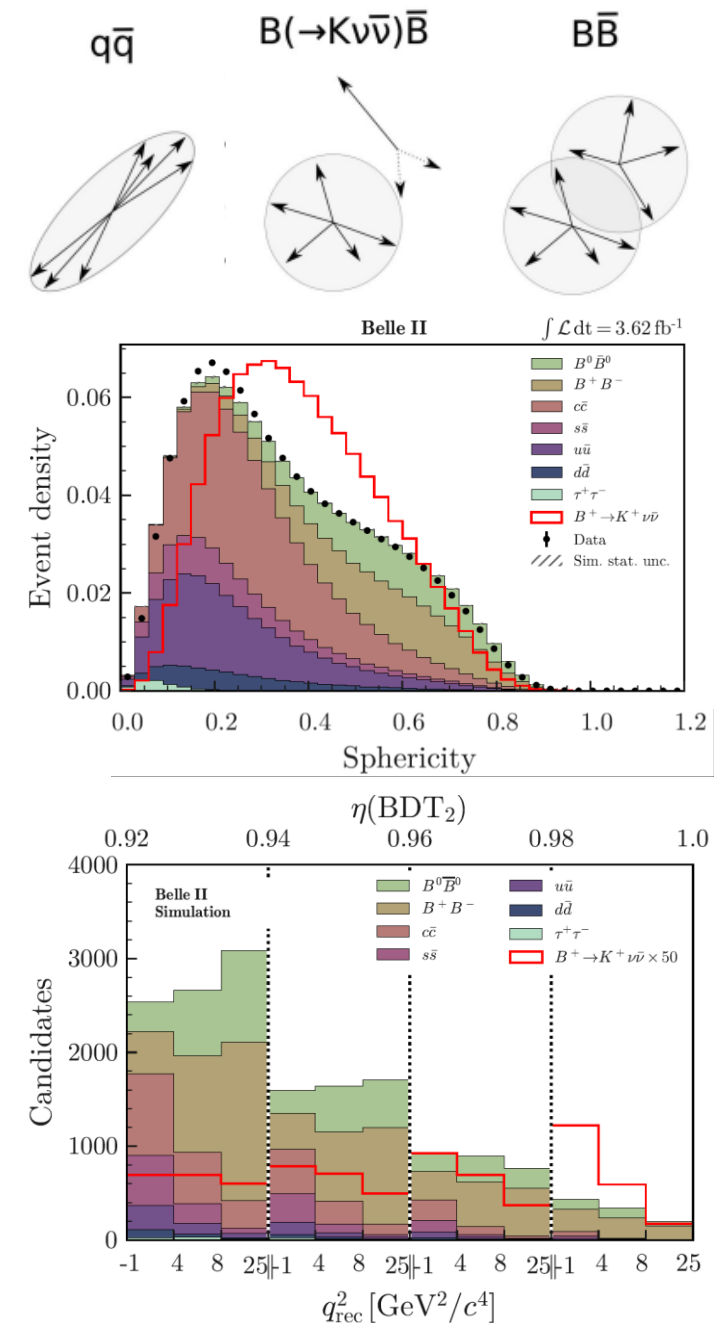
$B^+ \rightarrow K^+ \nu \bar{\nu}$: Motivation



- Well known in SM but very sensitive to BSM enhancements – 3rd gen
 - $B(B \rightarrow K^+ \nu \bar{\nu}) = (5.6 \pm 0.4) \times 10^{-6}$ [[arXiv:2207.13371](https://arxiv.org/abs/2207.13371)]
- Challenging experimentally
 - Low branching fraction with large background
 - No peak – two neutrinos leads to no good kinematic constraint

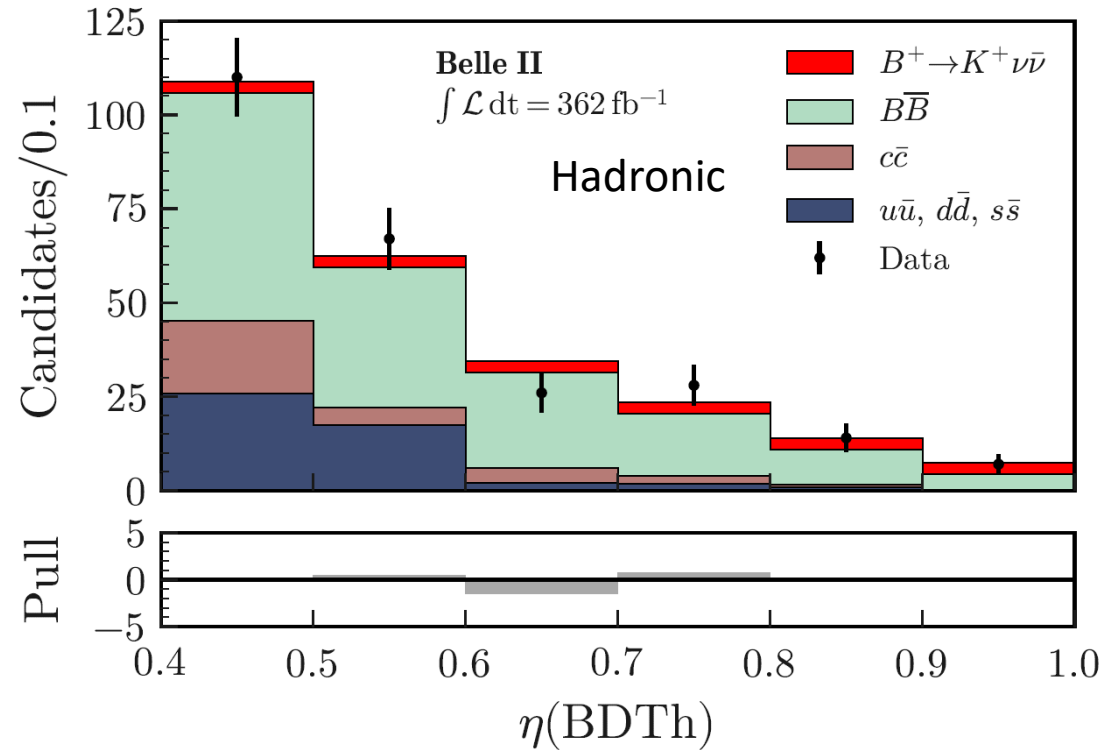
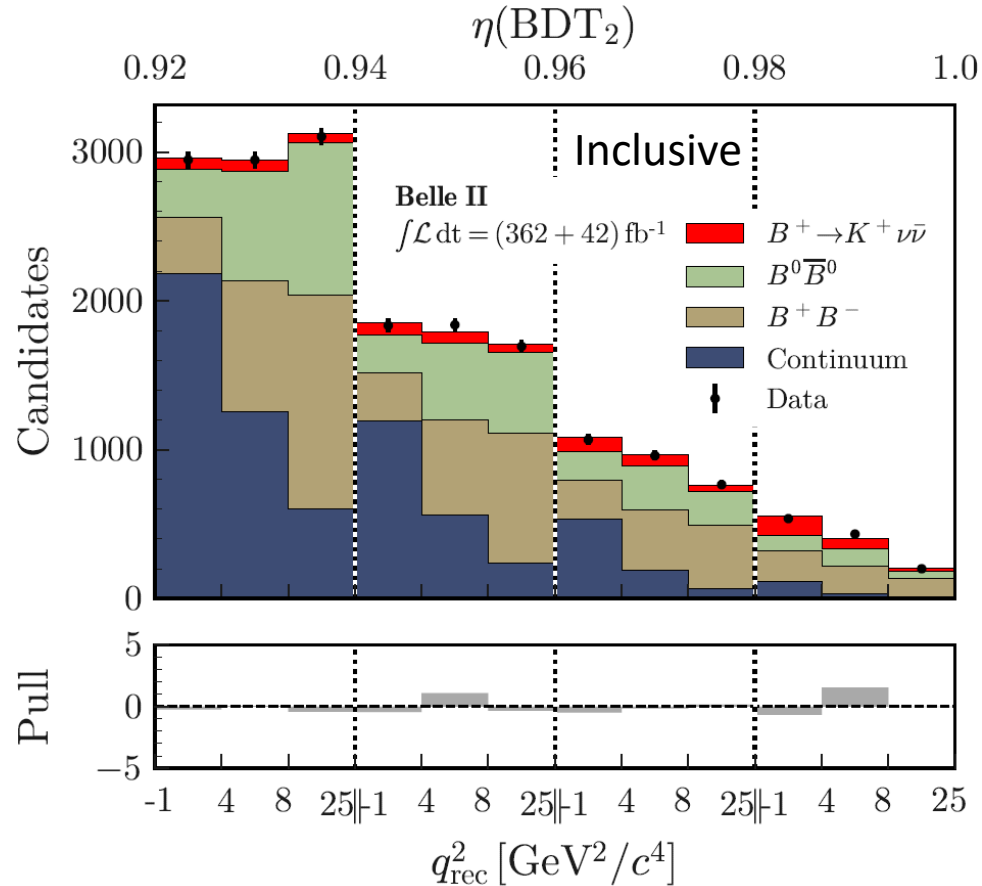
$B^+ \rightarrow K^+ \nu \bar{\nu}$: Analysis strategy

- Two methods: an inclusive tag (8% efficiency) and conventional hadronic tag (0.4% efficiency)
 - many common features except tag
- Inclusive event variables to suppress background
 1. preselect events where missing momentum and signal kaon well reconstructed
 2. First boosted decision tree (BDT1): 12 variables
 3. Second BDT2: 35 variables – 3 times sensitivity
 4. BDT2 fit extraction variable in bins of $\nu \bar{\nu}$ mass-squared – q^2
- Many systematic studies with data-driven corrections and checks with control samples



$B^+ \rightarrow K^+ \nu \bar{\nu}$: Results

arXiv:2311.14647 [hep-ex]
Accepted PRD



$$\text{BF}_{\text{inc}} = (2.7 \pm 0.5(\text{stat}) \pm 0.5(\text{syst})) \times 10^{-5}$$

$$\text{BF}_{\text{had}} = (1.1_{-0.8}^{+0.9}(\text{stat})_{-0.5}^{+0.8}(\text{syst})) \times 10^{-5}$$

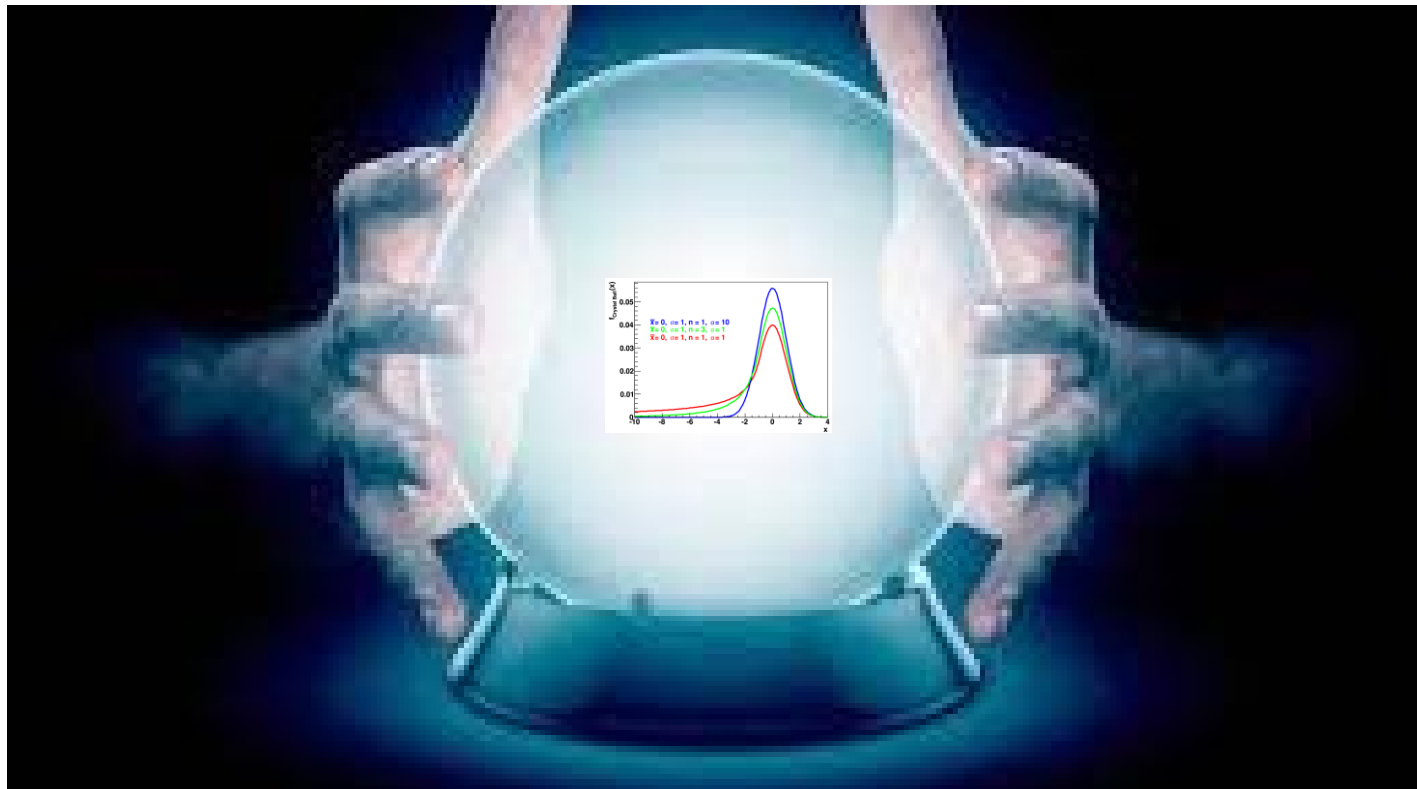
$$\text{BF}_{\text{comb}} = (2.3 \pm 0.5(\text{stat})_{-0.4}^{+0.5}(\text{syst})) \times 10^{-5}$$

Combined result

Evidence @ 3.5σ

Tension with SM (0.6×10^{-5})

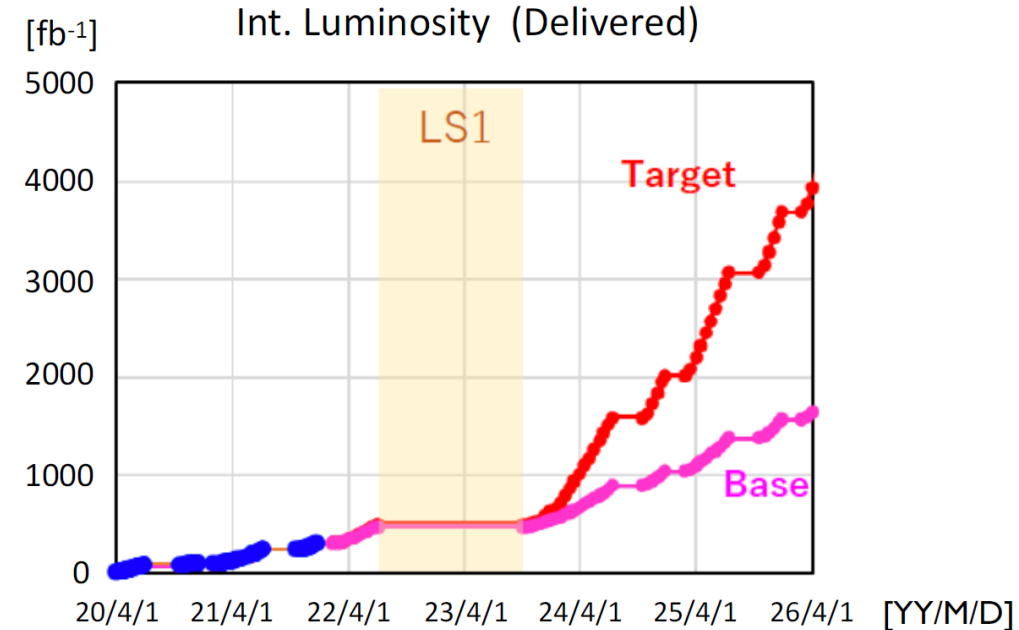
@ 2.7σ



5) Prospects and conclusion

Belle II: after current shutdown

- We have not collected the sample size planned to date
 - Beam conditions
- Since summer 2022 until **Feb 2024** shutdown for accelerator upgrades to mitigate background and increase luminosity
- Detector upgrades too
 - two-layer pixel detector installed
- **Path to $2 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ but new final focus to go beyond**
 - Proposed upgrade from 2028+
 - see C. Checci and M. Roney next



Goals with current data to a few inverse ab^{-1}

- Semileptonic decay:
 - V_{cb} can we make progress on the inclusive vs. exclusive tension
 - KEK report in preparation
 - **$R(D)$ - $R(D^*)$**
- Electroweak penguin
 - **Missing energy modes** like $B \rightarrow K\tau\tau$ and $K\nu\nu$
- CP violation
 - α and the **gluonic penguins**
- tau
 - **LFV and precision**
- Charm
 - final states with neutrals, e.g., $D \rightarrow \pi^0\pi^0$
- Quarkonium
 - $Y(10753)$ scan and isospin partners (ISR and B decay)
- Dark sector and low multiplicity
 - dark photon and $e^+e^- \rightarrow \pi^+\pi^-$

Our [Snowmass submission](#) is the most up to date prospects document

Conclusion

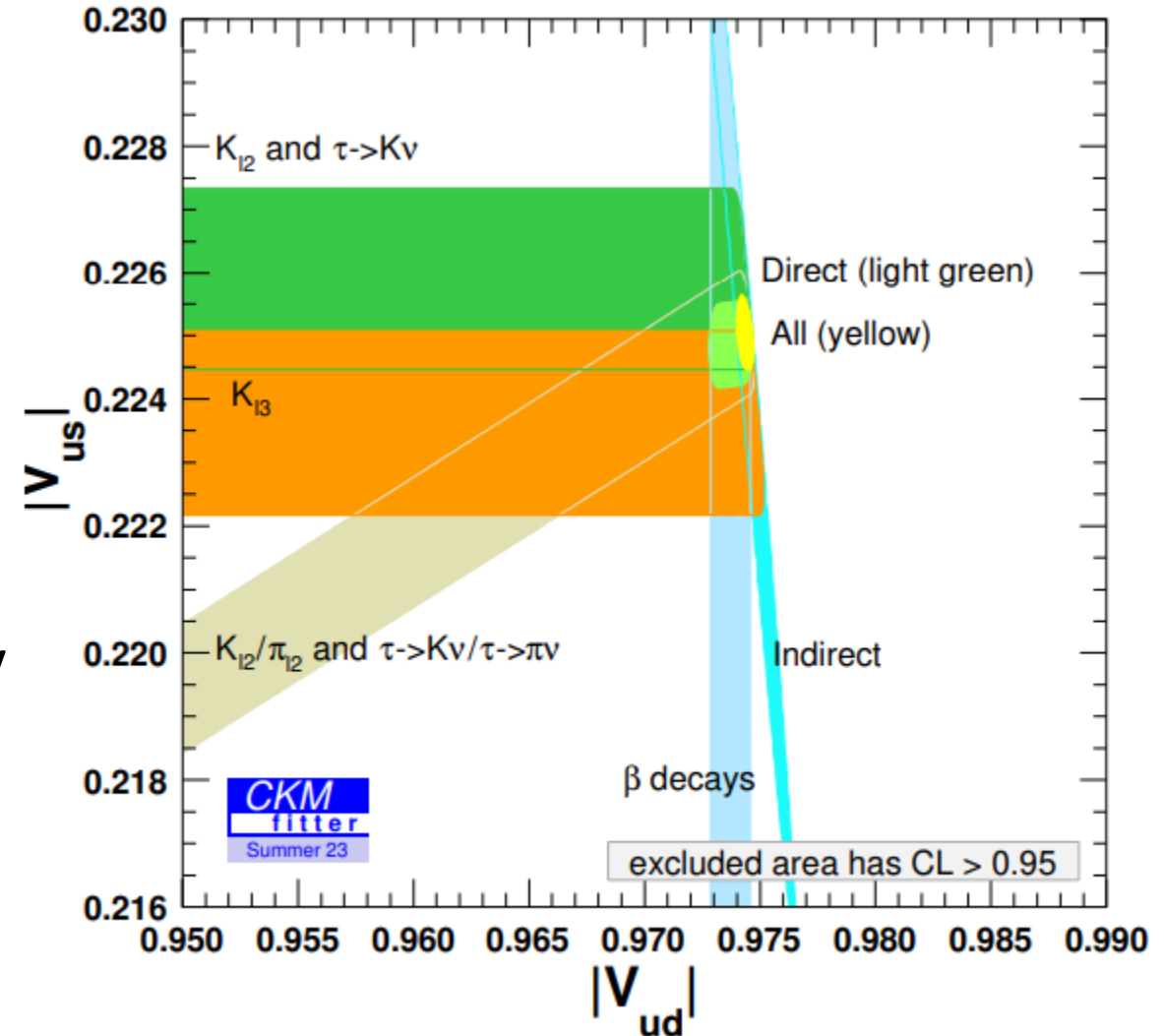
- e^+e^- has an important role to play in the future of flavour
 - Belle II is catching up to first generation sample size, we are producing competitive and exciting results
 - [37 papers](#) and 10 preliminary results with a paper in preparation
 - More before the summer with the Run 1 data
 - A lot more to come once we enter the “ 10^{35} era” of Run 2 which is just starting

Backup

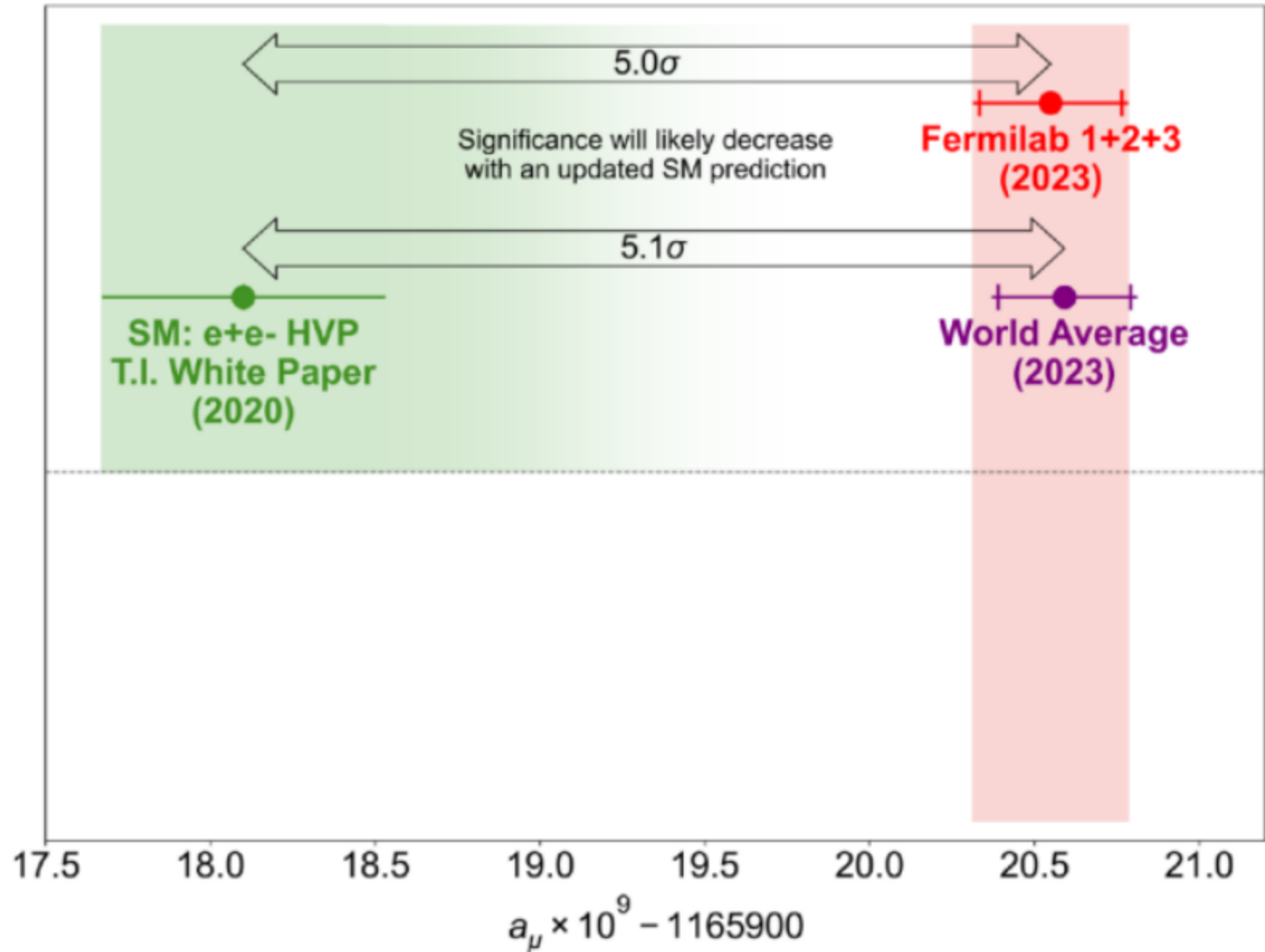
Tau physics motivation II

- **Precision measurements** of the τ lepton can have significant impact
- Example:
 - first row unitarity of CKM matrix – ‘Cabibbo angle anomaly’
 - $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu)$ proportional to $|V_{us}/V_{ud}|^2$
 - Combine with lattice QCD information to provide additional constraint
- Additionally, lepton-flavour universality and dipole moments
- **Mass** and lifetime important inputs to these calculations

Luiz Vale Silva (CKM 2023)

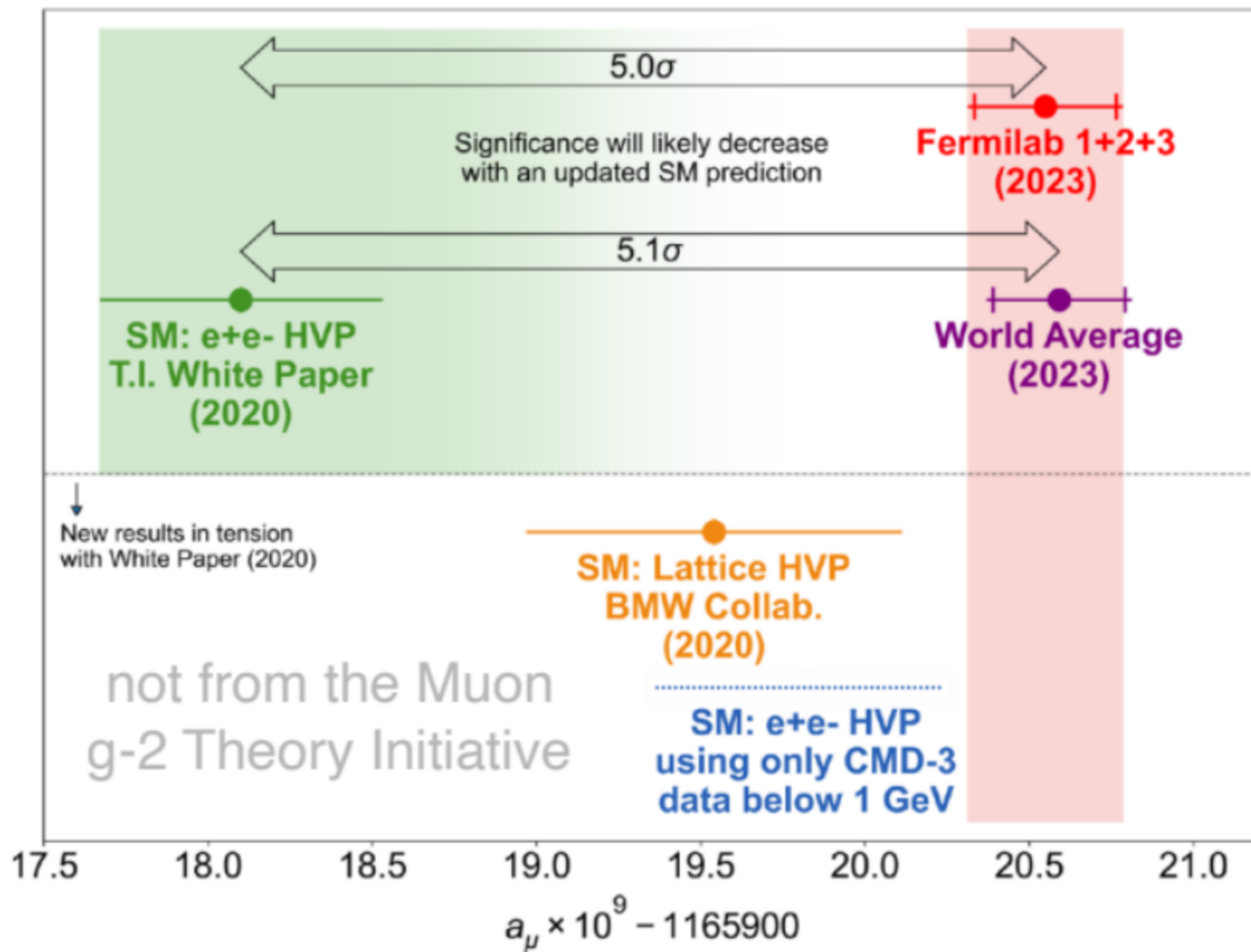


...away
from heavy
flavour
muon $g-2$



Plot from A. Keshavarzi talk at Lattice 2023

...away from heavy flavour muon $g-2$



Plot from A. Keshavarzi talk at Lattice 2023

$$\sigma(e^+e^- \rightarrow \pi^+\pi^-\pi^0)$$

Muon anomalous magnetic moment

$$a_\mu = \frac{g-2}{2} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{QCD}}$$

Hadron contribution term

$$a_\mu^{\text{QCD}} = a_\mu^{\text{HVP}} + a_\mu^{\text{HLbL}}$$

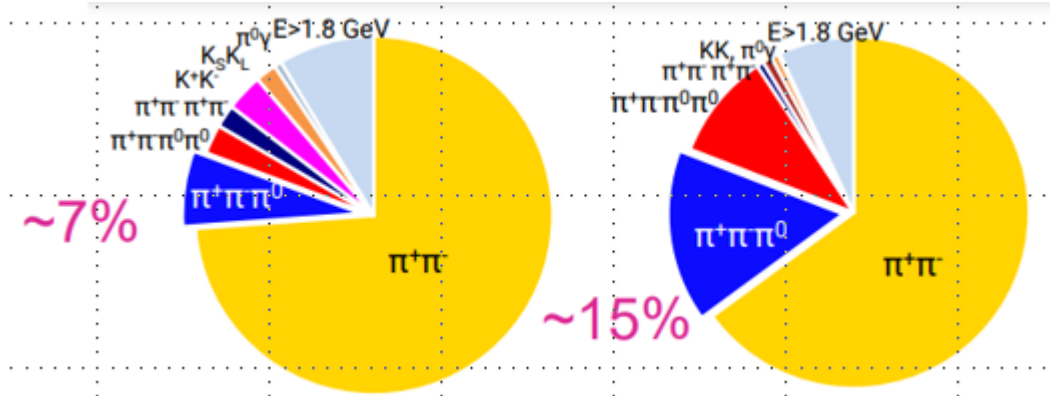
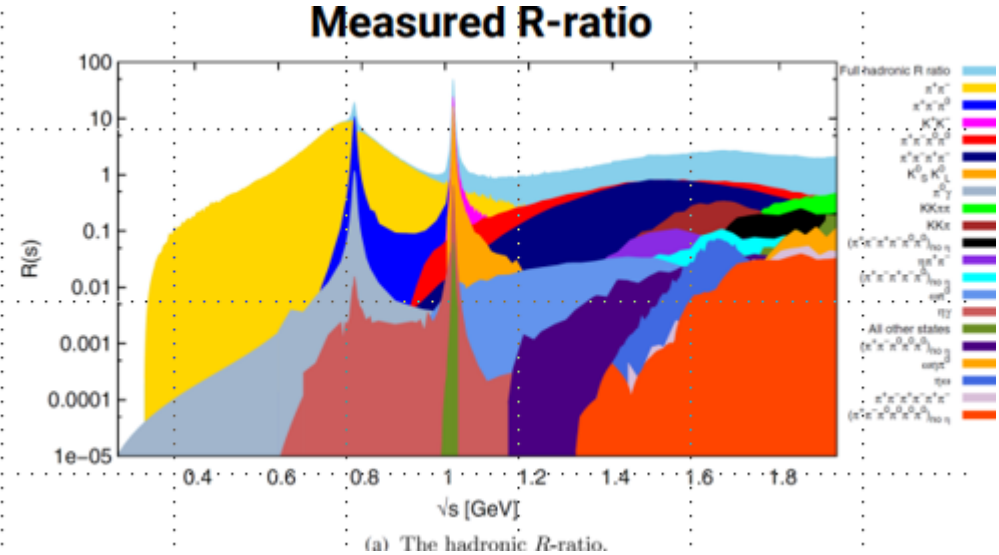
Leading-order HVP term

$$a_\mu^{\text{HVP,LO}} = \frac{\alpha^2}{3\pi^2} \int_{m_\pi^2}^{\infty} \frac{ds}{s} R(s) K(s)$$

Hadronic R-ratio

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

2nd largest contribution to the hadronic vacuum polarization estimate as region below 1 GeV in c.m. energy dominates



$$\sigma(e^+e^- \rightarrow \pi^+\pi^-\pi^0)$$

- Initial-state radiation technique – wide invariant mass range
- Partial Run 1 data set – 191 fb^{-1}
- Selection via kinematic fits
- Key challenge is π^0 efficiency
 - Custom determination using ω decay
- Background control samples for $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0\gamma_{ISR}$, $e^+e^- \rightarrow q\bar{q}\gamma_{ISR}$ and $e^+e^- \rightarrow K^+K^-\pi^0\gamma_{ISR}$

Signal process : $e^+e^- \rightarrow \gamma_{ISR}\pi^+\pi^-\pi^0(\rightarrow \gamma\gamma)$

Signal spectrum

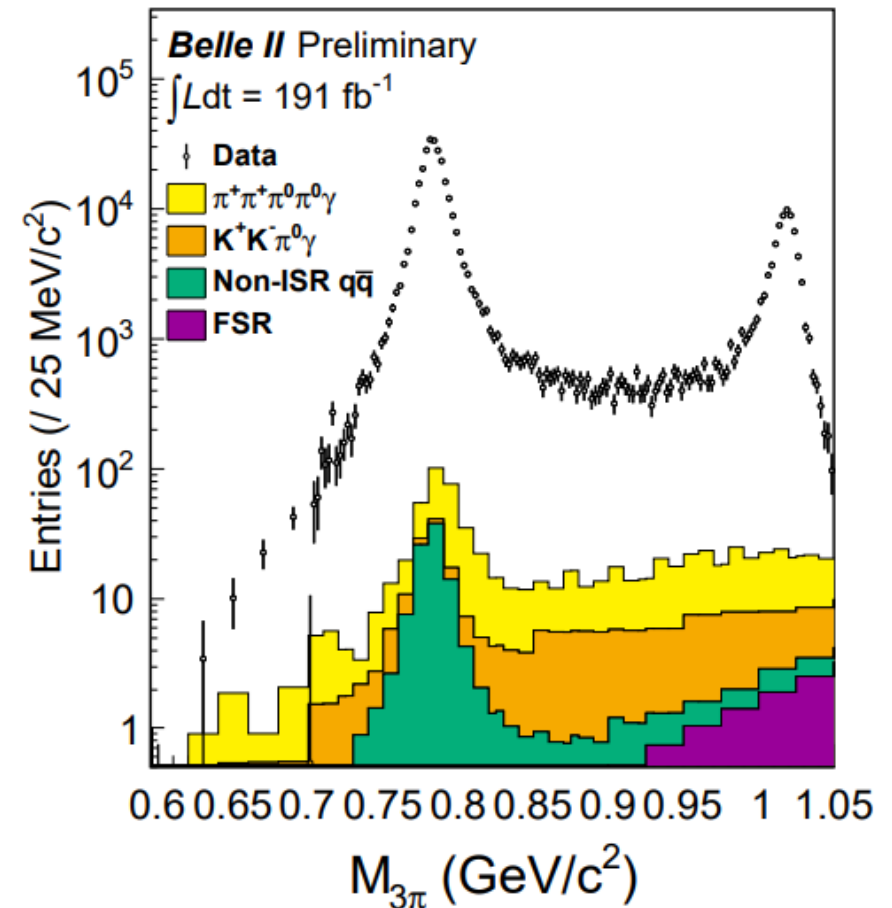
$$\frac{dN_{\text{signal}}}{dm} = \sigma_{ee \rightarrow 3\pi} \cdot \varepsilon \cdot \frac{d\mathcal{L}_{\text{eff}}}{dm}$$

3π mass

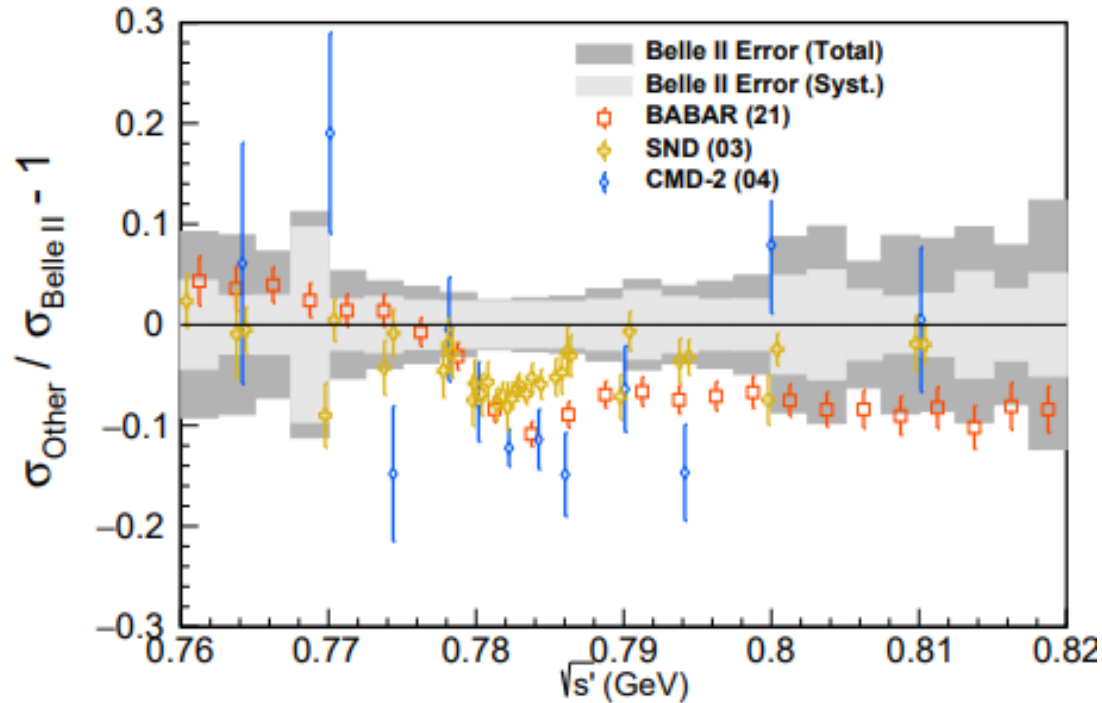
Cross section

Efficiency

Effective luminosity



$$\sigma(e^+e^- \rightarrow \pi^+\pi^-\pi^0)$$

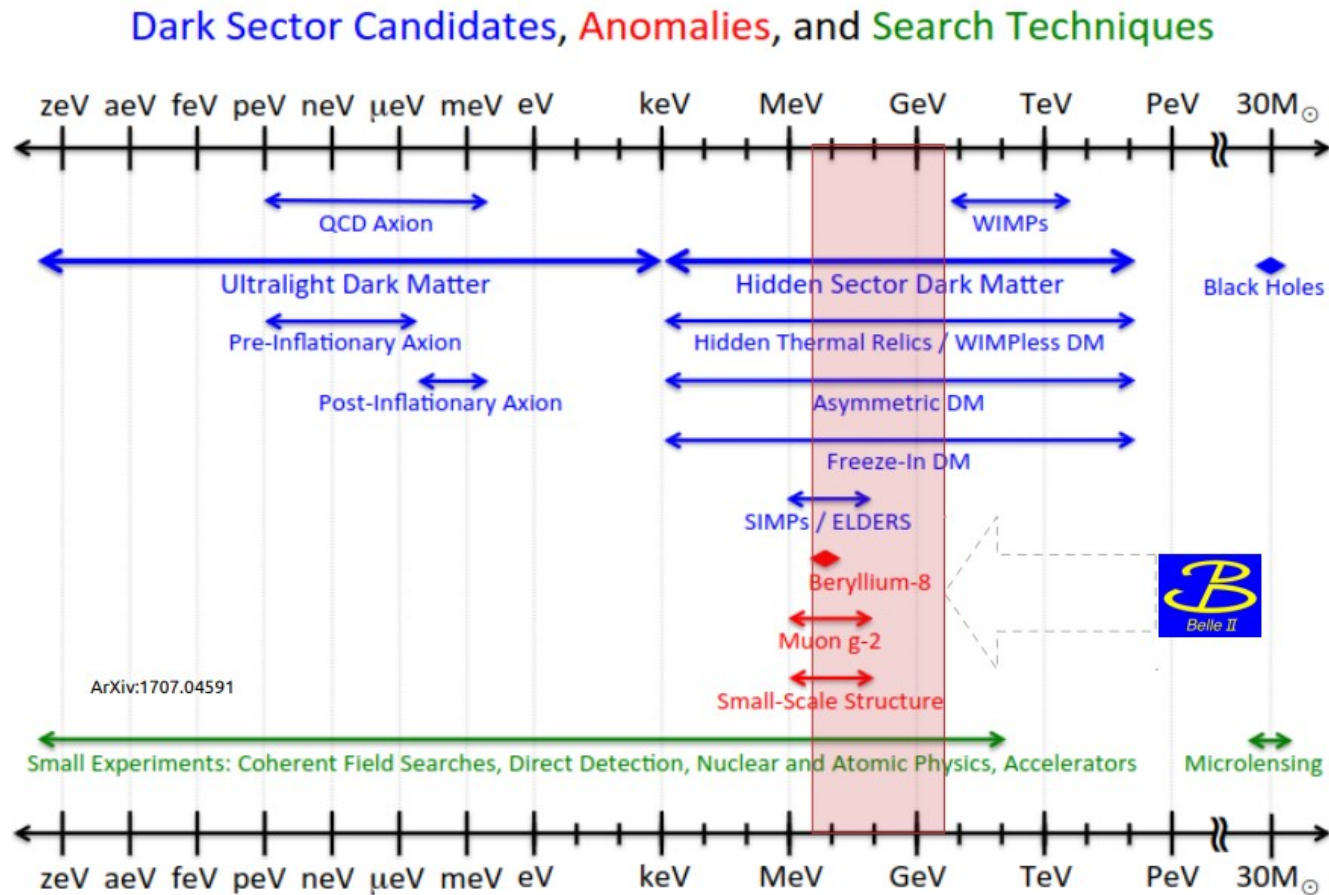


Source	0.62–1.05 GeV/c ²	
Trigger	0.1	(−0.09)
ISR photon detection	0.7	(+0.15)
Tracking	0.8	(−1.35)
π^0 detection	1.0	(−1.43)
Kinematic fit (χ^2)	0.6	(+0.0)
Event selection	0.2	(−1.90)
Generator	1.2	
Integrated luminosity	0.6	
Radiative corrections	0.5	
MC statistics	0.2	
Background subtraction	0.3–0.5	
Unfolding	0.7–15	
Total uncertainty (Total correction $\varepsilon/\varepsilon_{MC} - 1$)	2.2-15	(−4.61)

$$a_\mu^{3\pi} = (49.02 \pm 0.23 \pm 1.07) \times 10^{-10},$$

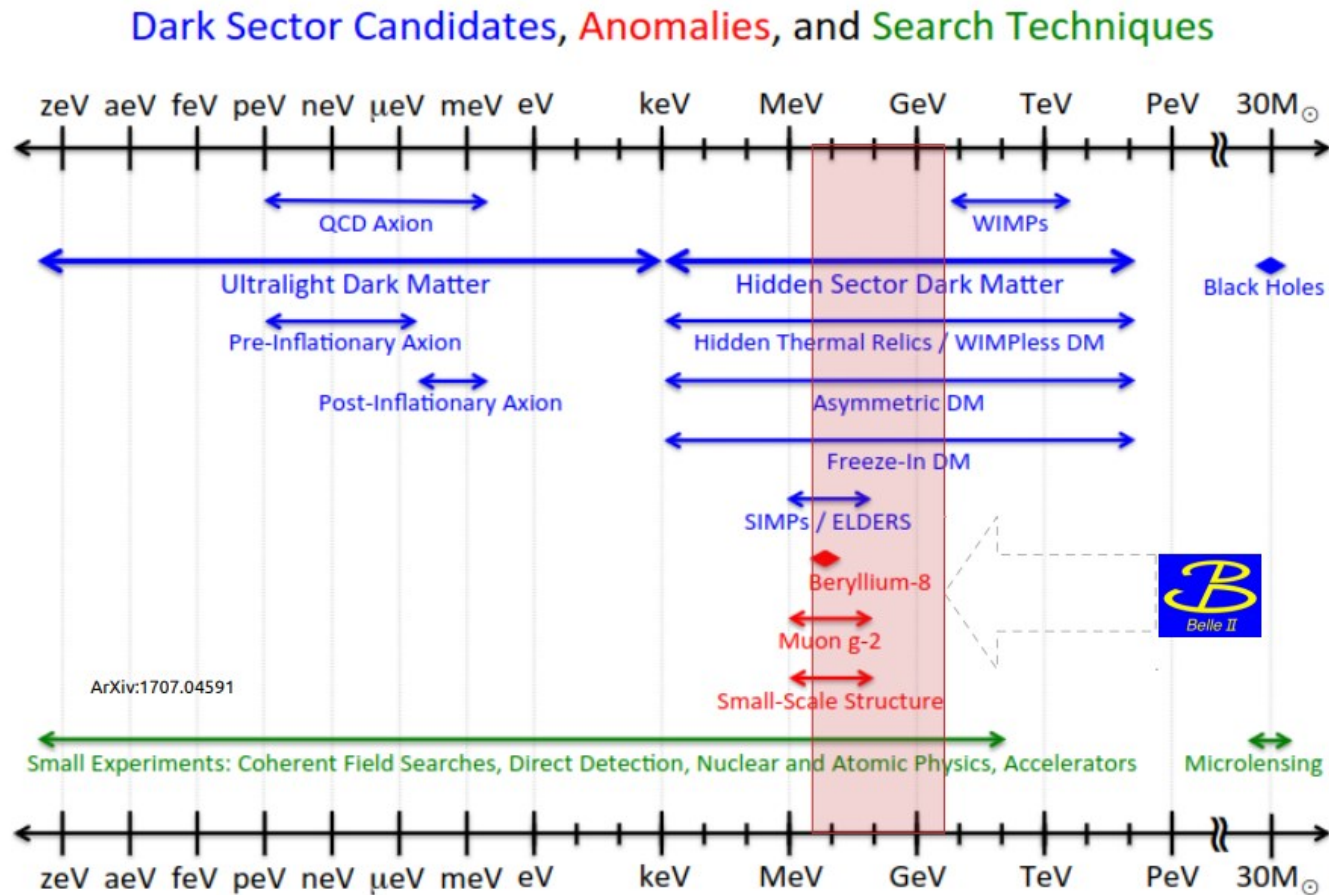
2.6 σ tension with BaBar

Light dark sector searches



- Can access the mass range favored by light dark sector
 - Possible sub-GeV scenario

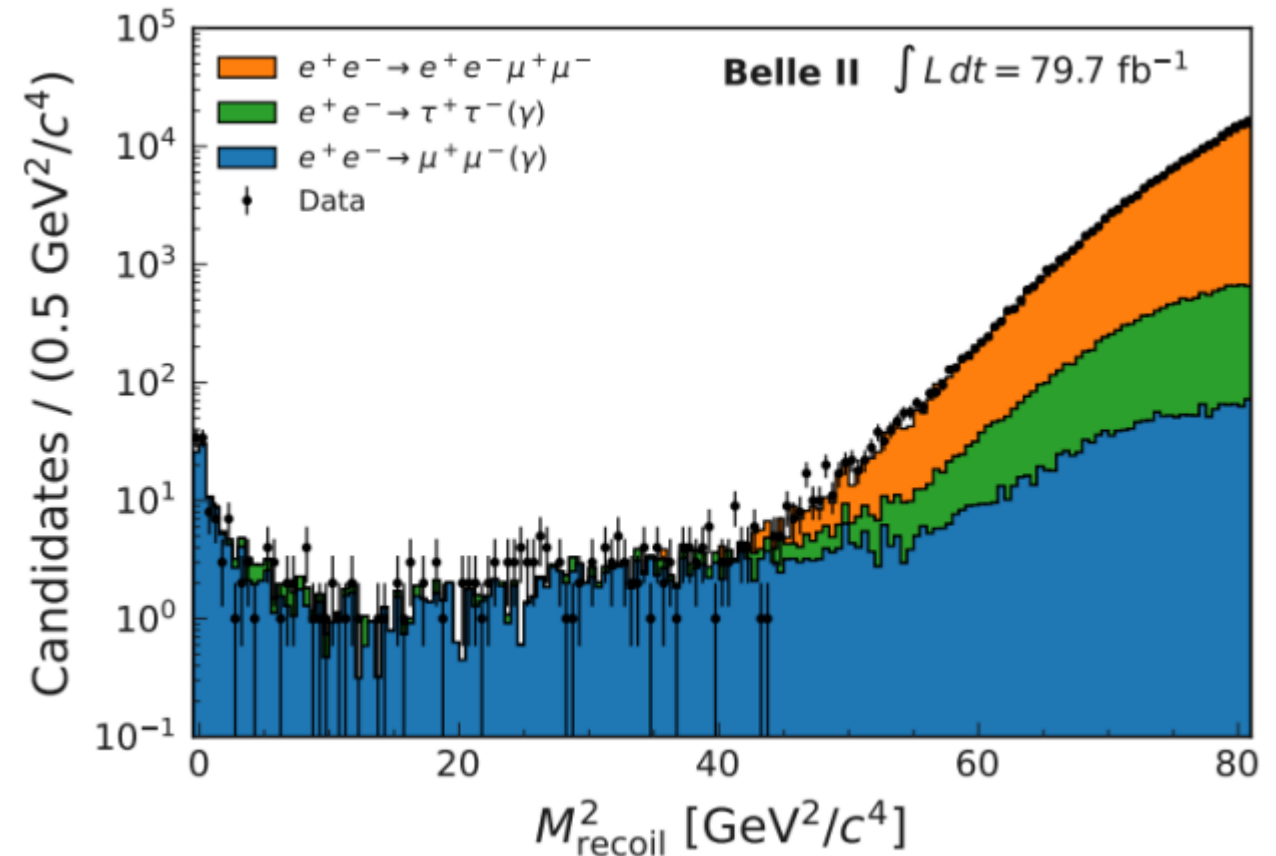
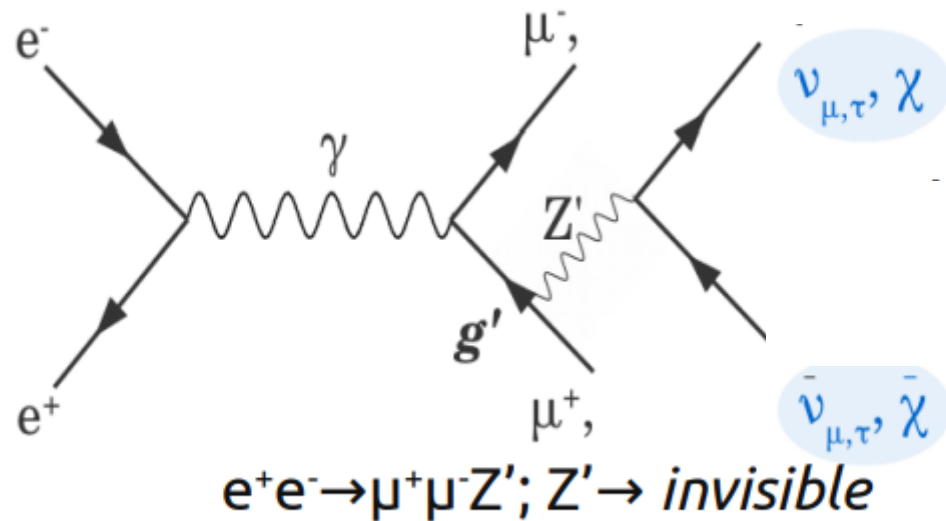
Light dark sector searches



- Can access the mass range favored by light dark sector
 - Possible sub-GeV scenario
- DM weakly coupled to SM through a light mediator X :
 - vector (Z' /dark photon), axion like particles (ALPs), scalar (dark Higgs) or fermions (sterile ν)
- Some links to anomalies, e.g., $g-2$

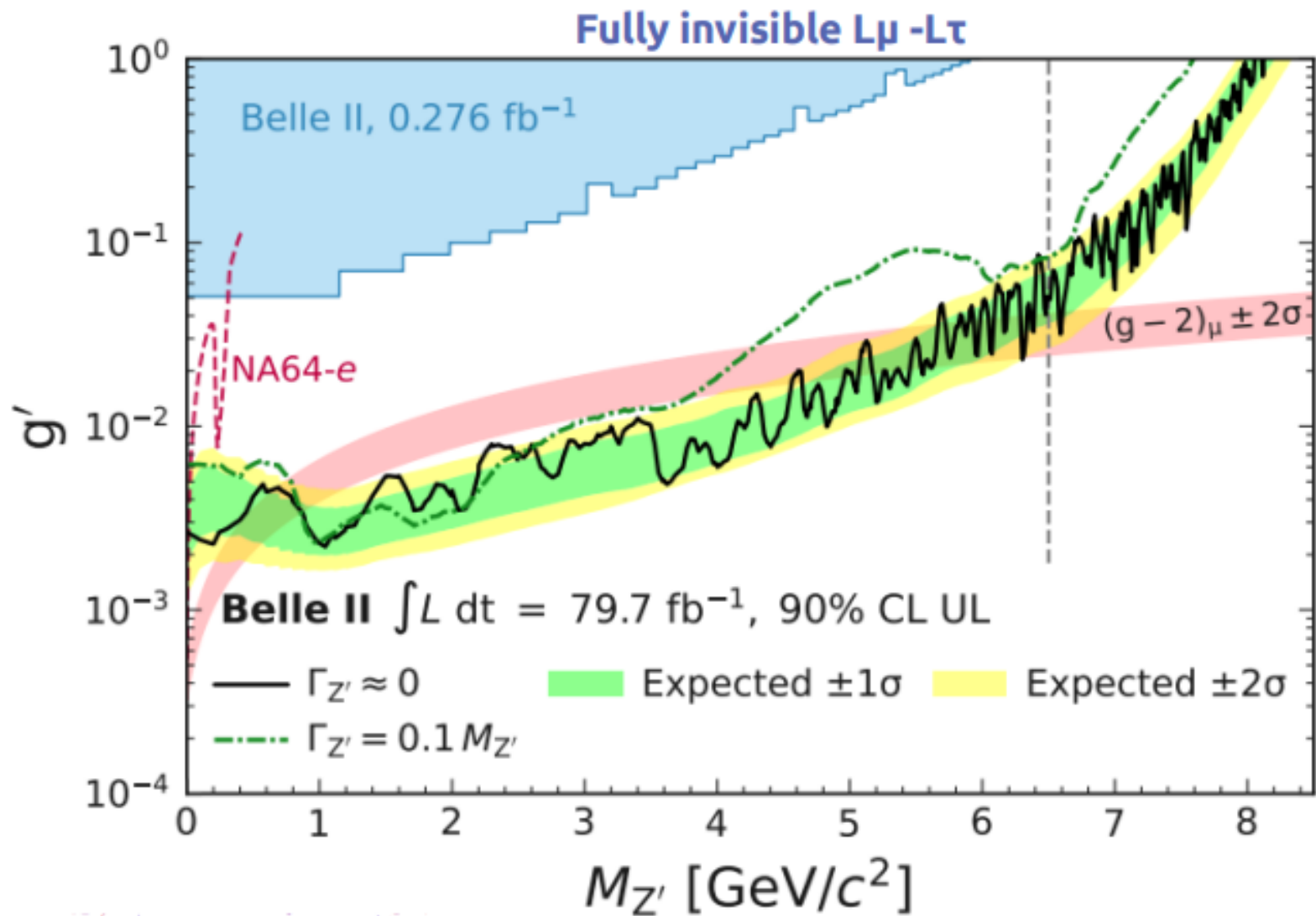
Invisible decay of Z' to dark matter

- Search for narrow peak in the recoil mass of dimuon pairs



Invisible decay of Z' to dark matter

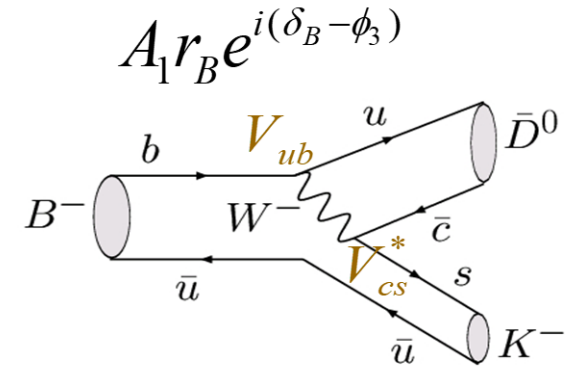
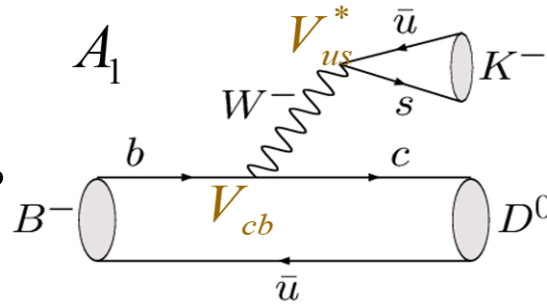
- Limits on Z' coupling g' and mass
- $g_\mu - 2$ region ruled out for masses from 0.8 to 5 GeV



Phys. Rev. Lett. 130, 231801 (2023)

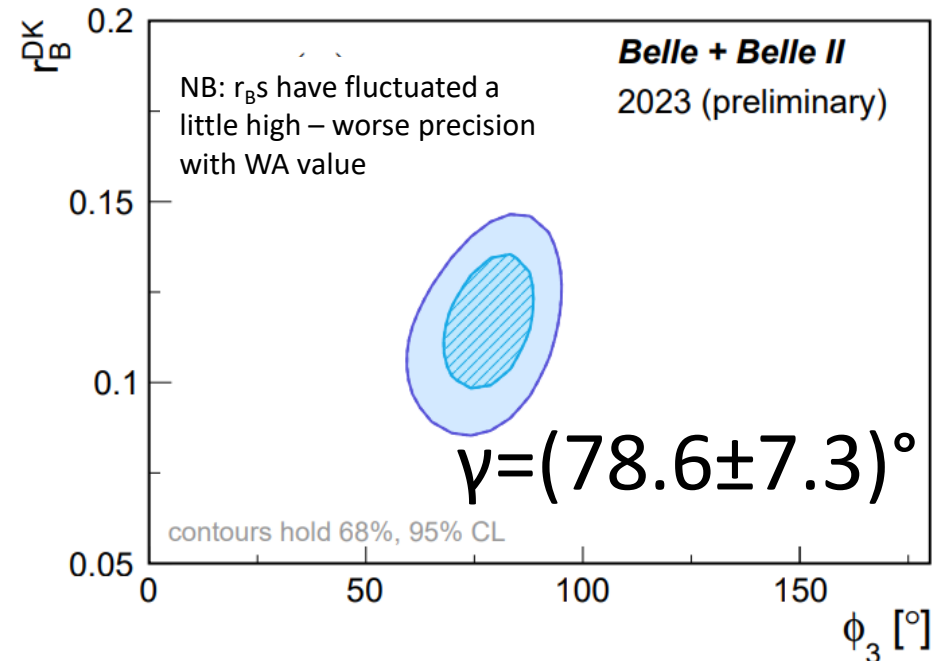
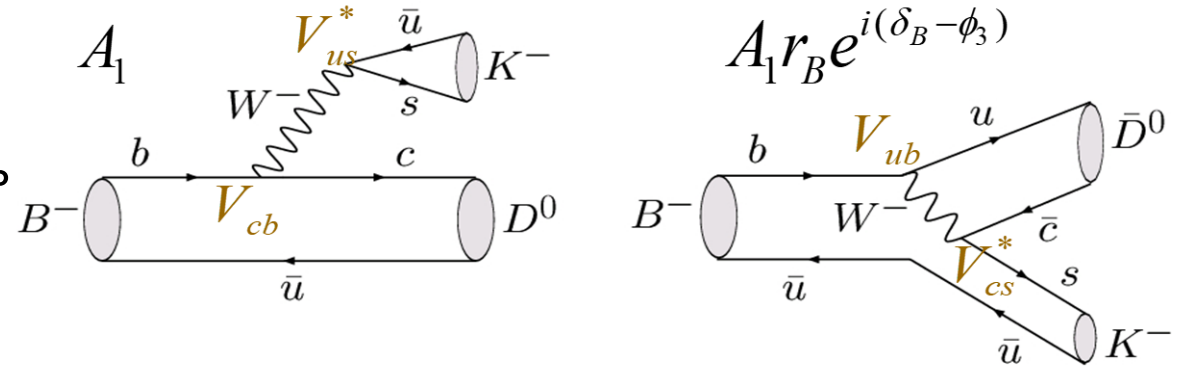
γ/ϕ_3 : power of Belle + Belle II

- Standard candle in the SM
 - Tree-level only + no theory unc.
- LHCb leads the way: $\gamma = (63.8 \pm 3.6)^\circ$
 - [LHCB-CONF-2022-003](#)



γ/ϕ_3 : power of Belle + Belle II

- Standard candle in the SM
 - Tree-level only + no theory unc.
- LHCb leads the way: $\gamma = (63.8 \pm 3.6)^\circ$
 - [LHCb-CONF-2022-003](#)
- Several Belle (711 fb^{-1}) + Belle II measurements (varying sample size) – total $O(1 \text{ ab}^{-1})$
 - $D \rightarrow K_S^0 hh$ - [JHEP 02 \(2022\) 063](#)
 - $D \rightarrow K_S^0 K\pi$ - [accepted by JHEP](#)
 - $D \rightarrow K_S^0 \pi^0, KK$ - [arXiv:2308.05048](#)
 - + Belle-only $D \rightarrow K\pi$ and others
- A few ab^{-1} will give a good cross check of this SM parameter



$B \rightarrow K\pi$ isospin sum rule

- Relates these various penguin modes to give a null test of the SM with O(1%) SM precision – [PRD 59, 113002 \(1999\)](#)

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$

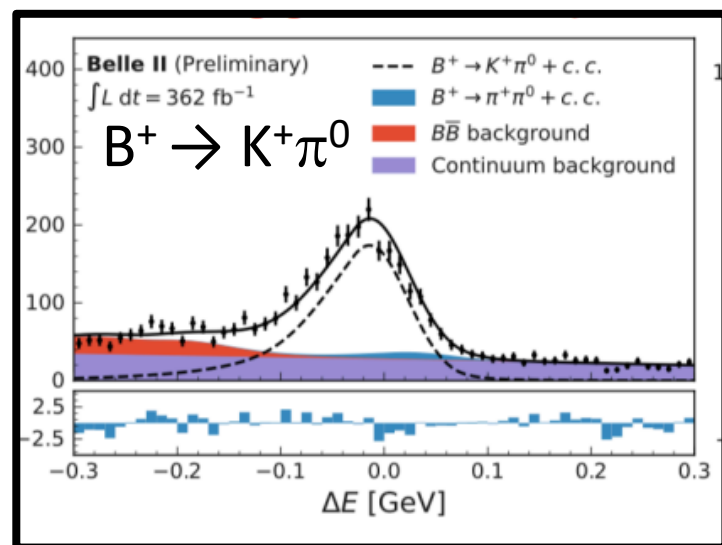
- All inputs measured at Belle II including ‘no vertex’ time-dependent CP asymmetry for $B \rightarrow K^0_S \pi^0$ – 362 fb⁻¹ sample

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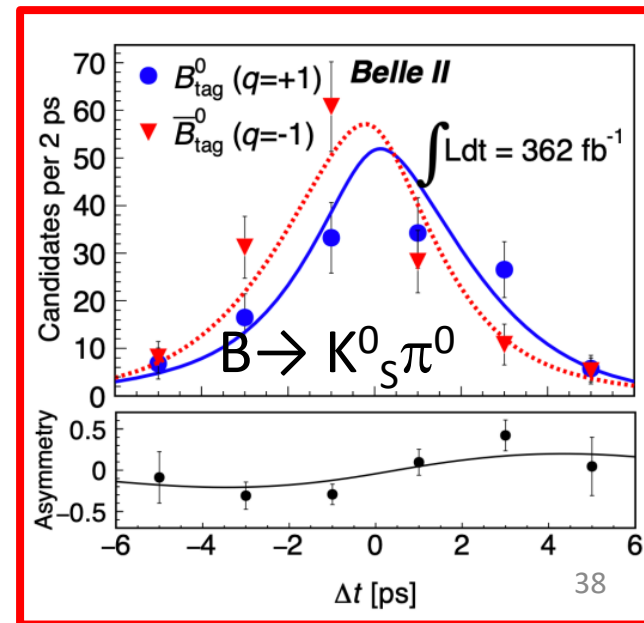


$$B = (14.2 \pm 0.4 \pm 0.9) \times 10^{-6}$$

Large π^0 efficiency syst.

$$A_{K^0} = -0.01 \pm 0.12 \pm 0.05$$

Combination of time-dependent and time-integrated analyses

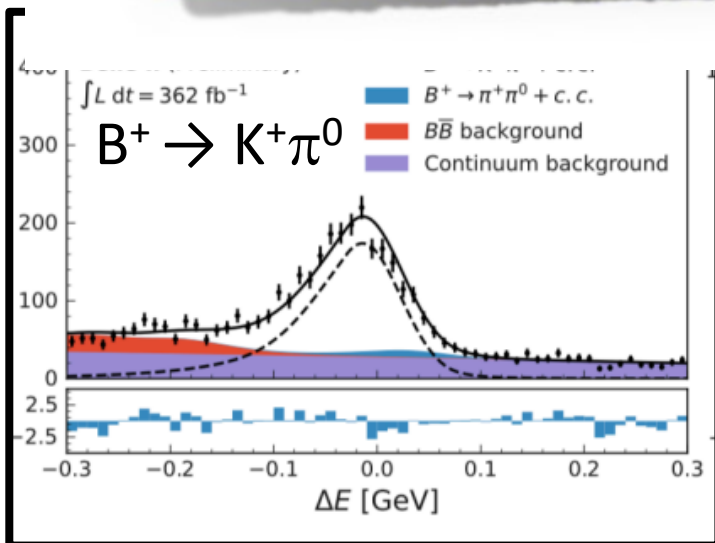


$B \rightarrow K\pi$ isospin sum rule

- Relates these various penguin modes to give a null test of the SM with O(1%) SM precision – [PRD 59, 113002 \(1999\)](#)

$$I_{K\pi} = (-3 \pm 13 \pm 5) \%$$

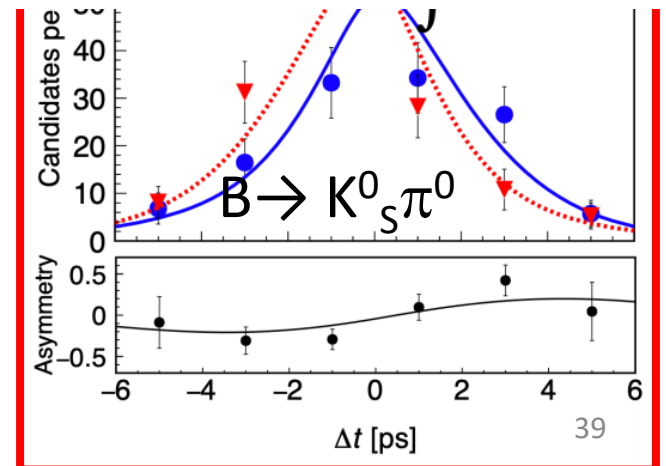
Agrees with SM. Competitive with WA: $(-13 \pm 11) \%$.



Large π^0 efficiency syst.

$A_{K^0} = -0.01 \pm 0.12 \pm 0.05$
 Combination of time-dependent and time-integrated analyses

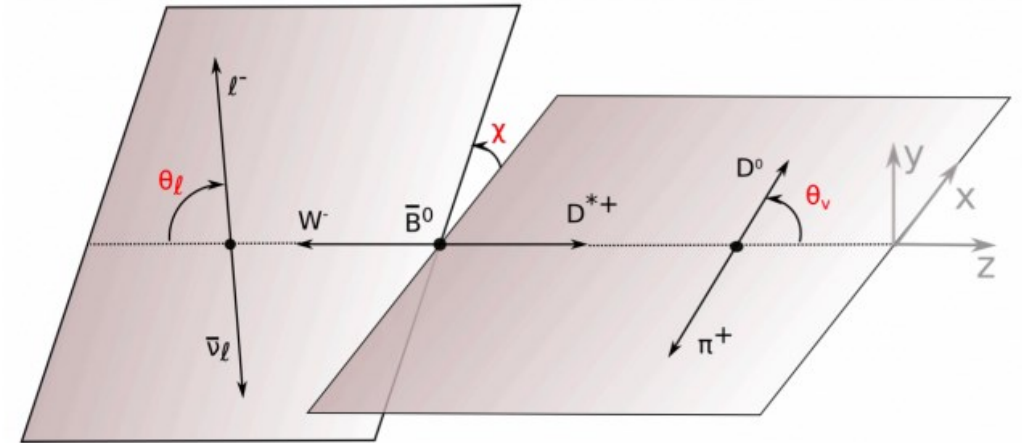
BaBar Symposium



Belle paper in preparation

Angular coefficients in $B \rightarrow D^* l \nu$ and V_{cb}

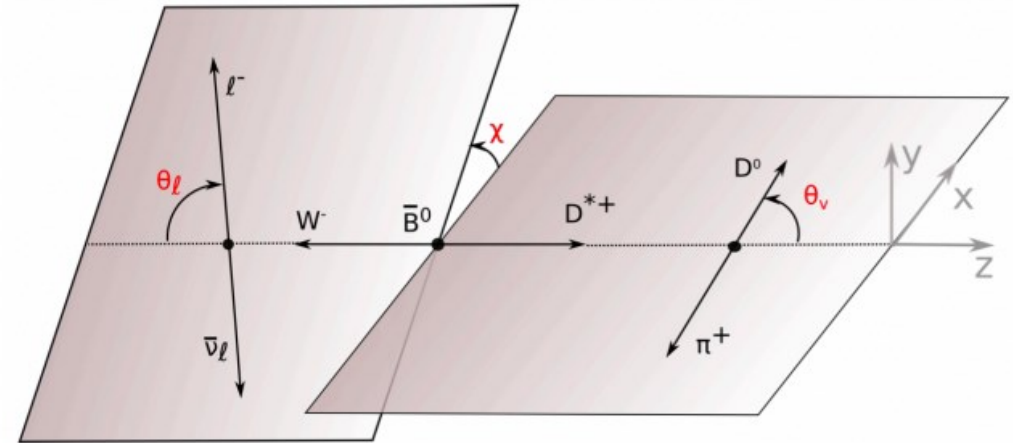
- Measure 4D-differential distribution in terms of decay angles and w
 - overall proportionality to $|V_{cb}|^2$
 - $w \geq 1$ is the hadronic recoil parameter – relates to mom. transfer to the leptonic system



Belle paper in preparation

Angular coefficients in $B \rightarrow D^* l \nu$ and V_{cb}

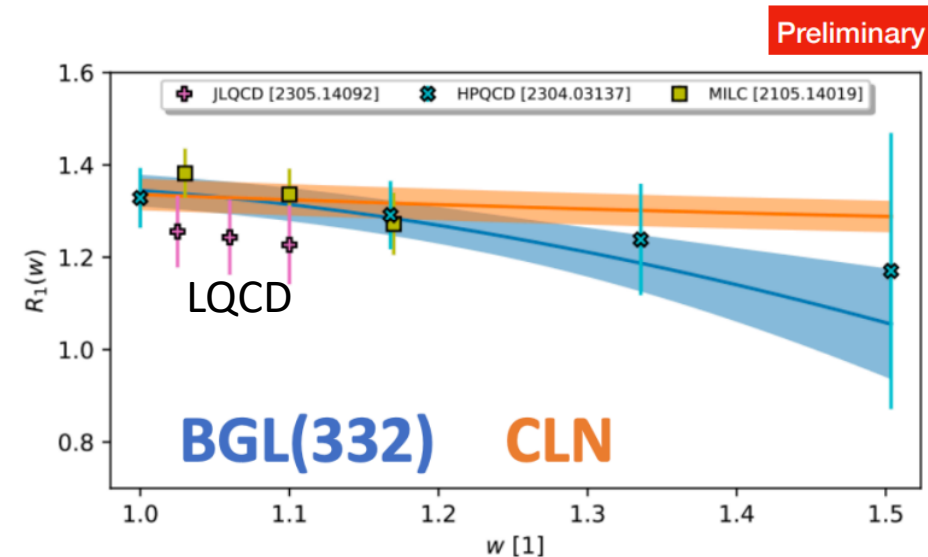
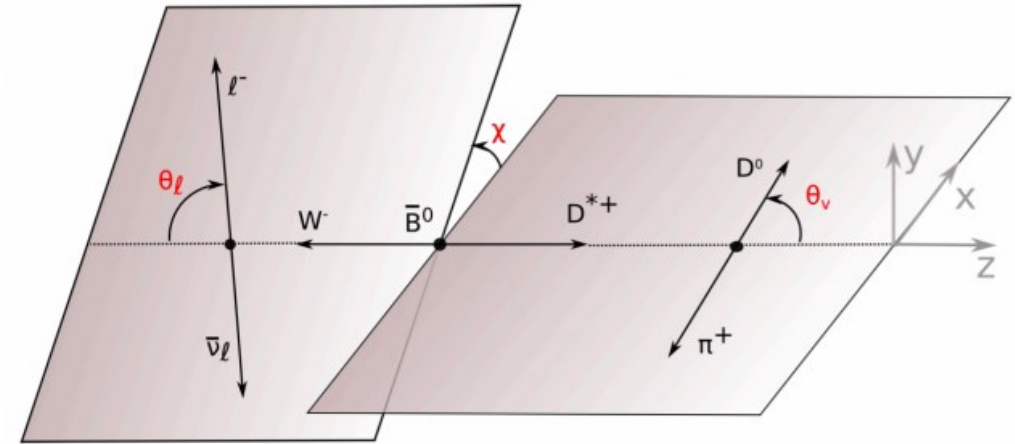
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 - hadronically tagged

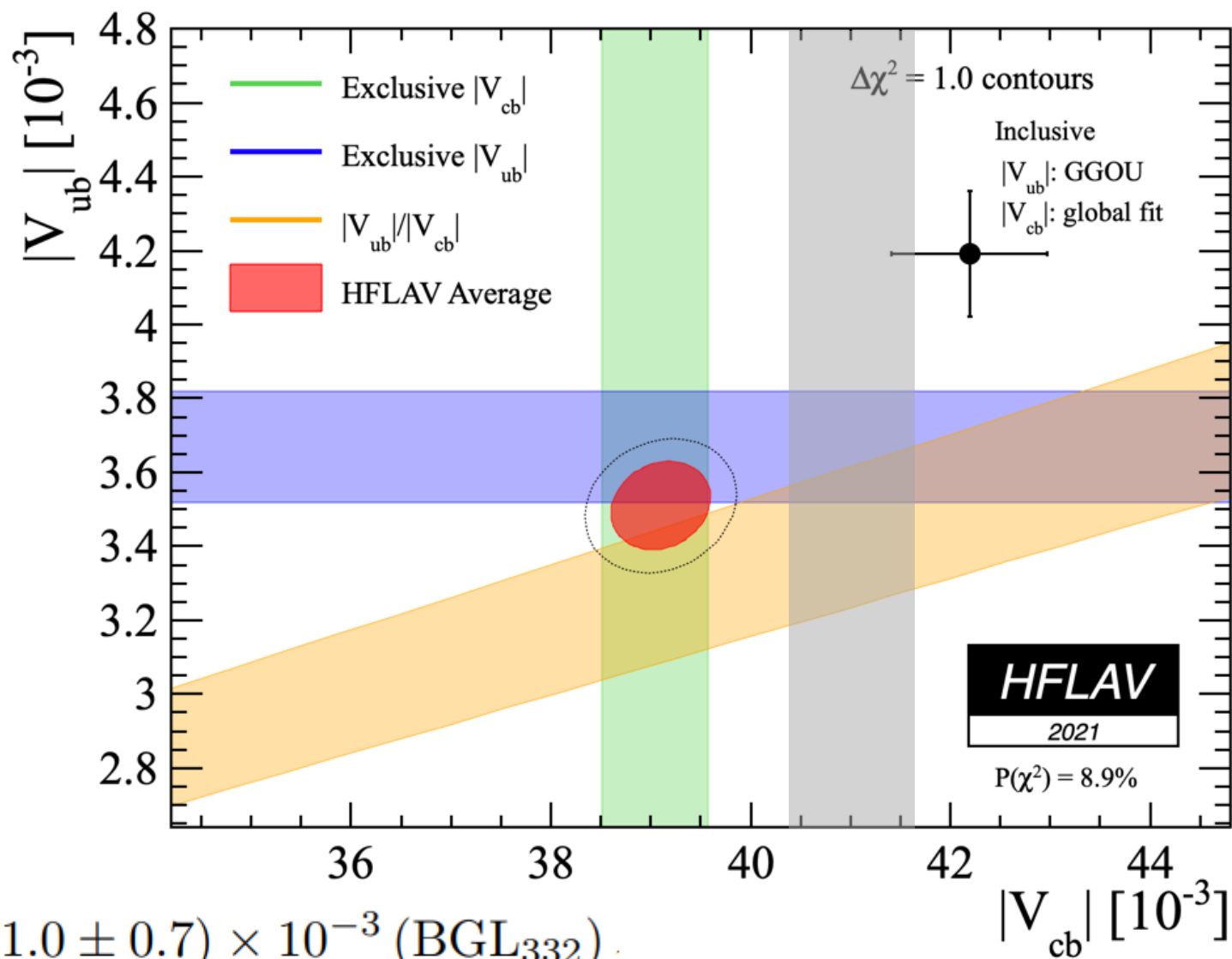


Belle paper in preparation

Angular coefficients in $B \rightarrow D^* l \nu$ and V_{cb}

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- Fit performed to coefficients in different form-factor parameterizations and with LQCD inputs to extract V_{cb} as well as parameters of the form-factor model
 - WA BF also taken externally



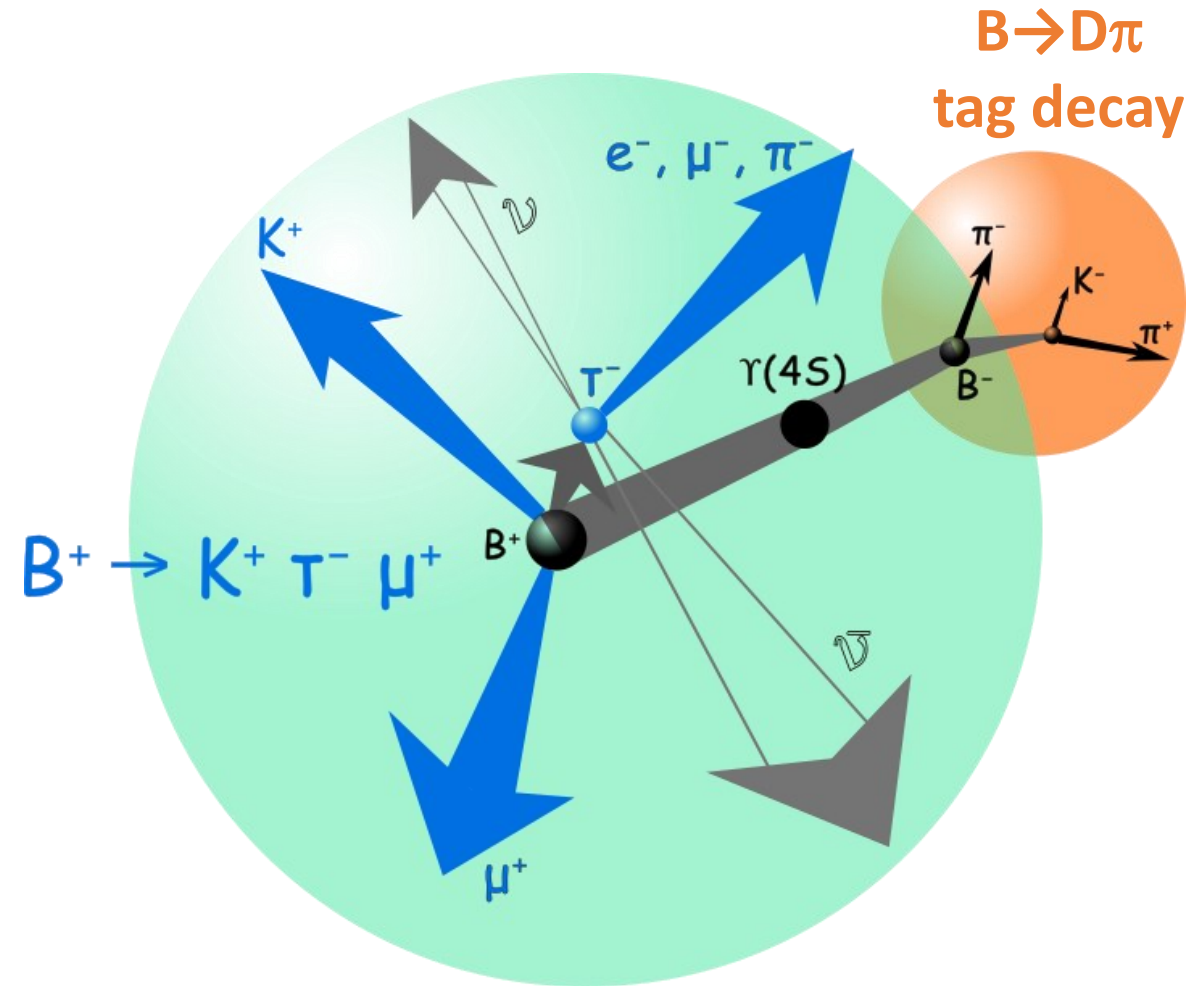


$$|V_{cb}| = (41.0 \pm 0.7) \times 10^{-3} \text{ (BGL}_{332}\text{)}$$

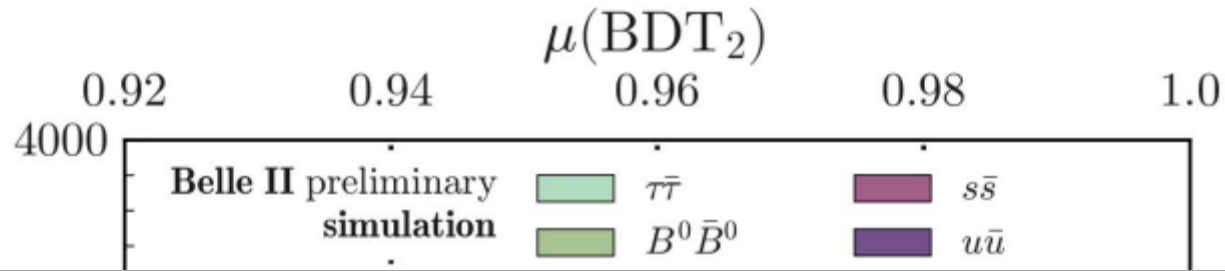
$$|V_{cb}| = (40.9 \pm 0.7) \times 10^{-3} \text{ (CLN)}$$

Hadronic tag

- Full-reconstruction of one B decay in a large number of high BF modes on one side
 - $B \rightarrow D^{(*)0} m\pi^{\pm} n\pi^0$, where $m \geq 1$ $n \geq 0$
 - BaBar Reconstruct other B as signal with missing energy
- Machine learning algorithm used to boost efficiency as much as possible
- Total efficiency $< 1\%$ but a powerful tool
- Requires calibration



$B^+ \rightarrow K^+ \nu \bar{\nu}$: Inclusive signal extraction

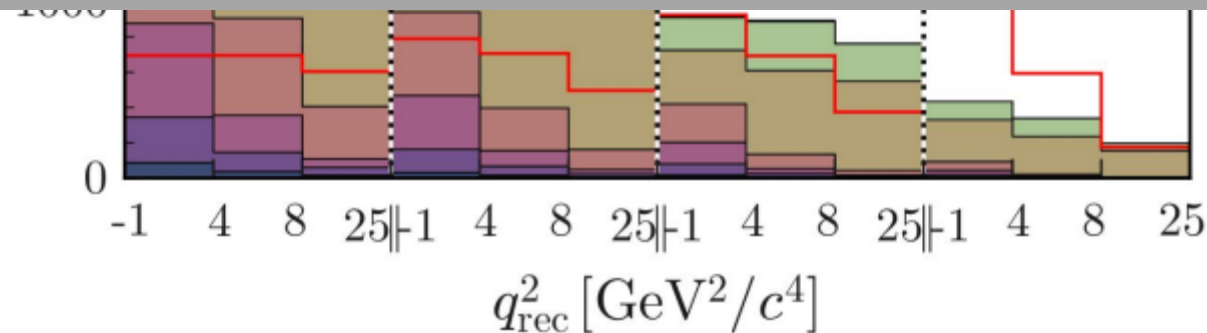


- 1 signal and 7 background templates from simulation

Candidates

Two questions

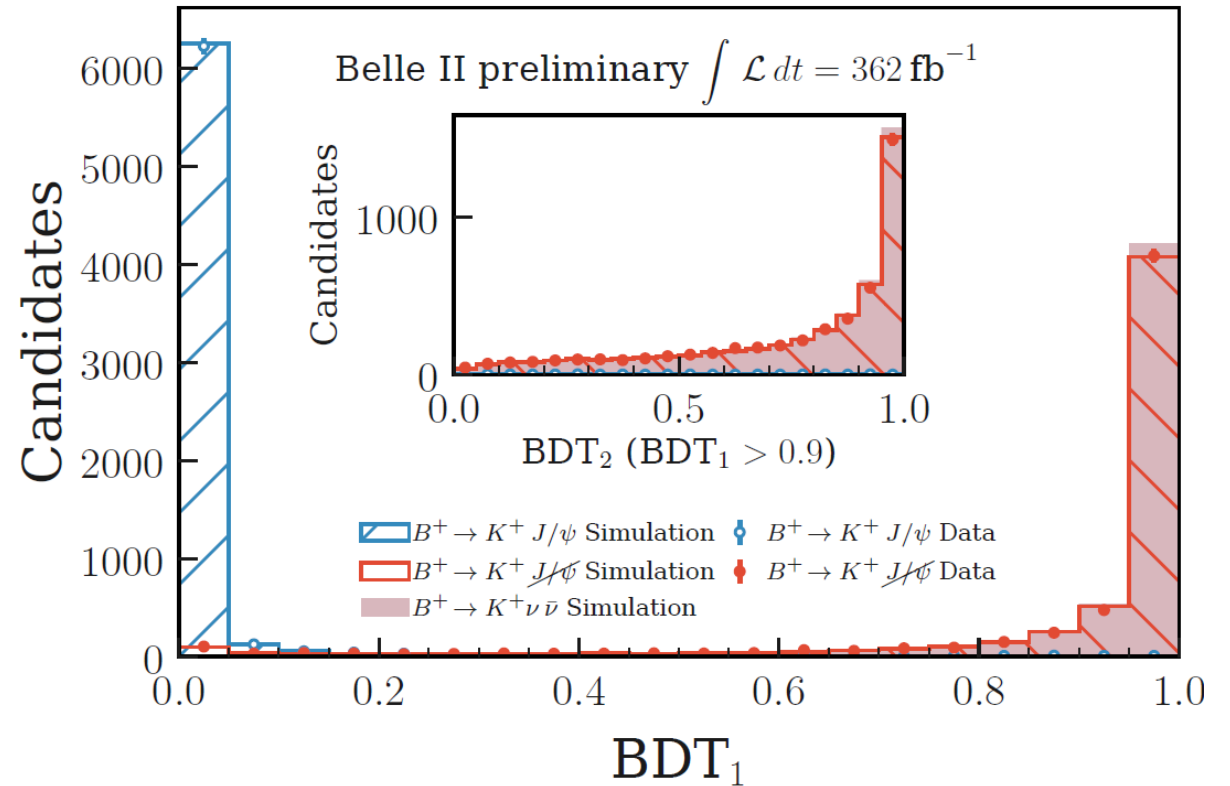
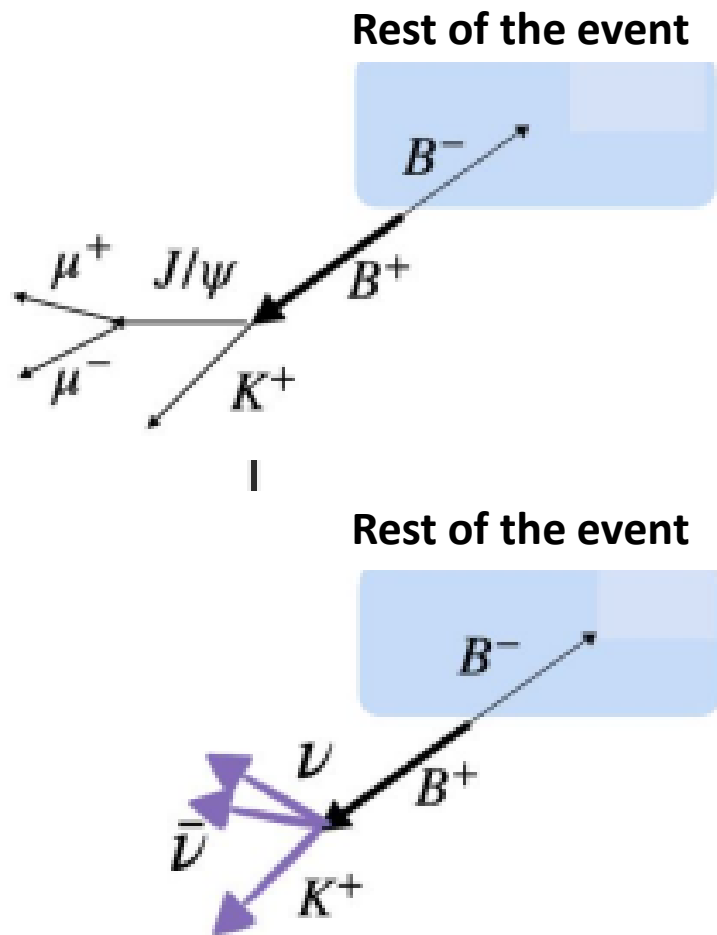
1. Is the signal efficiency, i.e., BDT, well modelled?
2. Is the B background understood?



- Continuum template constrained by off-resonance

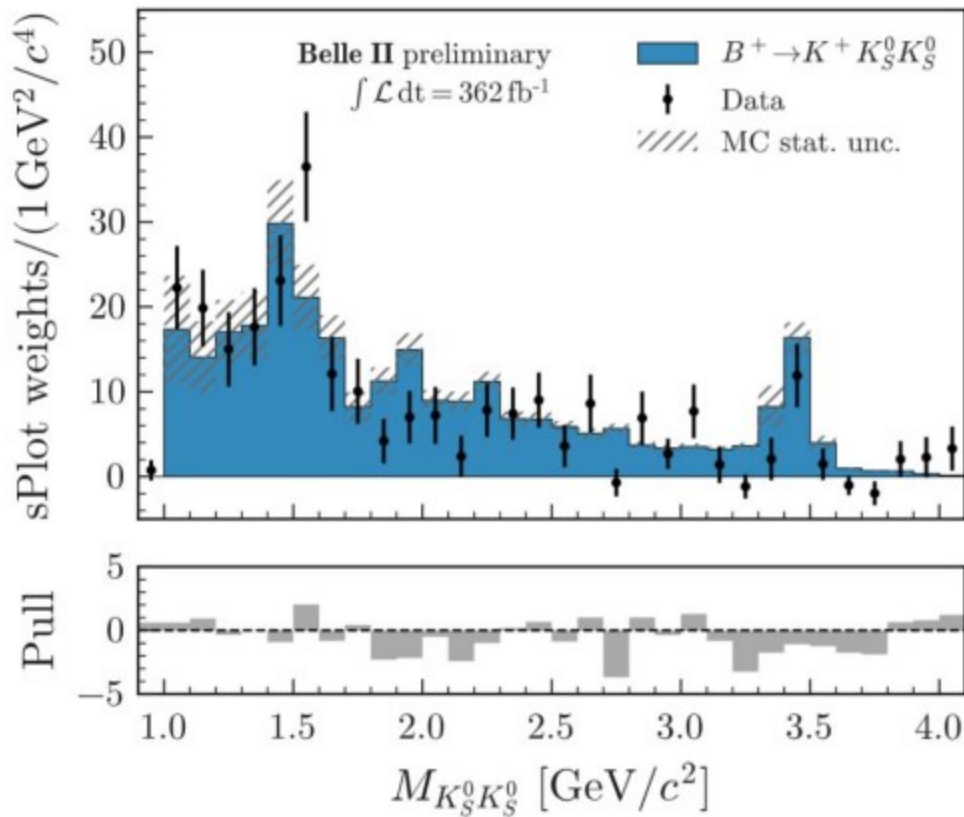
(3 bins in q_{rec}^2) x (4 bins in $\mu(\text{BDT}_2)$)

$B^+ \rightarrow K^+ \nu \bar{\nu}$: Efficiency validation



Ratio between selection on data and simulation for the control sample 1 with 3% uncertainty

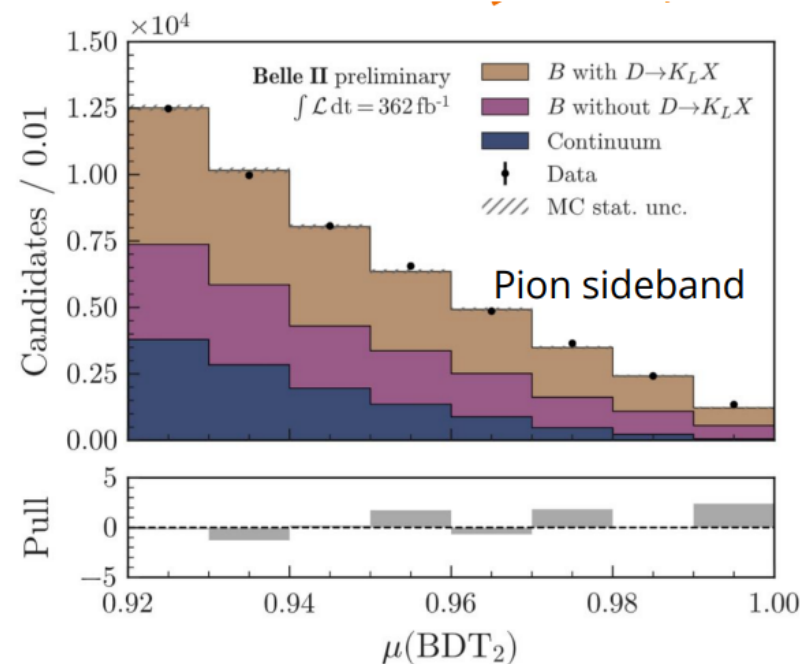
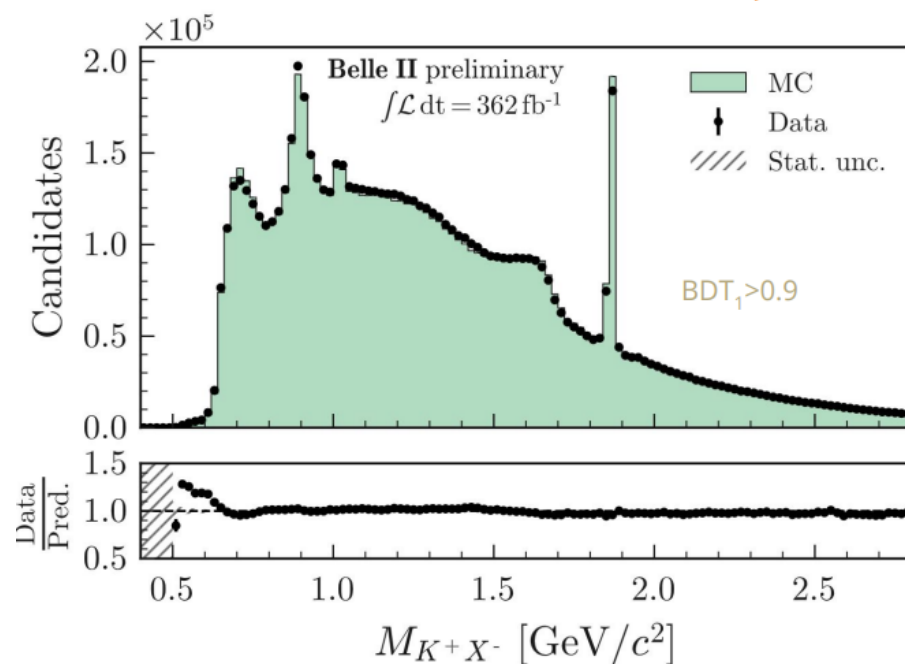
$B^+ \rightarrow K^+ \nu \bar{\nu}$: Background validation example



- An example of a difficult background is charmless $B^+ \rightarrow K^+ K_L^0 K_L^0$, where K_L^0 mesons escape detection
 - has an order of magnitude larger BF than signal
- Dedicated studies $B^+ \rightarrow K^+ K_S^0 K_S^0$ show good modelling
 - generous systematics assigned
- Similar studies for $B^+ \rightarrow K^+ n \bar{n}$, $B^+ \rightarrow K^+ K_L^0 K_S^0$

$$B^+ \rightarrow K^+ \nu \bar{\nu}:$$

>90% background from $B \rightarrow D(K^+ X) l \nu + B \rightarrow D(K_L X) K^+$



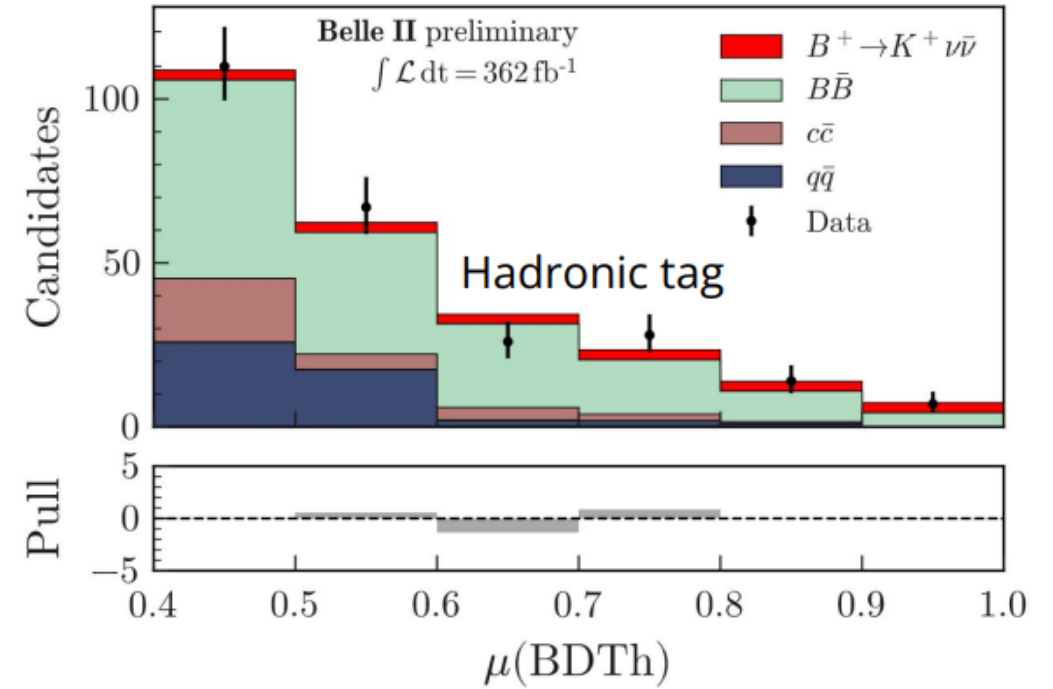
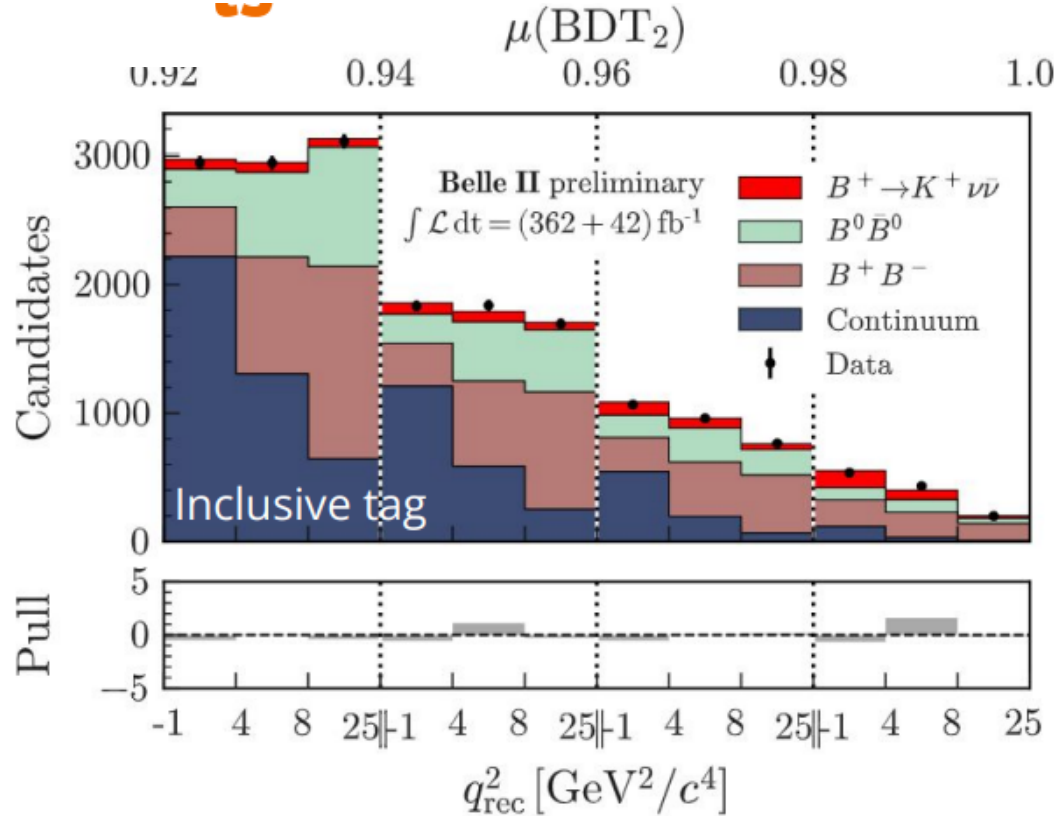
- KX system agrees well between data and MC
- Prompt K^+ production studied using prompt π^+ from $B^+ \rightarrow \pi^+ X$ decays
- Systematic uncertainties on decay branching fractions, enlarged for $D \rightarrow K_L X$ and $B \rightarrow D^{*} l \nu$

$B^+ \rightarrow K^+ \nu \bar{\nu}$: Systematic uncertainties

Source	Correction	Uncertainty type	Uncertainty size	Impact on σ_μ
Normalization of $B\bar{B}$ background	—	Global, 2 NP	50%	0.88
Normalization of continuum background	—	Global, 5 NP	50%	0.10
Leading B -decays branching fractions	—	Shape, 5 NP	$O(1\%)$	0.22
Branching fraction for $B^+ \rightarrow K^+ K_L^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1 NP	20%	0.49
p -wave component for $B^+ \rightarrow K^+ K_S^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1 NP	30%	0.02
Branching fraction for $B \rightarrow D^{(*)}$	—	Shape, 1 NP	50%	0.42
Branching fraction for $B^+ \rightarrow n\bar{n}K^+$	q^2 dependent $O(100\%)$	Shape, 1 NP	100%	0.20
Branching fraction for $D \rightarrow K_L X$	+30%	Shape, 1 NP	10%	0.14
Continuum background modeling, BDT _c	Multivariate $O(10\%)$	Shape, 1 NP	100% of correction	0.01
Integrated luminosity	—	Global, 1 NP	1%	< 0.01
Number of $B\bar{B}$	—	Global, 1 NP	1.5%	0.02
Off-resonance sample normalization	—	Global, 1 NP	5%	0.05
Track finding efficiency	—	Shape, 1 NP	0.3%	0.20
Signal kaon PID	p, θ dependent $O(10 - 100\%)$	Shape, 7 NP	$O(1\%)$	0.07
Photon energy scale	—	Shape, 1 NP	0.5%	0.08
Hadronic energy scale	-10%	Shape, 1 NP	10%	0.36
K_L^0 efficiency in ECL	-17%	Shape, 1 NP	8%	0.21
Signal SM form factors	q^2 dependent $O(1\%)$	Shape, 3 NP	$O(1\%)$	0.02
Global signal efficiency	—	Global, 1 NP	3%	0.03
MC statistics	—	Shape, 156 NP	$O(1\%)$	0.52

$B^+ \rightarrow K^+ \nu \bar{\nu}$: Results

[arXiv:2311.14647 \[hep-ex\]](https://arxiv.org/abs/2311.14647)



$$\text{BF}_{\text{inc}} = (2.8 \pm 0.5(\text{stat}) \pm 0.5(\text{syst})) \times 10^{-5}$$

$$\text{BF}_{\text{had}} = \left(1.1_{-0.8}^{+0.9}(\text{stat})_{-0.5}^{+0.8}(\text{syst}) \right) \times 10^{-5}$$

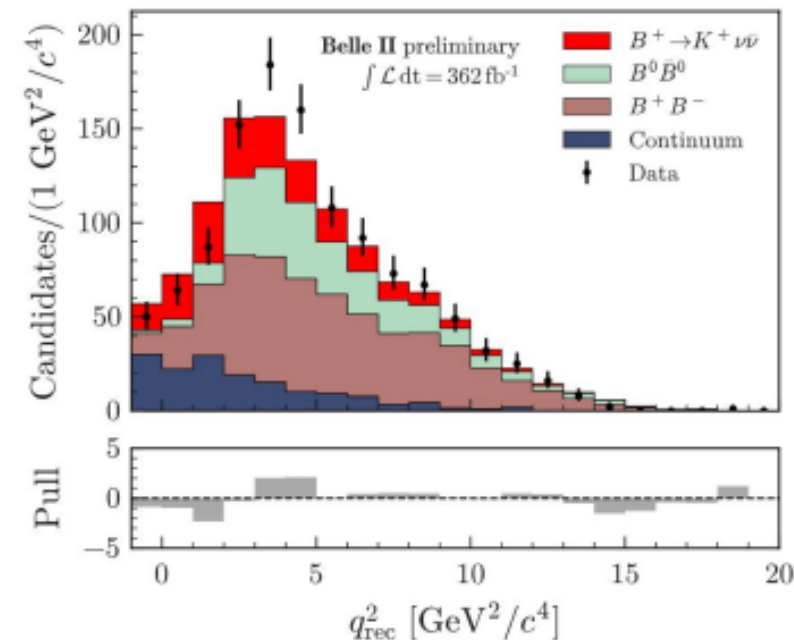
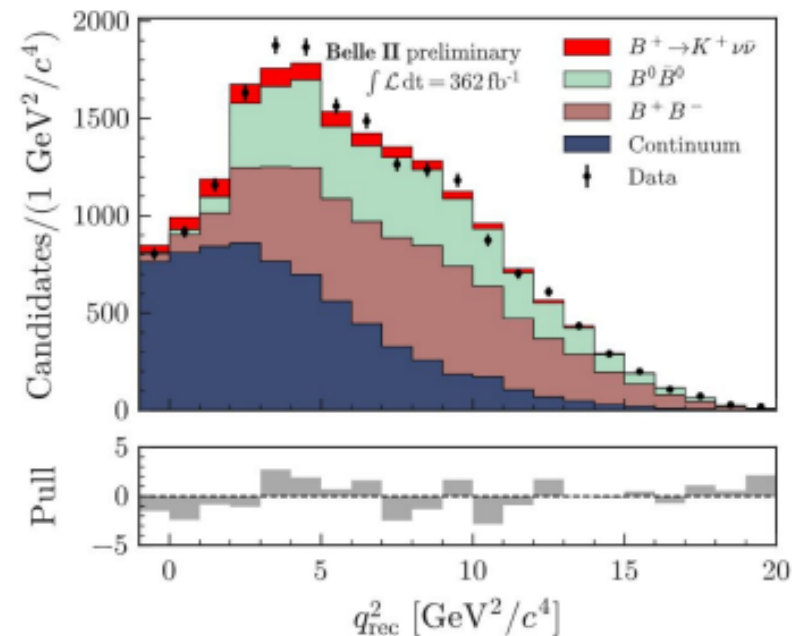
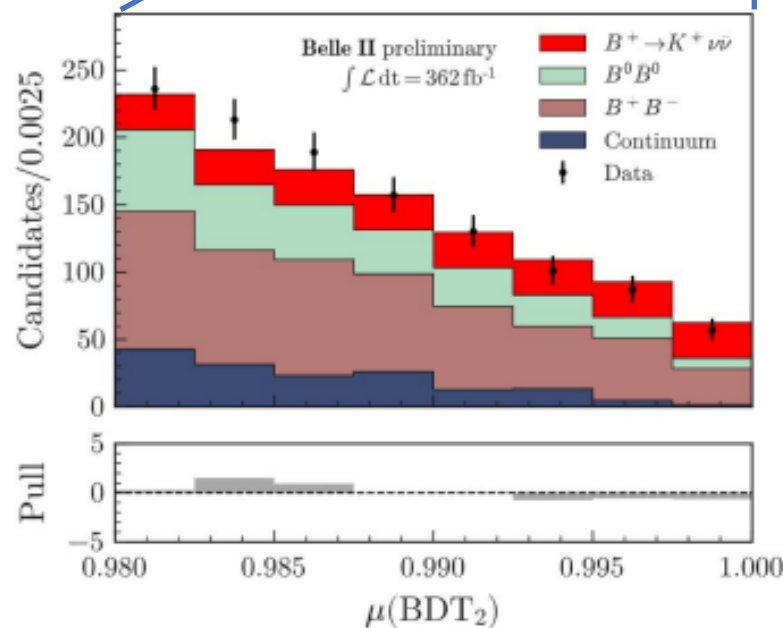
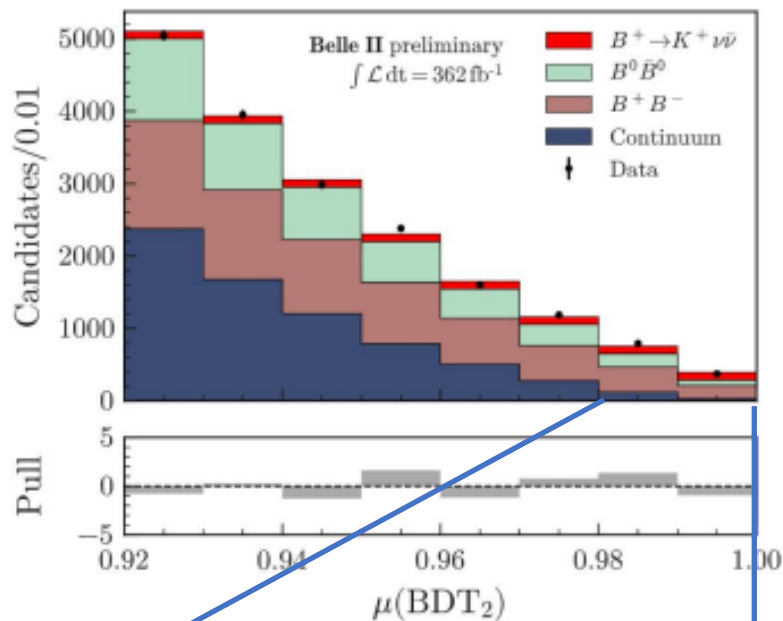
$$\text{BF}_{\text{comb}} = \left(2.4 \pm 0.5(\text{stat})_{-0.4}^{+0.5}(\text{syst}) \right) \times 10^{-5}$$

Post-fit distributions

Upper: full fit region

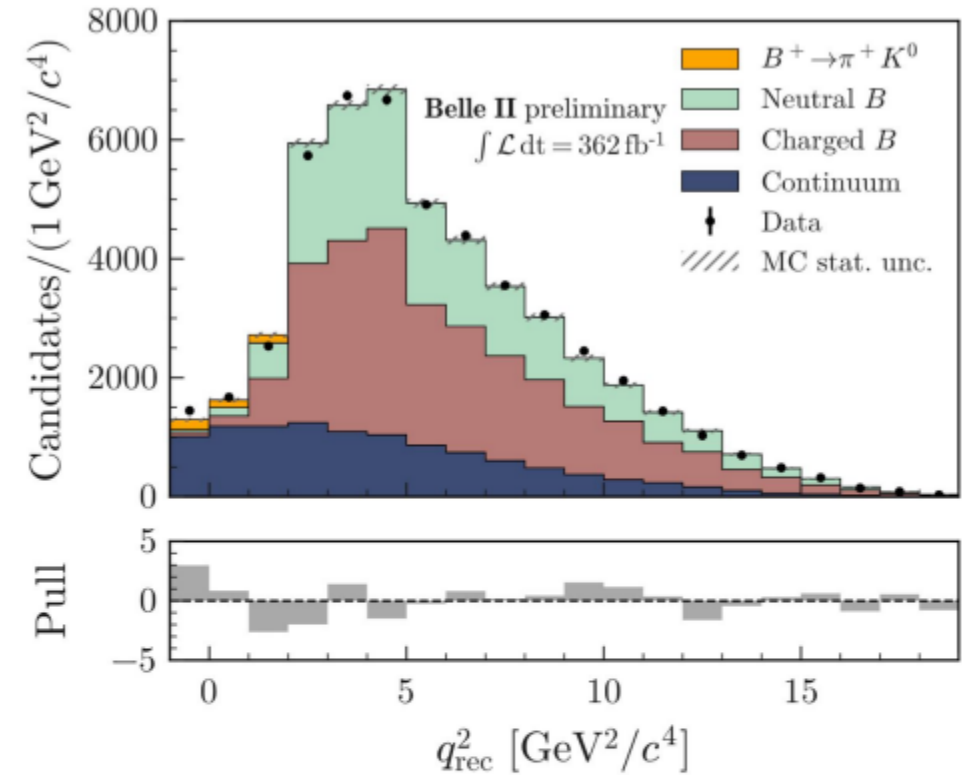
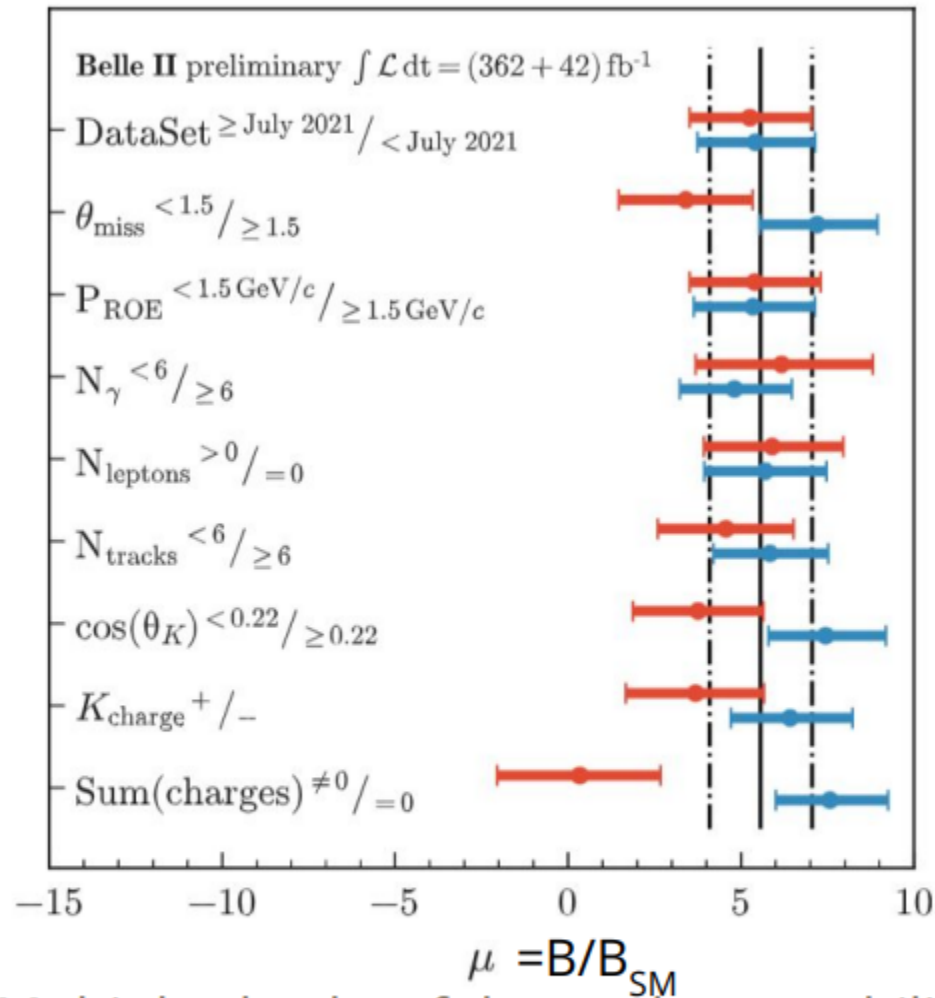
Lower: most sensitive region

[arXiv:2311.14647 \[hep-ex\]](https://arxiv.org/abs/2311.14647)



Cross checks

arXiv:2311.14647 [hep-ex]



$$B(B^+ \rightarrow \pi^+ K^0) = (2.5 \pm 0.5) \times 10^{-5}$$

$$\text{PDG: } (2.38 \pm 0.08) \times 10^{-5}$$

- Multiple checks of the analyses stability, including tests dividing data into approximately equal sub-samples. Reported here as measured branching fraction divided by SM expectation, $\mu = B/B_{\text{SM}}$.
- Control measurement of $B^+ \rightarrow \pi^+ K^0$ decay