

Recent Belle II results related to flavour anomalies

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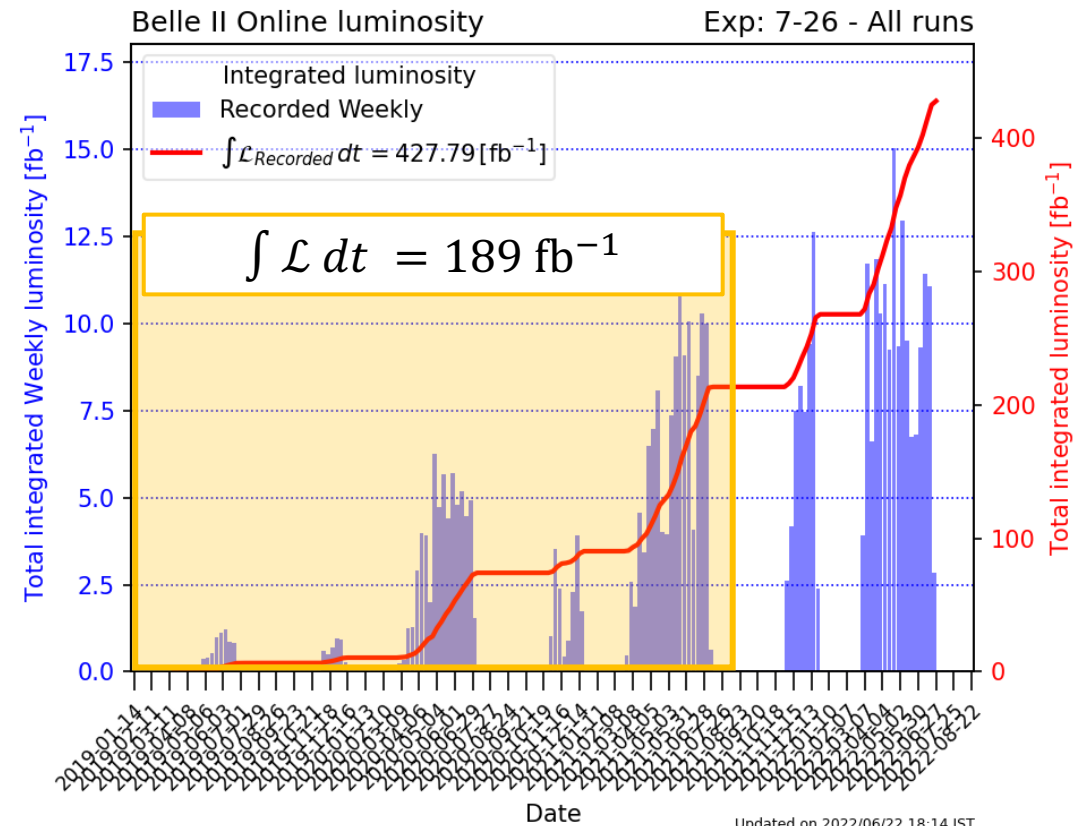
on behalf of the Belle II collaboration

30th Anniversary of the Rencontres du Vietnam

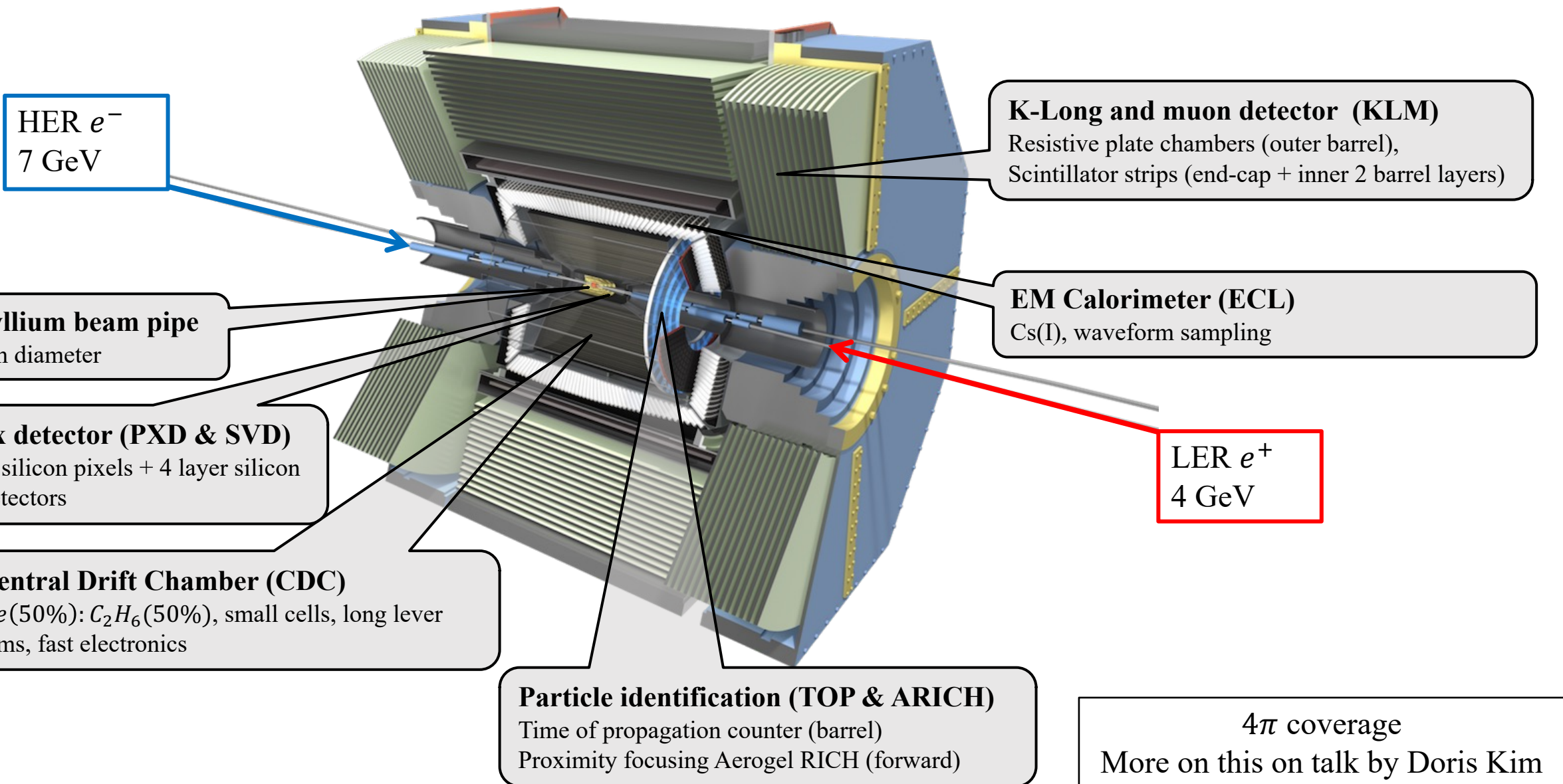
August 8th, 2023



- Electron-Positron (e^+e^-) collider
 e^- (7 GeV) \rightarrow \leftarrow (4 GeV) e^+
- E_{CM} at $\Upsilon(4S)$ resonance (10.58 GeV)
- B -factory $\Upsilon(4S) \rightarrow B\bar{B}$ (at least 96%)



The following Belle II measurements are done at $189 fb^{-1}$

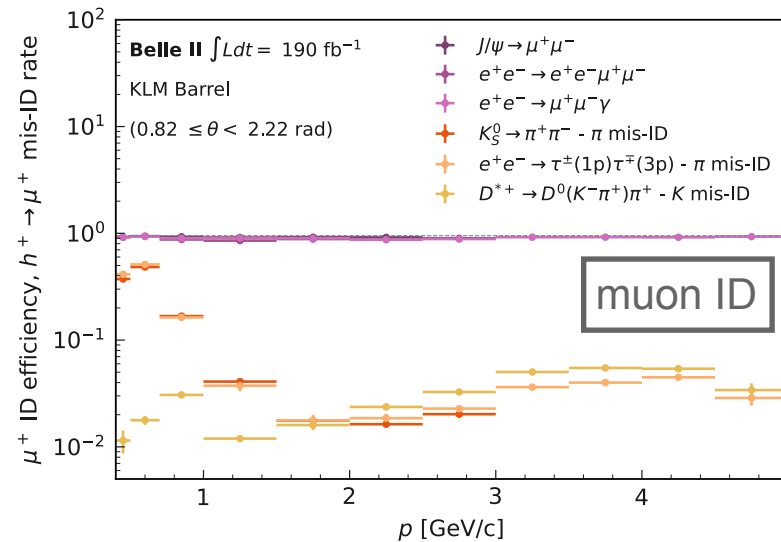
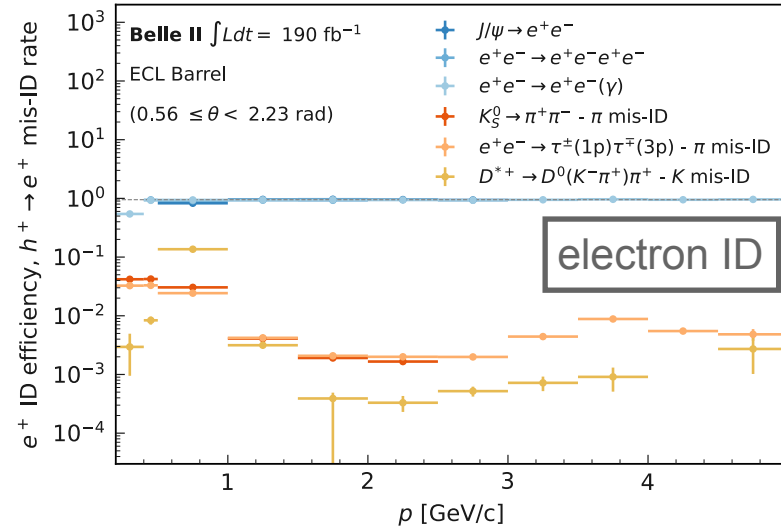


- Particle identification (PID) – identify “long-lived” particles passing through the detector by interacting with matter
- One of the most crucial part of determining the sensitivity of a measurement
- Lepton identification algorithm works based on likelihood ratio or BDT

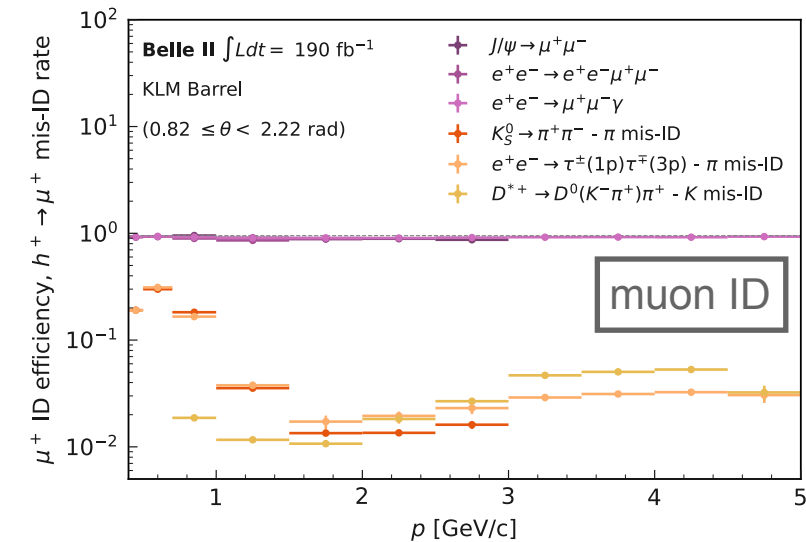
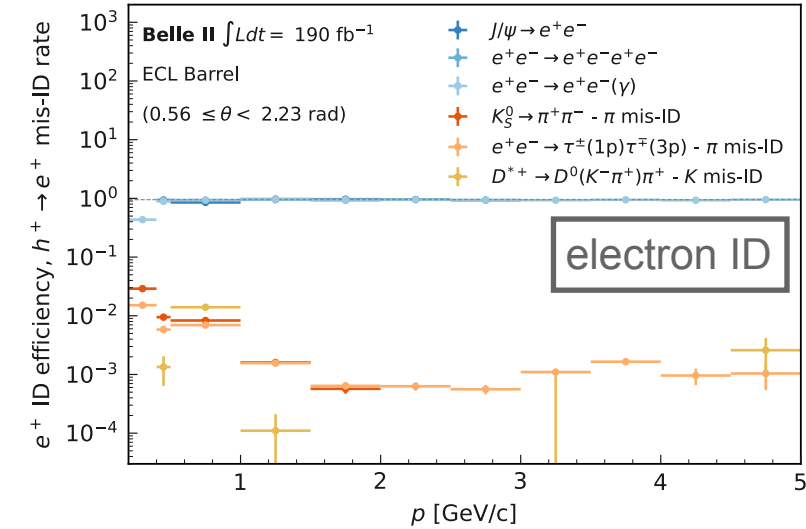
$$ID_{\mu} = \frac{\mathcal{L}_{\mu}}{\sum_i^{e, \mu, \pi, K, p, d} \mathcal{L}_i}$$

- New BDT-based lepton identification superior across the momentum spectrum, especially $< 0.6 \text{ GeV}/c$
- Data/MC correction factors have associated systematics for the efficiency at the 0.5-1.5% level

Likelihood Ratio



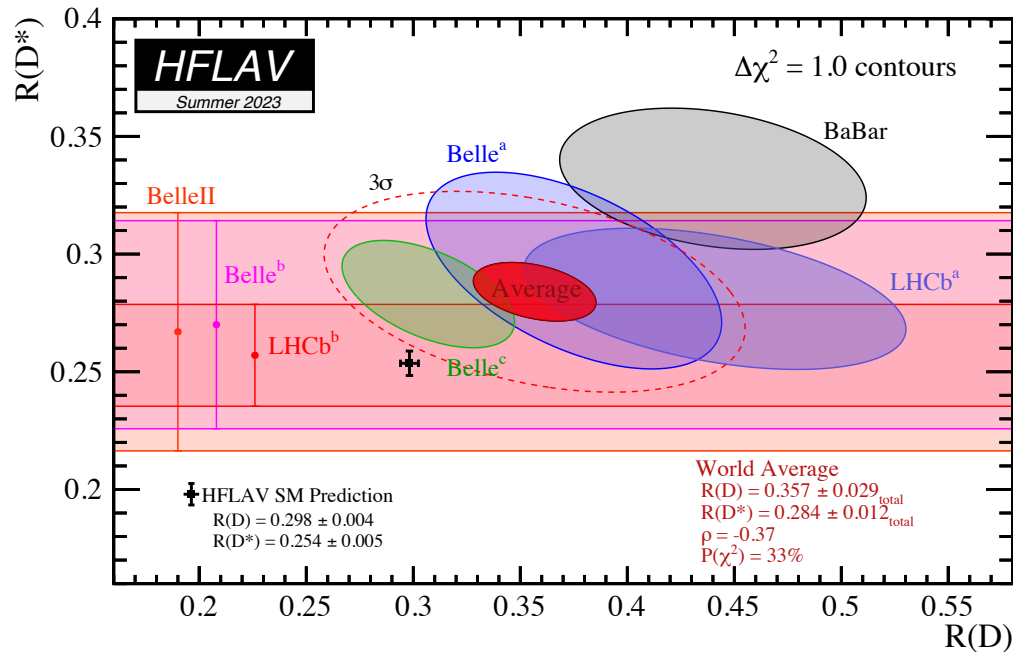
BDT-based



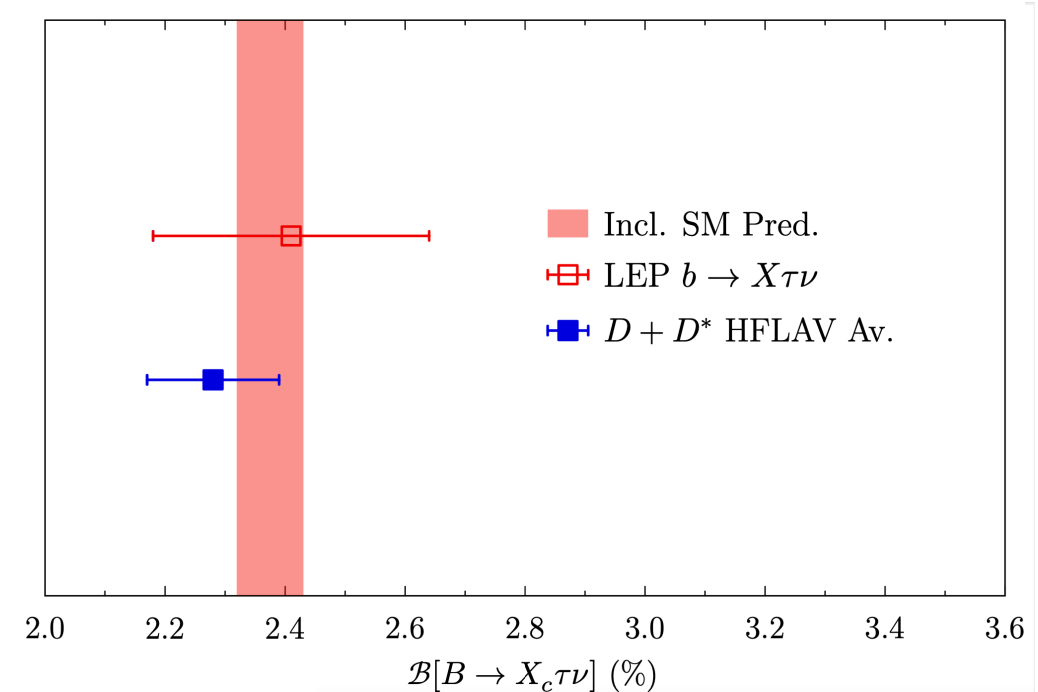
First $R(D^*)$ Measurement from Belle II

- Flavour anomalies have been observed due to deviations from the Standard model in processes involving leptons
- New physics could introduce additional interactions with each lepton, affecting the predicted rate of $b \rightarrow c$ decays
- New interactions involving the $b \rightarrow c$ quark transition can be probed in $R(D^{(*)})$ or $R(X_{\tau/\ell})$

$$R(D^{(*)}) = \frac{Br(B \rightarrow D^{(*)}\tau\nu)}{Br(B \rightarrow D^{(*)}\ell\nu)} \quad \longleftrightarrow \quad \ell \in \{e, \mu\} \quad \longleftrightarrow \quad R(X_{\tau/\ell}) = \frac{Br(B \rightarrow X\tau\nu)}{Br(B \rightarrow X\ell\nu)}$$



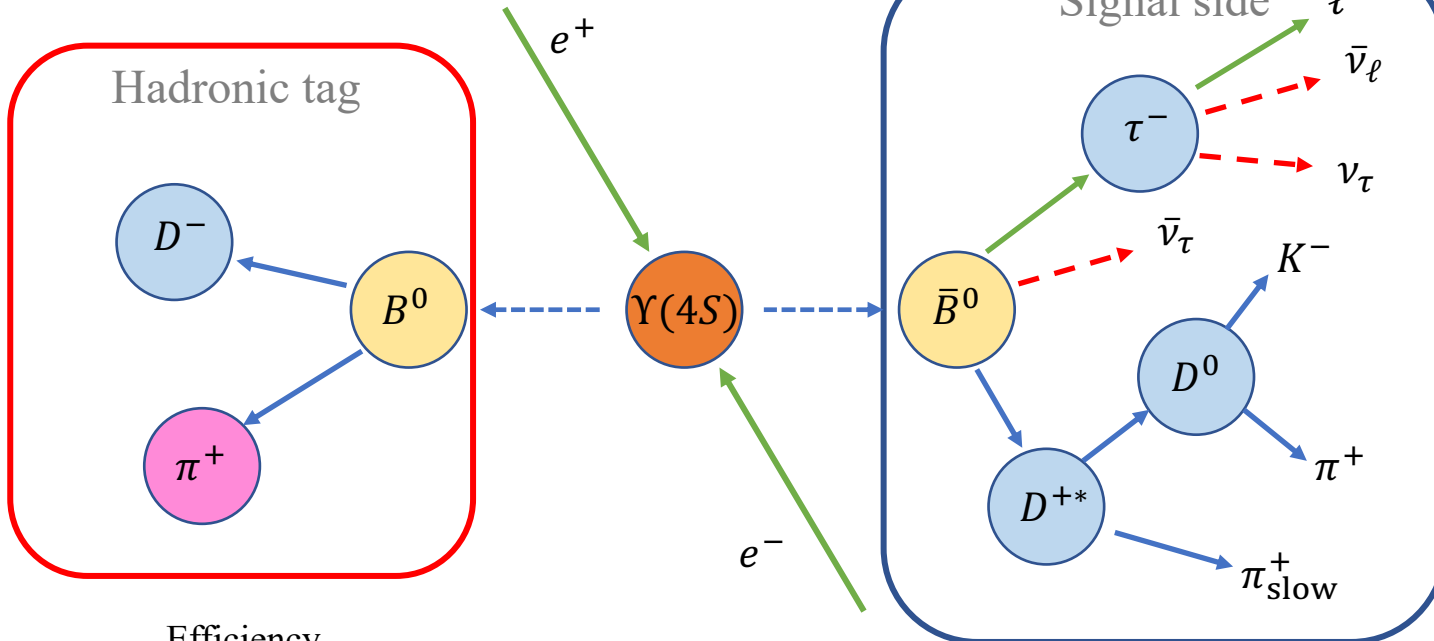
Tension with Standard model of $> 3\sigma$



Consistent with Standard Model expectation

Hadronic B-tagging
(Full Event Interpretation)

[Comp. and Soft. for Big Sci. 3, 6 \(2019\)](#)



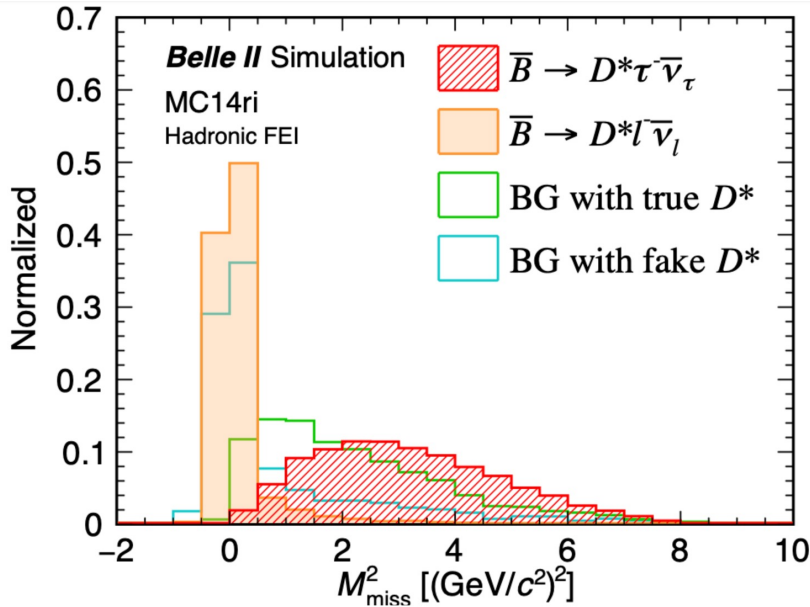
Efficiency
 B^0 : 0.27%, B^+ : 0.35%
[Belle II arXiv:2008.06096](#)

Precise knowledge of B_{tag} kinematics, strong kinematic reconstruction constraints for sig. side with 3 ν 's

Exclusive signal B modes
Reconstruct the signal-side B meson through specific decay channels

- Tag one B -meson from *hadronic* decays and analyse remaining B (**signal side**)
- Reconstruction of
 $\Rightarrow \overline{B^0} \rightarrow D^* \tau^- \bar{\nu}_\tau$
 $\Rightarrow \overline{B^0} \rightarrow D^* \ell^- \bar{\nu}_\ell, \ell \in \{e, \mu\}$
- Leptonic τ decays
- Three D^* decay channels:
 $\Rightarrow D^{*+} \rightarrow D^0 \pi^+$
 $\Rightarrow D^{*+} \rightarrow D^+ \pi^0$
 $\Rightarrow D^{*0} \rightarrow D^0 \pi^0$

- 2D extended binned maximum likelihood fit to missing mass squared (M_{miss}^2) and extra ECL energy (E_{ECL}^{extra})

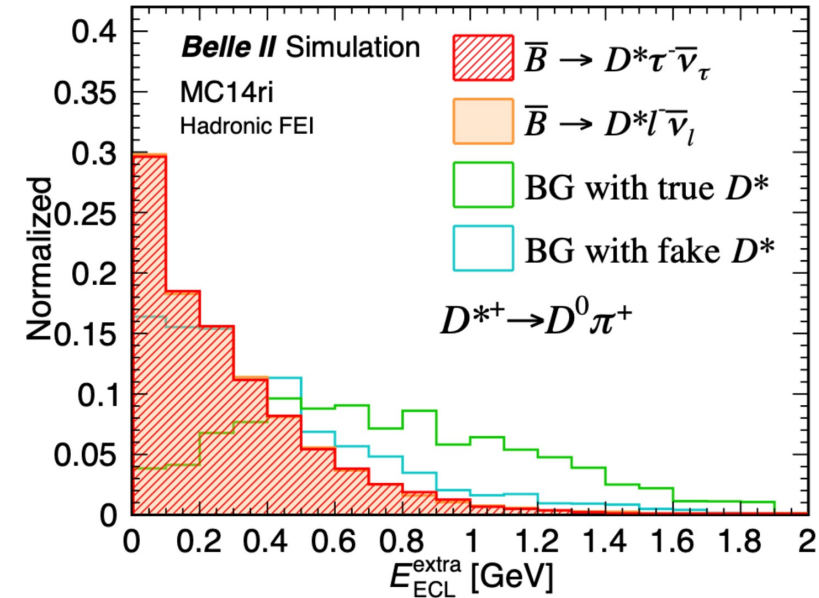


M_{miss}^2 distribution

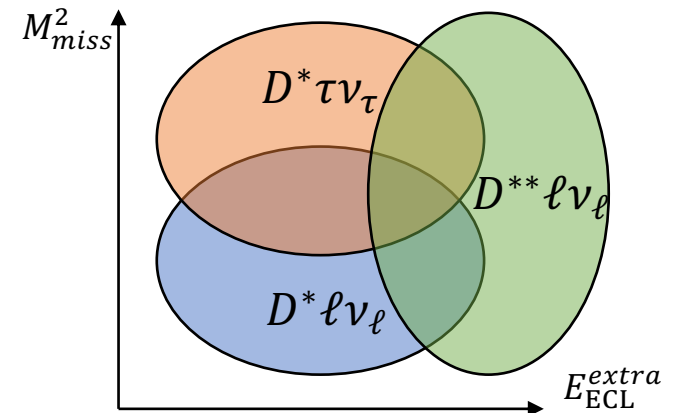
- $\bar{B} \rightarrow D^* \ell \nu$ events peak ~ 0 due to a single ν
- $\bar{B} \rightarrow D^* \tau \nu$ events larger M_{miss}^2 due to multiple ν from \bar{B}, τ
- Multiple ν causes broad peak $\bar{B} \rightarrow D^* \tau \nu$

E_{ECL}^{extra} distribution

- Background candidates have larger E_{ECL}^{extra} due to missing particles additional clusters



E_{ECL}^{extra} : Sum of cluster energy not used in reco.



$$M_{miss}^2 = (p_{e^+e^-} - p_{B_{tag}} - p_{D^*} - p_{\ell})^2$$

- Simultaneous fit the three D^* decays channels:

$$\Rightarrow D^{*+} \rightarrow D^0 \pi^+$$

$$\Rightarrow D^{*+} \rightarrow D^+ \pi^0$$

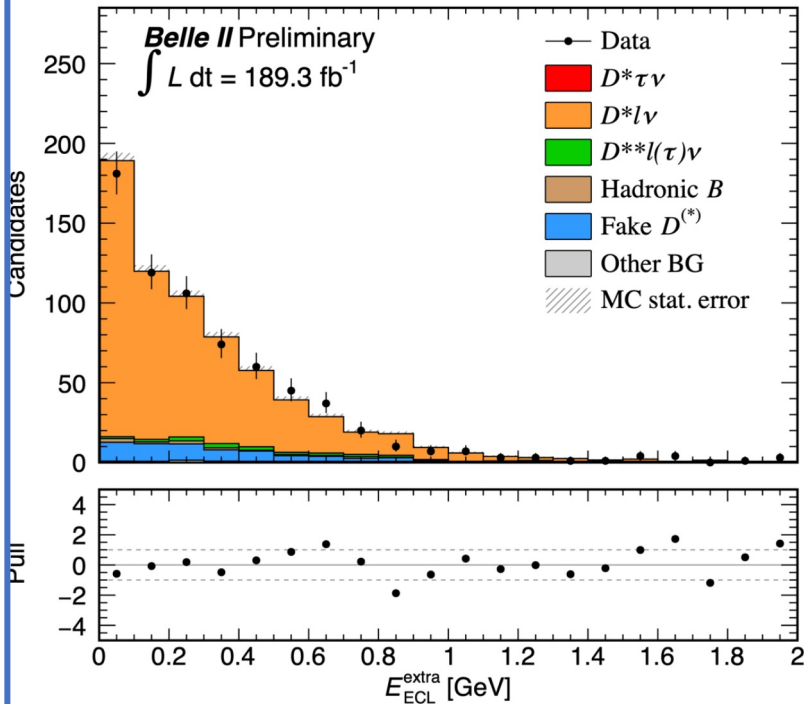
$$\Rightarrow D^{*0} \rightarrow D^0 \pi^0$$

- $R(D^*)$ extracted from fit using $R(D^*) = \frac{N_{D^* \tau \nu}}{(N_{D^* \ell \nu} / 2)} \cdot \frac{\varepsilon_{D^* \ell \nu}}{\varepsilon_{D^* \tau \nu}}$
 - N_{χ} : no. of χ events extracted from fit
 - ε_{χ} : reconstruction efficiency for χ events

$\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$ and major background contributions from $\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$ and fake D^* in three side-band regions are evaluated.

q^2 [GeV²/c²] side band for $\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$

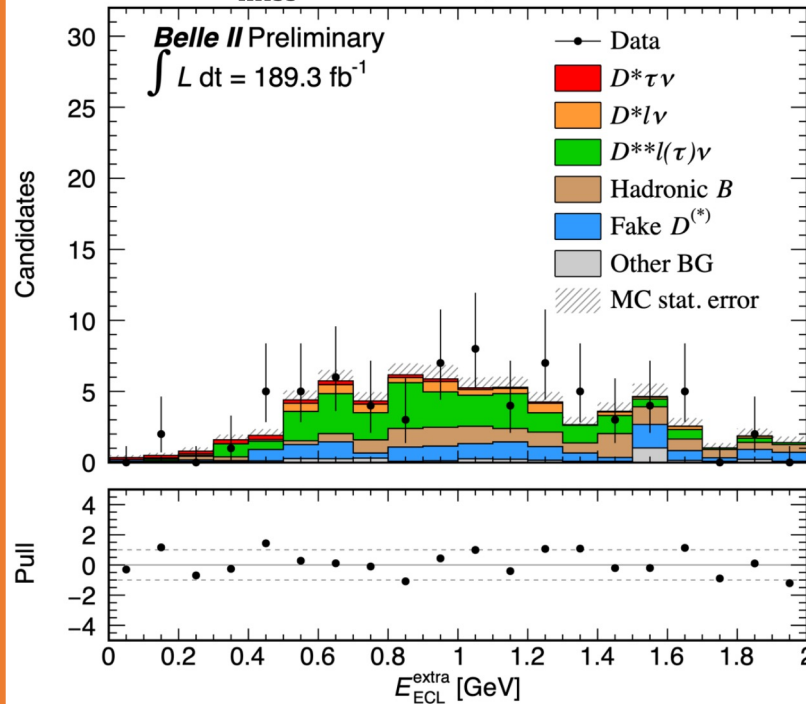
- $q^2 = (p_\ell + p_\nu)^2 < 3.5$ GeV
- Below m_τ threshold



$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$ enhanced side band

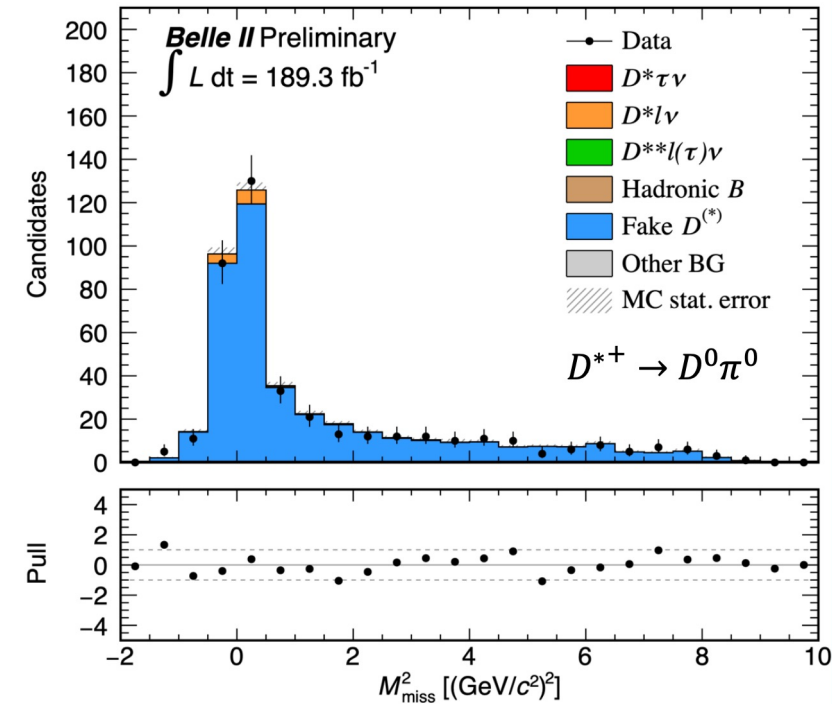
- An additional π^0 is required to $B\bar{B}$
- $\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$ have unknown rates and can mimic $\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau$

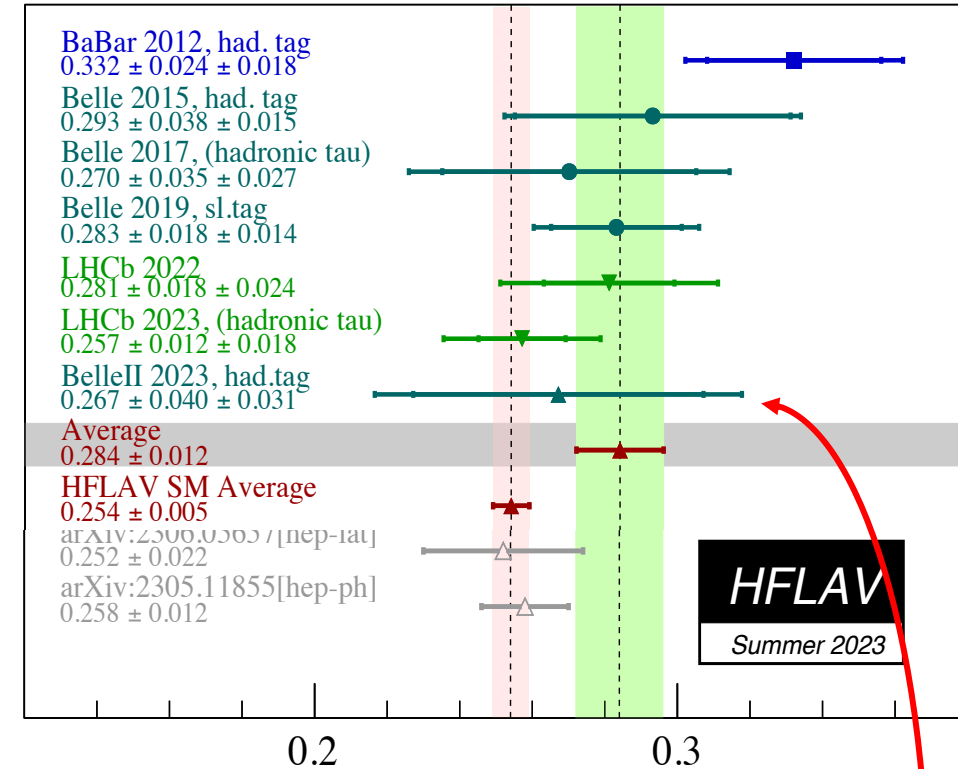
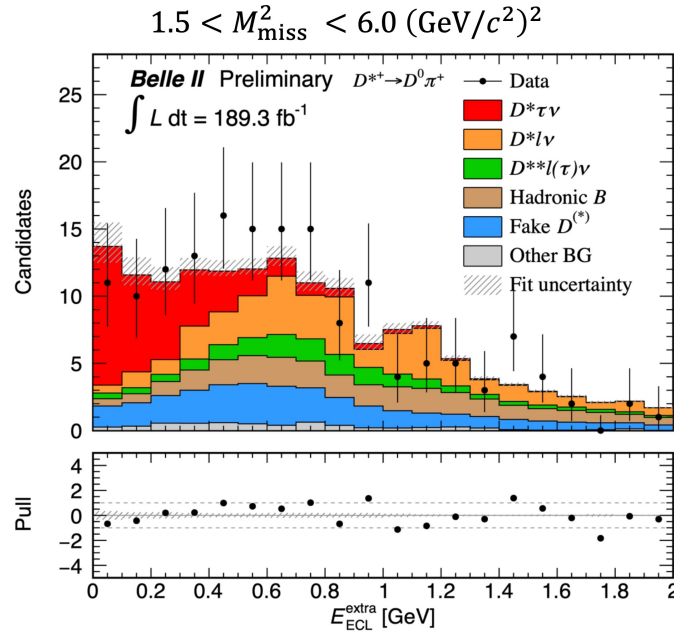
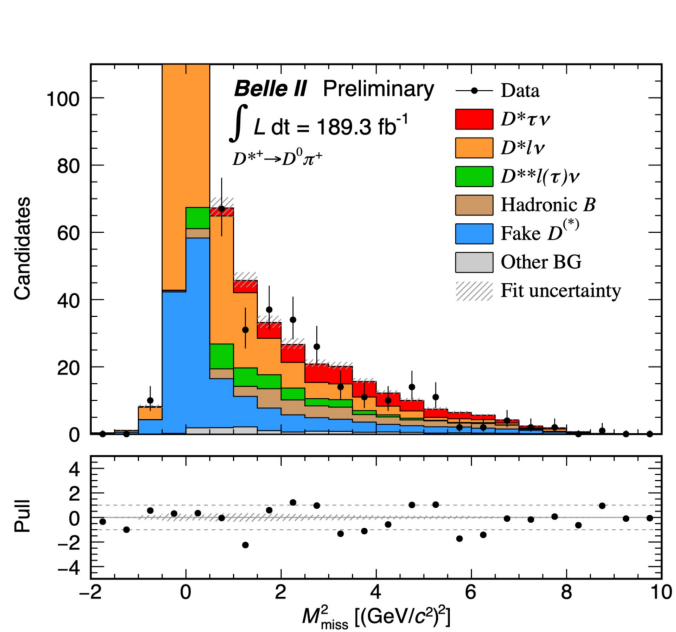
$$1.0 < M_{\text{miss}}^2 < 5.0 \text{ (GeV/c}^2\text{)}^2$$



$\Delta M_{D^*} = (M_{D^*} - M_D)$ side bands for fake D^*

- Constrain the fake D^* yields in the signal regions with calibration factors at the ΔM_{D^*} side bands.





- First $R(D^*)$ result from Belle II

$$R(D^*) = 0.267^{+0.041}_{-0.039} (\text{stat.}) \quad ^{+0.028}_{-0.033} (\text{syst.})$$

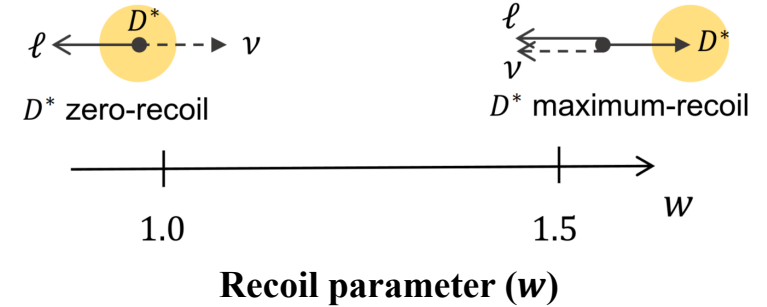
- 40% improvement in statistical precision over Belle result at the same sample size
- Systematic uncertainties dominated by PDF uncertainties and simulated sample size
- Result consistent with both SM prediction and HFLAV average

This measurement

Light-lepton Universality test in angular asymmetries

- Beyond the Standard Model effects in $R(D^{(*)})$ could affect angular asymmetries in $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$ [[Phys. Rev. D 106, 096015 \(2022\)](#)]
- This effect could induce a violation of the light-lepton (e, μ) flavour universality
- Five angular asymmetries of e, μ in $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$ are tested via the difference in angular observables:

$$\Delta \mathcal{A}_x(w) = \mathcal{A}_x^e(w) - \mathcal{A}_x^\mu(w)$$



Angular Observable

$$\mathcal{A}_x(w) = \left(\frac{d\Gamma}{dw} \right)^{-1} \left[\int_0^1 - \int_{-1}^0 \right] dx \frac{d^2\Gamma}{dw dx}$$

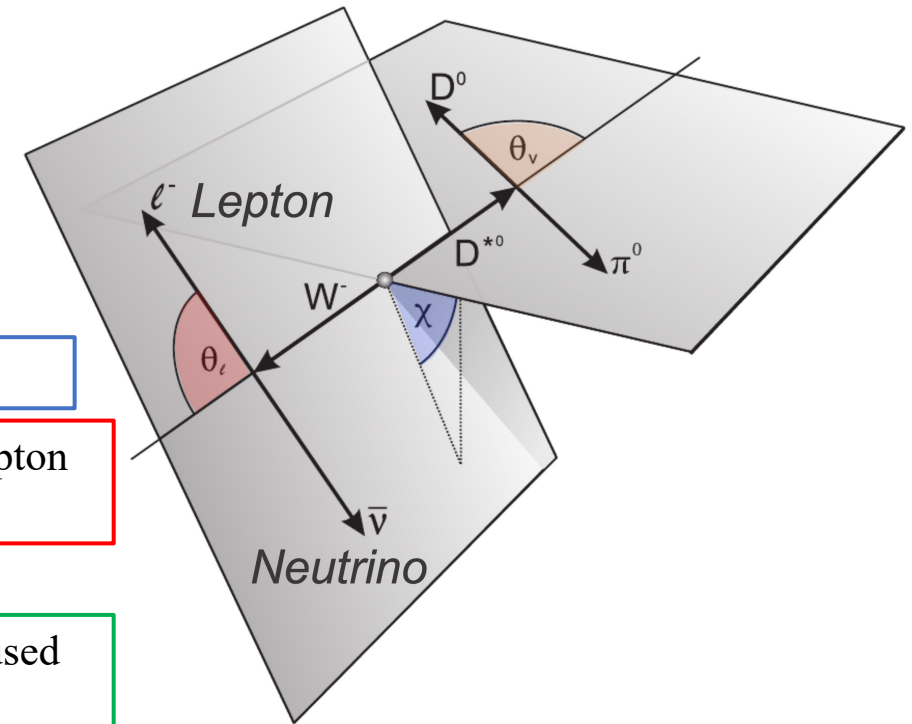
$$w = \frac{m_B^2 + m_{D^*}^2 - (p_B - p_{D^*})^2}{2m_B m_{D^*}}$$

$\mathcal{A}_x(w)$	dx
$A_{FB}(w)$	$d(\cos \theta_\ell)$
$S_3(w)$	$d(\cos 2\chi)$
$S_5(w)$	$d(\cos \chi \cos \theta_V)$
$S_7(w)$	$d(\sin \chi \cos \theta_V)$
$S_9(w)$	$d(\sin 2\chi)$

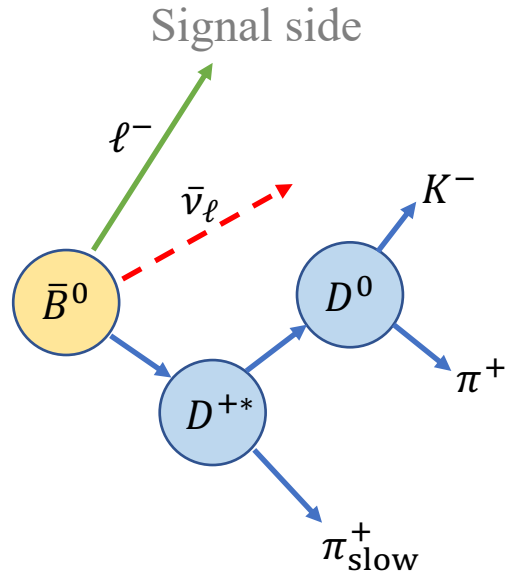
Commonly analysed

Highly sensitive to lepton flavour universality

Reduced sensitivity, used as control



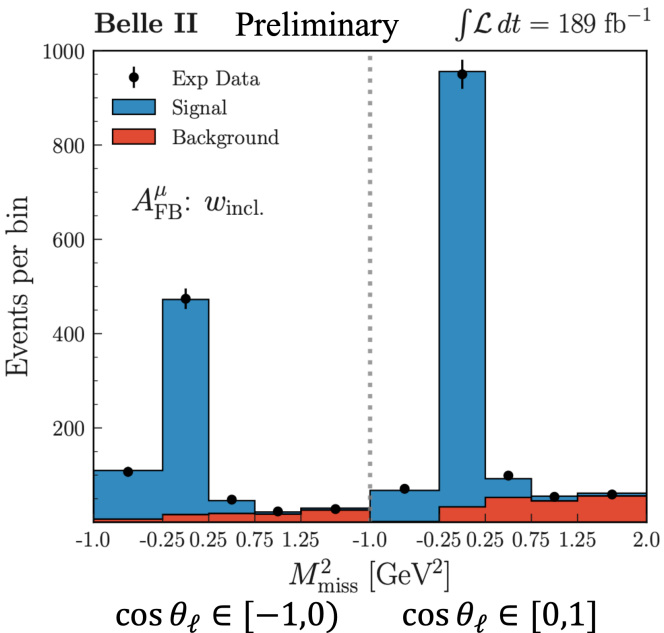
Helicity Angles ($\theta_\ell, \theta_V, \chi$)



- Tag one B -meson from *hadronic* decays – same as $R(D^*)$
- Analyse remaining B -meson(**signal side**)
- Reconstruction of

$$\Rightarrow \bar{B}^0 \rightarrow (D^{*+} \rightarrow D^0 \pi^+) \ell^- \bar{\nu}$$

- Require momentum of lepton above 0.4 GeV
- No tracks remaining apart from the ones used in reconstruction
- Constrain mass of D^{*+} to be as close as possible to PDG value for each event

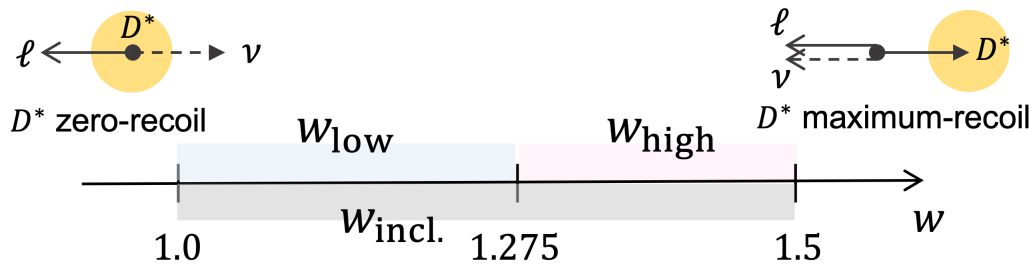


- The first universality test using a full set of angular observables as function of recoil w
- 1D binned maximum-likelihood fit to missing mass squared (M_{miss}^2)
- To maximise sensitivity to SM extensions, w separated into $w_{low}, w_{high}, w_{incl}$

$$\mathcal{A}_x(w) = \left(\frac{d\Gamma}{dw}\right)^{-1} \left[\int_0^1 - \int_{-1}^0 \right] dx \frac{d^2\Gamma}{dw dx}$$

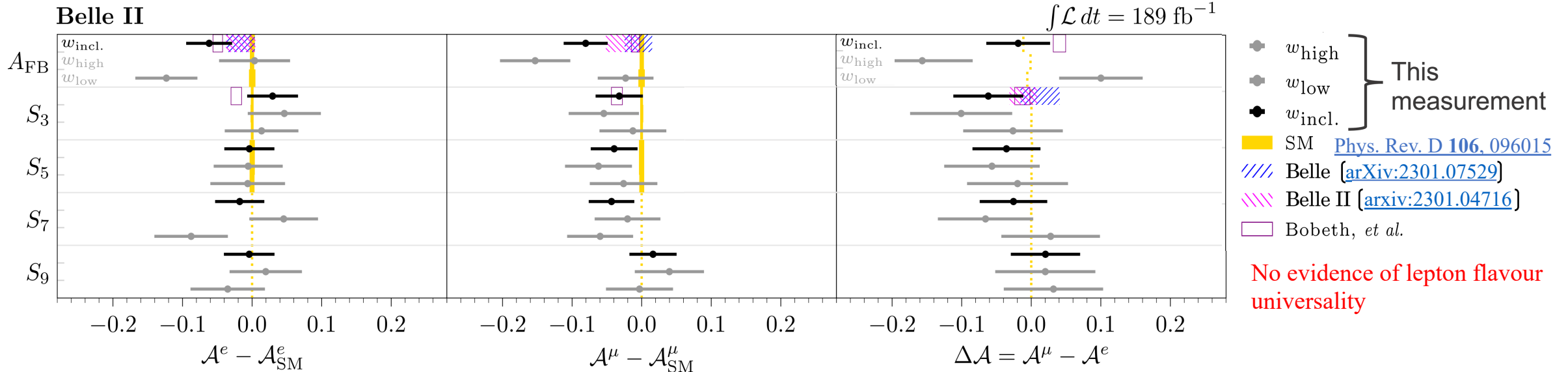
$$M_{miss}^2 = (p_{e^+e^-} - p_{B_{tag}} - p_{D^*} - p_\ell)^2$$

$$A_{FB}: dx = d(\cos \theta_\ell)$$



$\chi^2 / N_{dof} = 2.0/3$ ($p = 0.57$) on $A_{FB}, S_3, S_5 - w_{incl}$
 $\chi^2 / N_{dof} = 10.2/6$ ($p = 0.13$) on $A_{FB}, S_3, S_5 - w_{high,low}$

- Compare asymmetries between e, μ using $\Delta\mathcal{A}_x(w) = \mathcal{A}_x^e(w) - \mathcal{A}_x^\mu(w)$

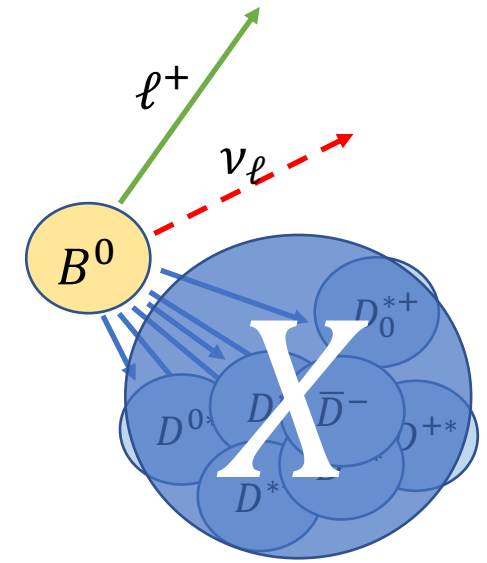
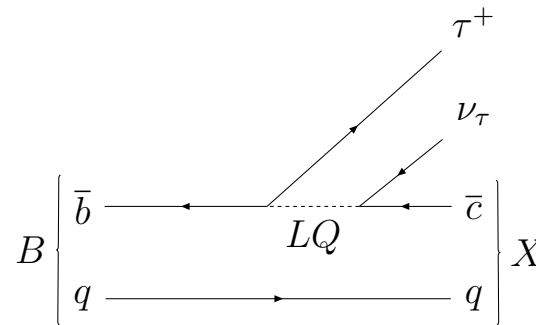
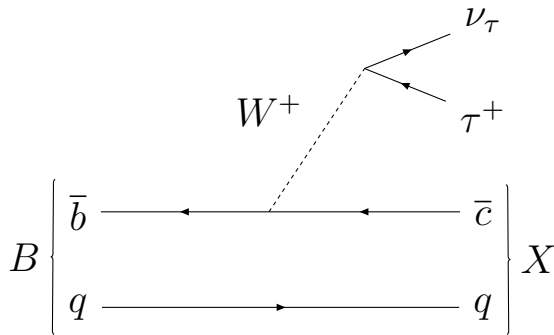


Light-lepton Universality test in $R(X_{e/\mu})$

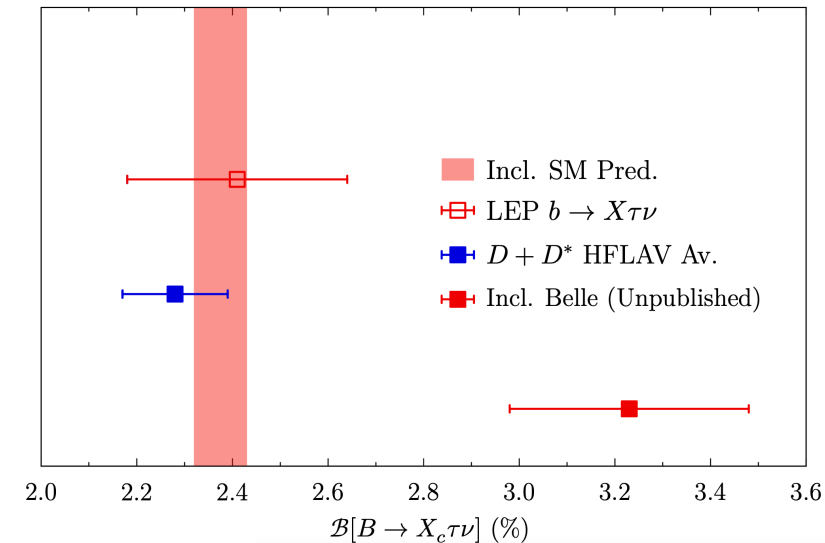
- As a first step towards measuring $R(X_{\tau/\ell})$, we measure $R(X_{e/\mu})$
- Beyond the Standard Model effects in $R(X_{\tau/\ell})$ could affect the light lepton ratio in $R(X_{e/\mu})$

$$R(X_{e/\mu}) = \frac{Br(B \rightarrow X e \nu)}{Br(B \rightarrow X \mu \nu)}$$

- X is the hadronic final state of semileptonic decay from $b \rightarrow c \ell \nu$, rarely $b \rightarrow u \ell \nu$
- Various leptoquark models have been presented to explain anomalies in $b \rightarrow c \ell \nu$



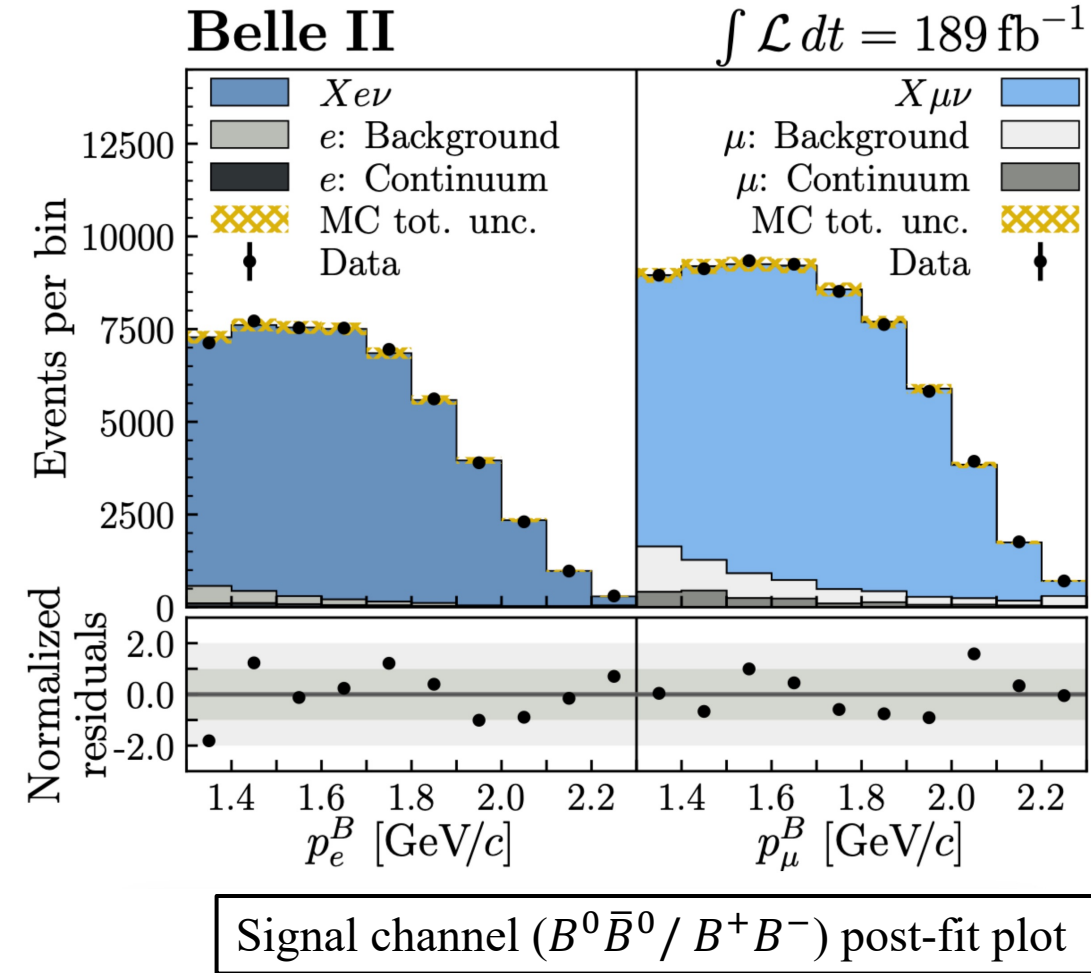
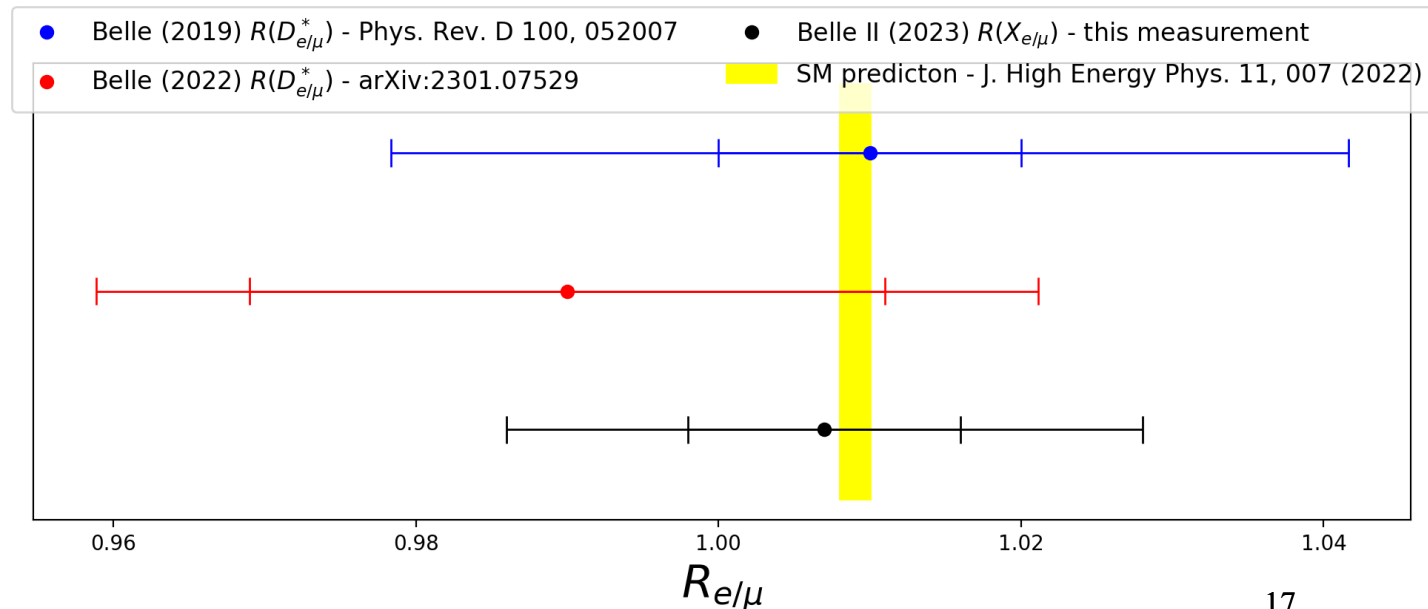
- Deviations from 1 in $R(X_{e/\mu})$ may indicate the presence of New Physics
- Inclusive reconstruction of the charm system signal-side B
- $p_\ell^B > 1.3$ GeV/c to suppress background



- 1D binned maximum-likelihood fit to lepton momentum of signal B rest-frame
- Control channel ($B^0 B^0 / B^+ B^+$) constrains background yield in signal channel ($B^0 \bar{B}^0 / B^+ B^-$) through simultaneous fit
- e and μ templates are fitted simultaneously in **10 p_ℓ^B bins** each

$$R(X_{e/\mu}) = 1.007 \pm 0.009 \text{ (stat.)} \pm 0.019 \text{ (sys.)}$$

- ✓ **Most precise LFU test with semileptonic B decays to date!**
- ✓ Measurement systematically limited by lepton ID-based uncertainties



Lepton Flavour Universality tests shed light on $b \rightarrow c$ decays anomalies.

Current deviations from the Standard Model expectations of $> 3\sigma$ characterise these anomalies.

Belle II performed three measurements to test lepton flavour universality:

- The first $R(D^*)$ result from Belle II

$$R(D^*) = 0.267^{+0.041}_{-0.039}(\text{stat.})^{+0.028}_{-0.033}(\text{syst.})$$

Consistent with both SM prediction and HFLAV average

- The first universality test using angular observables as function of recoil w

Consistent with Standard Model prediction

- The most precise Lepton Flavour Universality test with semileptonic B -decays to date

$$R(X_{e/\mu}) = 1.007 \pm 0.009(\text{stat.}) \pm 0.019(\text{syst.})$$

Consistent with Standard Model prediction

Thank you for listening!

Table 8.1: Summary of systematic uncertainties on $R(D^*)$.

Source	Uncertainty
E_{ECL} PDF shapes	+5.5% -9.3%
MC statistics	+7.0% -7.0%
Kernel density estimation	+1.0% -1.0%
$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$ branching ratios	+4.7% -2.7%
Reconstruction efficiency	+2.0% -2.0%
Hadronic B decay branching ratios	+1.6% -2.4%
M_{miss}^2 PDF shapes	+0.0% -0.6%
Form factors	+0.5% -0.1%
Peaking background on ΔM_{D^*}	+0.4% -0.4%
E_{ECL} fit range	+0.1% -0.1%
Total systematic uncertainty	+10.4% -12.4%

Obs.	w bin	Total	Stat.	MC stat.	LID	π_{slow}
A_{FB}^e	w_{low}	0.045	0.042	0.015	0.004	0.001
	w_{high}	0.051	0.048	0.017	0.004	0.001
	$w_{\text{incl.}}$	0.033	0.031	0.011	0.004	0.001
A_{FB}^μ	w_{low}	0.040	0.038	0.013	0.001	0.001
	w_{high}	0.051	0.048	0.016	0.002	0.001
	$w_{\text{incl.}}$	0.032	0.030	0.010	0.001	0.001
ΔA_{FB}	w_{low}	0.060	0.056	0.020	0.004	0.001
	w_{high}	0.073	0.068	0.024	0.004	0.001
	$w_{\text{incl.}}$	0.046	0.043	0.015	0.004	0.001