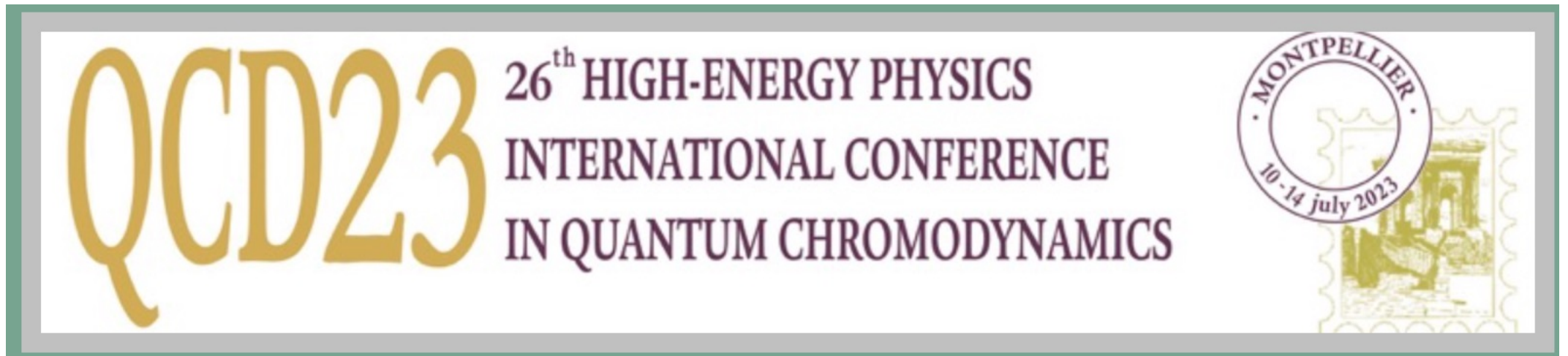


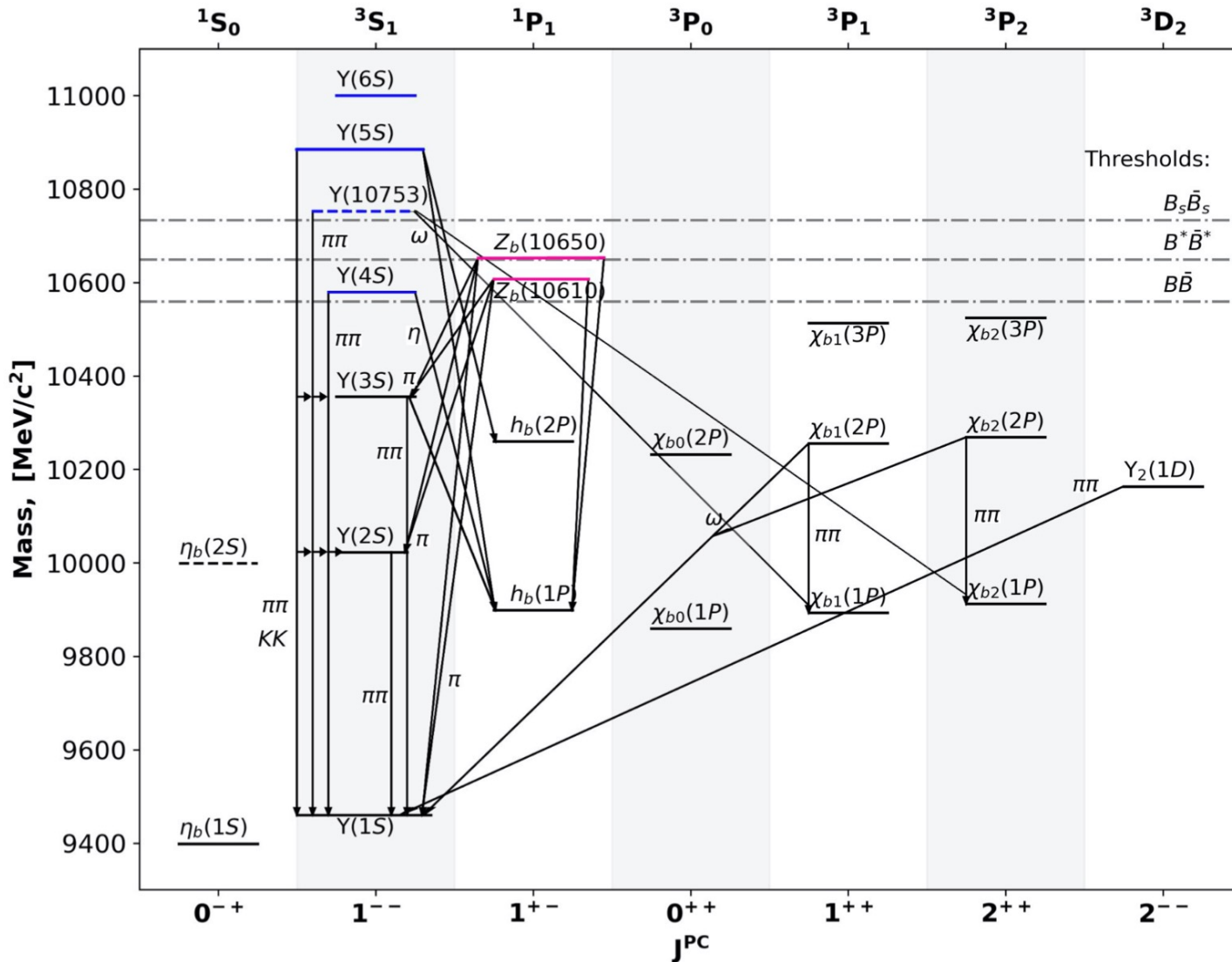


# Quarkonium at Belle II

Sen Jia (Southeast University)  
on behalf of the Belle II Collaboration



# Bottomonium



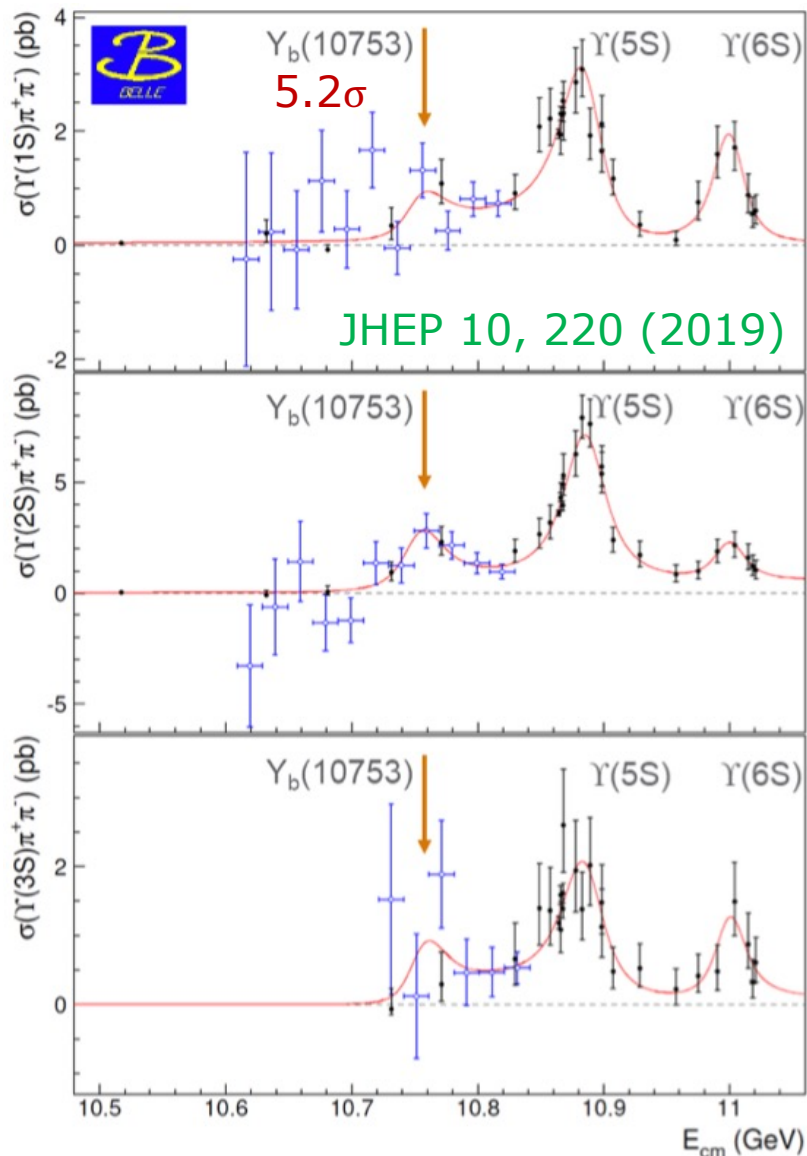
- Below  $B\bar{B}$  thresholds – bottomonia are well described by the potential models.

- Above  $B\bar{B}$  thresholds – bottomonia express unexpected properties:

- Two charged  $Z_b^+$  states are observed ( $B^{(*)}\bar{B}^*$  molecular?)
- Hadronic transitions are strongly enhanced (OZI rule violation);
- $\eta$  transitions are not suppressed compare to  $\pi^+\pi^-$  transitions (heavy quark spin-symmetry violation);

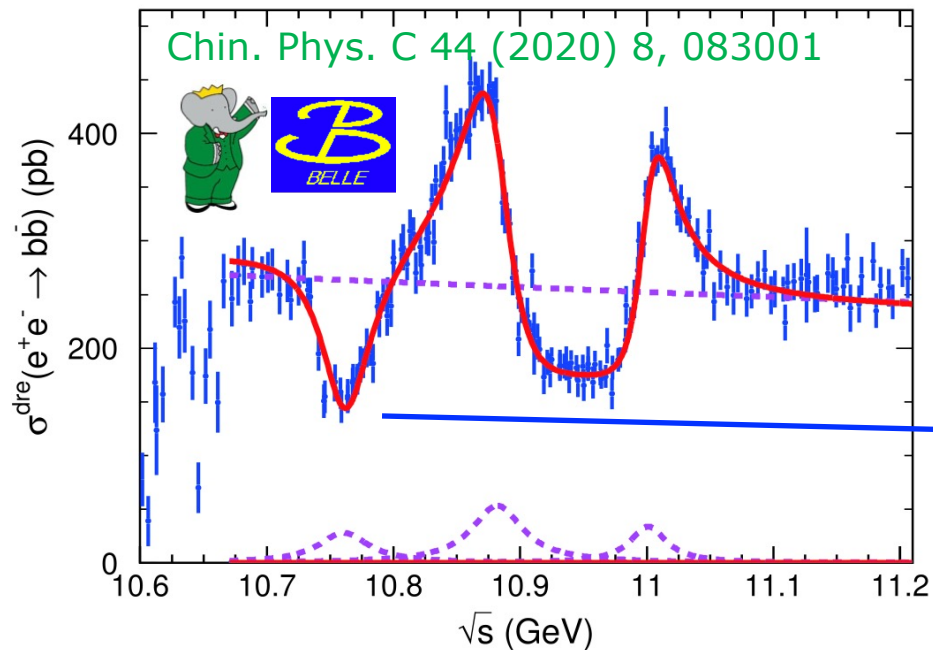
Conventional bottomonium (pure  $b\bar{b}$  states)  
 Bottomonium-like states (mix of  $b\bar{b}$  and  $B\bar{B}$ )  
 Exotic charged states ( $Z_b^+$ )

# Discovery of $\Upsilon(10753)$



- Belle: several  $\sim 1\text{fb}^{-1}$  scan points below  $\Upsilon(5S)$
- New structure observed in  $\pi^+\pi^-\Upsilon(nS)$  transitions

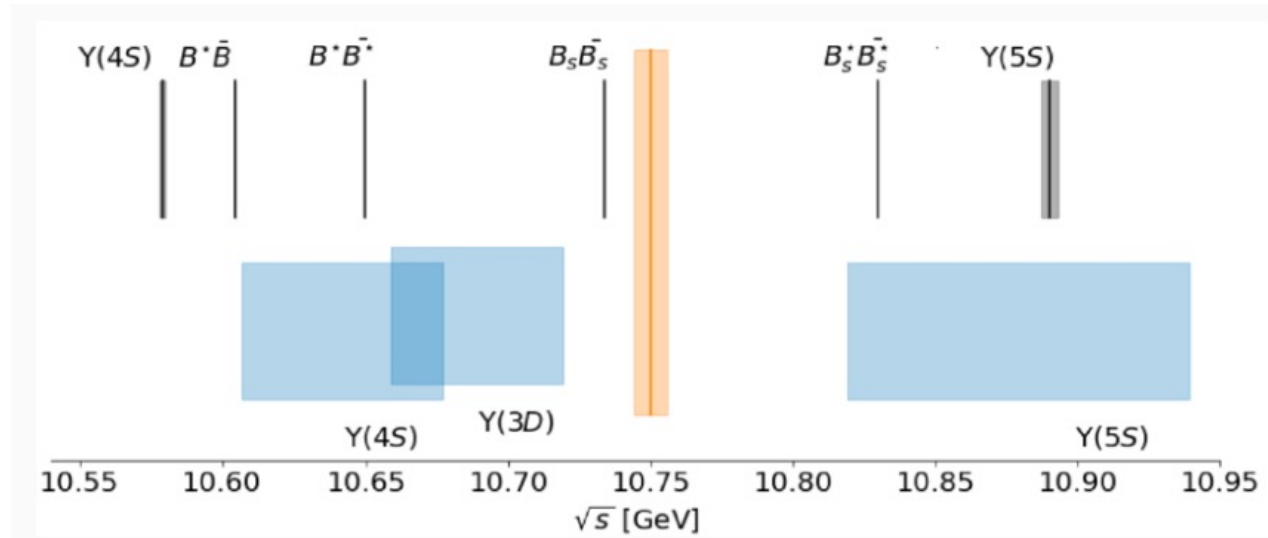
	$\Upsilon(10860)$	$\Upsilon(11020)$	New structure
$M$ (MeV/ $c^2$ )	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0}_{-4.5}{}^{+1.0}_{-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
$\Gamma$ (MeV)	$36.6^{+4.5}_{-3.9}{}^{+0.5}_{-1.1}$	$23.8^{+8.0}_{-6.8}{}^{+0.7}_{-1.8}$	$35.5^{+17.6}_{-11.3}{}^{+3.9}_{-3.3}$



A dip at 10.75 GeV may correspond to  $\Upsilon(10753)$ .

# Theoretical interpretations

Godfrey and Moats, PRD 92, 054034 (2015)



- Mass does not match  $Y(3D)$  theoretical predictions, and D-wave states are not seen in  $e^+e^-$  collisions.
- $Y(4S)$  -  $Y(3D)$  mixing can be enhanced due to hadron loops.

## □ Conventional bottomonium

Eur. Phys. J. C 80, 59 (2020)

Phys. Rev. D 101, 014020 (2020)

Phys. Rev. D 102, 014036 (2020)

Phys. Lett. B 803, 135340 (2020)

Phys. Rev. D 104, 034036 (2021)

Prog. Part. Nucl. Phys. 117, 103845 (2021)

Eur. Phys. J. Plus 137, 357 (2022)

Phys. Rev. D 105, 114041 (2022)

Phys. Rev. D 106, 094013 (2022)

Phys. Rev. D 105, 074007 (2022)

## □ Hybrid

Phys. Rept. 873, 1 (2020)

Phys. Rev. D 104, 034019 (2021)

## □ Tetraquark

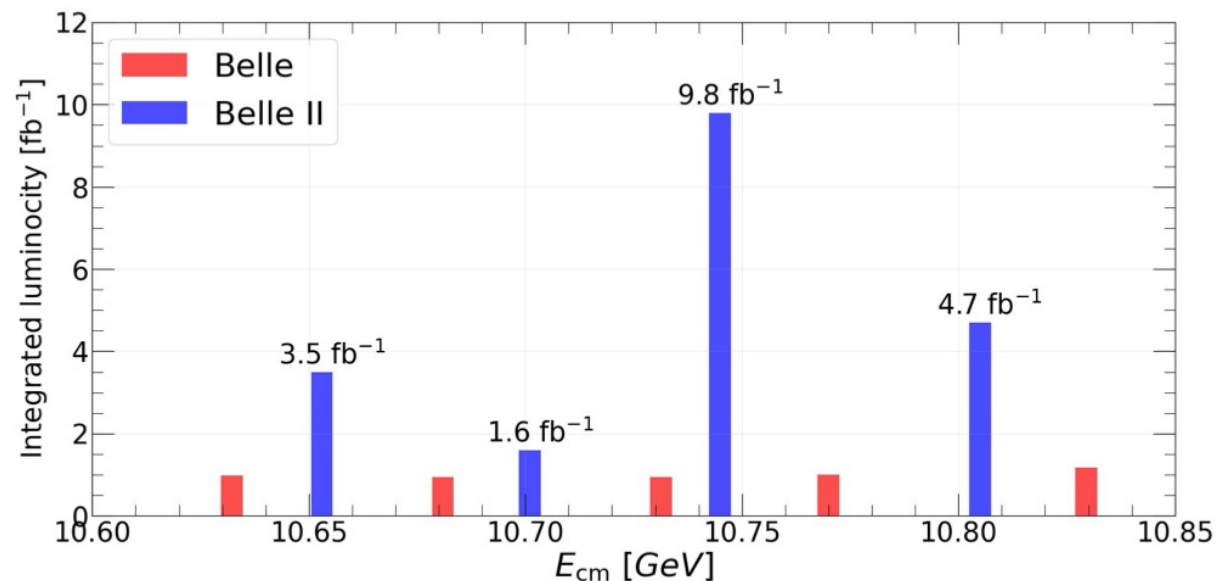
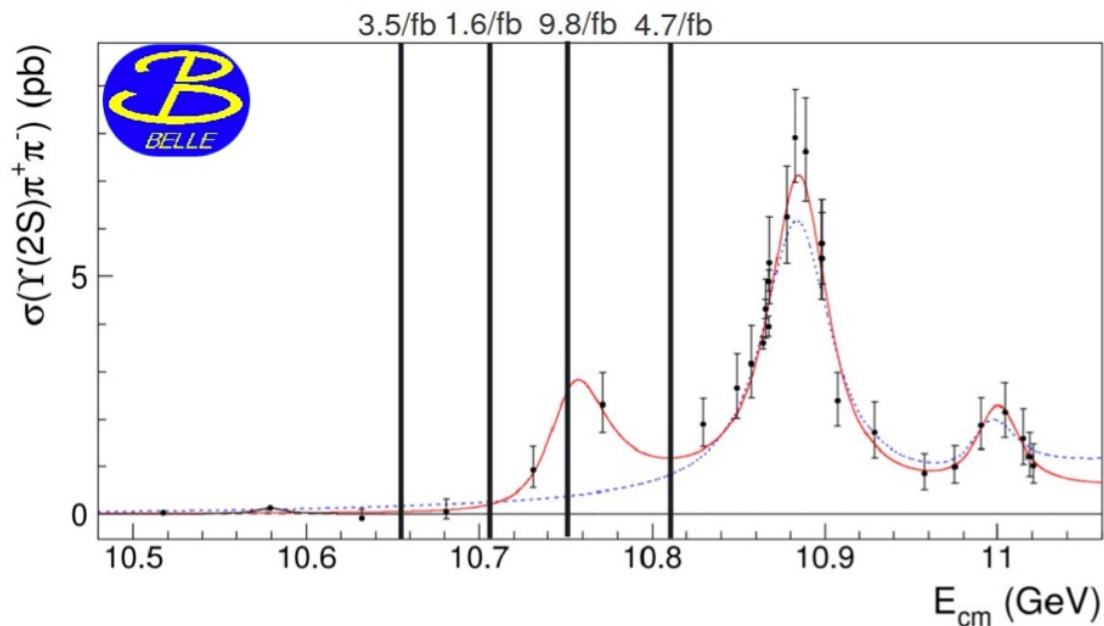
Chin. Phys. C 43, 123102 (2019)

Phys. Lett. B 802, 135217 (2020)

Phys. Rev. D 103, 074507 (2021)

Phys. Rev. D 107, 094515 (2023)

# Unique scan data near $\sqrt{s} = 10.75$ GeV



- In November 2021, Belle II collected  $19 \text{ fb}^{-1}$  of unique data at energies above the  $\Upsilon(4S)$ : four energy scan points around 10.75 GeV.
- Belle II collected the data in the gaps between Belle energy scan points.
- Physics goal: understand the nature of the  $\Upsilon(10753)$  energy region.

For the details on the SuperKEKB and Belle II detectors, please see Renu's report "Recent highlights from Belle II".

Three Belle II results will be presented:

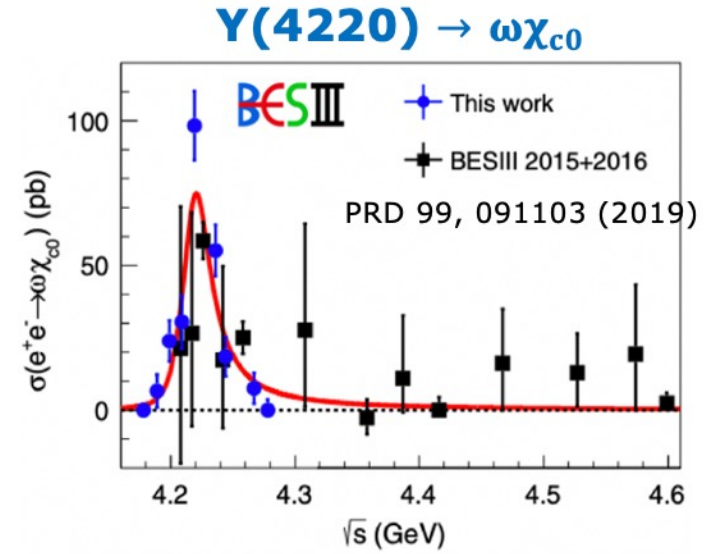
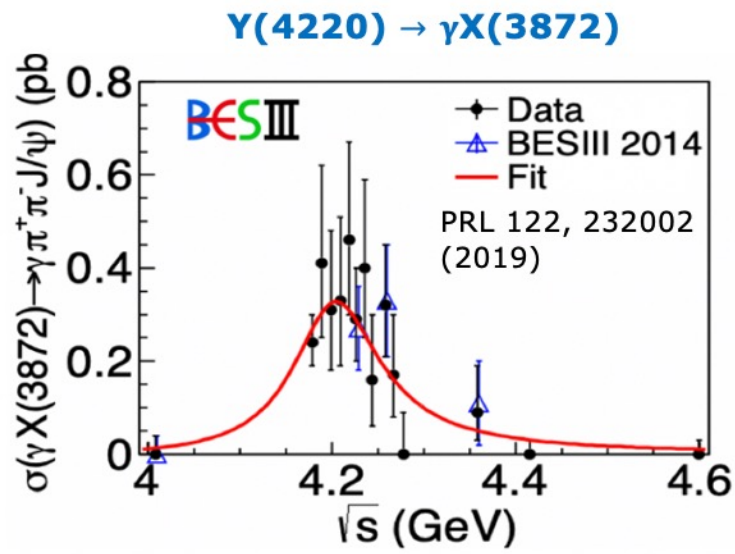
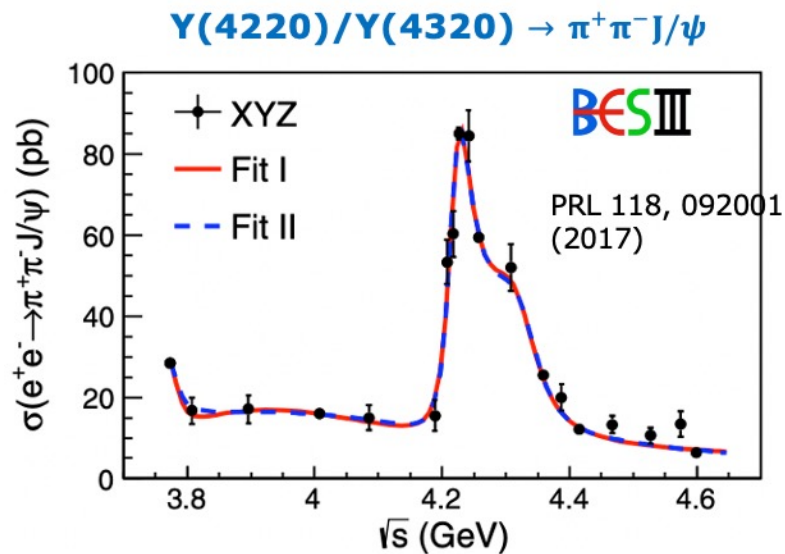
1.  $e^+e^- \rightarrow \omega\chi_{bJ}$  and  $X_b \rightarrow \omega\Upsilon(1S)$  [PRL 130, 091902 (2023)]
2.  $e^+e^- \rightarrow B\bar{B}, B\bar{B}^*$  and  $B^*\bar{B}^*$  [Preliminary]
3.  $e^+e^- \rightarrow \omega\eta_b(1S)$  and  $e^+e^- \rightarrow \omega\chi_{b0}(1P)$  [Preliminary]

# Motivation to search for $\Upsilon(10753) \rightarrow \omega\chi_{bJ}$

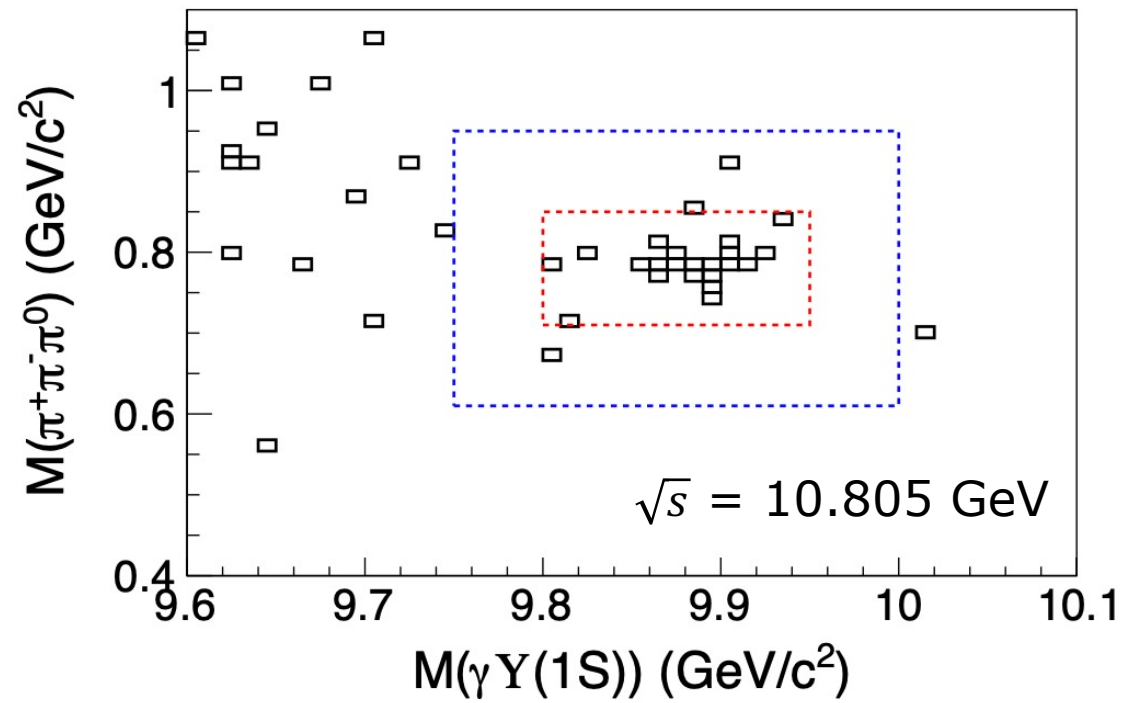
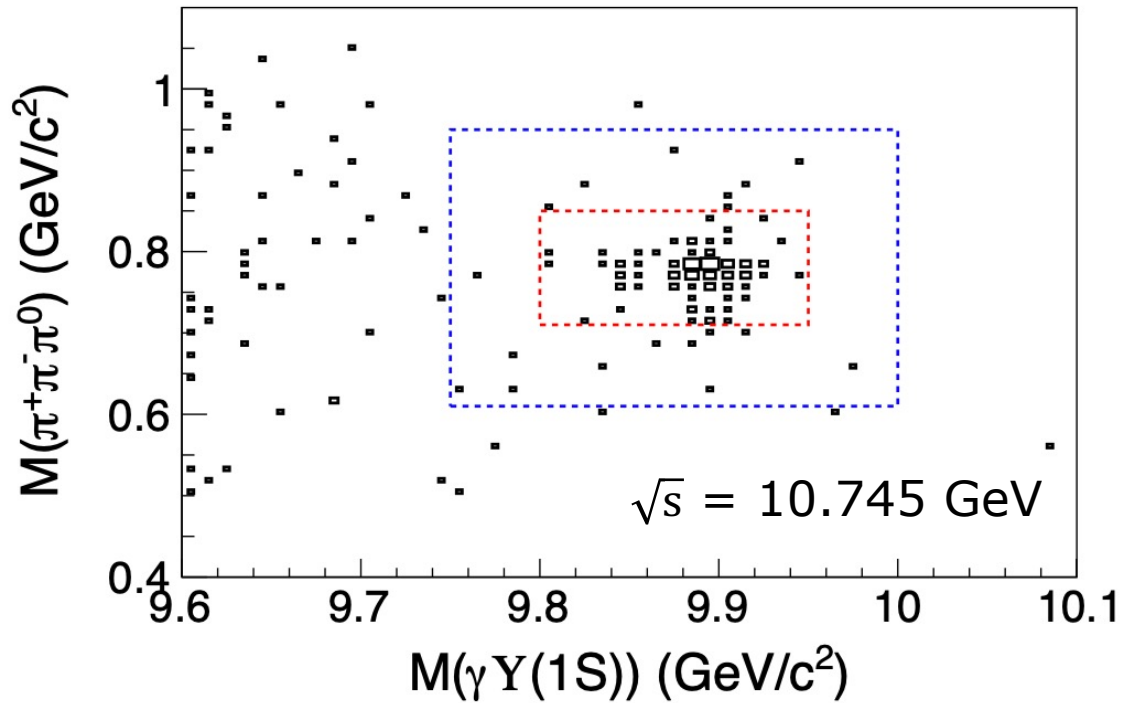
**Theory:** Branching fractions of  $10^{-3}$  for  $\Upsilon(10753) \rightarrow \omega\chi_{bJ}$  [PRD 104, 034036 (2021)] and  $\Upsilon(10753) \rightarrow \pi^+\pi^-\Upsilon(nS)$  [PRD 105, 074007 (2022)] assuming  $\Upsilon(4S) - \Upsilon(3D)$  mixing state for  $\Upsilon(10753)$ .

Charmonium sector:

- Two close peaks observed in the cross sections for  $e^+e^- \rightarrow \pi^+\pi^-J/\psi$  by BESIII and  $e^+e^- \rightarrow \pi^+\pi^-\Upsilon(nS)$  by Belle, respectively, may suggest similar nature.
- $\Upsilon(4220) \rightarrow \gamma X(3872)$  and  $\omega\chi_{c0}$  observed by BESIII.
- So we expect the observations of  $\Upsilon(10753) \rightarrow \gamma X_b$  and  $\omega\chi_{bJ}$ .



# Mass distributions



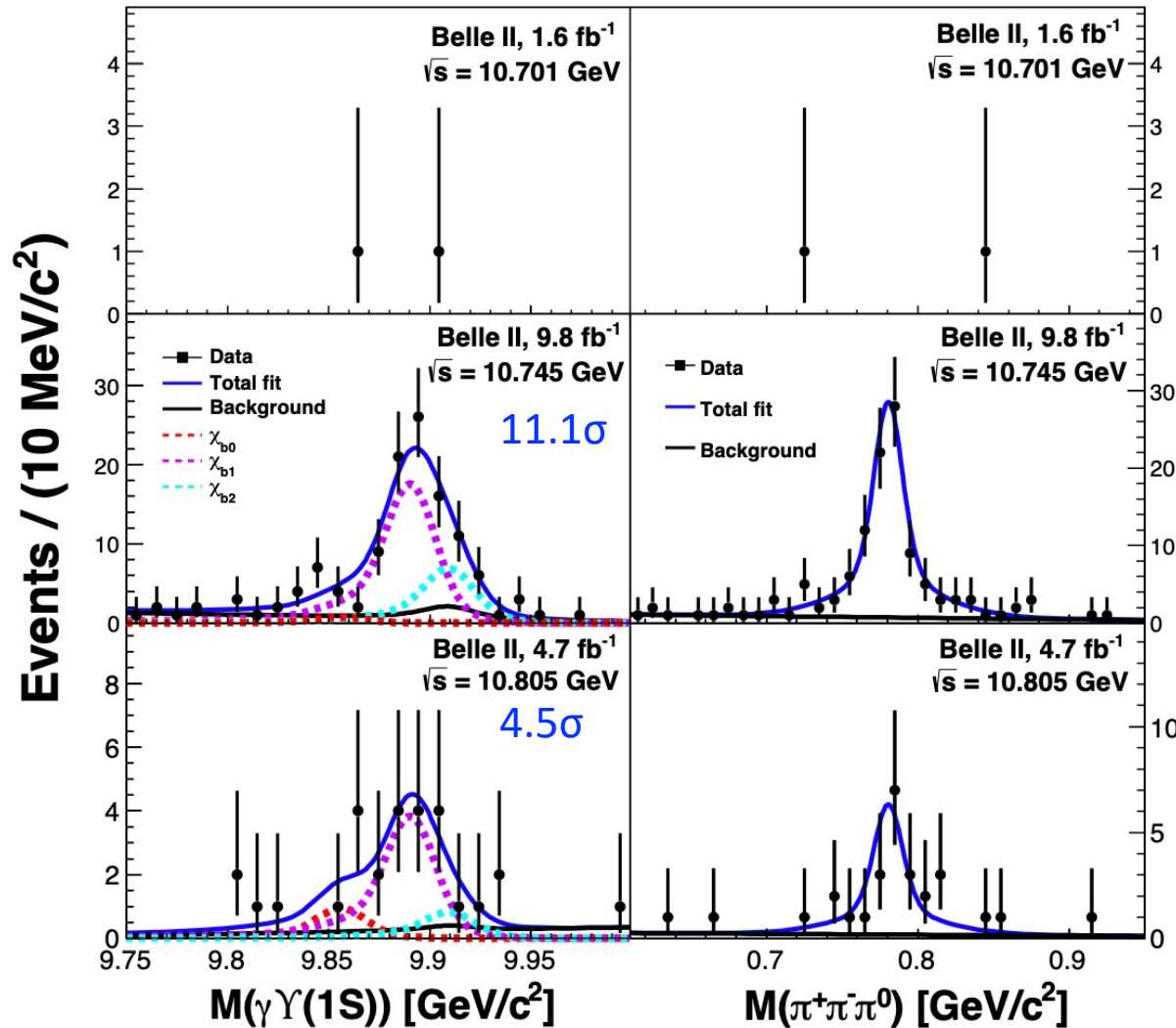
- Red boxes contains 95% of signals.
- Blue boxes show the fit ranges.



# Observation of $\Upsilon(10753) \rightarrow \omega\chi_{bJ}$

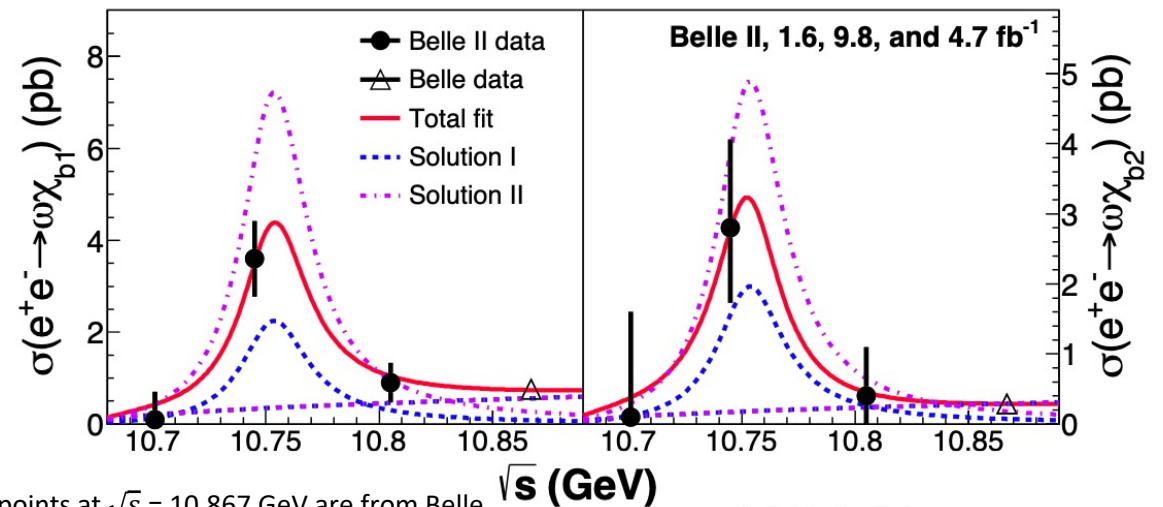
PRL 130, 091902 (2023)

Two dimensional unbinned maximum likelihood fits to the  $M(\gamma\Upsilon(1S))$  and  $M(\pi^+\pi^-\pi^0)$  distributions.



Channel	$\sqrt{s}$ (GeV)	$N^{\text{sig}}$	$\sigma_{\text{Born}}^{(\text{UL})}$ (pb)
$\omega\chi_{b1}$	10.745	$68.9_{-13.5}^{+13.7}$	$3.6_{-0.7}^{+0.7} \pm 0.4$
$\omega\chi_{b2}$		$27.6_{-10.0}^{+11.6}$	$2.8_{-1.0}^{+1.2} \pm 0.5$
$\omega\chi_{b1}$	10.805	$15.0_{-6.2}^{+6.8}$	1.6 @90% C.L.
$\omega\chi_{b2}$		$3.3_{-3.8}^{+5.3}$	1.5 @90% C.L.

The  $e^+e^- \rightarrow \omega\chi_{bJ}$  ( $J = 1, 2$ ) cross sections peak at  $\Upsilon(10753)$ .



The points at  $\sqrt{s} = 10.867$  GeV are from Belle measurements [PRL 113, 142001 (2014)].

# Discussion

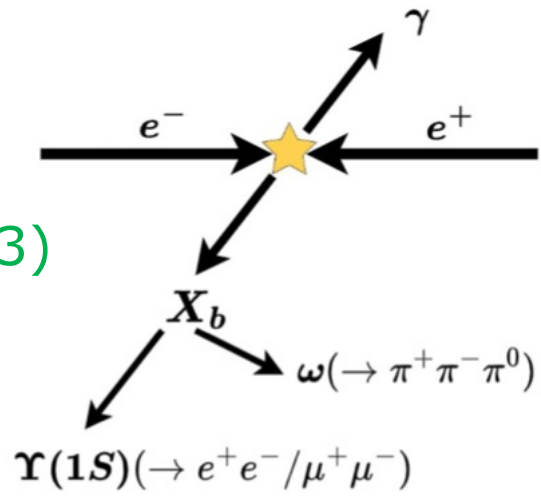
$$\frac{\sigma(e^+e^- \rightarrow \chi_{bJ}(1P)\omega)}{\sigma(e^+e^- \rightarrow Y(nS)\pi^+\pi^-)} \sim \begin{cases} \sim 1.5 \text{ at } \sqrt{s} = 10.745 \text{ GeV [PRL 130, 091902 (2023)]} \\ \sim 0.15 \text{ at } \sqrt{s} = 10.867 \text{ GeV [PRL 113, 142001 (2014)]} \end{cases}$$

- $Y(5S)$  and  $Y(10753)$  have same quantum numbers and similar masses, but the difference on the above ratio is large. This may indicate **the difference in the internal structures of these two states**.

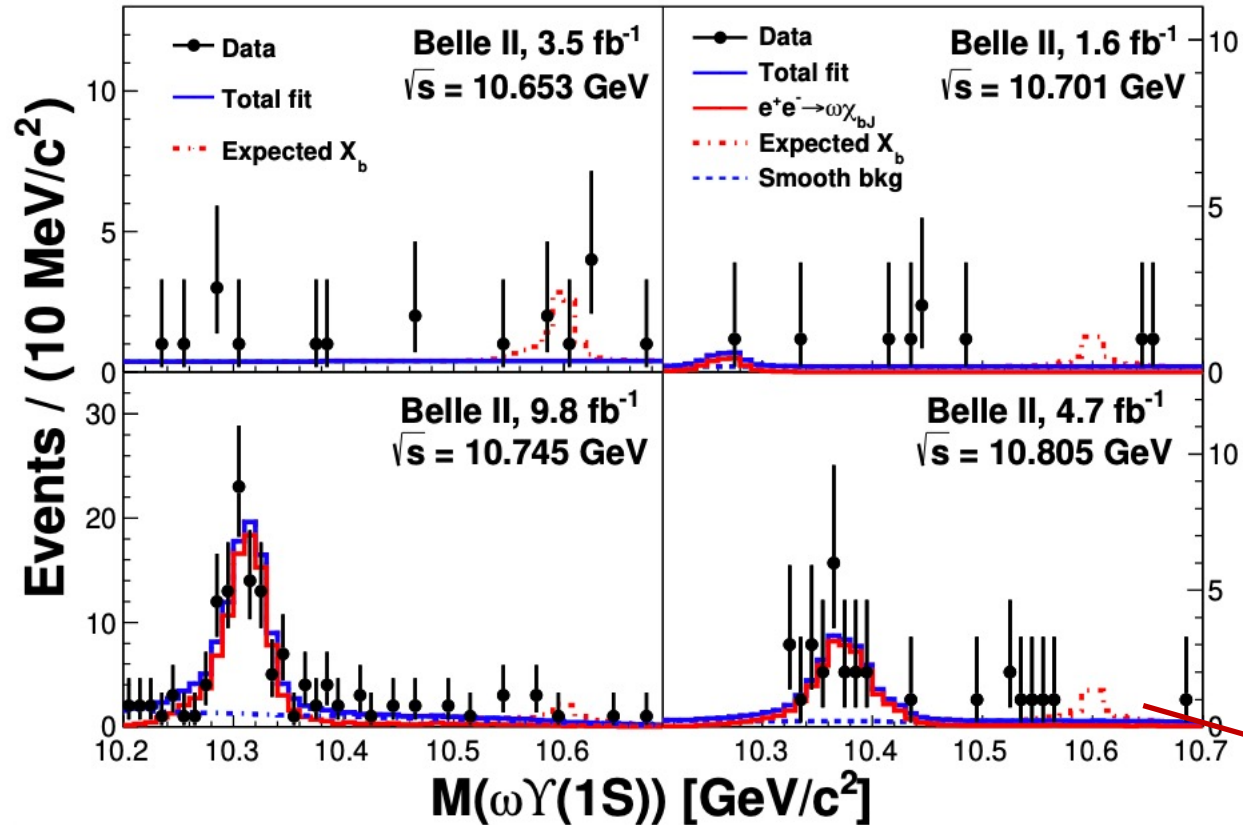
$$\frac{\sigma(e^+e^- \rightarrow \chi_{b1}(1P)\omega)}{\sigma(e^+e^- \rightarrow \chi_{b2}(1P)\omega)} = 1.3 \pm 0.6 \text{ at } \sqrt{s} = 10.745 \text{ GeV [PRL 130, 091902 (2023)]}$$

- **Contradicts the expectation for a pure D-wave bottomonium state of 15** [Phys. Lett. B 738, 172 (2014)]
- **An observation of  $1.8\sigma$  difference with the prediction for a S-D-mixed state of 0.2** [Phys. Rev. D 104, 034036 (2021)]

# Search for $X_b$



PRL 130, 091902 (2023)



- No significant  $X_b$  signal is observed.
- The peaks are the reflections of  $e^+e^- \rightarrow \omega\chi_{bJ}$ .

From simulated events with  $m(X_b) = 10.6 \text{ GeV}/c^2$   
The yield is fixed at the upper limit at 90% C.L.

Upper limits at 90% C.L. on $\sigma_B(e^+e^- \rightarrow \gamma X_b) \cdot \mathcal{B}(X_b \rightarrow \omega\Upsilon(1S))$ (pb)	$\sqrt{s}$ (GeV)	10.653	10.701	10.745	10.805
$m(X_b) = 10.6 \text{ GeV}/c^2$		0.46	0.33	0.10	0.14
$m(X_b) = (10.45, 10.65) \text{ GeV}/c^2$		(0.14, 0.55)	(0.25, 0.84)	(0.06, 0.14)	(0.08, 0.37)

# Measurement of the energy dependence of the $e^+e^- \rightarrow B\bar{B}$ , $B\bar{B}^*$ and $B^*\bar{B}^*$ cross sections

$\sqrt{s} = 10.745 \text{ GeV}, 9.8 \text{ fb}^{-1}$

- The  $B^{(*)}\bar{B}^{(*)}$  are expected to be dominant decay channels for excited bottomonium-like states. Their measurements are critical for understanding these states.

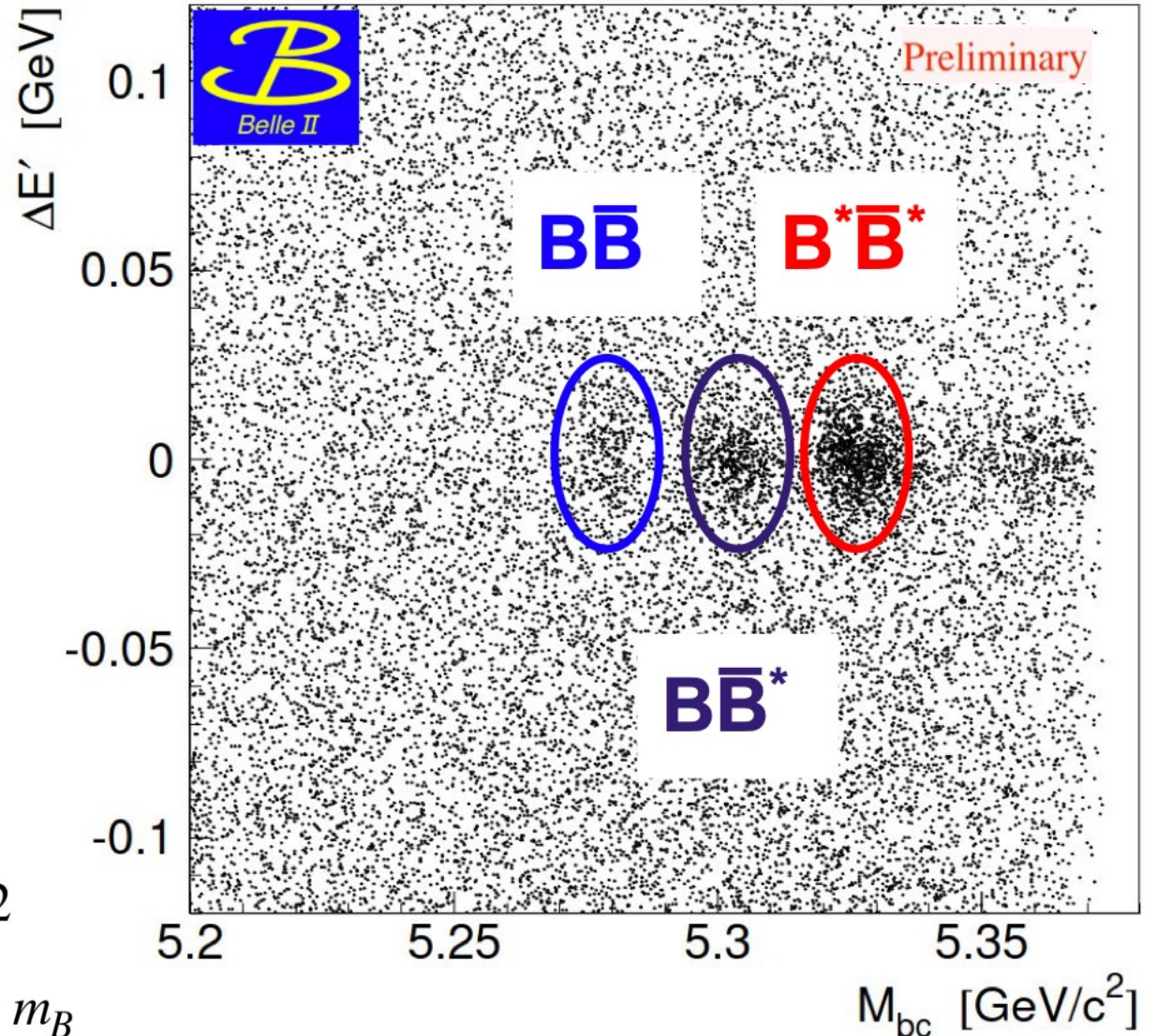
Method:

One B meson is reconstructed in hadronic channels, and signals are identified using

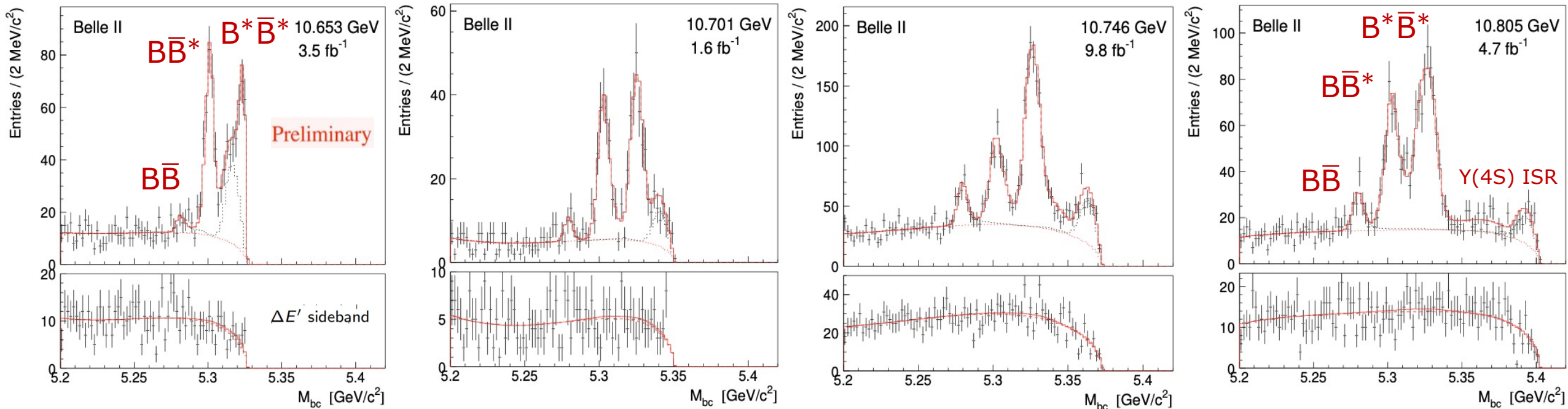
$$M_{bc} = \sqrt{(E_{cm}/2)^2 - p_B^2}$$

$$\Delta E = E_B - E_{cm}/2$$

$$\Delta E' = \Delta E + M_{bc} - m_B$$

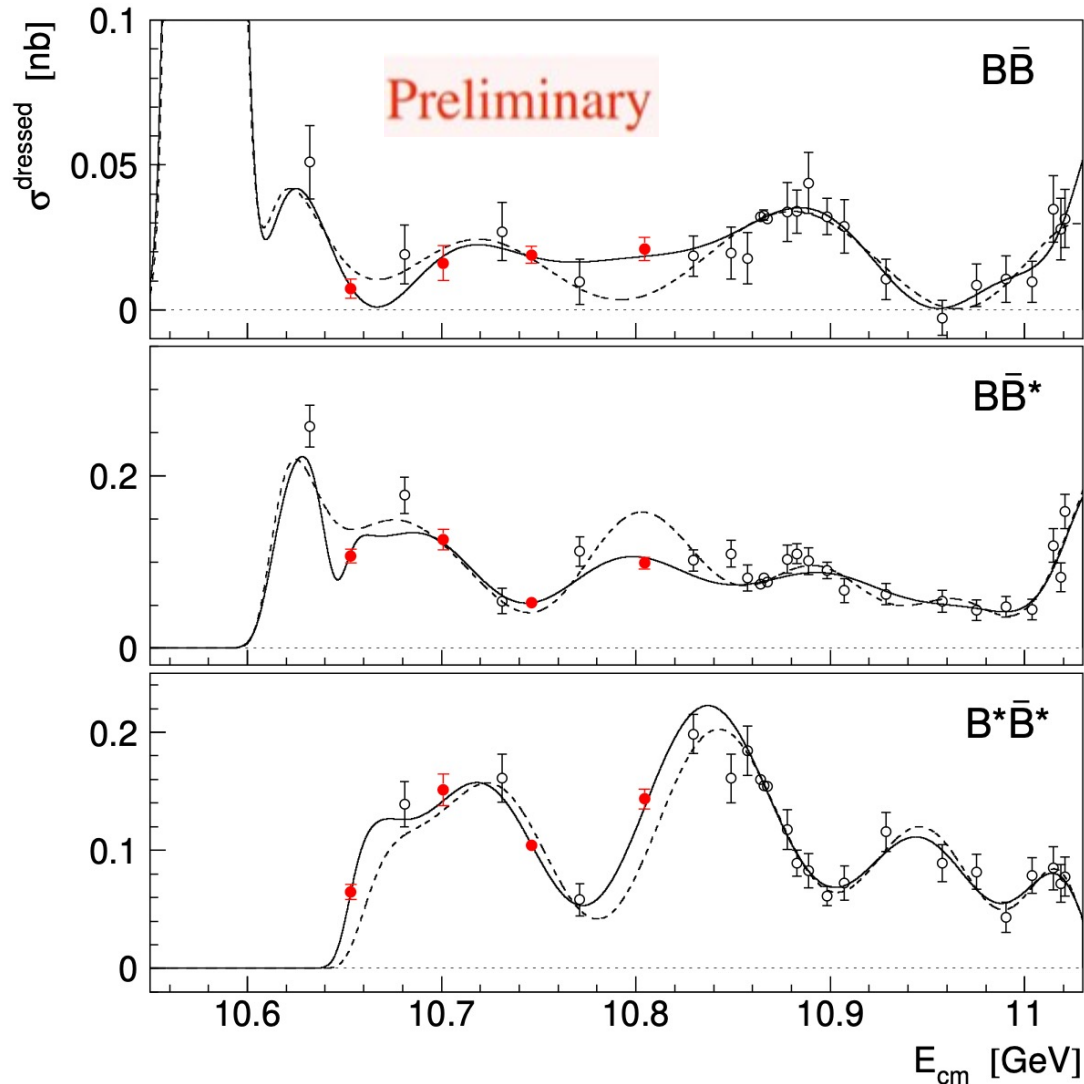


# $M_{bc}$ fit at scan energies



- $e^+e^- \rightarrow B\bar{B}, B\bar{B}^*$  and  $B^*\bar{B}^*$  signals at  $\sqrt{s} \sim 10.75$  GeV can be clearly observed
- Contribution of  $Y(4S) \rightarrow B\bar{B}$  production via ISR is visible well (black dotted histograms)
- At  $\sqrt{s} = 10.653$  GeV, the sharp cut of the data at right edge is due to threshold effect

# Energy dependence of the cross sections

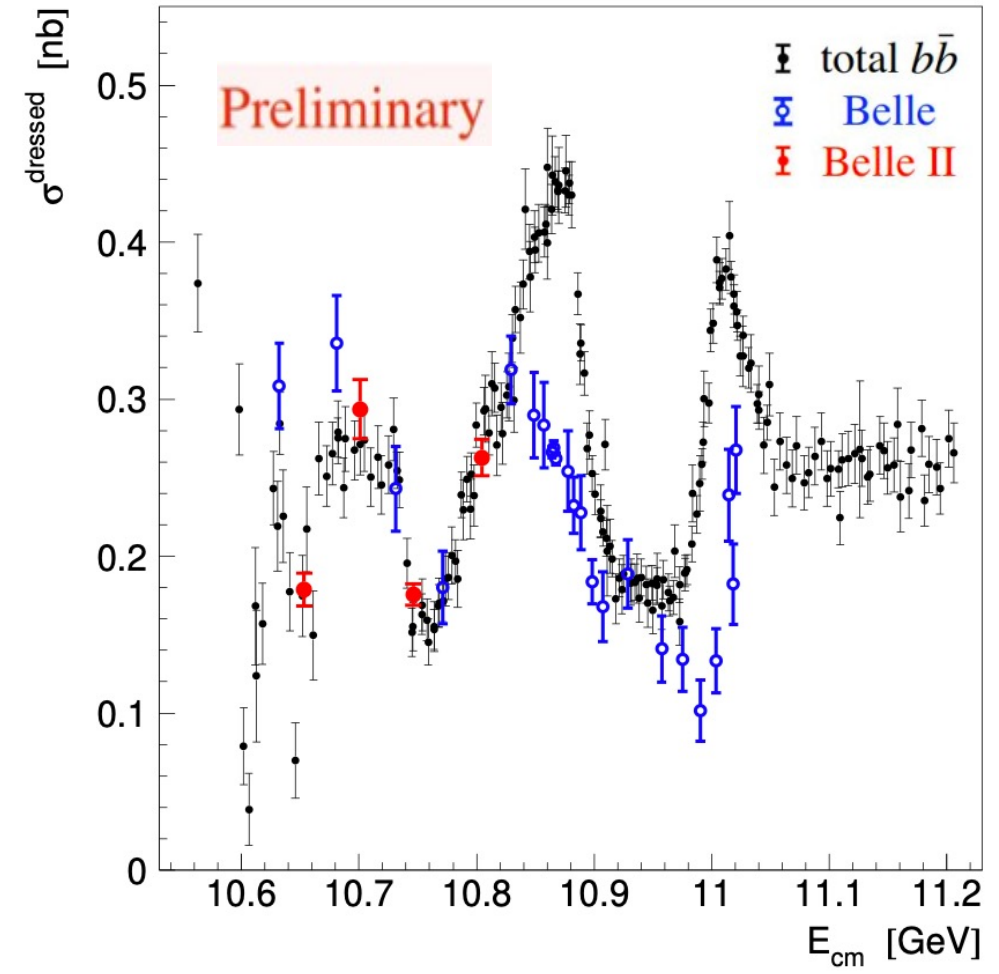
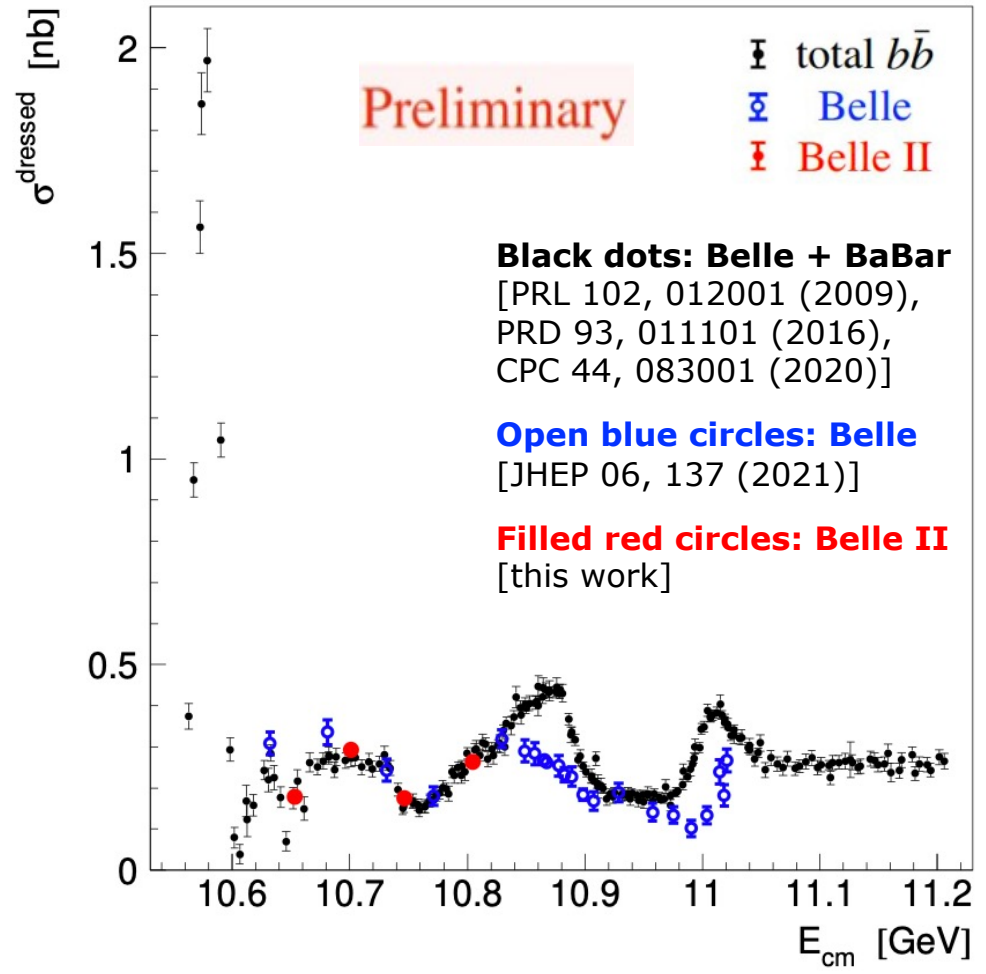


New: rapid increase of  $\sigma_{B^*\bar{B}^*}$  above the threshold

- Similar behaviour was seen for  $D^*\bar{D}^*$  cross section (PRD 97, 012002 (2018))
- Possible interpretation: **resonance or bound state** ( $B^*\bar{B}^*$  or  $b\bar{b}$ ) near threshold (MPL A 21, 2779 (2006))
- Also explains a narrow dip in  $\sigma(e^+e^- \rightarrow B\bar{B}^*)$  near  $B^*\bar{B}^*$  threshold by destructive interference between  $e^+e^- \rightarrow B\bar{B}^*$  and  $e^+e^- \rightarrow B^*\bar{B}^* \rightarrow B\bar{B}^*$
- Inelastic channels [ $\pi^+\pi^-\Upsilon(nS)$  and  $h_b(1P)\eta$ ] could also be enhanced (PRD 87, 094033 (2013))

Solid curve – combined Belle + Belle II data fit  
Dashed curve – Belle data fit only

# Comparison of $\sigma_{b\bar{b}}$ and $\sigma_{B\bar{B}} + \sigma_{B\bar{B}^*} + \sigma_{B^*\bar{B}^*}$



- Agreement at low energy
- Departure at high energy is due to  $B_s^{(*)}\bar{B}_s^{(*)}$ , multi-body  $B^{(*)}\bar{B}^{(*)}\pi(\pi)$ , and bottomonia

# Search for $e^+e^- \rightarrow \omega\eta_b(1S)$ and $e^+e^- \rightarrow \omega\chi_{b0}(1P)$

- Tetraquark (diquark-antidiquark) interpretation of this state predicts **enhancement of  $Y(10753) \rightarrow \omega\eta_b(1S)$  transition** [Chin. Phys. C 43, no.12, 123102 (2019)].

$$\frac{\Gamma(\eta_b \omega)}{\Gamma(\Upsilon \pi^+ \pi^-)} \sim 30$$

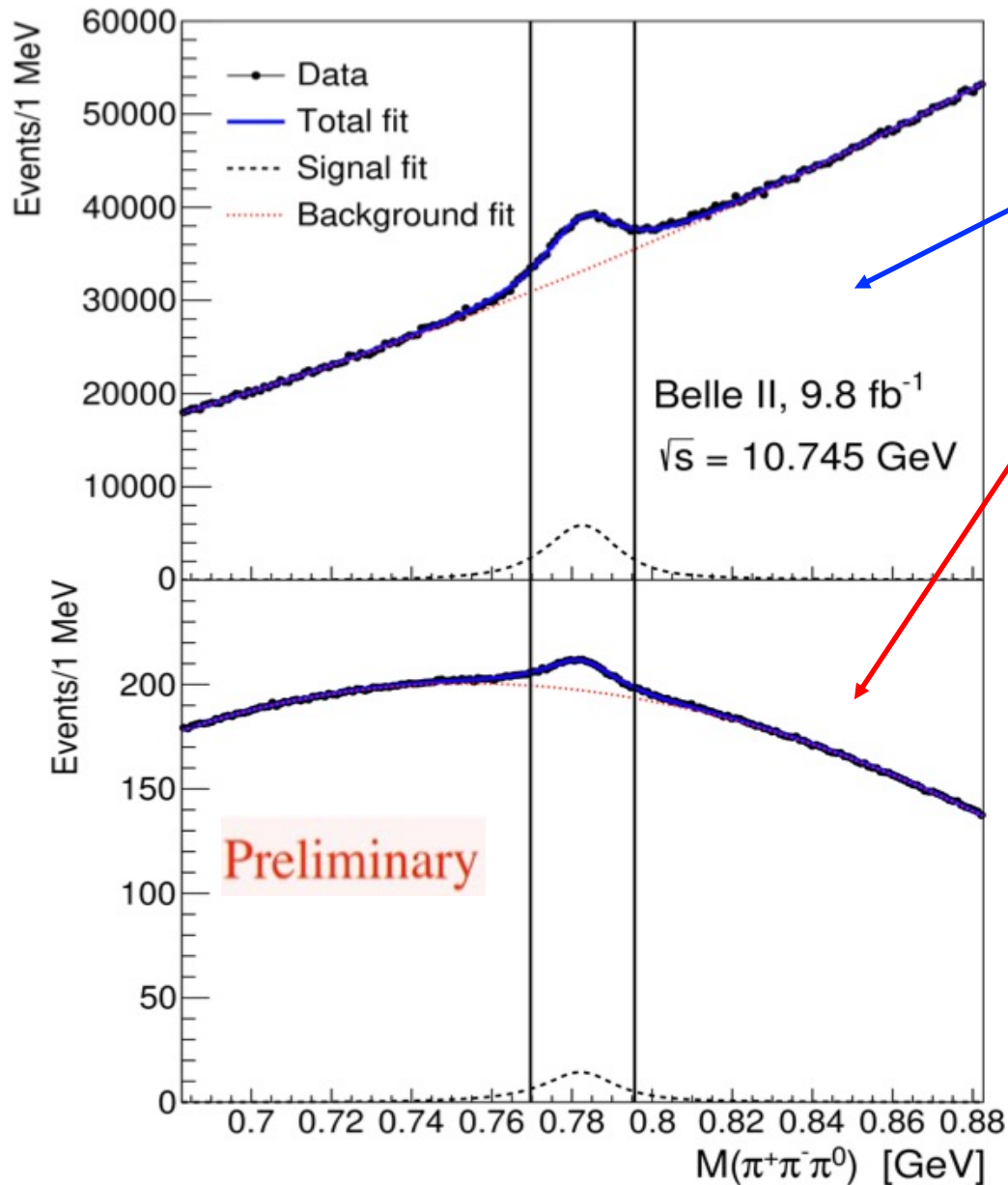
- The  $e^+e^- \rightarrow \omega\chi_{bJ}(1P)$  ( $J = 1, 2$ ) was found to be enhanced at  $\sqrt{s} = 10.745$  GeV (PRL 130, 091902 (2023)). The  $e^+e^- \rightarrow \omega\chi_{b0}(1P)$  transition was not observed due to low  $\mathcal{B}[\chi_{b0}(1P) \rightarrow \gamma Y(1S)] = (1.94 \pm 0.27)\%$ .

- We reconstruct only  $\omega \rightarrow \pi^+ \pi^- \pi^0$  and use **its recoil mass to identify the signal**.

$$M_{\text{recoil}}(\pi^+ \pi^- \pi^0) = \sqrt{\left(\frac{E_{\text{c.m.}} - E^*}{c^2}\right)^2 - \left(\frac{p^*}{c}\right)^2}$$



# Invariant mass distribution of $\pi^+\pi^-\pi^0$

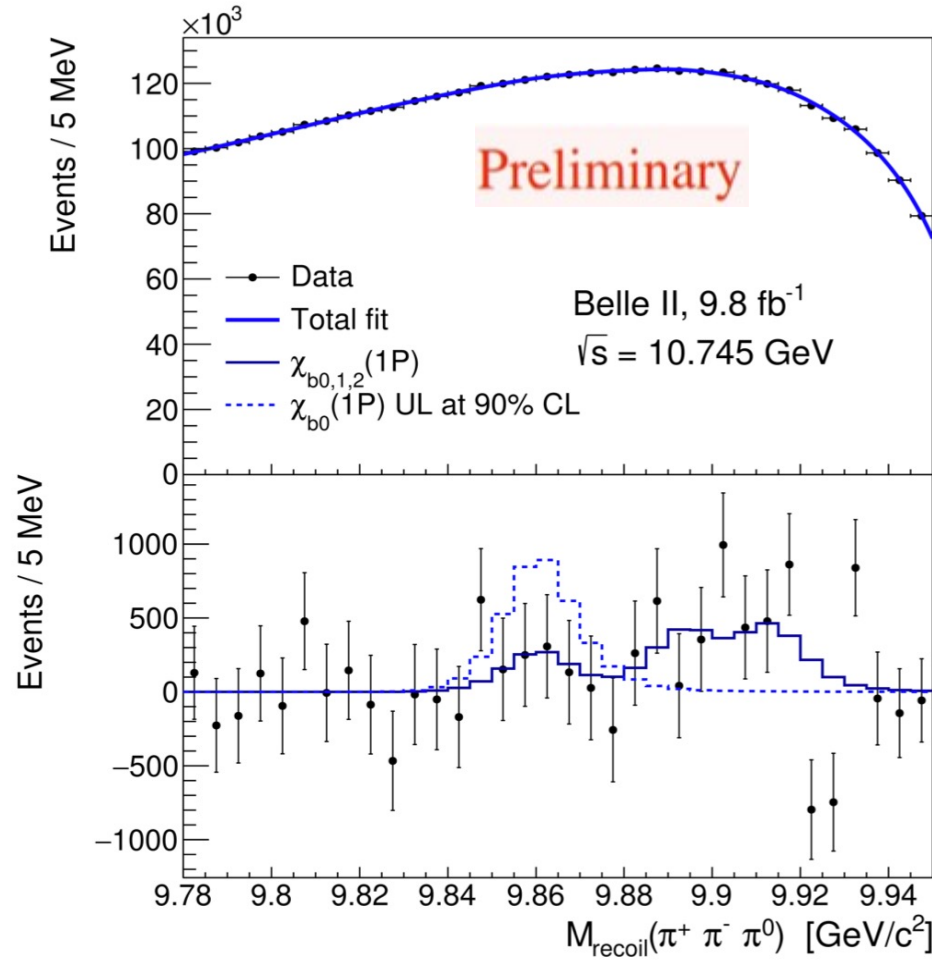
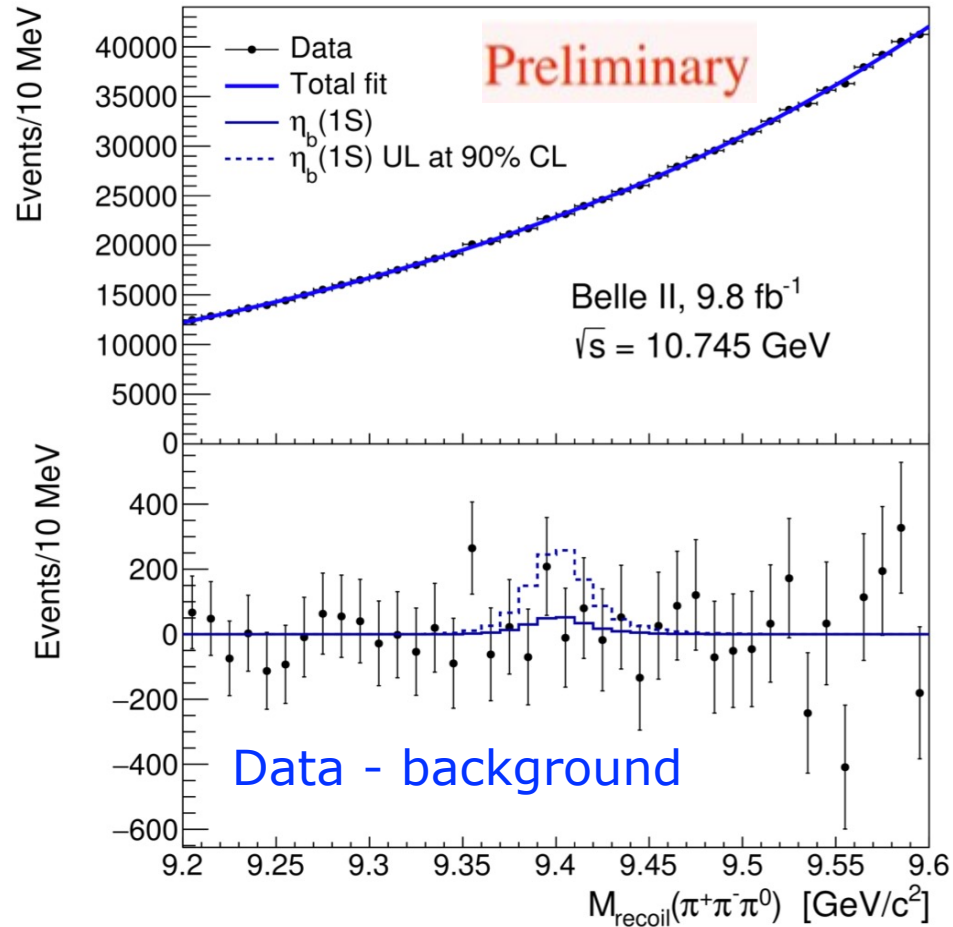


$9.2 < M_{\text{rec}}(\pi^+\pi^-\pi^0) < 9.6 \text{ GeV}/c^2$   
( $\eta_b(1S)$  included)

$9.78 < M_{\text{rec}}(\pi^+\pi^-\pi^0) < 9.95 \text{ GeV}/c^2$   
( $\chi_{bJ}(1P)$  included)

- A double-sided Crystal Ball + a Gaussian for  $\omega$  signal
- 2<sup>nd</sup> or 3<sup>rd</sup> order Chebyshev polynomials for backgrounds
- The purities of  $\omega$ -meson signals are 12.9% for  $\eta_b(1S)$  and 5.3% for  $\chi_{bJ}(1P)$

# Recoil mass spectra of $\pi^+\pi^-\pi^0$



- A 3<sup>rd</sup> polynomial for  $\eta_b(1S)$
- A product of a 4<sup>th</sup> polynomial and a square root function for  $\chi_{b0}(1P)$
- Polynomial orders are chosen with maximum p-values
- The yields for  $\chi_{b1}(1P)$  and  $\chi_{b2}(1P)$  are fixed [PRL 130, 091902 (2023)].

Channel	$e^+e^- \rightarrow \eta_b(1S)\omega$	$e^+e^- \rightarrow \chi_{b0}(1P)\omega$
Yield	$(0.23 \pm 0.49 \pm 0.25) \cdot 10^3$	$(1.2 \pm 1.4 \pm 0.9) \cdot 10^3$

No clear  $\eta_b(1S)$  and  $\chi_{b0}(1P)$  signals are observed.

# Born cross sections

$$\sigma_B[e^+e^- \rightarrow X\omega] = \frac{N \cdot |1 - \Pi|^2}{\varepsilon \cdot \mathcal{L} \cdot (1 + \delta_{\text{ISR}}) \cdot \mathcal{B}_{\text{int}}}$$

Preliminary

Channel	$e^+e^- \rightarrow \eta_b(1S)\omega$	$e^+e^- \rightarrow \chi_{b0}(1P)\omega$
Yield ( $10^3$ )	$0.23 \pm 0.49 \pm 0.25$	$1.2 \pm 1.4 \pm 0.9$
Born section section (pb)	$0.5 \pm 1.1 \pm 0.6$	$2.6 \pm 3.1 \pm 2.1$
Upper limit at 90% C.L. (pb)	$<2.5$	$<8.7$

Upper limits at the 90% CL are set using the Feldman-Cousins method [Phys. Rev. D 57, 3873 (1998)]

Tetraquark model in Ref. [CPC 43, 123102 (2019)]:

$$\Gamma(\Upsilon(10753) \rightarrow \eta_b(1S)\omega) = 2.64_{-1.69}^{+4.70} \text{ MeV}$$

$$\Gamma(\Upsilon(10753) \rightarrow \Upsilon\pi^+\pi^-) = 0.08_{-0.06}^{+0.20} \text{ MeV}$$

This measurement and JHEP 10, 220 (2019):

$$\sigma^B(\Upsilon(10753) \rightarrow \eta_b(1S)\omega) < 2.5 \text{ pb}$$

$$\sigma^B(\Upsilon(10753) \rightarrow \Upsilon(2S)\pi^+\pi^-) \approx (3 \pm 1) \text{ pb}$$

Our results do not support the prediction within the tetraquark model that the  $\Upsilon(10753) \rightarrow \omega\eta_b(1S)$  decay is enhanced.

# Summary

- We are at the beginning of a long program of quarkonium physics.
- The unique scan data near  $\sqrt{s} = 10.75$  GeV at Belle II provides an opportunity to understand the nature of the  $\Upsilon(10753)$  energy region, as well as the quarkonium spectroscopy.
- New decay modes of  $\Upsilon(10753) \rightarrow \omega\chi_{bJ}$  are observed for the first time [PRL 130, 091902 (2023)].
- The rapid increase of  $\sigma_{B^*\bar{B}^*}$  above the threshold may imply a resonance of  $B^*\bar{B}^*$  or  $b\bar{b}$ .
- The stringent upper limit is set for the  $e^+e^- \rightarrow \omega\eta_b(1S)$  at  $\sqrt{s} = 10.745$  GeV.

*Thanks for your attention!*