

Review of bottomonium decay results at Belle

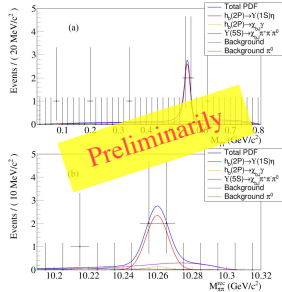
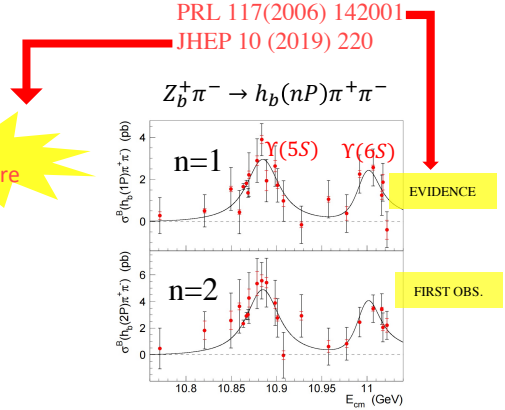
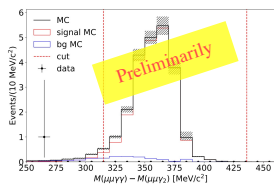
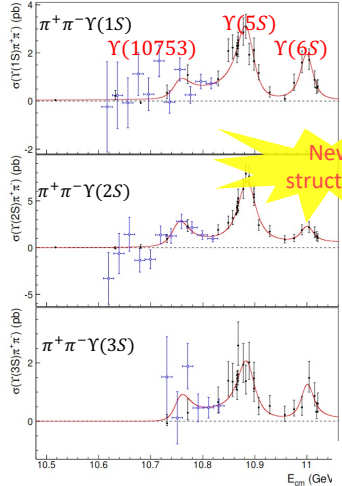
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Bottomonium at Belle

Alternative explanation is that the transitions $\Upsilon(nS) \rightarrow \Upsilon(ms)$ proceed via **exotic admixture**

Transition	Partial width (keV)
$\Upsilon(4S) \rightarrow$	
$\Upsilon(1S) \pi^+ \pi^-$	1.7 ± 0.2
$\Upsilon(1S) \eta$	4.0 ± 0.8
$\Upsilon(2S) \pi^+ \pi^-$	1.8 ± 0.3
$h_b(1P) \eta$	45 ± 7
$\Upsilon(5S) \rightarrow$	
$\Upsilon(1S) \pi^+ \pi^-$	238 ± 41
$\Upsilon(1S) \eta$	39 ± 11
$\Upsilon(1S) K^+ K^-$	33 ± 11
$\Upsilon(2S) \pi^+ \pi^-$	428 ± 83
$\Upsilon(2S) \eta$	204 ± 44
$\Upsilon(3S) \pi^+ \pi^-$	153 ± 31
$\chi_{b1}(1P) \omega$	84 ± 20
$\chi_{b1}(1P) (\pi^+ \pi^- \pi^0)_{\text{non-}\omega}$	28 ± 11
$\chi_{b2}(1P) \omega$	32 ± 15
$\chi_{b2}(1P) (\pi^+ \pi^- \pi^0)_{\text{non-}\omega}$	33 ± 20
$\Upsilon_J(1D) \pi^+ \pi^-$	~ 60
$\Upsilon_J(1D) \eta$	150 ± 48
$Z_b(10610) \pm \pi^\mp$	2070 ± 440
$Z_b(10650) \pm \pi^\mp$	1200 ± 300
$\Upsilon(6S) \rightarrow$	
$\Upsilon(1S) \pi^+ \pi^-$	137 ± 32
$\Upsilon(2S) \pi^+ \pi^-$	183 ± 43
$\Upsilon(3S) \pi^+ \pi^-$	77 ± 28
$Z_b(10610, 10650) \pm \pi^\mp$	$1300 - 6600$



Decay	BR	Model	Quality	Best fit
$\Upsilon(1S) \rightarrow \pi^+ \pi^-$	0.21 ± 0.02	Quark	Good	0.21
$\Upsilon(1S) \rightarrow \eta$	0.40 ± 0.08	Quark	Good	0.40
$\Upsilon(1S) \rightarrow K^+ K^-$	0.33 ± 0.11	Quark	Good	0.33
$\Upsilon(2S) \rightarrow \pi^+ \pi^-$	0.43 ± 0.08	Quark	Good	0.43
$\Upsilon(2S) \rightarrow \eta$	0.20 ± 0.04	Quark	Good	0.20
$\Upsilon(2S) \rightarrow K^+ K^-$	0.33 ± 0.15	Quark	Good	0.33
$\Upsilon(3S) \rightarrow \pi^+ \pi^-$	0.15 ± 0.03	Quark	Good	0.15
$\Upsilon(3S) \rightarrow \eta$	0.20 ± 0.04	Quark	Good	0.20
$\Upsilon(3S) \rightarrow K^+ K^-$	0.18 ± 0.04	Quark	Good	0.18
$\Upsilon(4S) \rightarrow \pi^+ \pi^-$	0.17 ± 0.02	Quark	Good	0.17
$\Upsilon(4S) \rightarrow \eta$	0.40 ± 0.08	Quark	Good	0.40
$\Upsilon(4S) \rightarrow K^+ K^-$	0.33 ± 0.11	Quark	Good	0.33
$\Upsilon(5S) \rightarrow \pi^+ \pi^-$	0.24 ± 0.04	Quark	Good	0.24
$\Upsilon(5S) \rightarrow \eta$	0.39 ± 0.11	Quark	Good	0.39
$\Upsilon(5S) \rightarrow K^+ K^-$	0.33 ± 0.11	Quark	Good	0.33
$\Upsilon(5S) \rightarrow \pi^+ \pi^- \pi^0$	0.28 ± 0.11	Quark	Good	0.28
$\Upsilon(5S) \rightarrow \eta \pi^+ \pi^-$	0.32 ± 0.15	Quark	Good	0.32
$\Upsilon(5S) \rightarrow \omega \pi^+ \pi^-$	0.33 ± 0.20	Quark	Good	0.33
$\Upsilon(5S) \rightarrow \eta \pi^+ \pi^- \pi^0$	~ 60	Quark	Good	60
$\Upsilon(5S) \rightarrow \eta \pi^+ \pi^- \pi^0$	150 ± 48	Quark	Good	150
$Z_b(10610) \rightarrow \pi^+ \pi^-$	2070 ± 440	Quark	Good	2070
$Z_b(10650) \rightarrow \pi^+ \pi^-$	1200 ± 300	Quark	Good	1200

And many others

Selected Topics



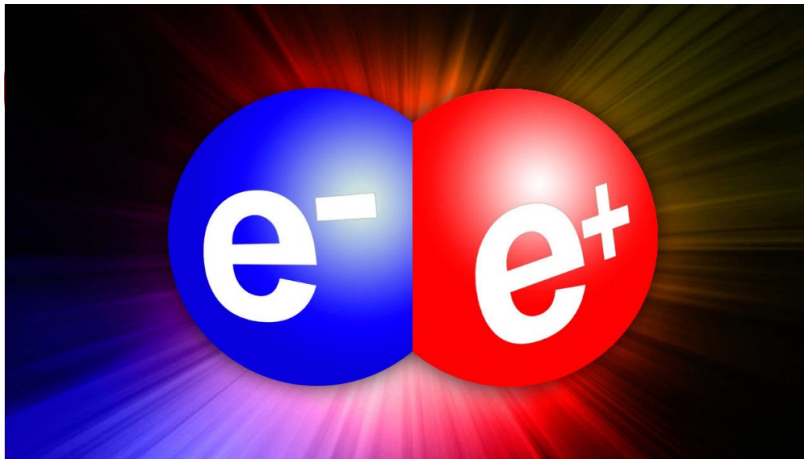
* Search for $h_b(2P) \rightarrow \gamma \chi_{bJ}(1P)$ [NEW];

* Evidence for $h_b(2P) \rightarrow \Upsilon(1S)\eta$ and search for $h_b(1P, 2P) \rightarrow \Upsilon(1S)\pi^0$ [NEW];

* The study of $\Upsilon(2S) \rightarrow D_s^{(*)+} + D_{sJ}^- + \text{c. c.}$ [PRD 108, 112015 (2023)].

TOPIC ONE

Search for $h_b(2P) \rightarrow \gamma \chi_{bJ}(1P)$



Motivation



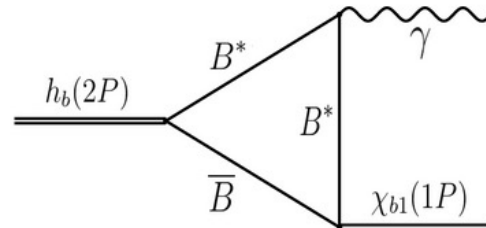
☞ The production of $b\bar{b}$ spin singlets is generally rare in e^+e^- collisions because it requires the spin flip of a heavy quark in a hadronic or radiative transition.

☞ The $h_b(2P)$ is produced via the $\Upsilon(10860) \rightarrow h_b(2P)\pi^+\pi^-$ transition with a surprisingly large rate^[1].

☞ $h_b(2P) \rightarrow \chi_{b1}\gamma$ decay is suppressed due to heavy quark spin symmetry.

Relativized Quark Model (RQM) predicts $\mathcal{B}[h_b(2P) \rightarrow \gamma\chi_{bJ}(1P)] = 10^{-6} - 10^{-5}$ ^[2].

☞ There could be enhancement due to hadron admixture in $h_b(2P)$. The coupled-channel model predicts $\mathcal{B}[h_b(2P) \rightarrow \gamma\chi_{bJ}(1P)] = 10^{-2} - 10^{-1}$ ^{[3][4]}.



<https://arxiv.org/abs/physics/9711021>

[1] PRL **108**, 032001 (2012), Belle collaboration.

[2] PRD **32**, 189 (1985), Stephen Godfrey et al.

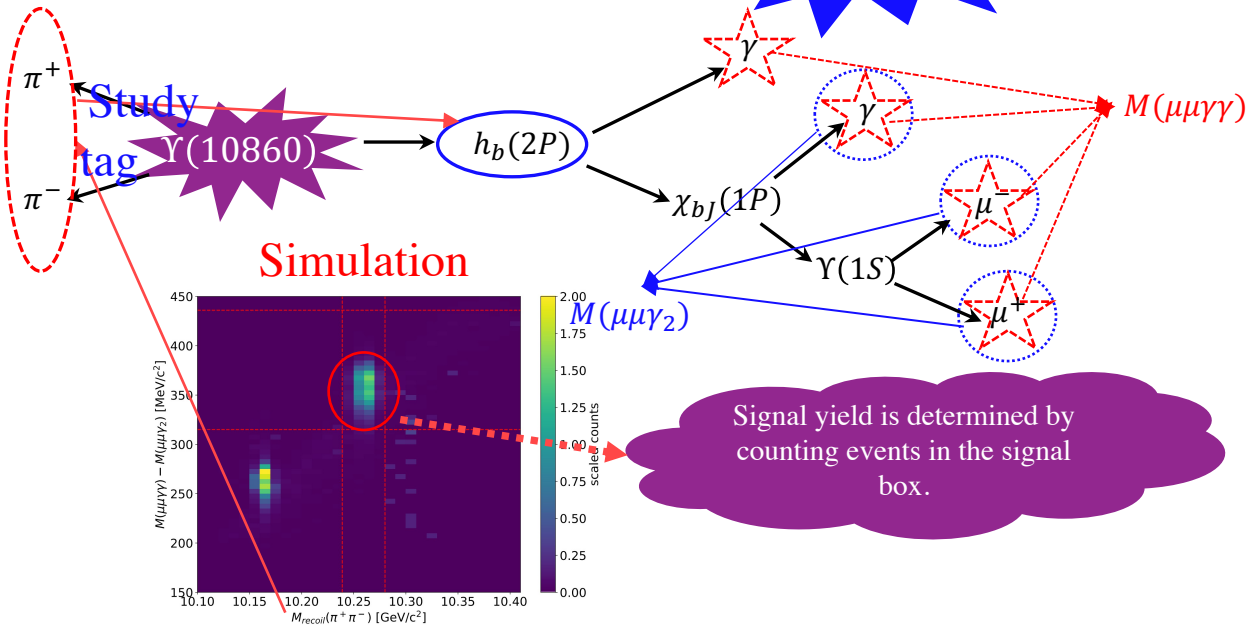
[3] PLB **760**, 417 (2016), Feng-Kun Guo et al.

[4] <https://arxiv.org/abs/physics/9711021>

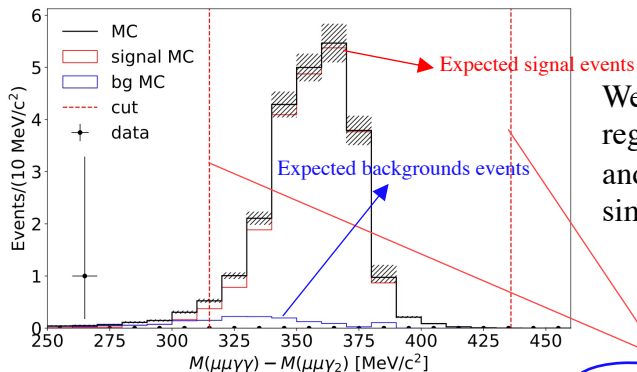
Search for $h_b(2P) \rightarrow \gamma\chi_{bJ}(1P)$



☞ Data samples:
 $\Upsilon(10860)$: 121.4 fb^{-1}



The Results for $h_b(2P) \rightarrow \gamma\chi_{bJ}(1P)$



We count the number of events in the signal region. No events are found in the signal box and the background count is $1.06^{+0.29}_{-0.20}$ on the simulated data.

Signal region

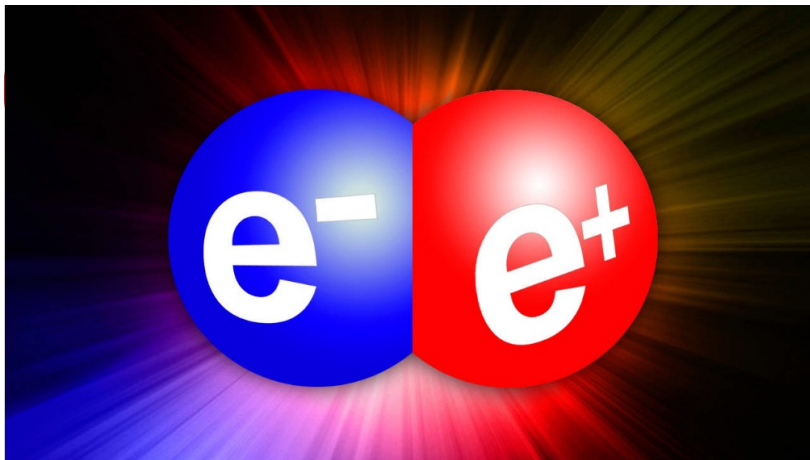
We set upper limits below :

Channel	B
$h_b(2P) \rightarrow \gamma\chi_{b2}(1P)$	$< 1.2 \times 10^{-2}$
$h_b(2P) \rightarrow \gamma\chi_{b1}(1P)$	$< 5.4 \times 10^{-3}$
$h_b(2P) \rightarrow \gamma\chi_{b0}(1P)$	$< 2.7 \times 10^{-1}$

The results is consistent with the RQM expectations and excludes the results from the coupled-channel model.

TOPIC TWO

Evidence for $h_b(2P) \rightarrow \Upsilon(1S)\eta$ and
search for $h_b(1P, 2P) \rightarrow \Upsilon(1S)\pi^0$



Motivation



- ☞ $h_b(2P) \rightarrow \Upsilon(1S)\eta$ decay is suppressed due to heavy quark spin symmetry.
- ☞ Hadronic transitions between heavy quarkonium states can be mostly described with the QCD multiple expansion model (*QCME*)^[1], including $h_b(1P, 2P)$ are expected to have decay properties similar to $\chi_b(1P, 2P)$ ^[2].
- ☞ Theoretical prediction: the $R_{h_b}(R_{\chi_{b1}})$ is the ratio of the annihilation rates for the $h_b(1P, 2P)(\chi_b(1P, 2P))$, the predicted value of $R_{h_b}/R_{\chi_{b1}}=1$ ^[3].
- ☞ Based on recent results, the $R_{h_b}/R_{\chi_{b1}}$ is 0.24 with 1.5σ discrepancy from unity and the discrepancy would further increase if the rate of $h_b(2P) \rightarrow \Upsilon(1S)\eta$ is as large as 10%.

[1] NPB **154**, 365 (1979) M. B. Voloshin.

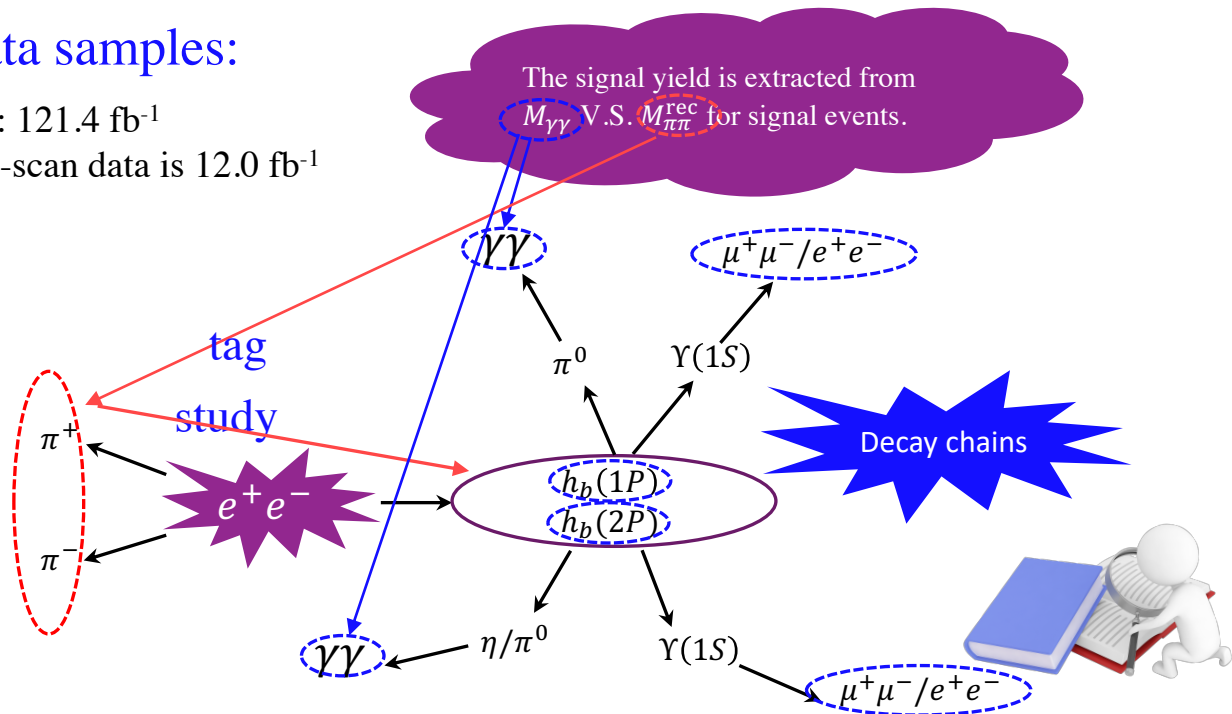
[2] PRD **66**, 014012 (2002) Stephen Godfrey.

[3] PRD **86**, 094013 (2012) Xin Li et al.

The study of $h_b(2P) \rightarrow \Upsilon(1S)\eta$ and $h_b(1P, 2P) \rightarrow \Upsilon(1S)\pi^0$

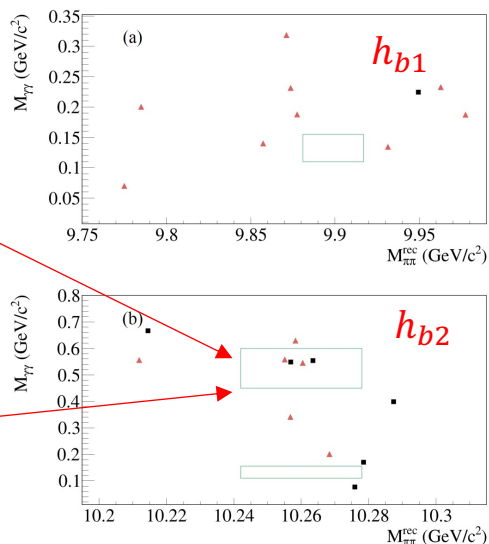
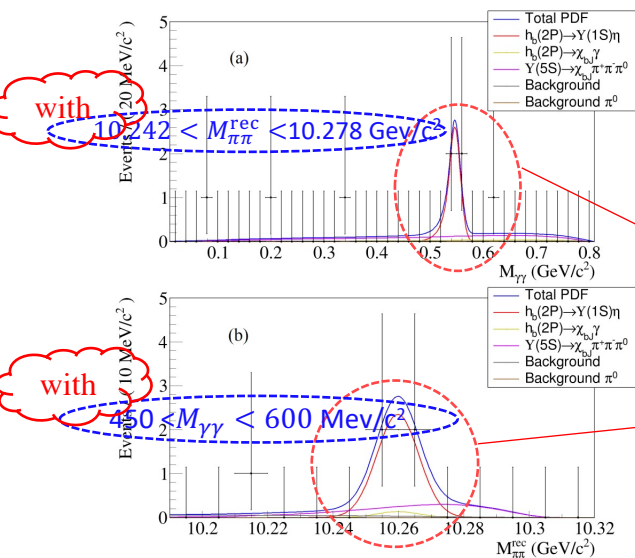
Data samples:

- $\Upsilon(5S) : 121.4 \text{ fb}^{-1}$
- Energy-scan data is 12.0 fb^{-1}



The Results of $h_b(2P) \rightarrow \Upsilon(1S)\eta$ and $h_b(1P, 2P) \rightarrow \Upsilon(1S)\pi^0$

- $\mathcal{B}[h_b(2P) \rightarrow \Upsilon(1S)\eta] = (7.1^{+3.7}_{-3.2} \pm 0.8) \times 10^{-3} \quad 3.5\sigma$
- $\mathcal{B}[h_b(2P) \rightarrow \Upsilon(1S)\pi^0] < 1.8 \times 10^{-3}$ at 90% confidence level.
- $\mathcal{B}[h_b(1P) \rightarrow \Upsilon(1S)\pi^0] < 1.8 \times 10^{-3}$ at 90% confidence level.



The hindered M1 decays between P-wave bottomonium state $h_b(2P) \rightarrow \chi_{bJ}(1P)\gamma$ with $J = 0, 1, 2$.

Results discussion



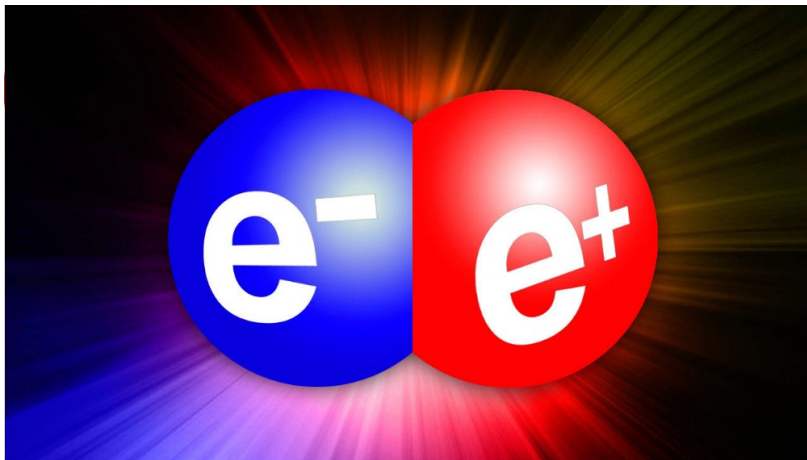
We see evidence of the $h_b(2P) \rightarrow \Upsilon(1S)\eta$ transition with significance of the signal is 3.5σ .

The obtained $\mathcal{B}[h_b(2P) \rightarrow \Upsilon(1S)\eta] = (7.1_{-3.2}^{+3.7} \pm 0.8) \times 10^{-3}$ noticeably differs from the expectation of 10% and the updated value of $R_{h_b}/R_{\chi_{b1}}$ is around 0.23.

We do not observe any signal for the isospin violating decays $h_b(1P, 2P) \rightarrow \Upsilon(1S)\pi^0$ and the upper limits are found to be $\mathcal{B}[h_b(1P) \rightarrow \Upsilon(1S)\pi^0] = 1.8 \times 10^{-3}$ and $\mathcal{B}[h_b(2P) \rightarrow \Upsilon(1S)\pi^0] = 1.8 \times 10^{-3}$.

TOPIC THREE

The study of $\Upsilon(2S) \rightarrow D_S^{(*)+} D_{SJ}^- + c.c.$

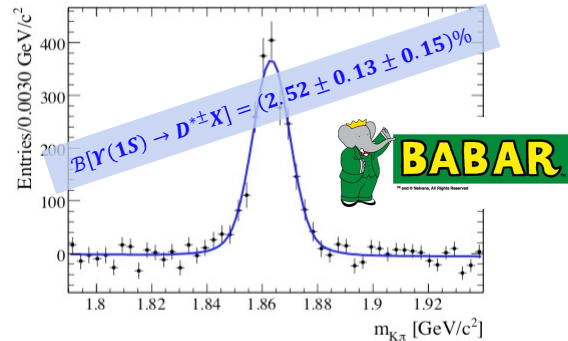
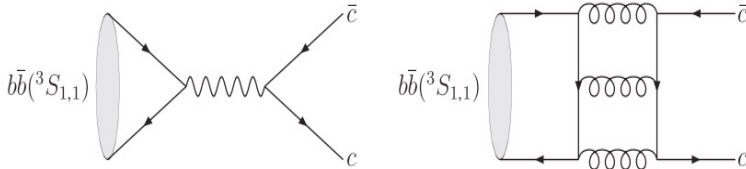


Motivation

☞ Rare decays involving $\Upsilon(1S, 2S) \rightarrow c\bar{c}$ due to the OZI suppressed.

☞ Bound states of heavy quarks provide a powerful testing ground for QCD, including the $\mathcal{B}(\Upsilon(1S) \rightarrow D^+D^-) \sim 10^{-5} - 10^{-4}$ [1], $\mathcal{B}(\Upsilon(1S) \rightarrow c\bar{c}) \approx 2.7\%$ [2].

☞ $\mathcal{B}[\Upsilon(1S) \rightarrow D^{*\pm}X]$ measured by BABAR Collaboration [3].



$\Upsilon(1S)$ using the decay chain $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$.
[PHYSICAL REVIEW D, 81,011102(R)(2010)]

- [1] PRD **74**, 094016(2006), Hai-Bo Li et al.
[2] PRD **78**, 094017(2008), Yu-Jie Zhang et al.
[3] PRD **81**,011102(R)(2010), BaBar collaboration.

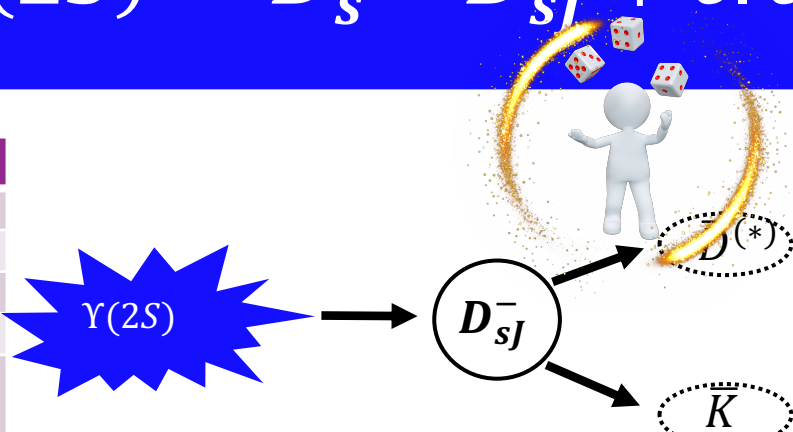
The study of $\Upsilon(2S) \rightarrow D_s^{(*)+} D_{sJ}^- + c.c.$

D_s^+ decay modes in on the table:

$D_s^+ \rightarrow$	BR(%)
$\phi(\rightarrow K^+K^-)\pi^+$	2.24 ± 0.08
$K_s^0(\rightarrow \pi^+\pi^-)K^+$	1.01 ± 0.07
$K^*(892)^0(K^-\pi^+)K^+$	2.58 ± 0.08
$\rho^+\phi$	4.08 ± 1.12
$\eta\pi^+$ ($\eta \rightarrow \gamma\pi^0 \Rightarrow \eta^+\pi^+\pi^-\pi^0$)	1.05 ± 0.05
$\eta\pi^+$ ($\eta \rightarrow \gamma\gamma \Rightarrow \eta \rightarrow \gamma\gamma, \pi^+\pi^-\pi^0$)	1.05 ± 0.05
Totally	12.13 ± 1.13

$[D_s^+ / D_s^{*+} (\rightarrow \gamma D_s^+)]_{\text{reconstructed}}$

$[K_s^0 / K^-]_{\text{tag}}$



$$M_{\text{rec}}(D_s^{(*)+}) = \sqrt{(E_{\text{C.M.}} - E_{D_s^{(*)+}})^2 - (\vec{P}_{\text{C.M.}} - \vec{P}_{D_s^{(*)+}})^2} \Rightarrow D_s^-$$

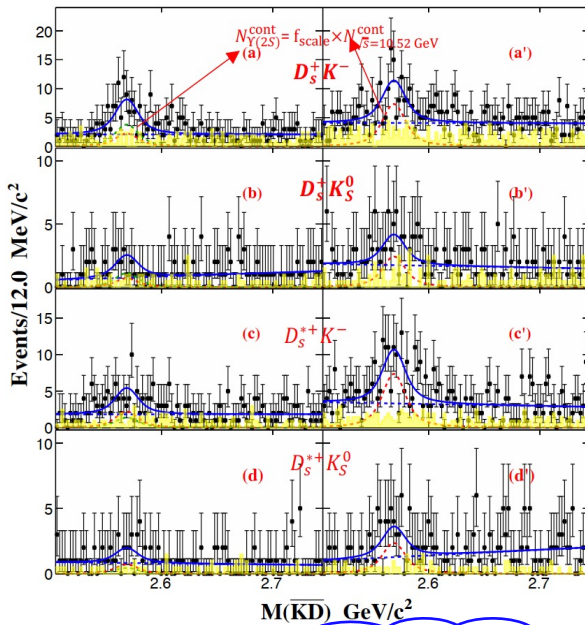
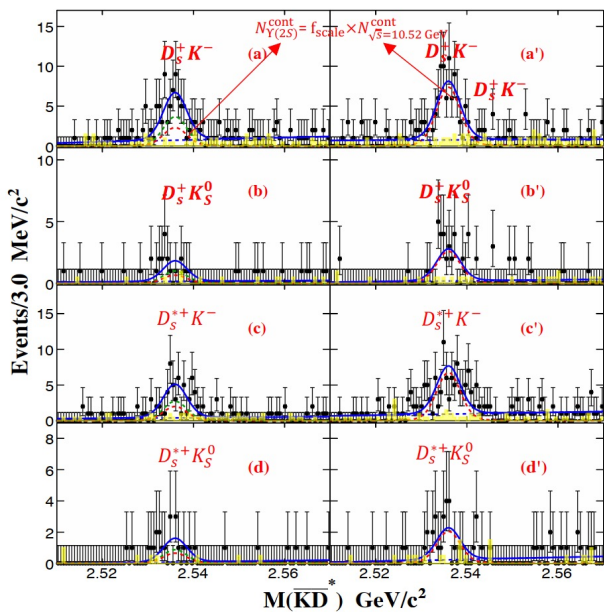
$$M_{\text{rec}}(D_s^{(*)+}K) = \sqrt{(E_{\text{C.M.}} - E_{D_s^{(*)+}} - E_K)^2 - (\vec{P}_{\text{C.M.}} - \vec{P}_{D_s^{(*)+}} - \vec{P}_K)^2} \Rightarrow D^{(*)0}/D^{(*)-}$$

$M_{\text{rec}}(D_s^{(*)+}) - M_{\text{rec}}(D_s^{(*)+}K) + m(\bar{D}^{(*)})$ are used to improve the resolutions of D_{sJ}^- .

Distributions of $M(\overline{K}D^*)$



$$\mathcal{B}(Y(2S) \rightarrow D_s^{(*)+} D_{s_j}^{(*)-}) \times \mathcal{B}(D_{s_j}^{(*)-} \rightarrow D^{(*)} K) = \frac{N_{\text{fit}}^{Y(2S)} - (N_{\text{fit}}^{Y(\text{cont})} \times f_{\text{scale}})}{\sum_i (\epsilon_i \times B_i) \times N_{\text{Tot}}} \quad \sigma(e^+e^- \rightarrow D_s^{(*)+} D_{s_j}^{(*)-}) \times \mathcal{B}(D_{s_j}^{(*)-} \rightarrow D^{(*)} K) = \frac{N_{\text{fit}}^{\text{cont}} \times |1 - \Pi|^2}{\sum_i (\epsilon_i \times B_i) \times \mathcal{L} \times (1 + \delta_{\text{ISR}})}$$



$$R_{\text{iso},1} = \frac{\mathcal{B}[D_{s1}(2536)^- \rightarrow D^*(2010)^0 K_S^0]}{\mathcal{B}[D_{s1}(2536)^- \rightarrow D^*(2007)^0 K^-]} = 0.48 \pm 0.07 \pm 0.02$$

$$R_{\text{iso},2} = \frac{\mathcal{B}[D_{s2}^*(2573)^- \rightarrow D^- K_S^0]}{\mathcal{B}[D_{s2}^*(2573)^- \rightarrow D^0 K^-]} = 0.49 \pm 0.10 \pm 0.02$$

There are in good agreement with expected values of 0.498 and 0.497 from isospin symmetry.

Fitting Results

$$\text{QED+QCD: } R_1 = \mathcal{B}(Y(2S) \rightarrow D_s^{(*)+} D_{sJ}^- + c.c.) / \mathcal{B}(Y(2S) \rightarrow \mu^+ \mu^-)$$

The fitting results of $\mathcal{B}(Y(2S) \rightarrow D_s^{(*)+} D_{sJ}^-) \mathcal{B}(D_{sJ}^- \rightarrow KD^{(*)})$ (K^- mode)			
Final states	$N_{Y(2S)}^{\text{sig}}$	significance(σ)	$\mathcal{B}(Y(2S) \rightarrow D_s^{(*)+} D_{sJ}^-) \mathcal{B}(D_{sJ}^- \rightarrow KD^{(*)}) (10^{-5})$
$D_s^+ D_{s1}(2536)^-$	$43 \pm 9 \pm 2$	5.3	$1.6 \pm 0.3 \pm 0.2$
$D_s^{*+} D_{s1}(2536)^-$	$43 \pm 9 \pm 2$	4.3	$1.4 \pm 0.4 \pm 0.2$
$D_s^+ D_{s2}^*(2573)^-$	$43 \pm 9 \pm 5$	3.8	$1.4 \pm 0.4 \pm 0.2$
$D_s^{*+} D_{s2}^*(2573)^-$	$43 \pm 9 \pm 2$	1.6	$0.9 \pm 0.5 \pm 0.2$

$$\text{QED: } R_2 = \sigma^{\text{Born}}(e^+ e^- \rightarrow D_s^{(*)+} D_{sJ}^- + c.c.) / \sigma^{\text{Born}}(e^+ e^- \rightarrow \mu^+ \mu^-)$$

The fitting results of $\sigma^{\text{B}}(e^+ e^- \rightarrow D_s^{(*)+} D_{sJ}^-) \mathcal{B}(D_{sJ}^- \rightarrow KD^{(*)})$ (K^- mode)			
Final states	$N_{\text{cont}}^{\text{sig}}$	significance(σ)	$\sigma^{\text{B}}(e^+ e^- \rightarrow D_s^{(*)+} D_{sJ}^-) \mathcal{B}(D_{sJ}^- \rightarrow KD^{(*)}) (\text{fb})$
$D_s^+ D_{s1}(2536)^-$	$86 \pm 10 \pm 2$	13.9	$67 \pm 8 \pm 6$
$D_s^{*+} D_{s1}(2536)^-$	$79 \pm 10 \pm 2$	11.8	$84 \pm 11 \pm 11$
$D_s^+ D_{s2}^*(2573)^-$	$102 \pm 17 \pm 21$	7.1	$56 \pm 9 \pm 13$
$D_s^{*+} D_{s2}^*(2573)^-$	$102 \pm 16 \pm 6$	7.6	$106 \pm 17 \pm 12$

$R_1/R_2 = 9.8 \pm 2.5, 8.0 \pm 2.4, 9.7 \pm 3.0$ and 4.4 ± 2.8 for the $D_s^+ D_{s1}(2536)^-, D_s^{*+} D_{s1}(2536)^-, D_s^+ D_{s2}^*(2573)^-$ and $D_s^{*+} D_{s2}^*(2573)^-$ final states in the $D_{sJ}^- \rightarrow K^- \bar{D}^{(*)0}$ modes, respectively.

The measured R_1/R_2 values indicate that the strong decay dominates in the $Y(2S) \rightarrow D_s^{(*)+} D_{sJ}^-$ processes.

Summary

- ✓ We study the hindered M1 decays between P-wave bottomonium state $h_b(2P) \rightarrow \chi_{bJ}(1P)\gamma$ with $J = 0, 1, 2$ and set limits on $h_b(2P) \rightarrow \chi_{bJ}(1P)\gamma$ processes.
- ✓ We found the first evidence of the $h_b(2P) \rightarrow Y(1S)\eta$ transition with significance of 3.5σ and set limits on $h_b(1P, 2P) \rightarrow Y(1S)\pi^0$ processes.
- ✓ We observe the charmed strange meson pair $D_s^{(*)+}D_{sJ}^-$ production in $Y(2S)$ decays and e^+e^- annihilation at $\sqrt{s} = 10.52$ GeV for the first time, where D_{sJ}^- is $D_{s1}(2536)^-$ or $D_{s2}^*(2573)^-$.
- ✓ These results are in good agreement with expected isospin symmetry and indicate that the strong decay dominates in the $Y(2S) \rightarrow D_s^{(*)+}D_{sJ}^-$ processes.

Thank for your attention!



Backup

Selections for studying of $\Upsilon(2S) \rightarrow D_s^{(*)+} D_{sJ}^- + c.c.$

For charged tracks

1. kaons: $\mathcal{L}(K)/\mathcal{L}(K)+\mathcal{L}(\pi)>0.6$. Pions: $\mathcal{L}(K)/\mathcal{L}(K)+\mathcal{L}(\pi)<0.4$, $P_T>0.1$ GeV/c
2. $|\text{drl}|<0.5$ cm and $|\text{ldz}|<2.0$ cm.
3. K_S^0 is selected by nisKsFinder package select good candidates.

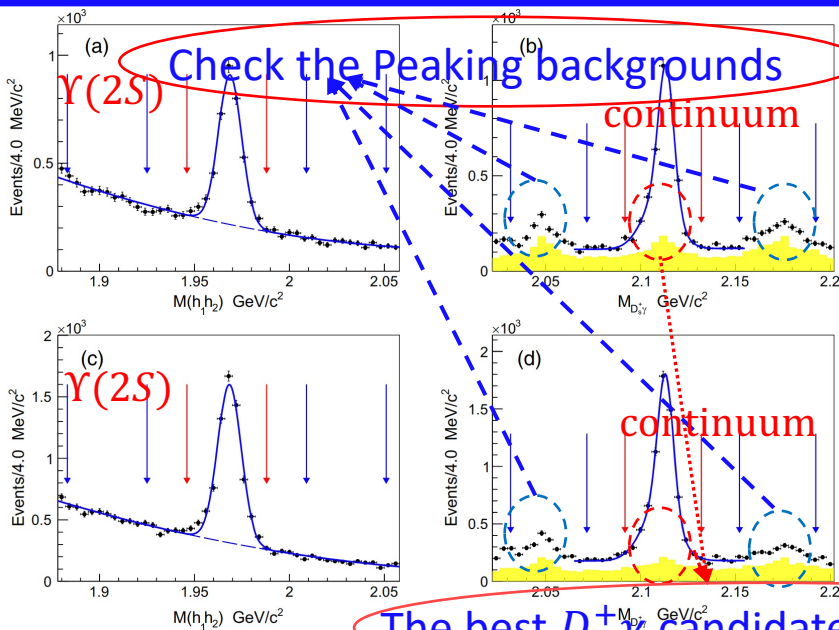
For γ candidates

1. For $\pi^0 \rightarrow \gamma\gamma$
 $E_\gamma > 25$ MeV in barrel, $E_\gamma > 50$ MeV in endcap.
2. For $\eta (\rightarrow \gamma\gamma)$
 $E_\gamma > 150$ MeV in barrel and endcap.
3. For γ_{tag} (decay from D_s^{*+}) candidates
 $E_\gamma > 50$ MeV in barrel, $E_\gamma > 100$ MeV in endcap.

For $D_s^{(*)+}$ candidates

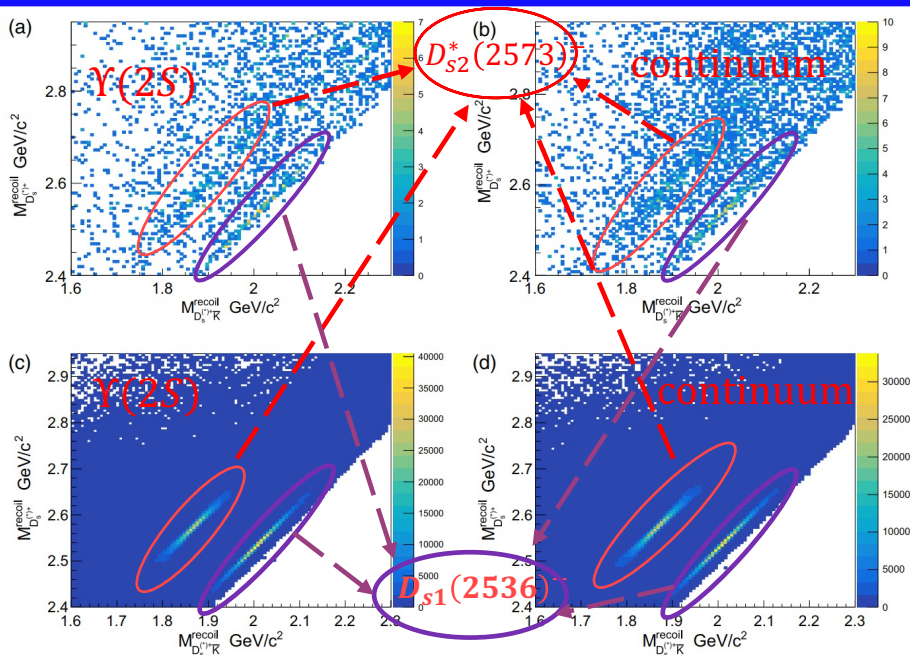
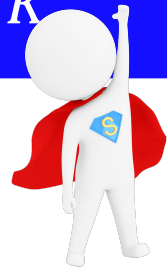
1. Vertex Fit and Mass Constraint for $D_s^{(*)+}$.
2. The best $D_s^+ \gamma$ combination per a event with the best mass fit χ^2 to avoid multiple combinations.

$D_s^{(*)+}$ signal distributions



- ✳ D_s^+ signal mass window is defined as $|M(h_1 h_2) - m(D_s^+)| < 3\sigma_{D_s^+} (\approx 7 \text{ MeV}/c^2)$.
- ✳ D_s^{*+} signal mass window is defined as $|M(D_s^+ \gamma) - m(D_s^{*+})| < 3\sigma_{D_s^{*+}} (\approx 7 \text{ MeV}/c^2)$.
- ✳ The yellow shade histogram is from D_s^+ sidebands

Distributions of $M_{D_S^{(*)}+}^{\text{recoil}}$ v.s. $M_{D_S^{(*)}+\bar{K}}^{\text{recoil}}$



There are clear bands in the distributions of data corresponding to the productions of the $D_{s1}(2536)^-$ and $D_{s2}^*(2573)^-$.