



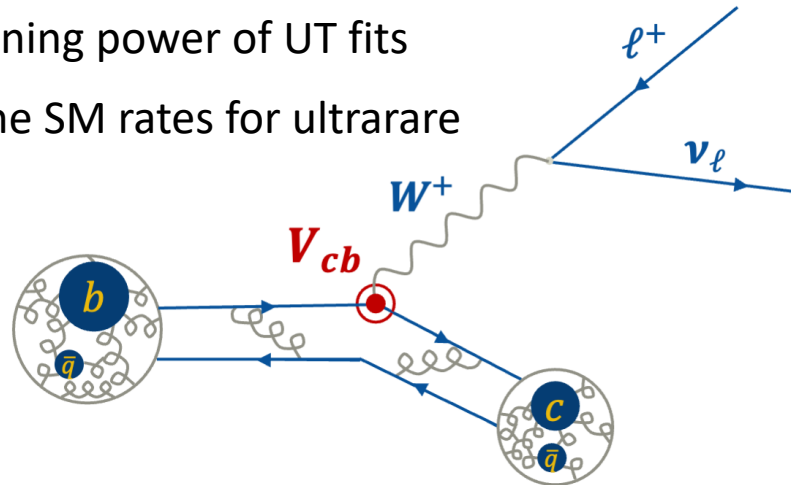
MORIOND QCD: MARCH 28, 2023

# SEMILEPTONIC $B$ -MESON DECAYS INCLUDING $b \rightarrow c$ ANOMALIES AT BELLE II

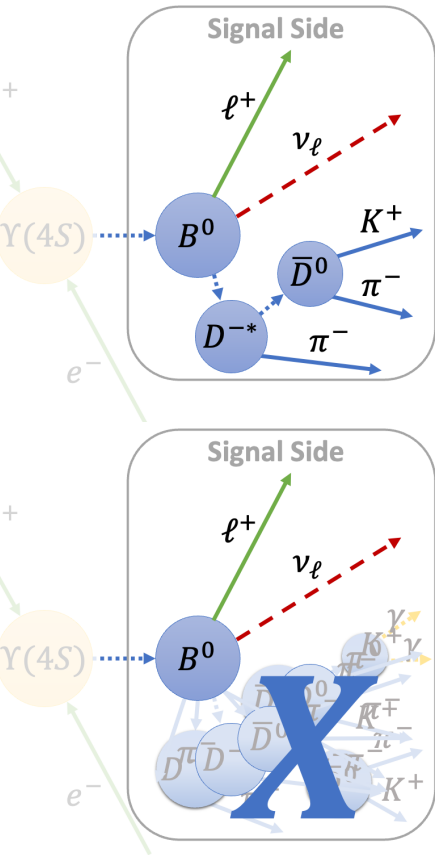
Henrik Junkerkalefeld\* on behalf of the collaboration

# $|V_{cb}|$ & $|V_{ub}|$ MEASUREMENTS

- SL  $B$  decays are studied to **determine the CKM elements  $|V_{cb}|$  and  $|V_{ub}|$** 
  - $|V_{xb}|$  are limiting the global constraining power of UT fits
  - Important inputs in predictions of the SM rates for ultrarare decays such as  $K \rightarrow \pi\nu\nu$



# EXPERIMENTAL STATUS $|V_{cb}|$ AND $|V_{ub}|$

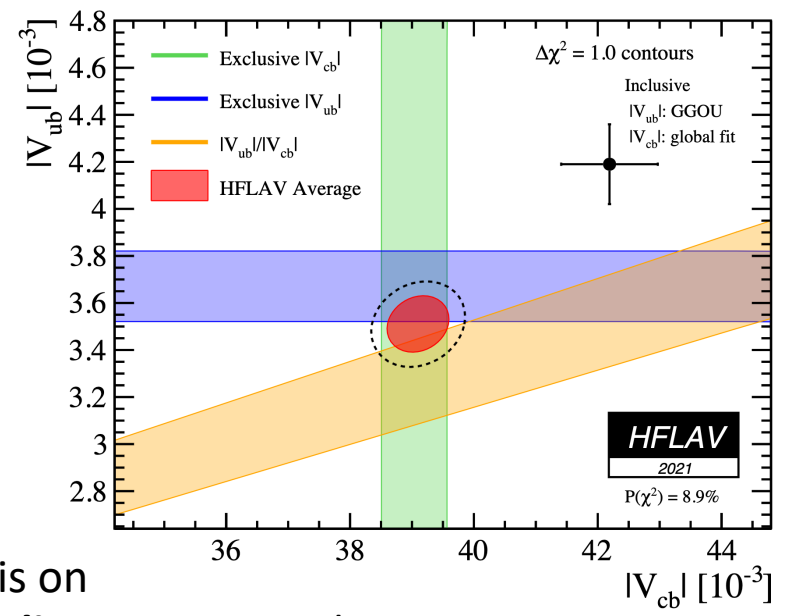


Experimentally clean  
Theoretically challenging

- Determination of both  $|V_{cb}|$  &  $|V_{ub}|$  exhibit a discrepancy at the level of  $\approx 3\sigma$  between **exclusive** (from a single final state) and **inclusive** (sensitive to all final states)

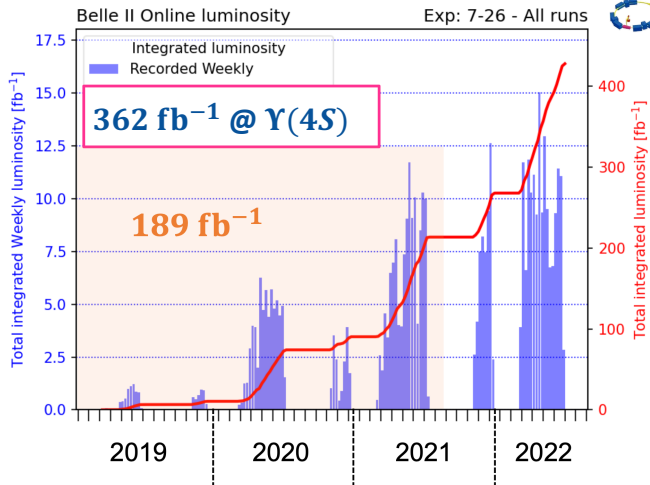
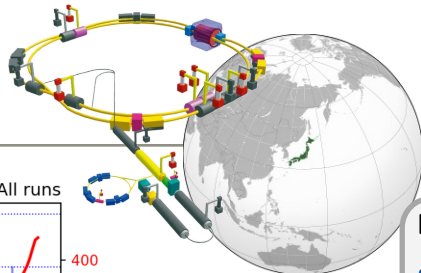
Experimentally challenging  
Theoretically clean

- The current experimental **focus** is on **understanding** the origin of **this discrepancy**, as this inconsistency limits the power of precision flavor physics



# SUPERKEKB

# & BELLE II DETECTOR



- Asymmetric  $e^+e^-$  collider at (and near)  $E_{c.m.} = 10.58$  GeV (resonant  $\Upsilon(4S)$  production)
- $\int L dt = 424 \text{ fb}^{-1}$  on tape (similar to BaBar's dataset)

## EM Calorimeter:

- **$e$  identification:**  
1 – 0.01 %  $\pi, K$  fake rate at  $\epsilon_e = 95$  %

Nearly  $4\pi$  coverage to reconstruct inclusive states & neutrinos

## Particle Identification:

- **$K/\pi$  identification**  
(1.8 %  $\pi$  fake rate at  $\epsilon_K = 90$  %)

$e^-$  (7 GeV)

$e^+$  (4 GeV)

## Vertex detectors:

- **Vertex resolution**  
 $\approx 15 \mu\text{m}$

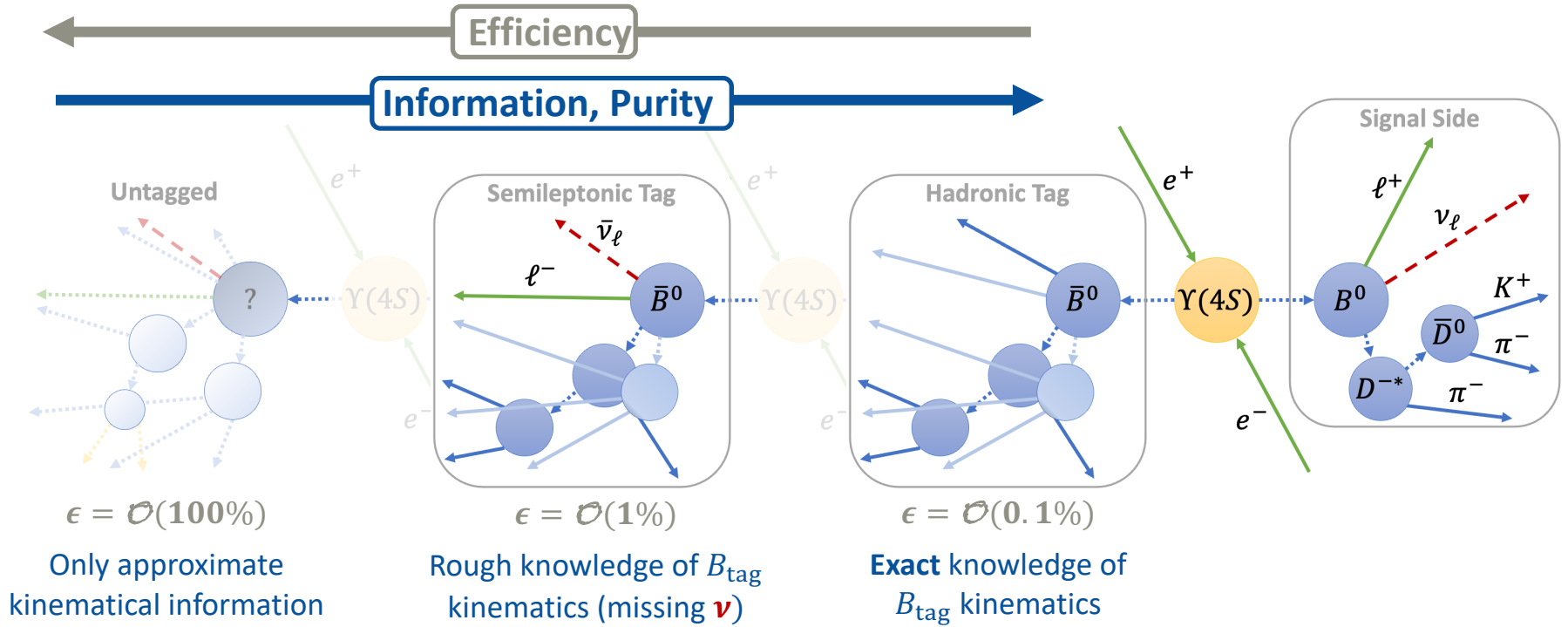
## $K_L$ and $\mu$ detector:

- **$\mu$  identification:** 2 – 1 %  $\pi, K$  fake rate at  $\epsilon_\mu = 95$  %

## Central Drift Chamber:

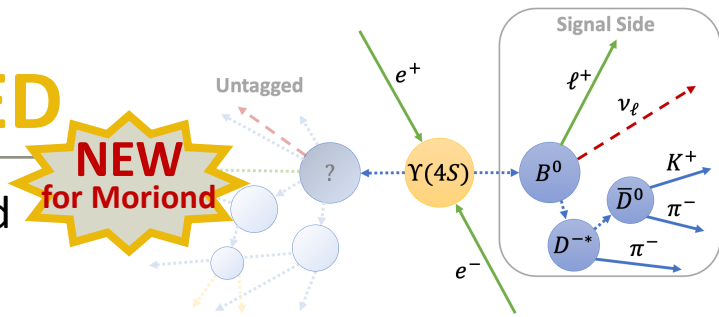
- **$p_T$  resolution**  $\approx 0.4$  %

# B-MESON FLAVOR TAGGING



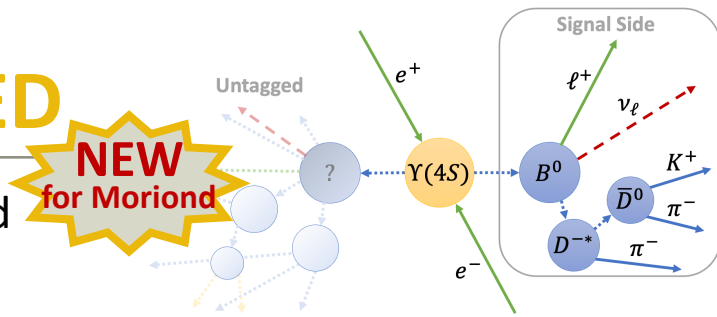
# $|V_{cb}|: B^0 \rightarrow D^{*-} \ell^+ \nu$ UNTAGGED

- Challenging due to lack of clean kinematic signatures and missing knowledge of the  $B_{\text{sig}}$  direction



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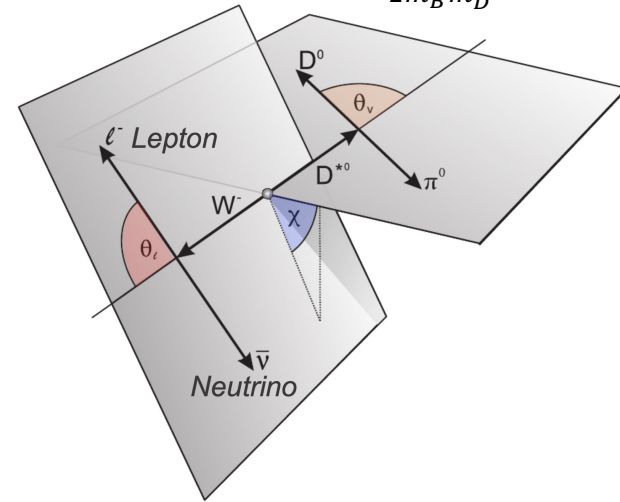


## $|V_{cb}|$ extraction and decay parametrization

$$\frac{d^4\Gamma}{dw d\cos\theta_\ell d\cos\theta_V d\chi} \propto |V_{cb}|^2 \times F^2(w, \cos\theta_\ell, \cos\theta_V, \chi)$$

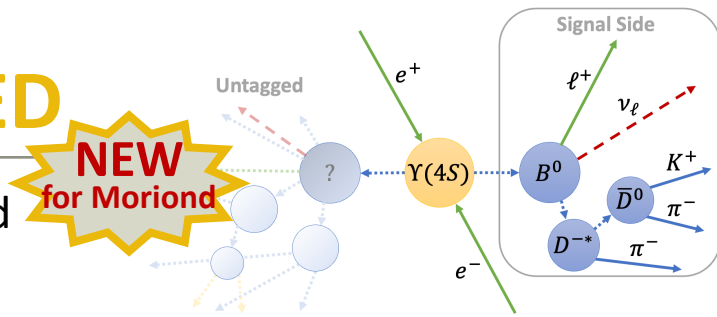
3 form factors as functions of  $w$   
parametrize the non-perturbative physics

Recoil parameter  $w = \frac{m_B^2 + m_{D^{*0}}^2 - q^2}{2m_B m_{D^{*0}}}$



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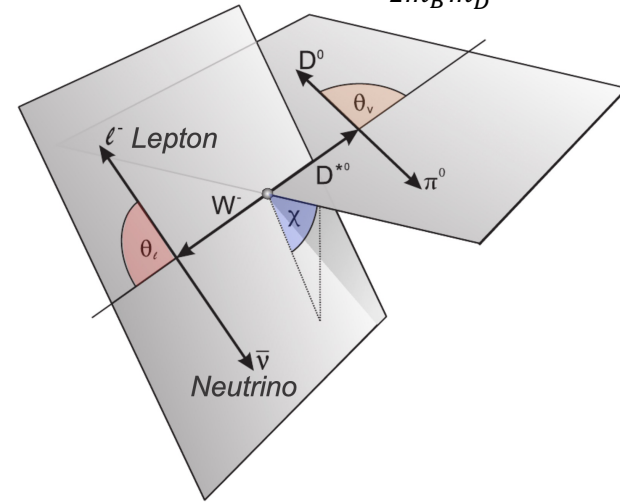


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3 form factors as functions of  $w$   
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Recoil parameter  $w = \frac{m_B^2 + m_{D^{*0}}^2 - q^2}{2m_B m_{D^{*0}}}$



The  $B_{\text{sig}}$  direction is estimated in a **novel approach** using

- The known **angle  $\cos\theta_{BY}$**  between the  $B_{\text{sig}}$  and the  $Y = D^* + \ell$

$$\cos\theta_{BY} = \frac{2E_B^{\text{c.m.}} E_Y^{\text{c.m.}} - m_B^2 c^4 - m_Y^2 c^4}{2|\vec{p}_B^{\text{c.m.}}| |\vec{p}_Y^{\text{c.m.}}| c^2}$$

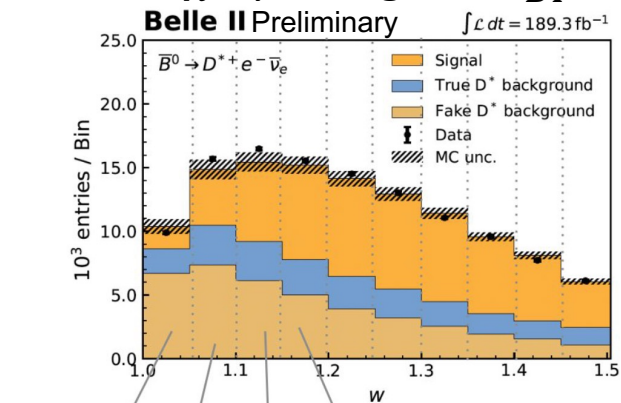
- inclusive information** of the **untagged event side**
- the **angular distribution** of  $Y(4S) \rightarrow B\bar{B}$  w.r.t. the beam axis



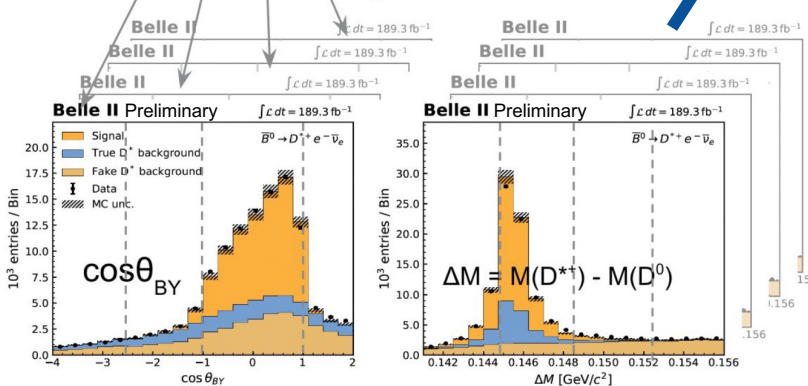
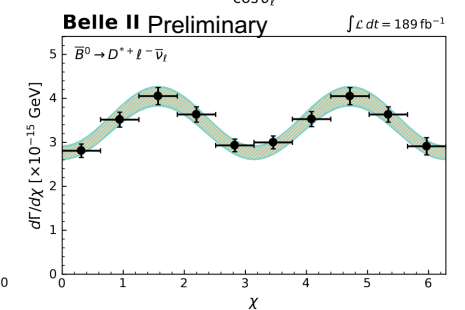
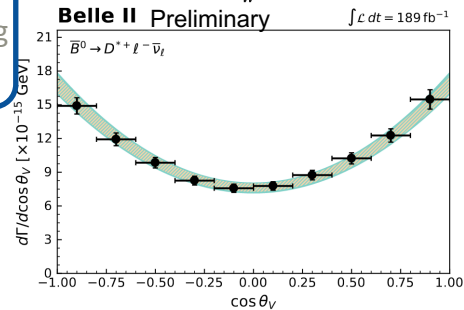
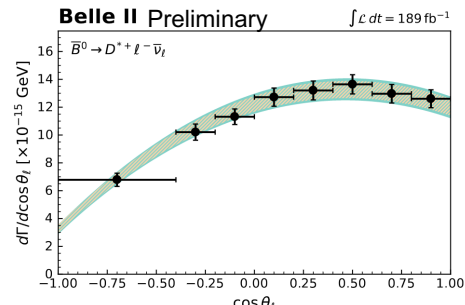
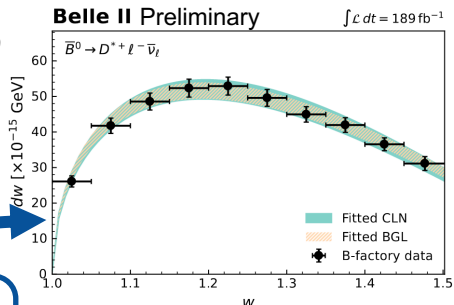
# $|V_{cb}|: B^0 \rightarrow D^{*-} \ell^+ \nu$ UNTAGGED



- The yield is extracted in 10 (8) bins of  $w$ ,  $\cos \theta_\ell$ ,  $\cos \theta_\nu$  and  $\chi$  by fitting  $\cos \theta_{BY}$  and  $\Delta M = M_{D^{*-}} - M_{D^0}$



Bin-to-bin migration corrected with SVD unfolding  
[arXiv:hep-ph/9509307](https://arxiv.org/abs/hep-ph/9509307)



# $|V_{cb}|: B^0 \rightarrow D^{*-} \ell^+ \nu$ UNTAGGED



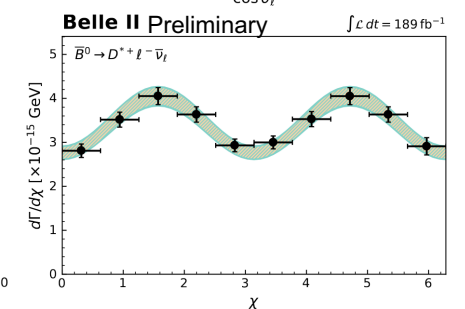
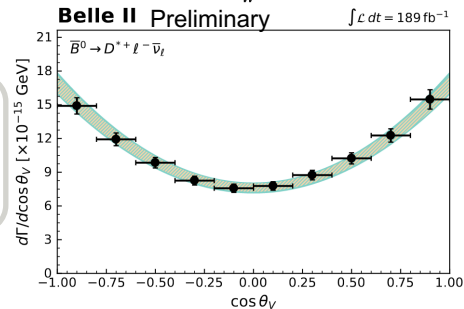
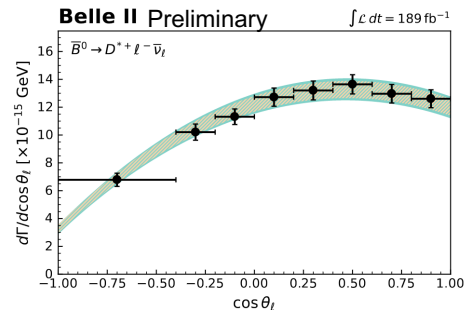
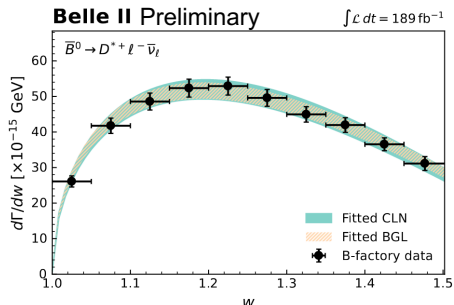
BGL truncation order determined by Nested Hypothesis Test  
[Phys. Rev. D 100, 013005](#)

	Values	Correlations				$\chi^2/\text{ndf}$
$\tilde{a}_0 \times 10^3$	$0.89 \pm 0.05$	1.00	0.26	-0.27	0.07	40/31
$\tilde{b}_0 \times 10^3$	$0.54 \pm 0.01$	0.26	1.00	-0.41	-0.46	
$\tilde{b}_1 \times 10^3$	$-0.44 \pm 0.34$	-0.27	-0.41	1.00	0.56	
$\tilde{c}_1 \times 10^3$	$-0.05 \pm 0.03$	0.07	-0.46	0.56	1.00	

LQCD input used for normalization at zero recoil  
[FNAL/MILC Phys. Rev. D 89, 114504](#)

$$|V_{cb}|_{\text{BGL}} = (40.9 \pm 0.3^{\text{stat}} \pm 1.0^{\text{syst}} \pm 0.6^{\text{theo}}) \times 10^{-3}$$

$$|V_{cb}|_{\text{CLN}} = (40.4 \pm 0.3^{\text{stat}} \pm 1.0^{\text{syst}} \pm 0.6^{\text{theo}}) \times 10^{-3}$$

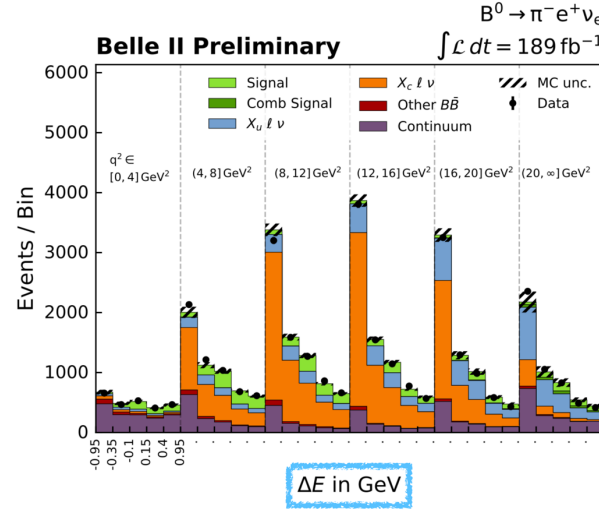
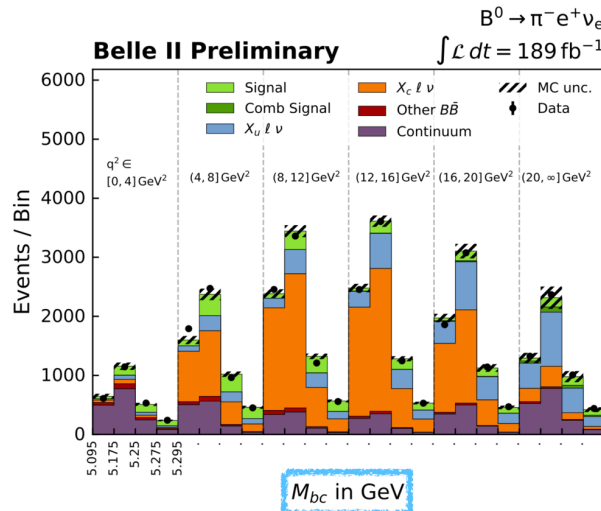
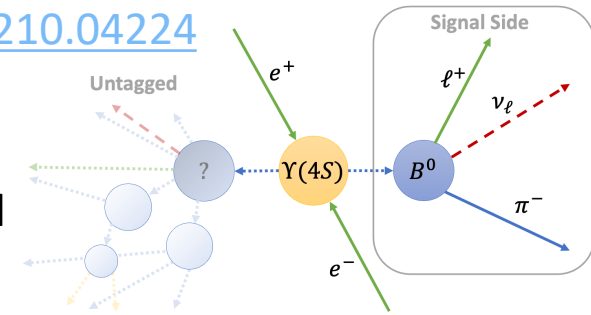


- In good agreement with **exclusive** and **inclusive** world averages
- FNAL/MILC predictions<sup>[1]</sup> of form factors beyond zero recoil probed but found to be in tension with fits at exp. favored BGL order. Suggested  $|V_{cb}|$  value only shifts slightly.

[1] = [Eur. Phys. J. C 82, 1141 \(2022\)](#)

# $|V_{ub}|: B^0 \rightarrow \pi^- \ell^+ \nu$ UNTAGGED

- Challenging due to low branching ratios, large backgrounds and lack of clean kinematic signatures
- Backgrounds suppressed using BDTs,  $B_{\text{sig}}$  direction derived inclusively
- The differential rates in 6 bins of  $q^2$  are determined in a fit to  $M_{bc}$  vs.  $\Delta E$



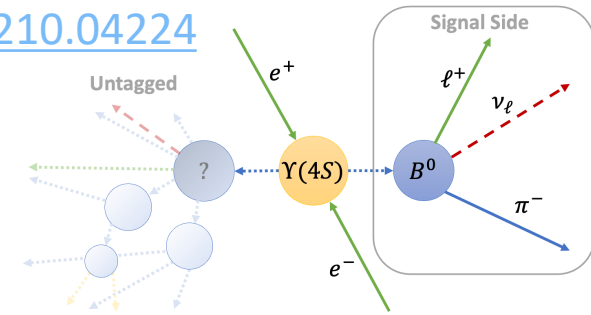
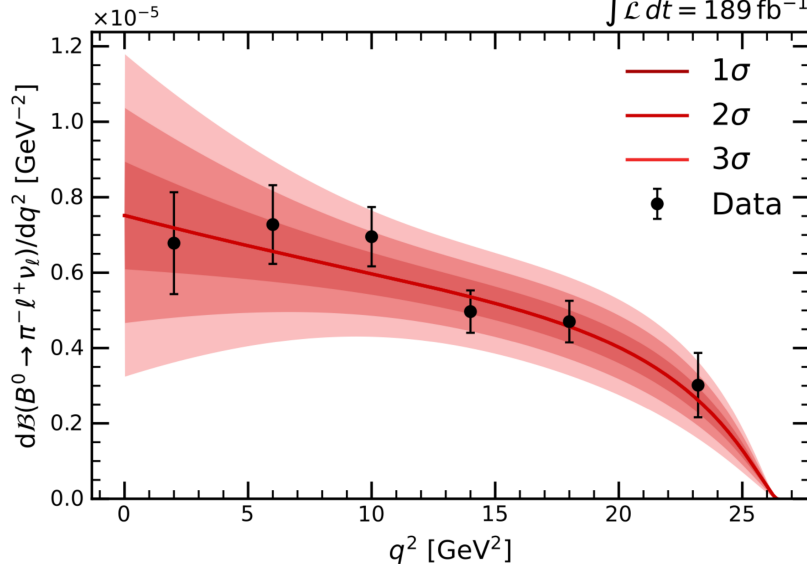
# $|V_{ub}|: B^0 \rightarrow \pi^- \ell^+ \nu$ UNTAGGED

$|V_{ub}|$  is determined in fit to BCL expansion

[Phys. Rev. D 82, 099902](#)

**Belle II Preliminary**

$\int \mathcal{L} dt = 189 \text{ fb}^{-1}$



LQCD input from FNAL/MILC

[Phys. Rev. D 92, 014024](#)

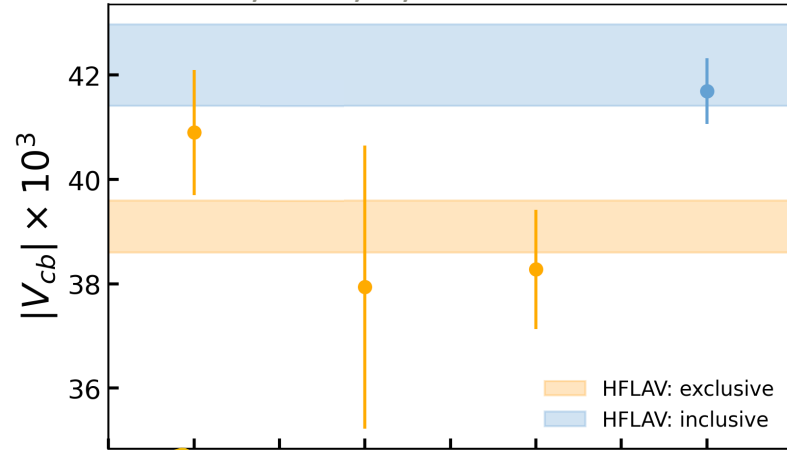
$$|V_{ub}| = (3.55 \pm 0.12^{\text{stat}} \pm 0.13^{\text{syst}} \pm 0.17^{\text{theo}}) \times 10^{-3}$$

$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.426 \pm 0.056^{\text{stat}} \pm 0.125^{\text{syst}}) \times 10^{-4}$$

- Experimental uncertainties dominated by  $e^+e^- \rightarrow q\bar{q}$  and  $B \rightarrow \rho \ell \nu$  modeling

# BELLE II'S RECENT $|V_{cb}|$ & $|V_{ub}|$ SUMMARIZED

Plotted by Chaoyi Lyu



Untagged  $D^* l \nu$

Tagged  $D^* l \nu$

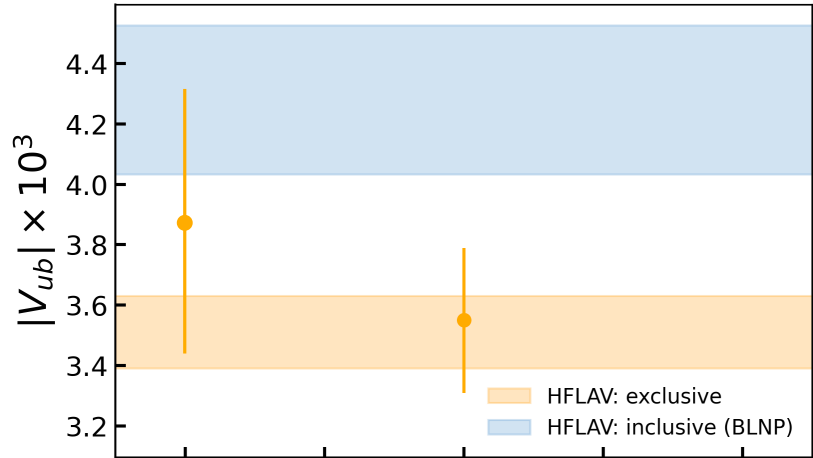
Untagged  $D l \nu$

Inclusive  $X_c l \nu$

[arXiv:2210.13143](https://arxiv.org/abs/2210.13143)

[arXiv:2301.04716](https://arxiv.org/abs/2301.04716)

Novel  $|V_{cb}|$  extraction method<sup>[1]</sup>  
based on measured  $q^2$  moments  
by Belle<sup>[2]</sup> & Belle II<sup>[3]</sup>



Tagged  $\pi l \nu$

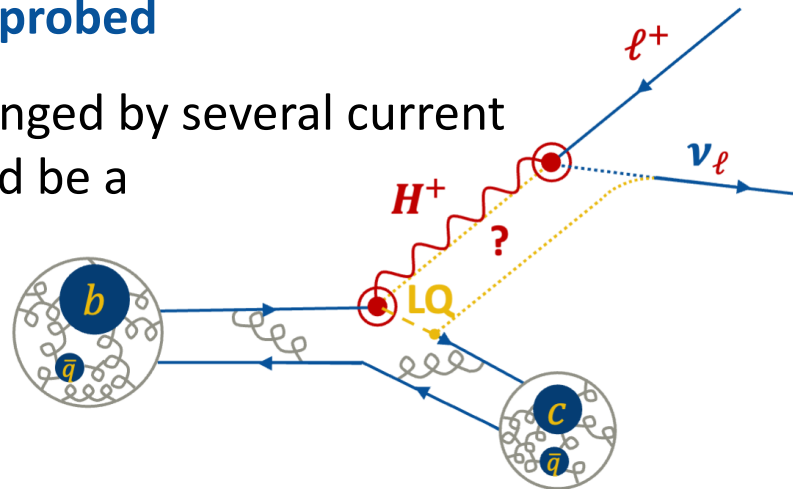
Untagged  $\pi l \nu$

[arXiv:2206.08102](https://arxiv.org/abs/2206.08102)

[arXiv:2210.04224](https://arxiv.org/abs/2210.04224)

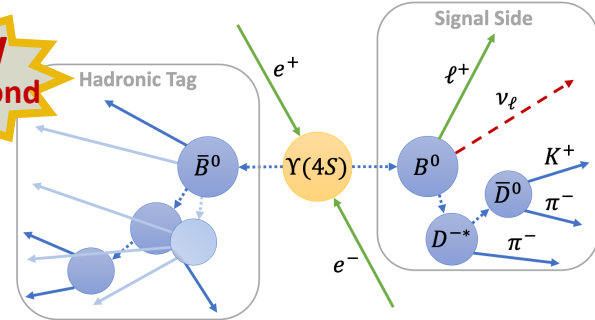
# LIGHT LEPTON UNIVERSALITY

- The **universality of the lepton coupling,  $g_\ell$  ( $\ell = e, \mu, \tau$ )**, to the electroweak gauge bosons **can be probed**
  - Lepton universality (LU) is challenged by several current measurements. Deviations would be a clear sign of BSM physics



# LU: ANGULAR ASYMMETRIES

**NEW**  
for Moriond



- Light lepton universality tested by measuring a **complete set** of **five angular asymmetries** of  $e$  and  $\mu$ ,  $\Delta\mathcal{A}_x = \mathcal{A}_x^e - \mathcal{A}_x^\mu$  using  $B^0 \rightarrow D^{*-}\ell^+\nu$  decays.

$$\mathcal{A}_x(w) = \left(\frac{d\Gamma}{dw}\right)^{-1} \left[ \underbrace{\int_0^1}_{+} - \underbrace{\int_{-1}^0}_{-} \right] dx \frac{d^2\Gamma}{dw dx}$$

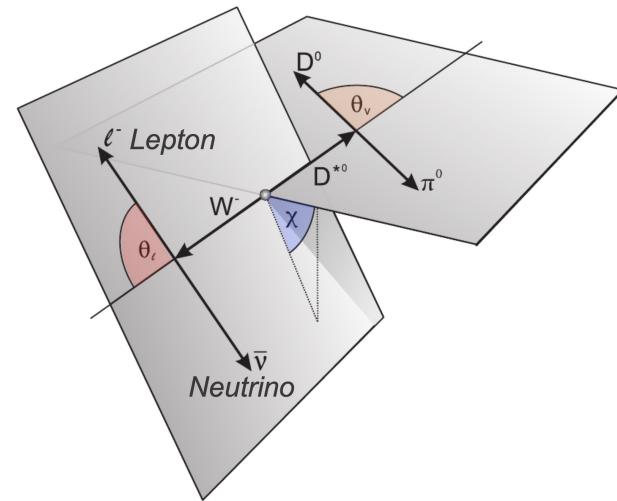
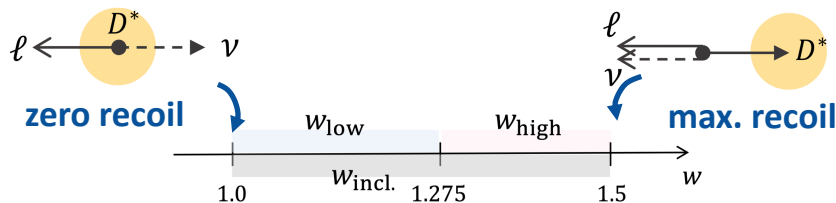
$$A_{\text{FB}}(w): dx = d(\cos \theta_\ell)$$

$$S_3(w) : dx = d(\cos 2\chi)$$

⋮

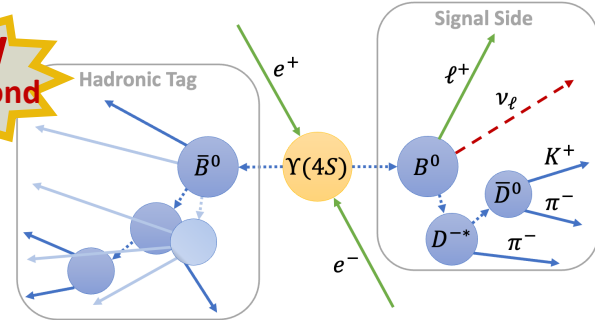
$$\text{Recoil parameter } w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

- The simultaneous determination of all asymmetries in **different  $w$  ranges** is performed

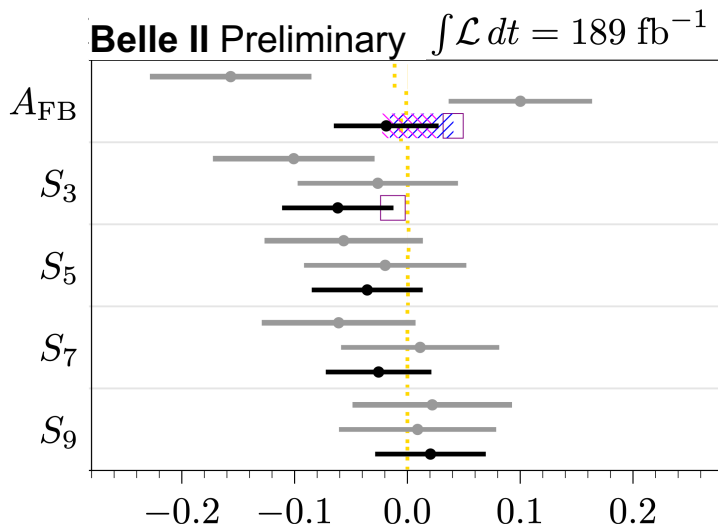
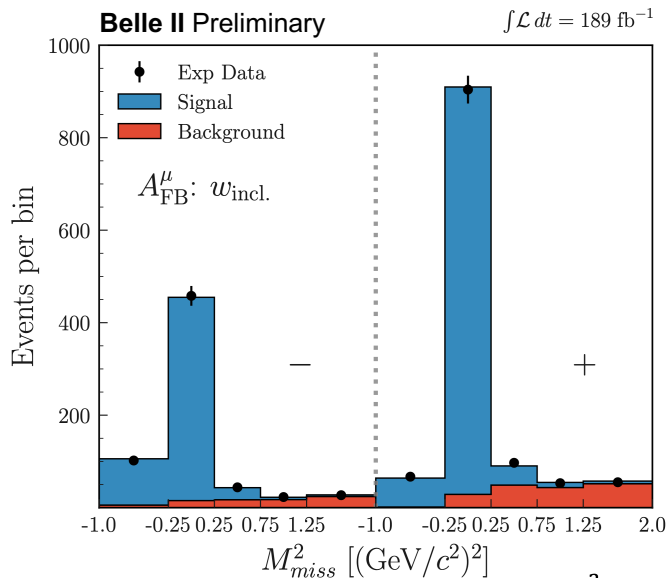


# LU: ANGULAR ASYMMETRIES

**NEW**  
for Moriond



- The signal yields are extracted through a binned maximum-likelihood fit to  $M_{miss}^2$  distributions



Uncertainties  
**statistically dominated**

- $w_{\text{high}}$
- $w_{\text{low}}$
- $w_{\text{incl.}}$
- SM
- Belle (2023) [\[2301.07529\]](#)
- Belle II (2023) **NEW**
- Bobeth, *et al.*

[EPJC 81, 984 \(2021\)](#)

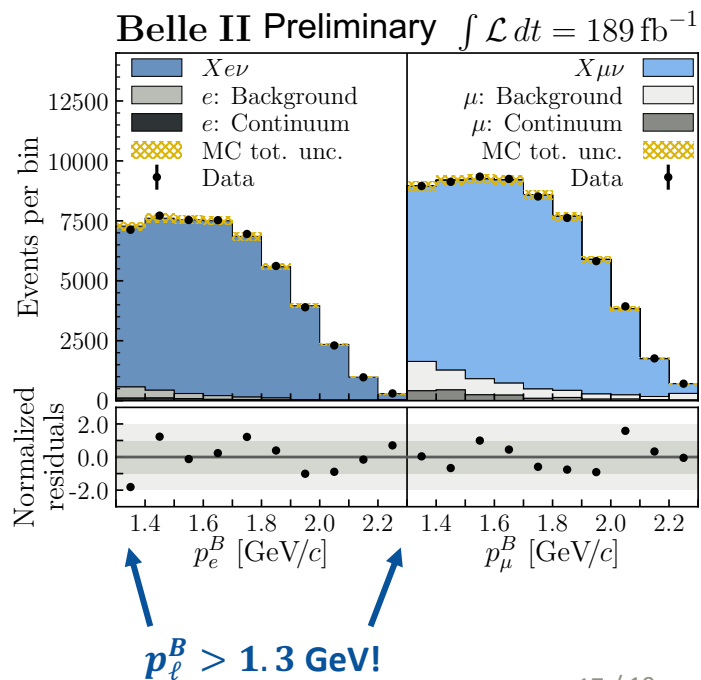
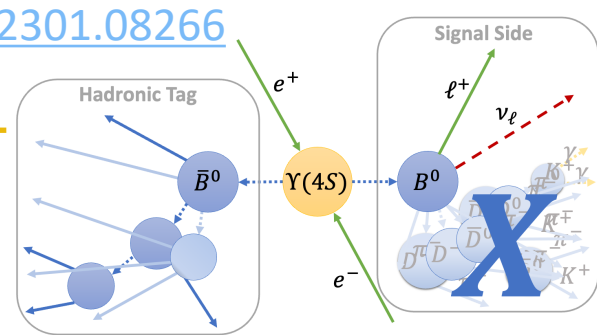
➤ **No evidence of lepton universality violation found**

$$\Delta \mathcal{A} = \mathcal{A}^\mu - \mathcal{A}^e$$



$$\text{LU: INCLUSIVE } R(X_{e/\mu}) = \frac{\mathcal{B}(B \rightarrow X e \nu)}{\mathcal{B}(B \rightarrow X \mu \nu)}$$

- Challenging to model & control miscellaneous backgrounds
- Same flavor  $B$  pair used as background-enriched control sample, high momentum cut to suppress backgrounds
- Signal extracted in simultaneous fit on the **lepton momentum in the  $B_{\text{sig}}$  rest frame,  $p_{\ell}^B$** .



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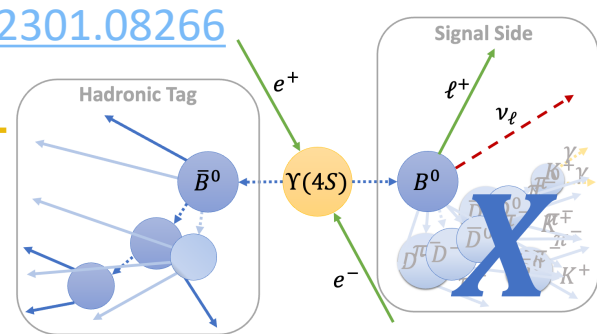
Preliminary

$$R(X_{e/\mu}) = 1.033 \pm 0.010^{\text{stat}} \pm 0.019^{\text{syst}}$$

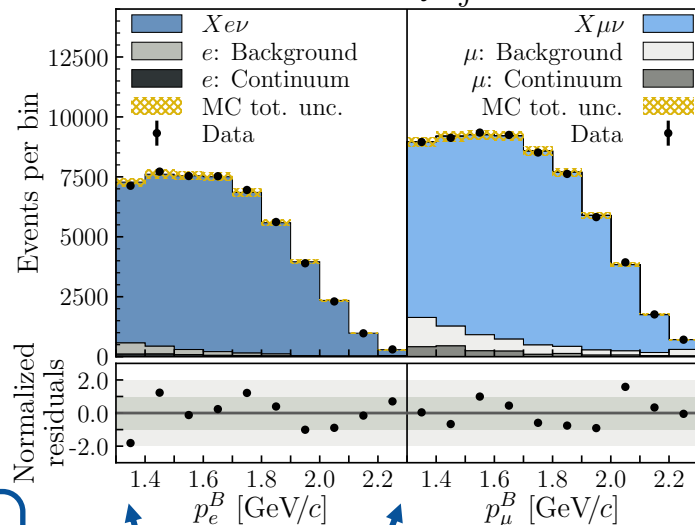
- **Most precise** BF based lepton universality test in semileptonic  $B$ -meson decays to date
- **First inclusive** measurement
- Syst. unc. dominated by **lepton ID**

Consistent with  
SM<sup>[1]</sup> within 1.2  $\sigma$

[1] = JHEP 11, 007 (2022)



Belle II Preliminary  $\int \mathcal{L} dt = 189 \text{ fb}^{-1}$



$p_{\ell}^B > 1.3 \text{ GeV!}$

# SUMMARY AND CONCLUSION

---

- Belle II's **full coverage + constrained  $B\bar{B}$  production** enables **unique kinematic control of semileptonic  $B$ -meson decays** despite the neutrino(s)
- The long-standing discrepancy between **exclusive and inclusive** determinations of  $|V_{cb}|$  &  $|V_{ub}|$  limits our understanding of these fundamental parameters
- Belle II is trying to resolve the situation by
  - Probe existing analyses on **independent data sets with improved experimental tools**
  - Addressing potential issues in previous analyses like form factor dependence or slow pion tracking
- **Lepton universality** is challenged by several measurements
  - Already with half its current dataset, Belle II is able to provide **world-leading and unique** measurements to probe LU

**BACKUP**

# FORM FACTORS AND LATTICE CONSTRAINTS

LQCD input only used for normalization at zero recoil ( $w = 1$ ):

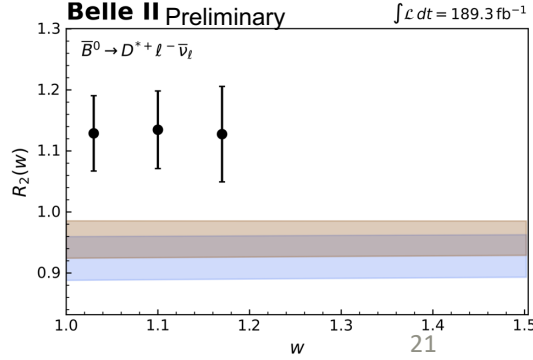
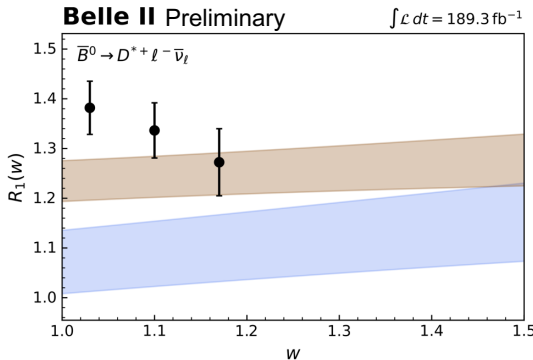
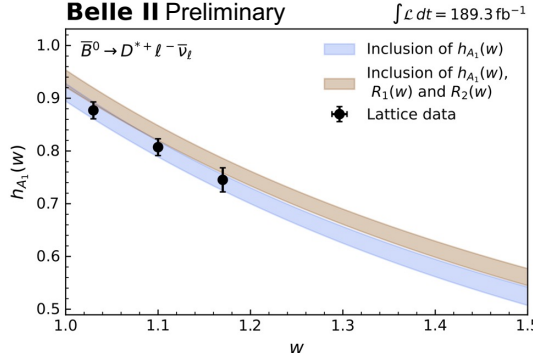
FNAL/MILC [Phys. Rev. D 89, 114504](#)

BGL truncation order determined by Nested Hypothesis Test

[Phys. Rev. D 100, 013005](#)

Preliminary	Values	Correlations			$\chi^2/\text{ndf}$
$\tilde{a}_0 \times 10^3$	$0.89 \pm 0.05$	1.00	0.26	-0.27	0.07
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$|V_{cb}| = 40.9 \pm 1.2$



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40/31

$$|V_{cb}| = 40.9 \pm 1.2$$

FNAL/MILC predictions of  $h_{A_1}$  at  $w = 1.03, 1.10, 1.17$ :

[Eur. Phys. J. C 82, 1141 \(2022\)](#)

Preliminary	Values	Correlations					
$ V_{cb}  \times 10^3$	$40.4 \pm 1.2$	1	-0.31	-0.57	-0.1	0.02	-0.26
$a_0 \times 10^3$	$22.0 \pm 1.4$	-0.31	1	0.27	0.1	-0.18	0.31
$b_0 \times 10^3$	$13.2 \pm 0.2$	-0.57	0.27	1	-0.18	0.13	-0.12
$b_1 \times 10^3$	$9.0 \pm 14.5$	-0.1	0.1	-0.18	1	-0.88	0.52
$b_2$	$-0.5 \pm 0.4$	0.02	-0.18	0.13	-0.88	1	-0.36
$c_1 \times 10^3$	$-0.7 \pm 0.8$	-0.26	0.31	-0.12	0.52	-0.36	1

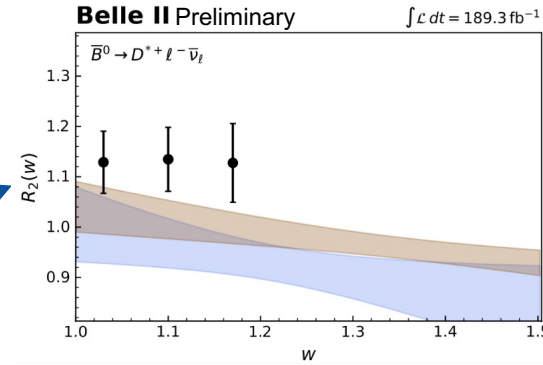
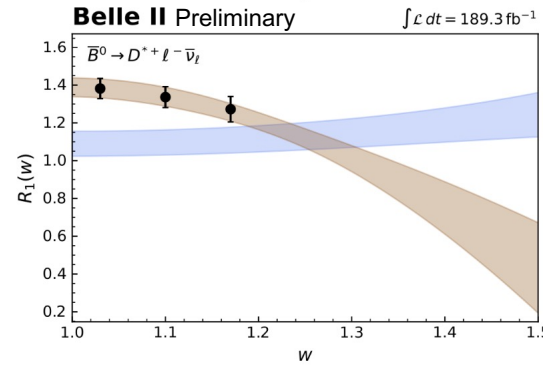
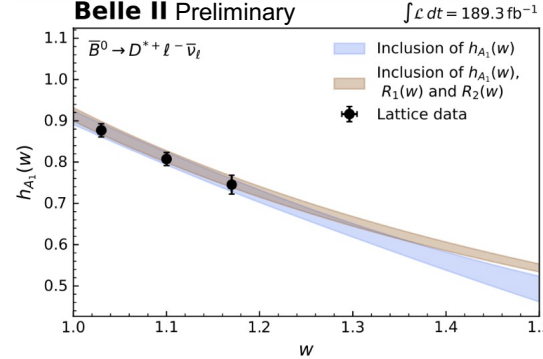
$$|V_{cb}| = 40.4 \pm 1.2$$

FNAL/MILC predictions of  $h_{A_1}$ ,  $R_1$ , and  $R_2$  at  $w = 1.03, 1.10, 1.17$ :

Preliminary

Preliminary	Values	Correlations						
$ V_{cb}  \times 10^3$	$40.0 \pm 1.2$	1	-0.16	0.02	-0.09	-0.61	-0.17	0.1
$a_0 \times 10^3$	$28.3 \pm 1.0$	-0.16	1	-0.08	-0.19	0.17	0.12	-0.03
$a_1 \times 10^3$	$-31.5 \pm 66.6$	0.02	-0.08	1	-0.85	-0.04	-0.07	0.11
$a_2$	$-5.8 \pm 2.5$	-0.09	-0.19	-0.85	1	0.1	0.1	-0.13
$b_0 \times 10^3$	$13.3 \pm 0.2$	-0.61	0.17	-0.04	0.1	1	0.11	-0.13
$c_1 \times 10^3$	$-3.2 \pm 1.4$	-0.17	0.12	-0.07	0.1	0.11	1	-0.9
$c_2 \times 10^3$	$59.1 \pm 31.1$	0.1	-0.03	0.11	-0.13	-0.13	-0.9	1

$$|V_{cb}| = 40.0 \pm 1.2$$



# $|V_{xb}|$ : UNTAGGED: EXPERIMENTAL UNCERTAINTIES

$$B^0 \rightarrow D^{*-} \ell^+ \nu$$

Relative uncertainty (%)	Preliminary			
	$\tilde{a}_0$	$\tilde{b}_0$	$\tilde{b}_1$	$\tilde{c}_1$
Statistical	3.3	0.7	44.8	35.4
Finite MC samples	3.0	0.7	39.4	33.0
Signal modelling	3.0	0.4	40.0	30.8
Background subtraction	1.2	0.4	24.8	18.1
Lepton ID efficiency	1.5	0.3	3.1	2.5
Slow pion efficiency	1.5	1.5	18.4	22.0
Tracking of $K, \pi, \ell$	0.5	0.5	0.6	0.5
$N_{B\bar{B}}$	0.8	0.8	1.1	0.8
$f_{+-}/f_{00}$	1.3	1.3	1.7	1.3
$\mathcal{B}(D^{*+} \rightarrow D^0 \pi^+)$	0.4	0.4	0.5	0.4
$\mathcal{B}(D^0 \rightarrow K^- \pi^+)$	0.4	0.4	0.5	0.4
$B^0$ lifetime	0.1	0.1	0.2	0.1
Total	6.1	2.5	78.3	64.1

$$B^0 \rightarrow \pi^- \ell^+ \nu$$

Preliminary	Systematic uncertainties on the yields (%)												
	Source	$B^0 \rightarrow \pi^- e^+ \nu_e$						$B^0 \rightarrow \pi^- \mu^+ \nu_\mu$					
		$q1$	$q2$	$q3$	$q4$	$q5$	$q6$	$q1$	$q2$	$q3$	$q4$	$q5$	$q6$
Detector	1.2	1.0	1.1	1.4	2.3	2.4	2.3	3.2	3.3	1.2	1.9	3.8	
MC sample size	4.0	2.0	2.4	2.8	3.9	5.6	3.9	2.0	2.3	2.7	3.4	4.8	
Continuum	13.1	5.5	4.4	7.8	10.5	33.9	53.3	8.8	3.2	4.5	8.0	11.4	
$B \rightarrow \rho \ell \nu$	9.5	12.5	9.7	6.9	3.4	12.9	8.7	11.6	8.6	6.3	3.3	14.3	
$B \rightarrow X_u \ell \nu$	3.3	1.9	2.1	2.1	1.8	3.7	3.4	2.3	2.0	2.3	2.1	6.0	
$B \rightarrow X_c \ell \nu$	2.3	3.0	1.1	0.8	0.5	2.4	2.4	1.5	1.5	0.8	0.5	2.2	
Total syst.	17.2	14.3	11.2	11.1	12.0	37.0	53.4	15.2	10.3	8.7	9.7	20.3	
Stat.	10.2	6.01	6.86	8.08	10.3	13.2	10.4	6.0	6.4	7.8	9.7	13.4	
Total	20.2	15.5	13.2	13.7	15.9	39.2	54.5	16.4	12.2	11.6	13.7	24.3	

# LU: ANGULAR ASYMMETRIES

- Light lepton universality tested by measuring a **complete set** of **five angular asymmetries** of  $e$  and  $\mu$ ,  $\Delta\mathcal{A}_x = \mathcal{A}_x^e - \mathcal{A}_x^\mu$  using  $B^0 \rightarrow D^{*-} \ell^+ \nu$  decays.

$$\mathcal{A}_x(w) = \left( \frac{d\Gamma}{dw} \right)^{-1} \left[ \underbrace{\int_0^1}_{+} - \underbrace{\int_{-1}^0}_{-} \right] dx \frac{d^2\Gamma}{dw dx}$$

Highly sensitive to lepton universality violation

$$A_{FB}(w) : dx = d(\cos \theta_\ell)$$

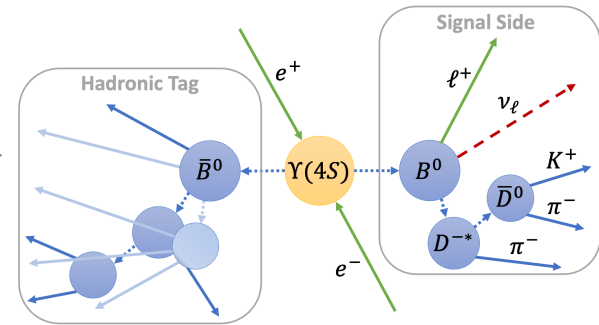
$$S_3(w) : dx = d(\cos 2\chi)$$

$$S_5(w) : dx = d(\cos \chi \cos \theta_V)$$

Less sensitive or insensitive to NP.  
Control tests of the analysis method

$$S_7(w) : dx = d(\sin \chi \cos \theta_V)$$

$$S_9(w) : dx = d(\sin 2\chi)$$



Recoil parameter  $w = \frac{m_B^2 + m_{D^{*0}}^2 - q^2}{2m_B m_{D^{*0}}}$

