

Prospects of the new physics search at Belle II by precise measurements of the CKM matrix elements

Yun-Tsung Lai*

Kavli IPMU, Univ. of Tokyo

On behalf of the Belle II Collaboration

1

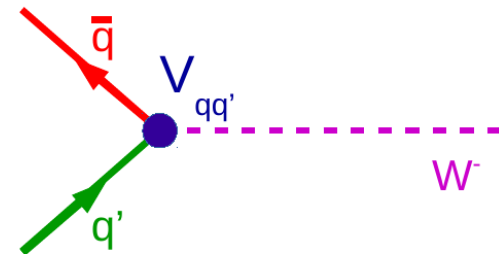
2022 Spring JPS 15pA561

15th Mar., 2022



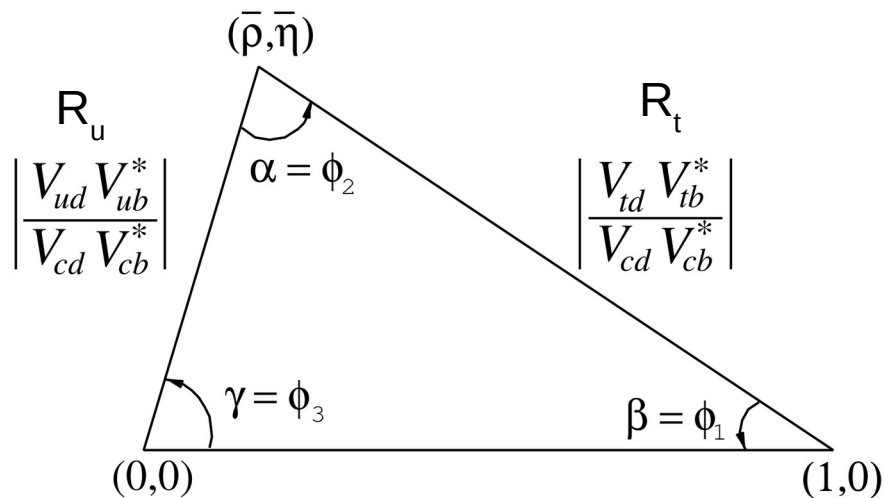
Introduction

- Cabibbo-Kobayashi-Maskawa (CKM) matrix
 - Three generations of quarks.
 - Each element ($V_{qq'}$) describes mixing of quarks via weak interaction in Standard Model (SM).



$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- Unitarity triangle:



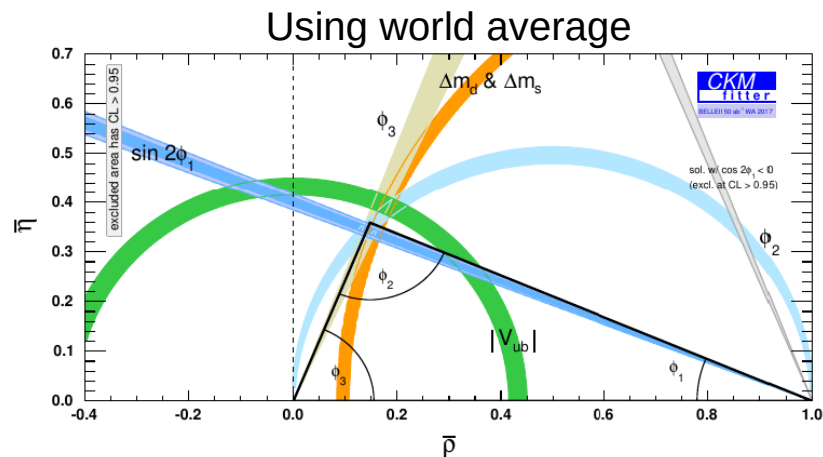
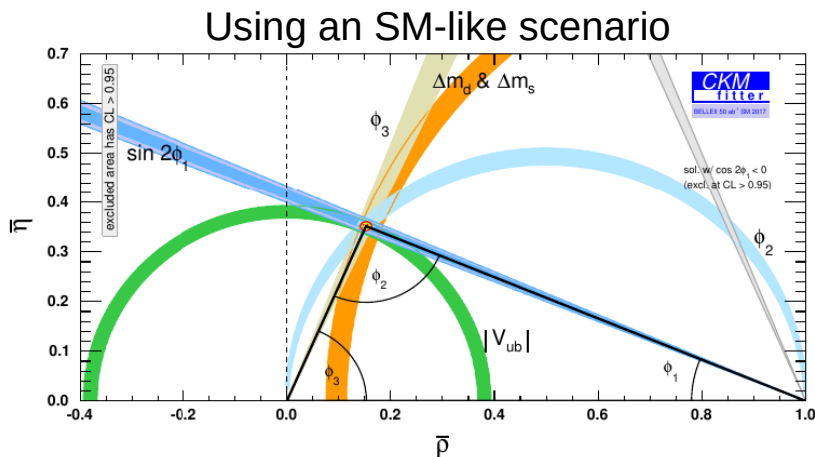
$$\beta = \phi_1 = \arg \left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} \right)$$

$$\alpha = \phi_2 = \arg \left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right)$$

$$\gamma = \phi_3 = \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

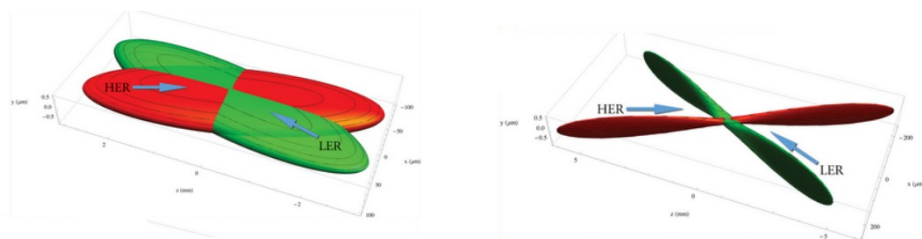
- Precise measurement on UT angles and sides is a powerful SM test at energised much higher than directly achieved at the energy frontier.
 - Deviation from theoretical results may indicate to new physics (NP).
- The potential of Belle II:
 - Much larger data set (target at 50 ab^{-1}) thanks to SuperKEKB.
 - New hardware and software tools also improve the detection resolution and reduce systematic uncertainty in various aspects.
 - Belle II has unique/world leading access to many key decay modes, specially those involving neutral particle: K^0 , π^0 , $\eta^{(\prime)}$, and missing particle (ν).

Extrapolation @ 50 ab^{-1}

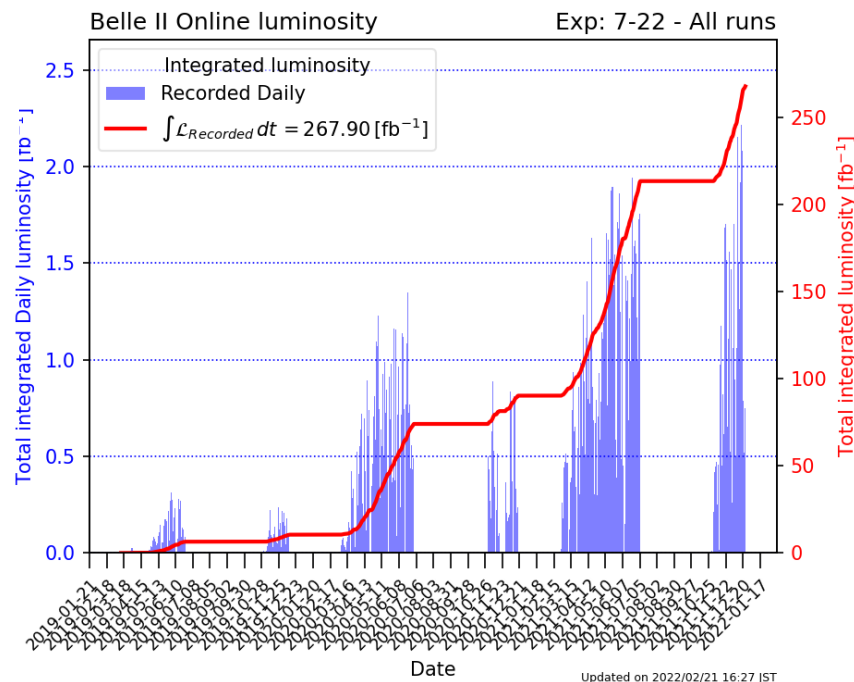


SuperKEKB

- Asymmetric energy collider:
 - 7.0 GeV e^- and 4.0 GeV e^+ for $Y(4S) \rightarrow B\bar{B}$.
- Upgrade from KEKB.
 - More than 30 times larger luminosity of KEKB with nano beam scheme.

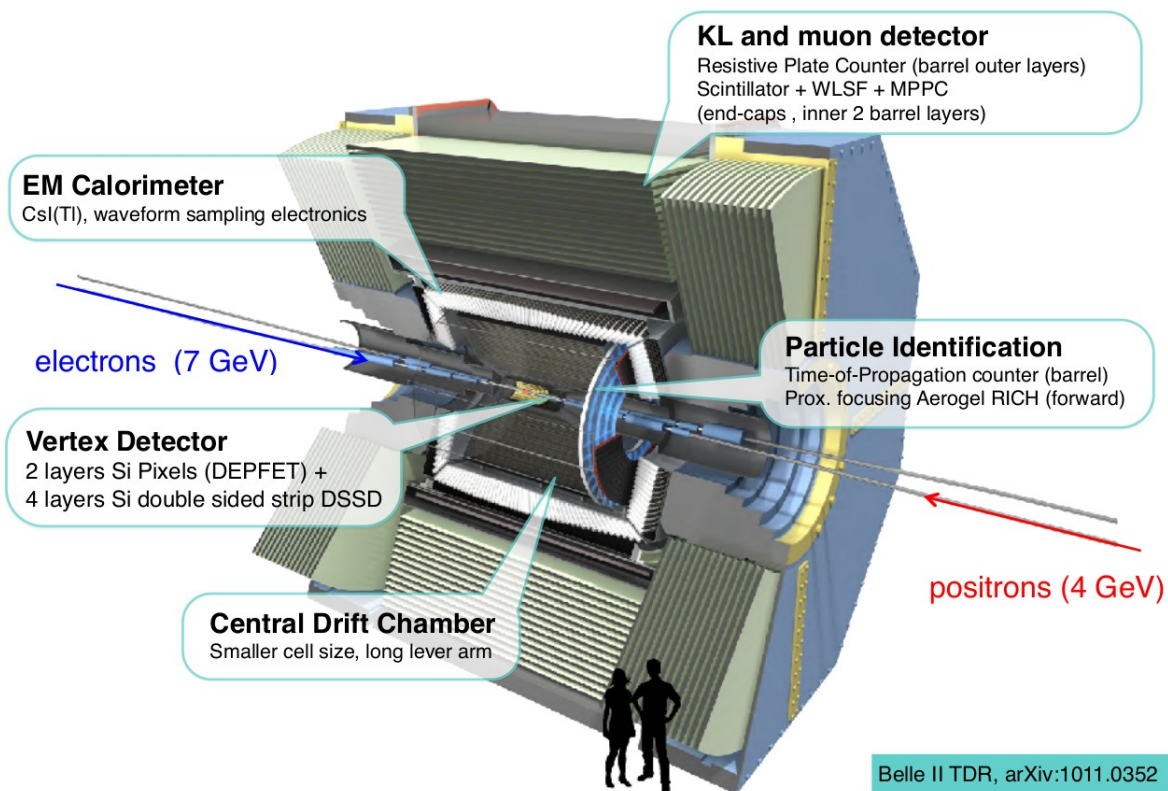


- Achievement so far:
 - $L_{\text{int}} = 267.9 \text{ fb}^{-1}$ up to Dec. 2021.
 - $L_{\text{peak}} = 3.8 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$,
new world record
with smaller beam currents than
those of KEKB.
- Goal: $> 6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$



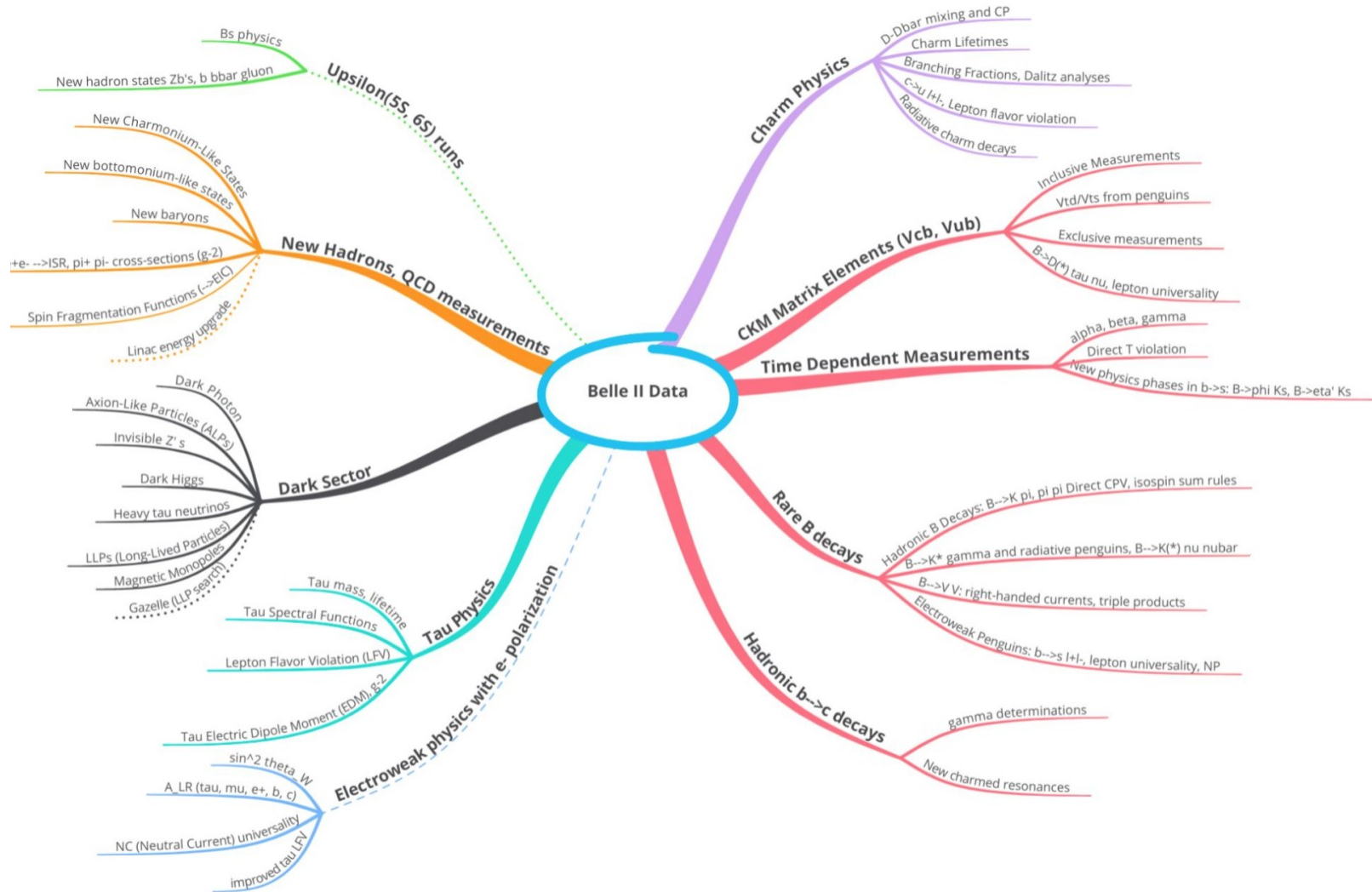
Belle II detector

- Newly-designed sub-detectors set to improve detection performance.
 - Vertexing: 1.5 ~ 2 times improvement compared with Belle.
 - PID: $\sim 4\sigma$ for K/ π suppression.
 - Pixel detector full installation will be complete in 2022 shut down.



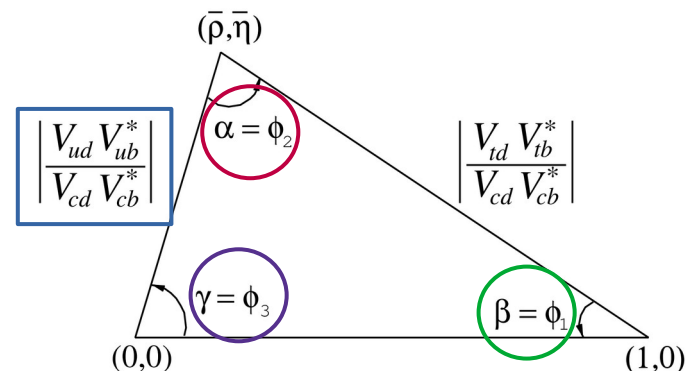
Trigger and DAQ system:
Required to handle high data rate and high beam background.

Belle II physics program



Outline

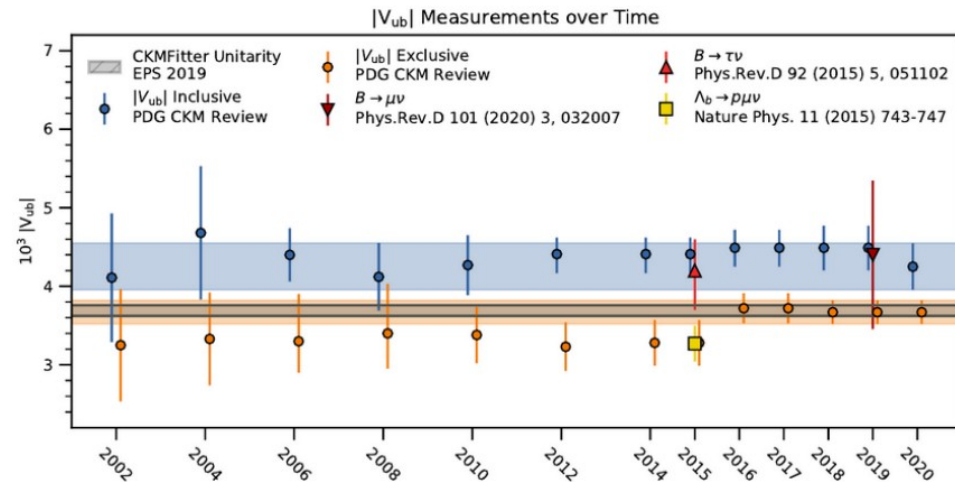
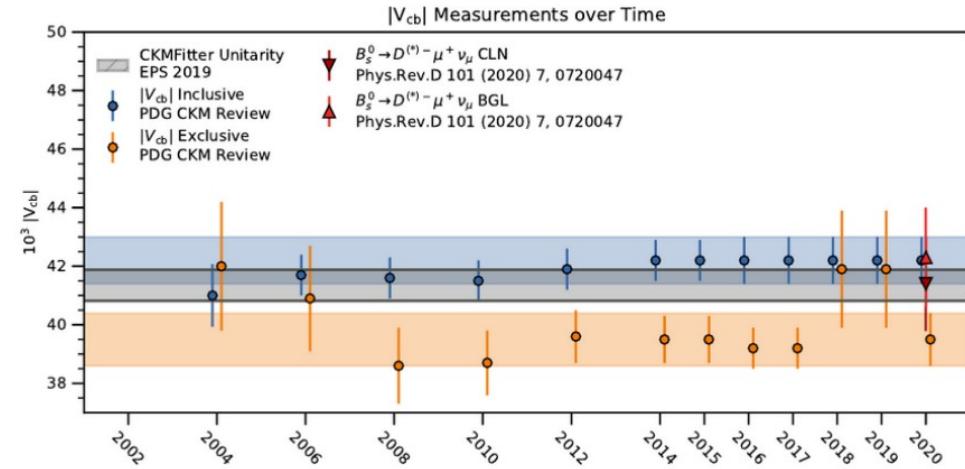
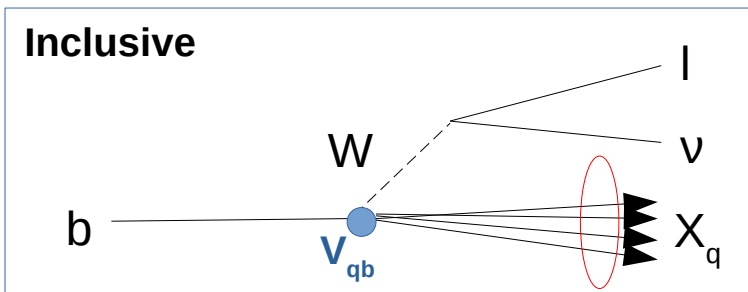
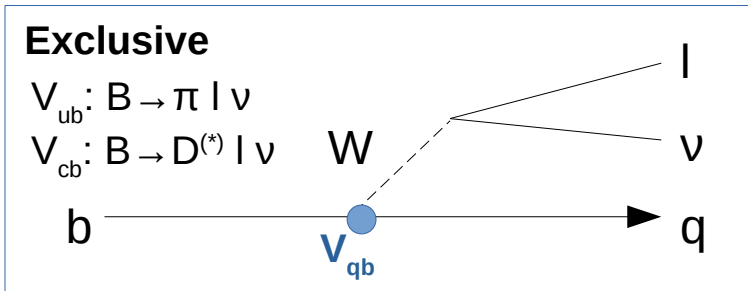
- This report will mainly introduce the methodology of measuring them, improvement and prospect in Belle II.
- Recent results will be also reported.



UT element	Mode	Methodology	Improvement from Belle II (other than statistics)
$ V_{ub} $	$B \rightarrow \pi l \nu$ (excl.) $B \rightarrow X_u l \nu$ (incl.)	Tagged / Untagged	Tagging package (FEI)
$ V_{cb} $	$B \rightarrow D^{(*)} l \nu$ (excl.) $B \rightarrow X_c l \nu$ (incl.)	Tagged / Untagged	Tagging package (FEI)
ϕ_1	$b \rightarrow c \bar{c} s$ $b \rightarrow s \bar{q} \bar{q}$	Time-dependent CP violation	Vertexing, flavor tagging
ϕ_2	$B \rightarrow hh$ ($h=\pi, \rho$)	Isospin study with BF, A_{CP} , Time-dependent CP violation	Time-dependent CP violation of $B^0 \rightarrow \pi^0 \pi^0$
ϕ_3	$B \rightarrow D^{(*)} K^{(*)}$	Amplitude ratio between D eigenstates	More decay modes with neutral particles

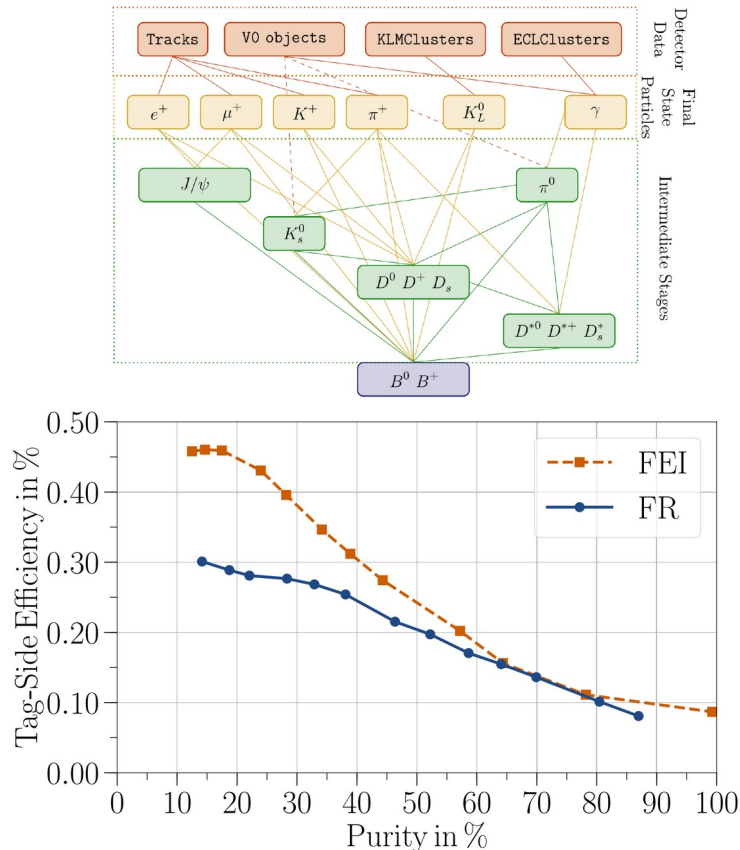
$|V_{ub}|$ & $|V_{cb}|$

- $|V_{ub} / V_{cb}|$: Constrains the length opposite to ϕ_1 (R_u) in the unitary condition.
- SM reference as mainly from tree-level.
- Using **semileptonic B decay**.
 - Longstanding discrepancy ($\sim 3\sigma$) between **inclusive and exclusive** results.
 - Hint of NP such as right-handed current? [PRD 90, 094003 \(2014\)](#)

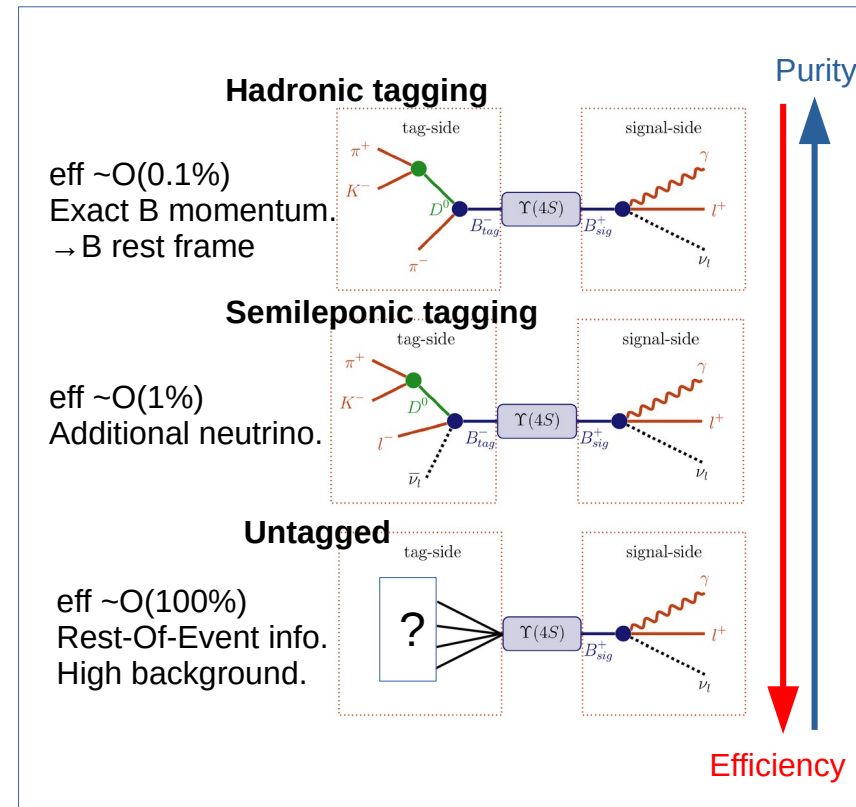


Tagging method

- New full event interpretation (FEI) package for Belle II from the Belle version (FR). [Comput Softw Big Sci 3, 6 \(2019\)](#)
[NIM A 654, 432-440 \(2011\)](#)
- Hierarchical reconstruction on > 5000 B decays with MVA tool.
- Reduce systematic uncertainty due to tag-side calibration.
- 30%~50% increase on efficiency with same purity.



Tagging methods

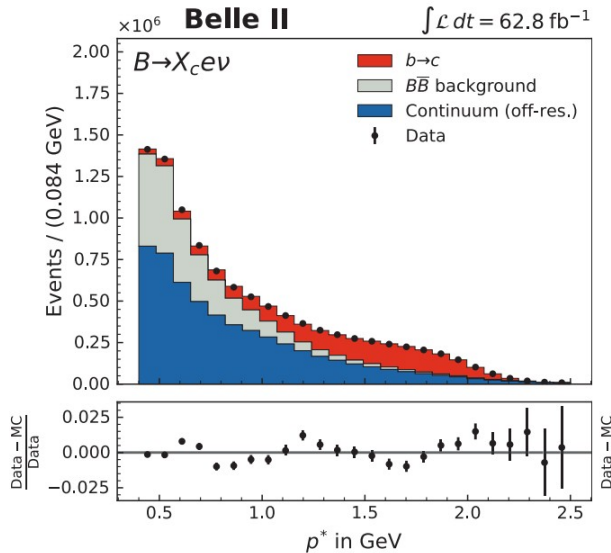


$|V_{cb}|$ inclusive: $B \rightarrow X_c \ell \nu$

- $|V_{cb}|$ is extracted by differential branching fraction (dBF) on the spectral moments (of lepton energy or hadron mass). [JHEP 02 \(2019\) 177](#)
- Non-perturbative elements can be determined at the same time.

Belle II $B \rightarrow X_c \ell \nu$
62.8 fb⁻¹ Untagged

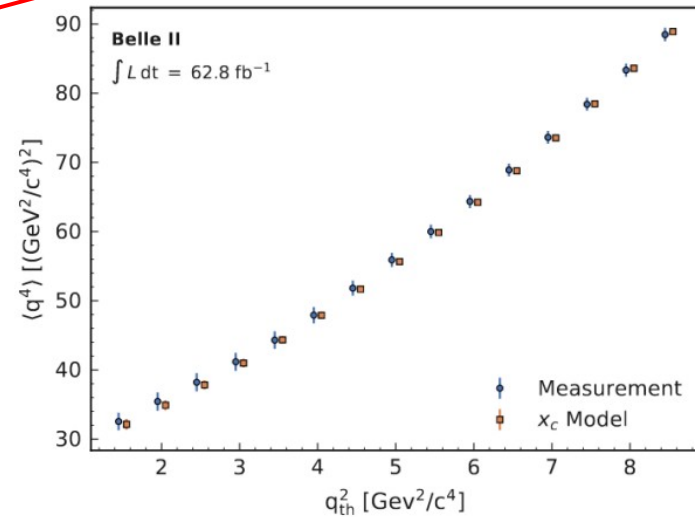
[arXiv: 2111.09405 \[hep-ex\]](#)



Belle II $B \rightarrow X_c \ell \nu$
62.8 fb⁻¹ tagged

To be submitted to PRD

New for JPS



$$\mathcal{B}(B \rightarrow X_c \ell \nu_e) = (9.97 \pm 0.03(\text{stat}) \pm 0.38(\text{syst}))\%$$

$$\mathcal{B}(B \rightarrow X_c \mu \nu_\mu) = (9.47 \pm 0.05(\text{stat}) \pm 0.45(\text{syst}))\%$$

$$\mathcal{B}(B \rightarrow X_c \ell \nu_\ell) = (9.75 \pm 0.03(\text{stat}) \pm 0.47(\text{syst}))\%$$

Main source of syst.: X_c composition.

q^2 ($=(\mathbf{p}_\ell + \mathbf{p}_\nu)^2$) moment for $n = 1-4$ order determined as a function of q^2 threshold.

$|V_{cb}|$ exclusive: $B \rightarrow D^{(*)} l \nu$

- Fit on data to obtain dBF on hadron recoil parameter (w)
- Extract $|V_{cb}|$ by dBF/dw with phenomenological form-factor.

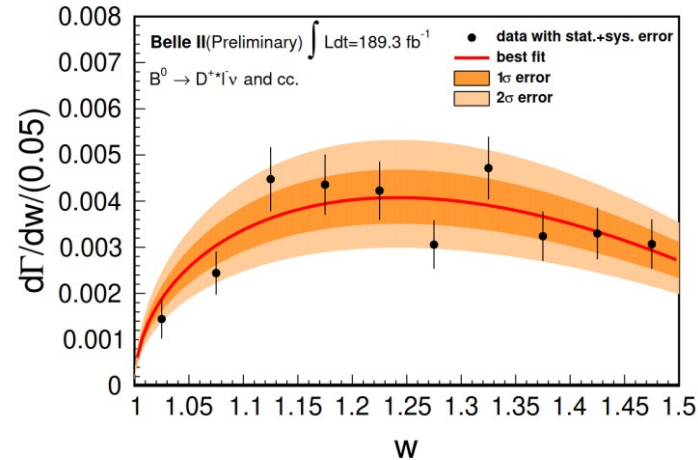
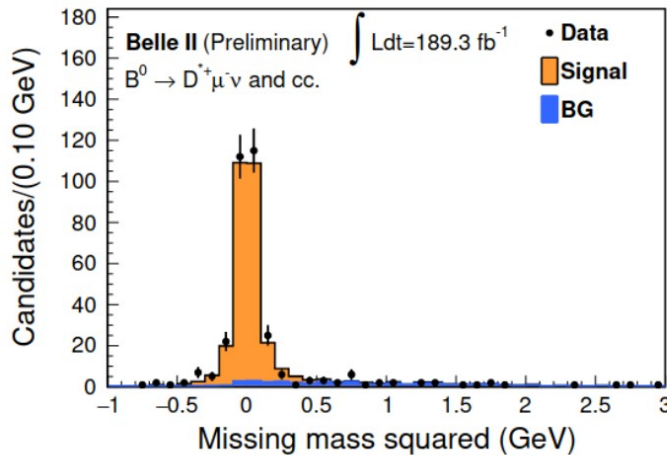
**Belle II $B^0 \rightarrow D^{*+} l \nu$
189.3 fb⁻¹ Tagged**

New for JPS

$$\frac{d\Gamma}{dw} = \frac{\eta_{EW}^2 G_F^2}{48\pi^3} m_{D^{*+}}^3 (m_B - m_{D^{*+}})^2 g(w) F^2(w) |V_{cb}|^2$$

$$w = \frac{m_B^2 + m_{D^{*+}}^2 - q^2}{2m_B m_{D^{*+}}}$$

Nucl. Phys. B 196 (1982) 83-92
PRD 79 (2009) 014506
Nucl. Phys. B 530 (1998) 153-181



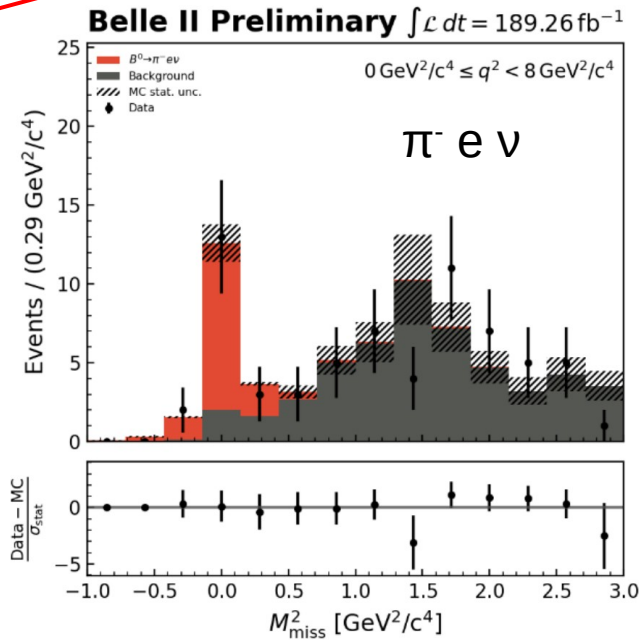
$$\mathcal{B}(B^0 \rightarrow D^{*+} l \nu_\ell) = 0.0527 \pm 0.0022(\text{stat.}) \pm 0.0038(\text{syst.})$$

$$|V_{cb}| = 0.0373 \pm 0.0029 (\text{stat.} + \text{syst.})$$

$|V_{ub}|$ exclusive: $B \rightarrow \pi l \nu$

New for JPS

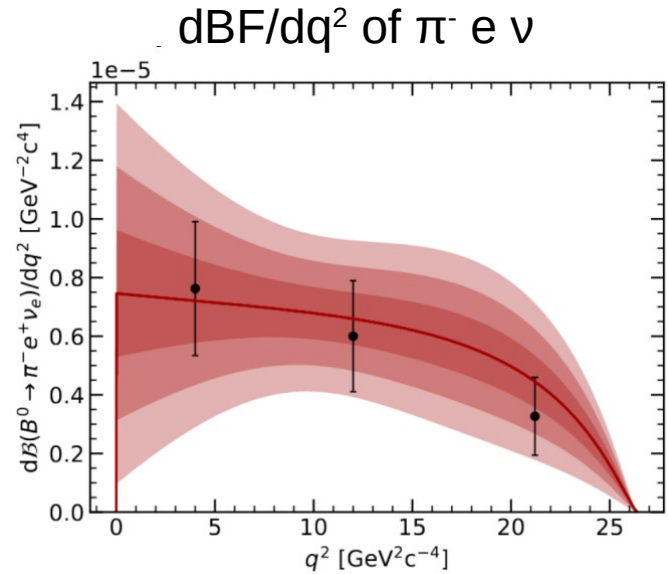
**Belle II $B \rightarrow \pi l \nu$
189.3 fb⁻¹ tagged**



Decay mode	Fitted $ V_{ub} $
$B^0 \rightarrow \pi^- e^+ \nu_e$	$(3.71 \pm 0.55) \times 10^{-3}$
$B^+ \rightarrow \pi^0 e^+ \nu_e$	$(4.24 \pm 0.55) \times 10^{-3}$
Combined fit	$(3.94 \pm 0.42) \times 10^{-3}$

- Tagging by FEI.
- Fit on $M_{\text{miss}}^2 = (p(e^+e^-) - p(B_{\text{tag}}) - p(\pi) - p(l))^2$ to extract signal within q^2 ($= (p_l + p_\nu)^2$) bins.
- Extract $|V_{ub}|$ by the dBF(q^2) with form factor.

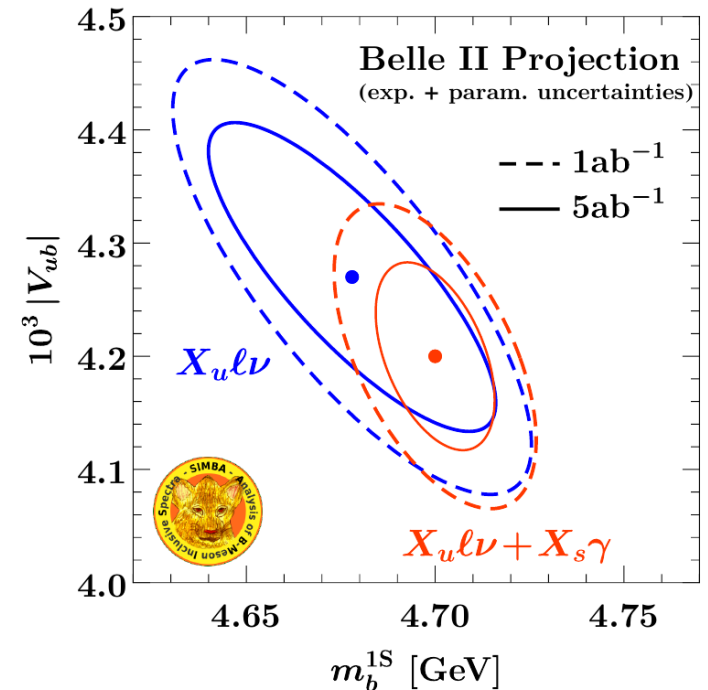
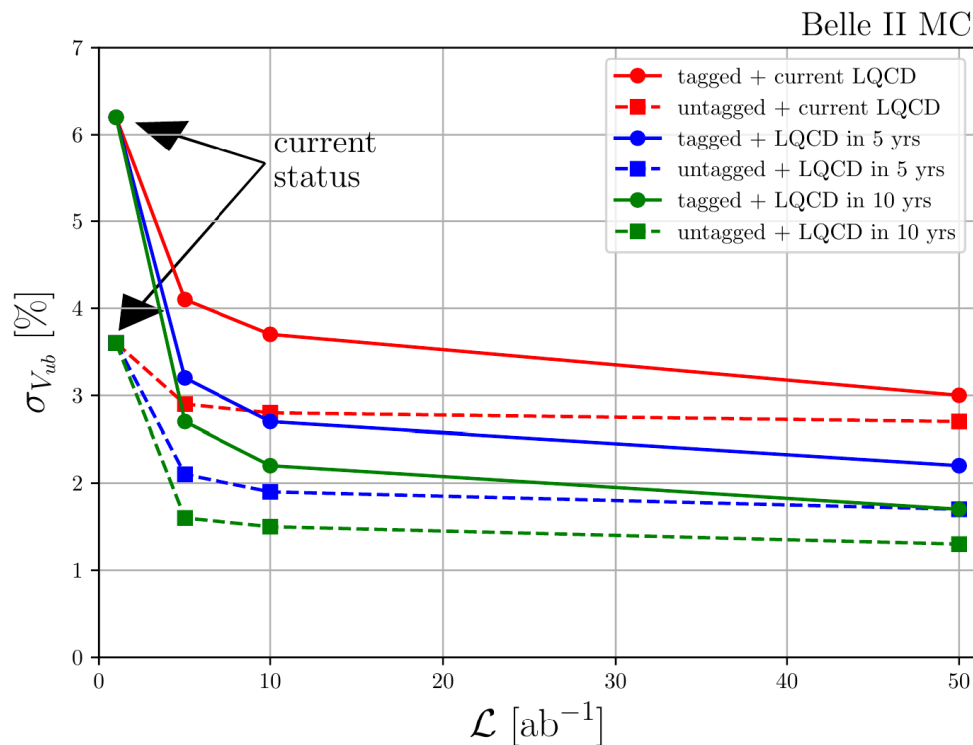
$$\frac{d\mathcal{B}(B \rightarrow \pi l \nu)}{dq^2} = |V_{ub}|^2 \frac{G_F^2 \tau_B}{24\pi^3} p_\pi^3 |f_+^{B\pi}(q^2)|^2$$



LQCD: PRD 92 (2015) 1 014024

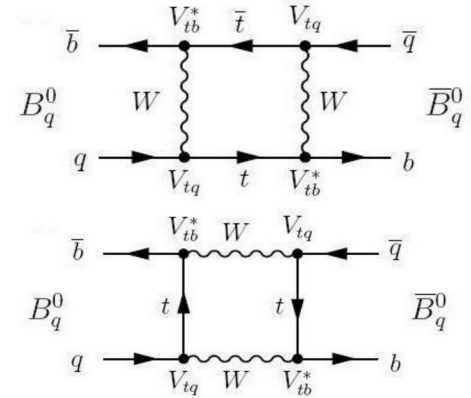
$|V_{ub}|$ & $|V_{cb}|$: Belle II prospect

- Belle II: both inclusive and exclusive measurement.
LHCb: mainly exclusive Λ_b and B_s decays
- Exclusive: Uncertainty from lattice QCD dominates for now.
- Inclusive $|V_{ub}|$: Unknown shape function (b quark motion with B meson).
 - Simultaneous fit on $X_c | \nu + X_u | \nu + X_s \gamma$.



Time-dependent CP violation

- Time-dependent CP violation (TDCPV)
 - To determine ϕ_1 (mixing) and ϕ_2 (mixing + $b \rightarrow u$).
- Decay rate asymmetry as a function of decay time:
 - Δm_B : Mass difference between eigenstates.

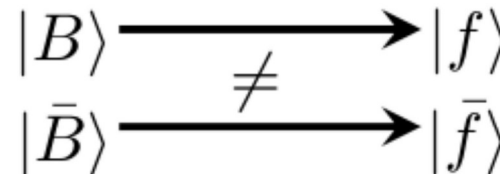
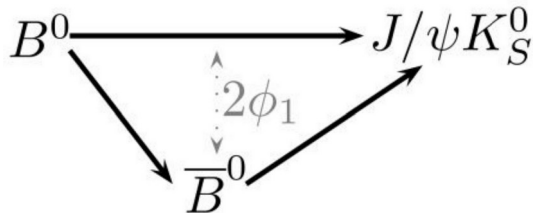


$$\mathcal{A}_f(\Delta t) = \frac{\Gamma(\bar{B}^0 \rightarrow J/\psi K_S^0) - \Gamma(B^0 \rightarrow J/\psi K_S^0)}{\Gamma(\bar{B}^0 \rightarrow J/\psi K_S^0) + \Gamma(B^0 \rightarrow J/\psi K_S^0)}$$

$$= \boxed{S_f} \sin(\Delta m_B \Delta t) + \boxed{A_f} \cos(\Delta m_B \Delta t)$$

S_f : mixing-induced CPV

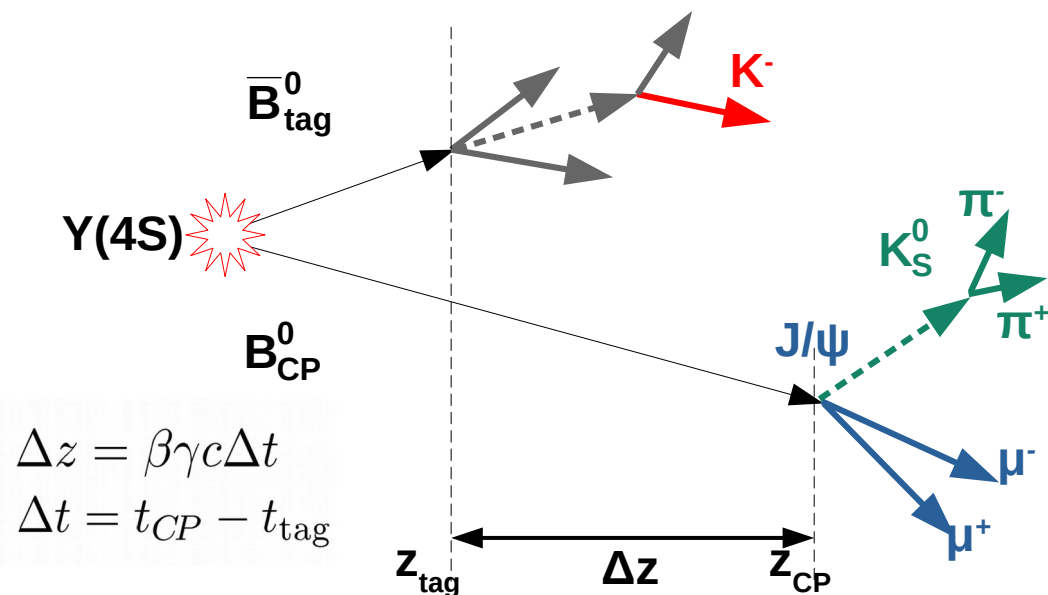
A_f : Direct CPV



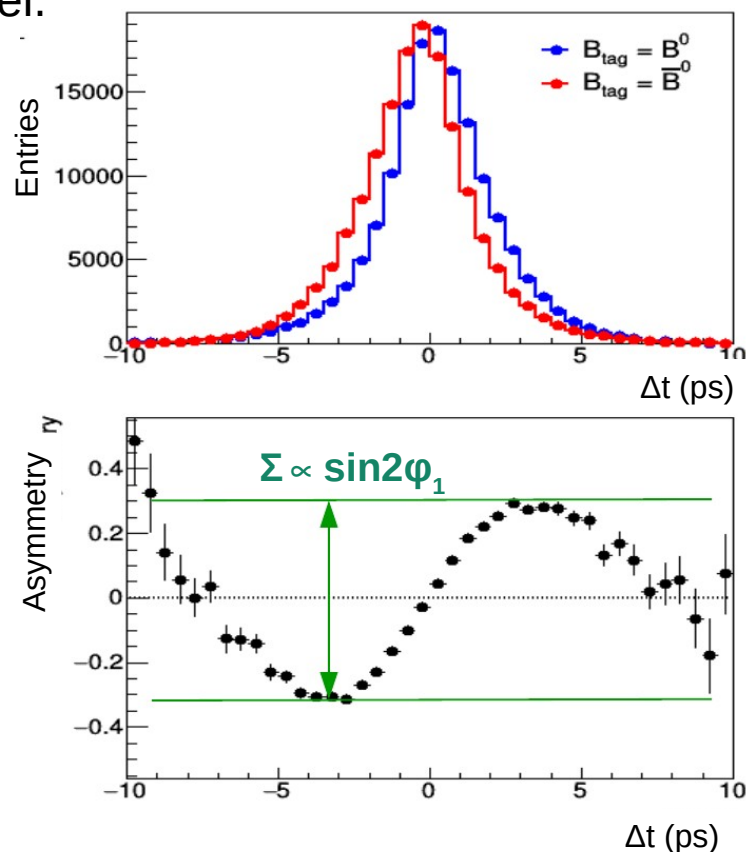
At tree-level: $S_f \sim \sin 2\phi_1$, $A_f \sim 0$

TDCPV measurement @ Belle II

- **1. Flavor tagging:** Obtain the flavor of B mesons.
- **2. Vertexing:** $\Delta z \rightarrow \Delta t$.
- **3. Δt distributions** for B^0 and \bar{B}^0 separately.
- **4. Asymmetry(Δt):** $S_f \sim \sin(2\phi_1)$ at tree-level.



Belle II simulation



Flavor tagging

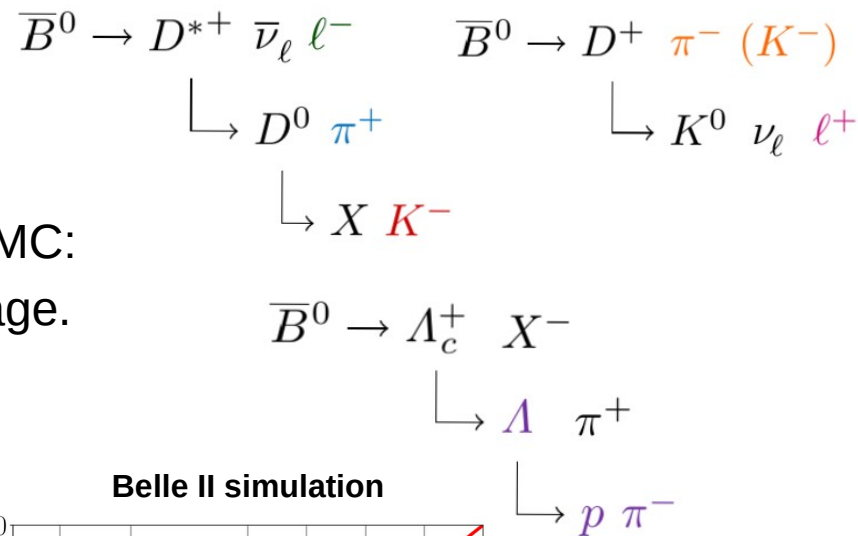
- Study B^0 - \bar{B}^0 mixing and CP violation by identify the flavor of B mesons.

- Belle II new algorithm: [arXiv:2110.00790 \[hep-ex\]](https://arxiv.org/abs/2110.00790)
[arXiv:2008.02707 \[hep-ex\]](https://arxiv.org/abs/2008.02707)
MVA-based, more variables included.

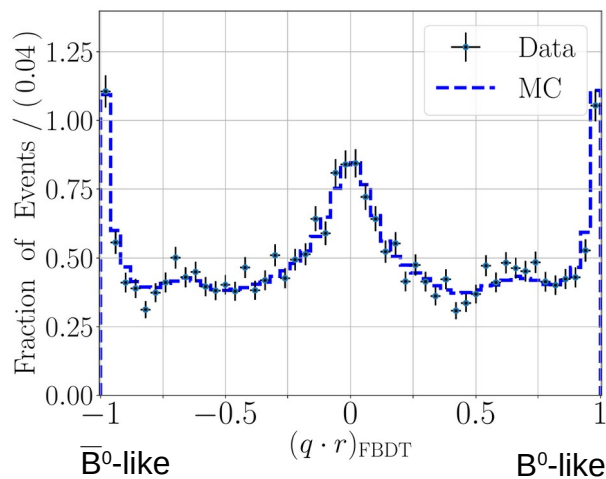
- Effective tagging efficiency with Belle II MC:
 - **(37.16±0.03)%** , ~30% for Belle package.
 - Validated with Belle MC/data.

Concept:

1. Final state info (kaon, pion, proton, lepton).
2. Flavor of charmed particle (D , Λ_c).
3. Flavor of B.

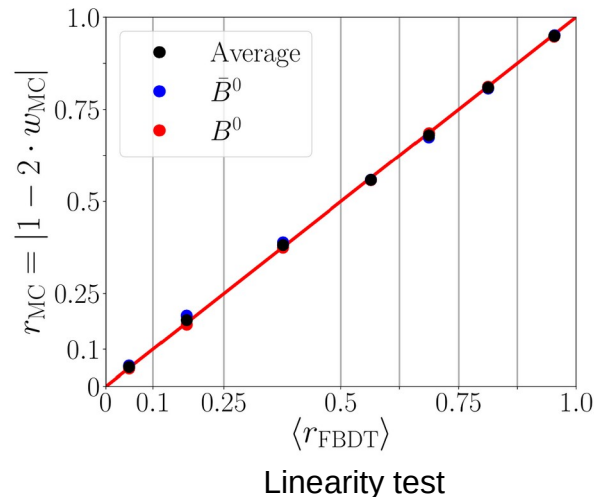


Validation with Belle data/MC



q: tagged flavor
r: quality flag

Belle II simulation



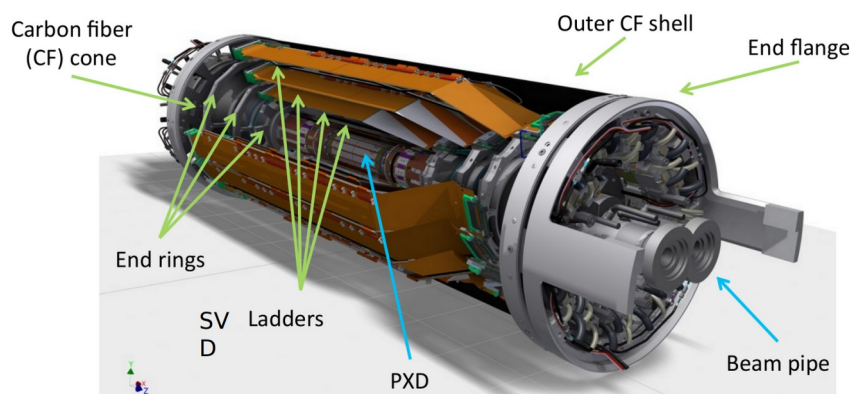
Decay time measurement

- Improved resolution in spite of reduced boost ($\beta\gamma$):
 - New inner vertex detectors: pixel vertex detector and silicon strip tracker.
 - Improved vertex fit softwares. [IEEE TNS, 58, 434 – 444 \(2011\)](#)
[CMS-NOTE-2008-033](#)
[NIMA552, 566–575 \(2005\)](#)
- A factor of 1.5~2 improvement compared to that of Belle.

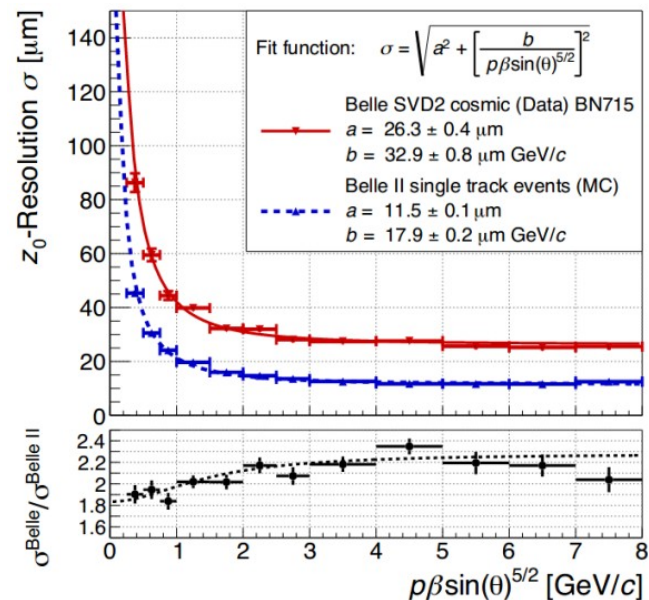
$$\Delta z = \beta\gamma c\Delta t$$

$$\Delta t = t_{CP} - t_{tag}$$

Belle II pixel vertex detector

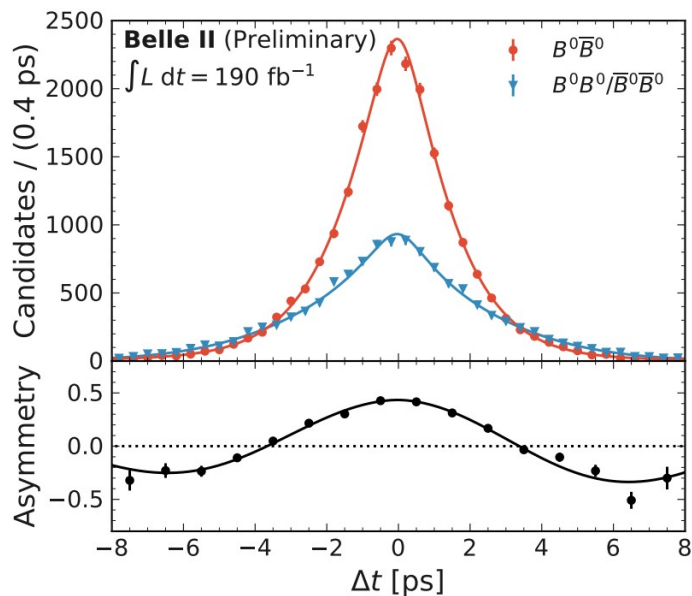


z resolution
Belle data v.s. Belle II MC



Time-dependent mixing measurement

- Δm_B : Mass difference between eigenstates.
 - From B^0 - \bar{B}^0 mixing measurement using flavor tagging.
- Belle II recent result:
 - Systematic uncertainty is smaller than that in Belle and BaBar.



New for JPS

**Belle II $B^0 \rightarrow D^{(*)-} K/\pi$
190 fb^{-1}**

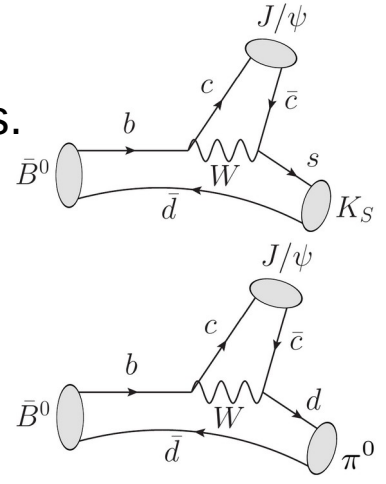
$$\Delta m_B = (0.516 \pm 0.008 \text{ (stat.)} \pm 0.005 \text{ (syst.)}) \text{ ps}^{-1}$$

$$\text{World average: } \Delta m_B = (0.5065 \pm 0.0019) \text{ ps}^{-1}$$

$\varphi_1: \bar{b} \rightarrow \bar{c}c\bar{s}$

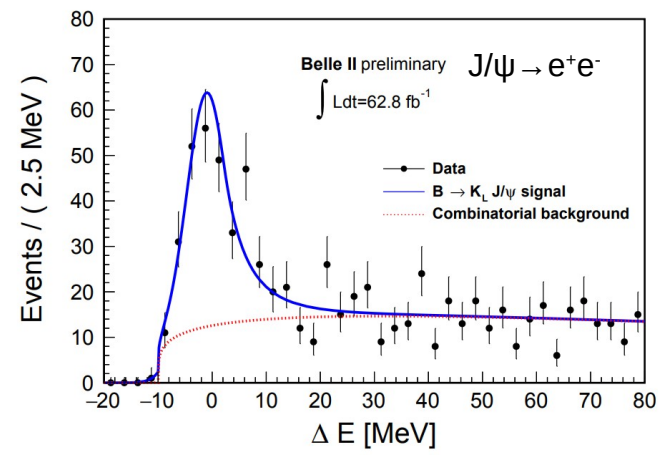
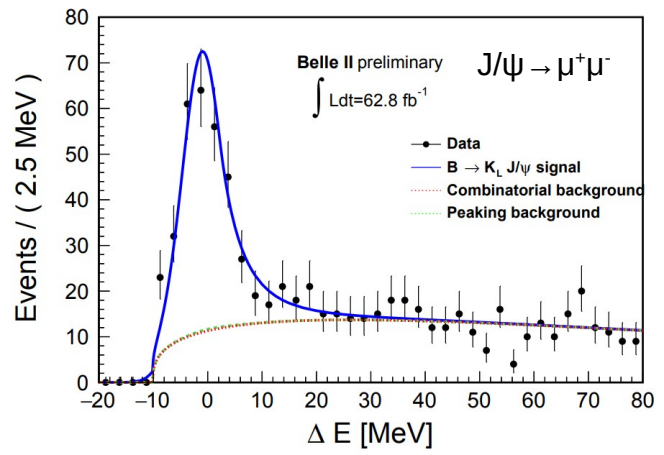
$$\beta = \phi_1 = \arg \left(- \frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} \right)$$

- φ_1 measurement with $\bar{b} \rightarrow \bar{c}c\bar{s}$
 - Theoretical clean. Small contribution from other diagrams.
 - $S_f \sim \xi_f \sin 2\varphi_1$, ξ_f : CP eigenstate.
 - $B^0 \rightarrow J/\psi K^0$ golden mode. [PRL 95, 221804 \(2005\)](#)



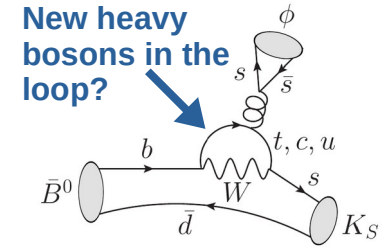
- $\sin(2\varphi_1)$ world average: 0.699 ± 0.017
- Belle II sensitivity of $B^0 \rightarrow J/\psi K_S^0$ @ 50 ab^{-1}
 - Penguin pollution is not negligible: Constraint from $b \rightarrow \bar{c}c\bar{d}$ e.g. $B^0 \rightarrow J/\psi \pi^0$ or other SU(3) related modes.
 - Systematic uncertainty dominates.
 - < 0.01 uncertainty on S_f .

Belle II $B^0 \rightarrow J/\psi K_L^0$ 62.8 fb^{-1}
[arXiv: 2106.13547 \[hep-ex\]](#)



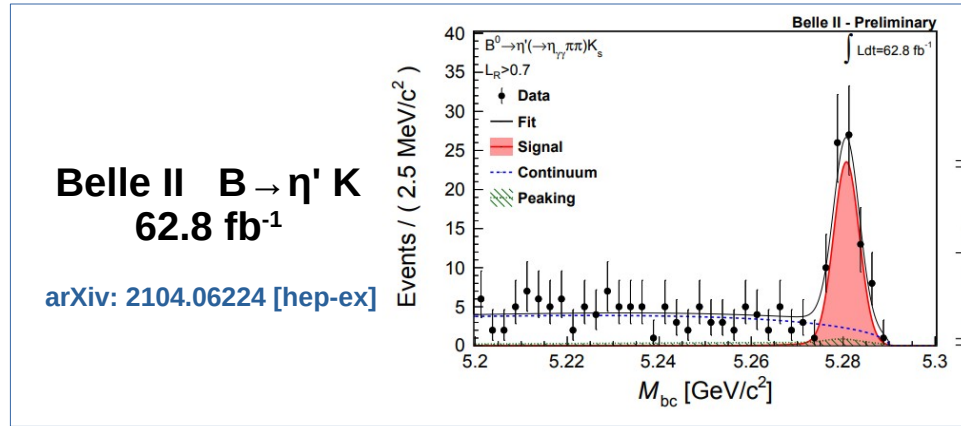
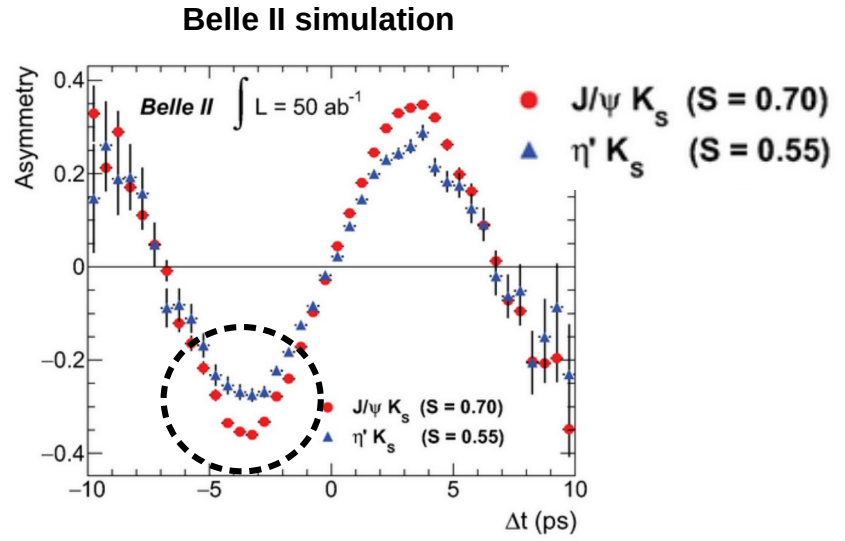
$\varphi_1: b \rightarrow sq\bar{q}$

- $b \rightarrow sq\bar{q}$:
 - $S_f = -\xi_f \sin 2\varphi_1^{\text{eff}} \sim -\xi_f \sin 2\varphi_1$ assuming only SM penguin.
 - Difference from $b \rightarrow ccs$: NP in penguin loop.



- Belle II Golden modes: $B^0 \rightarrow \eta' K^0$, $B^0 \rightarrow \phi K^0$, $B^0 \rightarrow K^0 K^0 K^0$.
 - Advantage: neutral particle. Expect to have the best sensitivity.

- Belle II simulation @ 50 ab^{-1}
 - S_f of $B^0 \rightarrow \eta' K^0$ and $B^0 \rightarrow J/\psi K^0$
 - Able to see the difference if any.

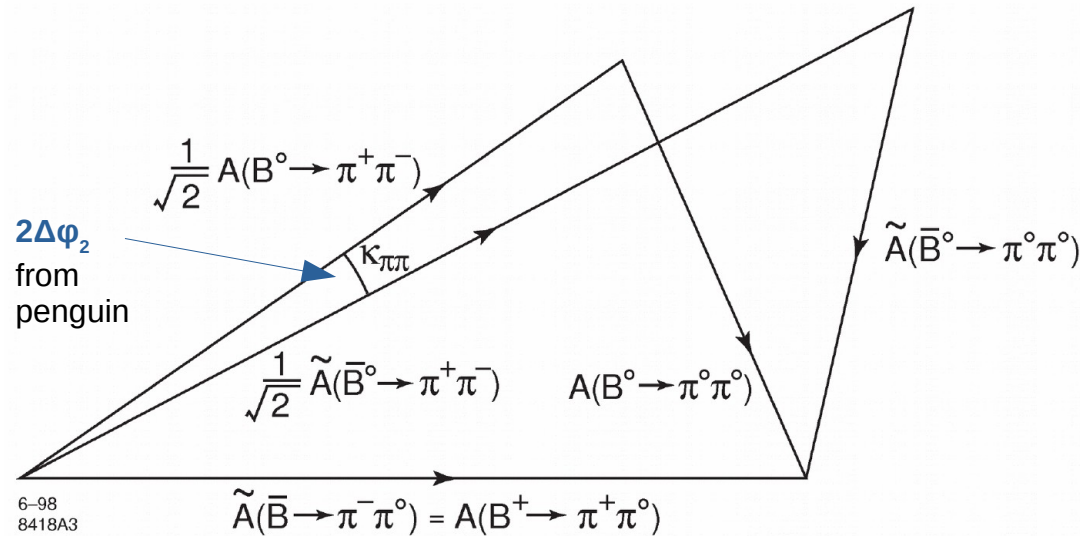
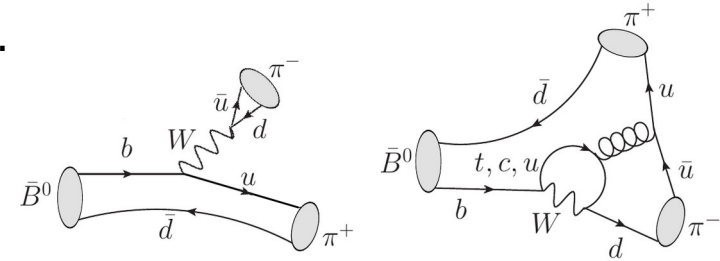


**Belle II $B \rightarrow \eta' K$
62.8 fb⁻¹**
arXiv: 2104.06224 [hep-ex]

$$M_{bc} \equiv \sqrt{s/(4c^4) - (p_B^*/c)^2}$$

Channel	This analysis	World average [9]
$B^\pm \rightarrow \eta' K$	$63.4^{+3.4}_{-3.3}(\text{stat}) \pm 3.4(\text{syst})$	70.4 ± 2.5
$B^0 \rightarrow \eta' K^0$	$59.9^{+5.8}_{-5.5}(\text{stat}) \pm 2.7(\text{syst})$	66 ± 4

- φ_2 measurement: From $b \rightarrow u$ tree with non-negligible $b \rightarrow d$ penguin.
 - Isospin analysis with $B \rightarrow hh$ modes ($h=\pi,\rho$).
- Compared with LHCb, Belle II can measure all of these isospin modes.



6-98
8418A3

Eur. Phys. J. C77 (2017) no. 8, 574

- Charmless hadronic B decays:
 - Challenge: large combinatorial background from $e^+e^- \rightarrow q\bar{q}$ continuum process.
 - PID: K/ π suppression.
 - Continuum suppression: Based on MVA tool (BDT).

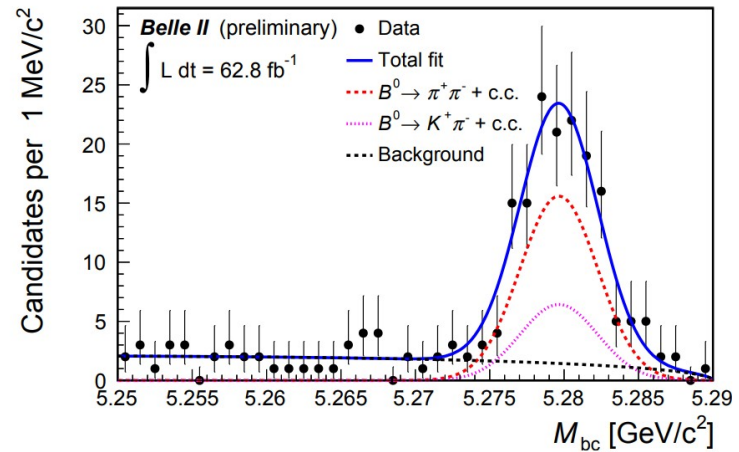
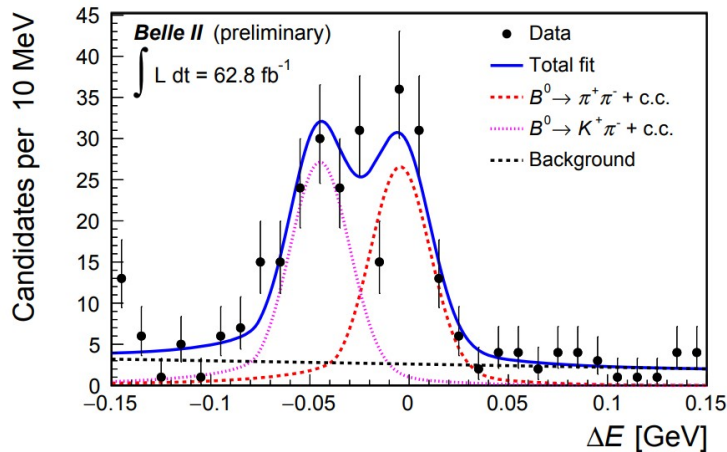
- Belle II recent results:
 - 2D fit with ΔE and M_{bc} .

$$\Delta E \equiv E_B^* - \sqrt{s}/2$$

$$M_{bc} \equiv \sqrt{s/(4c^4) - (p_B^*/c)^2}$$
 defined in center-of-momentum frame

Belle II $B^0 \rightarrow h^+\pi^-$ 62.8 fb⁻¹

[arXiv:2106.03766 \[hep-ex\]](https://arxiv.org/abs/2106.03766)



$$\mathcal{B}(B^0 \rightarrow \pi^+\pi^-) = [5.8 \pm 0.7(\text{stat}) \pm 0.3(\text{syst})] \times 10^{-6}$$

Also see: **Belle II $B^+ \rightarrow h^+\pi^0$ 62.8 fb⁻¹** [arXiv:2105.04111 \[hep-ex\]](https://arxiv.org/abs/2105.04111)

$\phi_2: B \rightarrow \rho\rho$

Preliminary

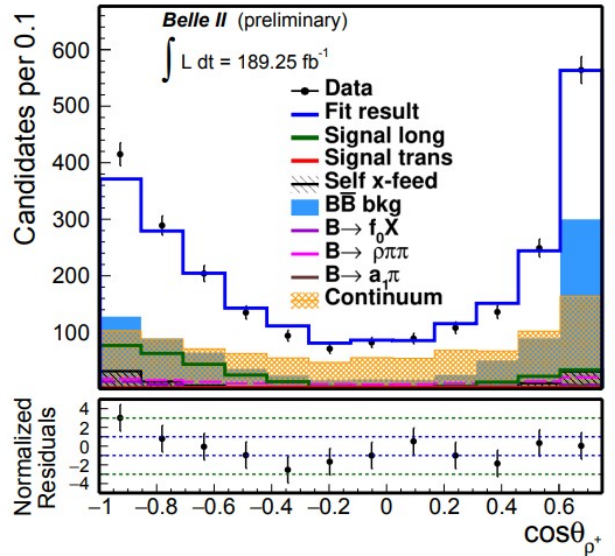
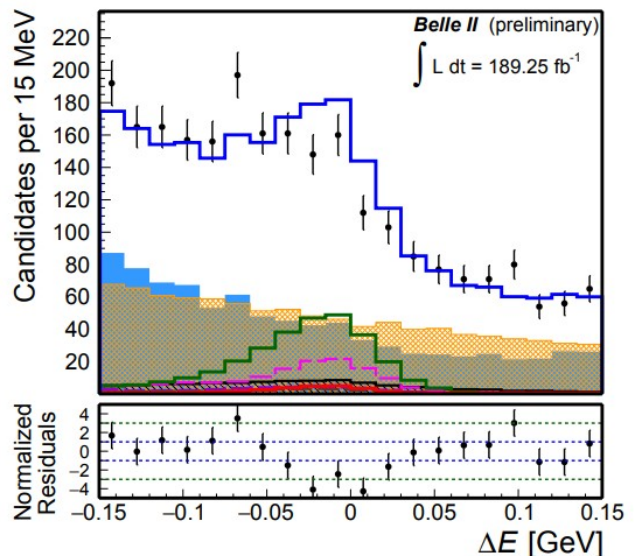
- $B^0 \rightarrow \rho^0\rho^0$: Golden mode for ϕ_2 determination.
- $B^+ \rightarrow \rho^0\rho^+$: Estimate penguin pollution
- Challenge:
Combinatorial background due to pion-only final state and wide ρ peak.
- 6D fit:
 - Angular analysis: need to measure longitudinal polarization fraction (f_L).
 - ΔE , continuum suppression, ρ masses (2), cosine of the helicity angle of ρ (2).

$$\mathcal{B}(B^+ \rightarrow \rho^+\rho^0) = [22.1_{-2.0}^{+2.1}(\text{stat}) \pm 2.6(\text{syst})] \times 10^{-6},$$

$$f_L = 0.943_{-0.033}^{+0.035}(\text{stat}) \pm 0.026(\text{syst}),$$

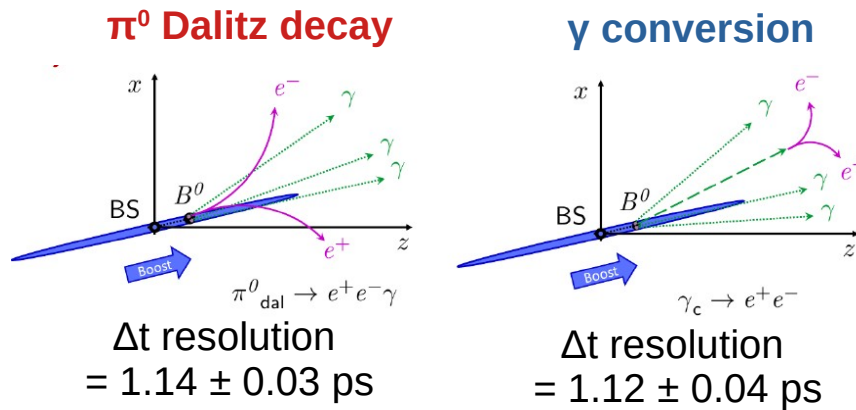
$$\mathcal{A}_{CP} = -0.069 \pm 0.068(\text{stat}) \pm 0.039(\text{syst}).$$

Belle II $B^+ \rightarrow \rho^+\rho^0$ 189.3 fb⁻¹

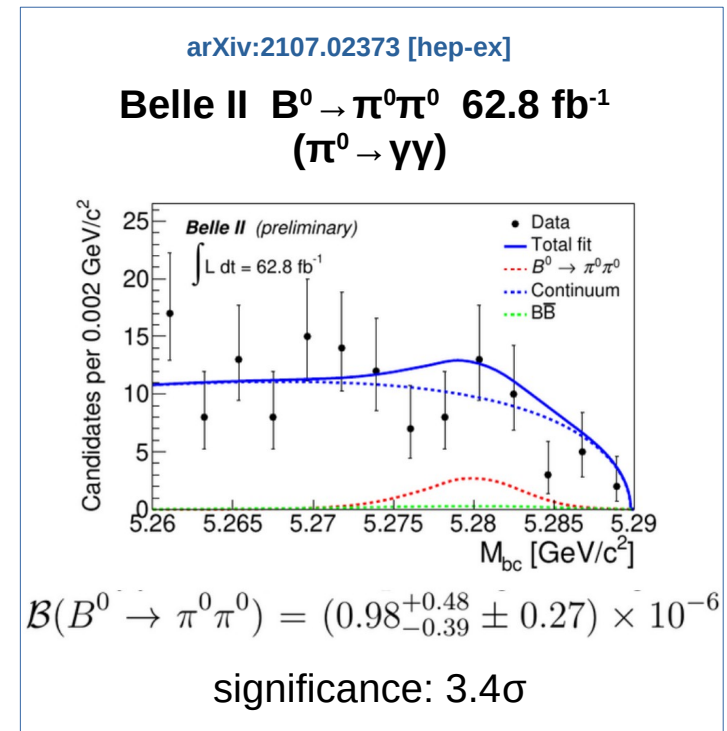


ϕ_2 : Belle II prospect

- TDCPV of $B^0 \rightarrow \pi^0 \pi^0$ is unique for Belle II with target full data.
 - Use **π^0 Dalitz decay ($\rightarrow \gamma e^+ e^-$)** and **γ ($\rightarrow e^+ e^-$) conversion** for vertexing.
 - @ 50 ab^{-1} : Expect ~ 270 signal yields, uncertainty of $S(\pi^0 \pi^0) \sim 0.28$

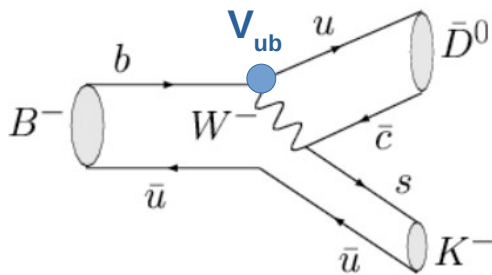


- Belle II prospect:
 - $S(\pi^0 \pi^0)$: reduce the ambiguity in ϕ_2 determination by a factor of 2 or 4.
 - Combining all $\rho\rho + \pi\pi + S(\pi^0 \pi^0)$: ϕ_2 sensitivity $\sim 0.6^\circ$ @ 50 ab^{-1}

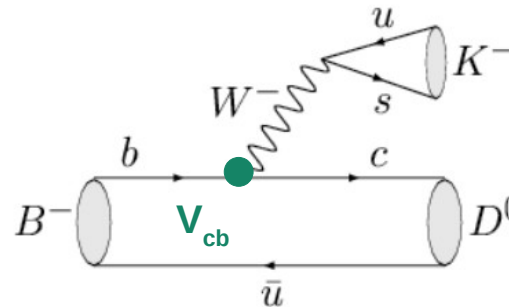


- ϕ_3 is measured by the phase difference between tree amplitudes of $B \rightarrow D^{(*)}K^{(*)}$ decays
 - Interference between $b \rightarrow c$ (favored) and $b \rightarrow u$ (suppressed).
 - As no penguin contribution, theoretical uncertainty is small.
 $\delta\phi_3/\phi_3 \sim 10^{-7}$ [JHEP 01, 015 \(2014\)](#)

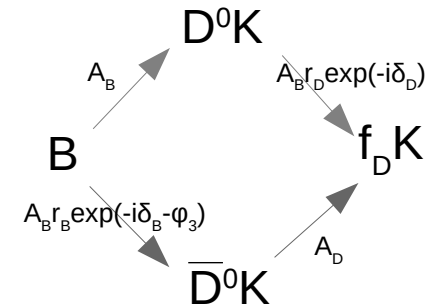
$b \rightarrow u$ (suppressed)



$b \rightarrow c$ (favored)



Using self-conjugate D^0 decay



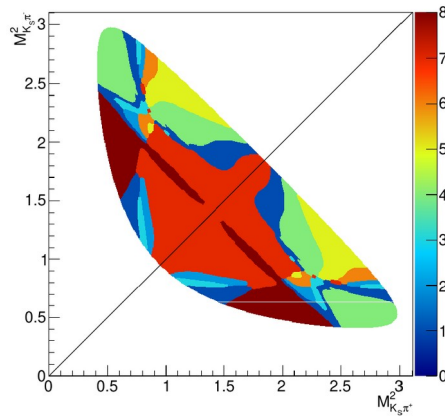
$$\frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} = r_B e^{i(\delta_B - \phi_3)}$$

r_B : ratio of amplitudes ~ 0.1

[HFLAV16, Eur. Phys. J. C 77 \(2017\) 895](#)

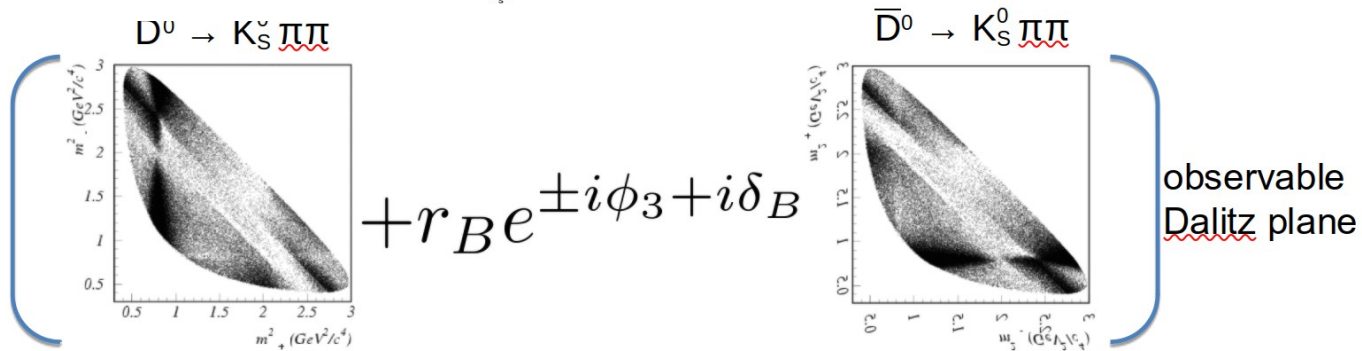
δ_B : strong phase difference. External input from charm factory.

- Belle II Golden mode: GGSZ with amplitude analysis
 - Model-independent amplitude analysis:
 - ~9% uncertainty due to amplitude modeling at Belle and BaBar.
 - Fit on symmetrical bins to obtain yields from D flavor eigenstates.



Dalitz binning (from CLEO)

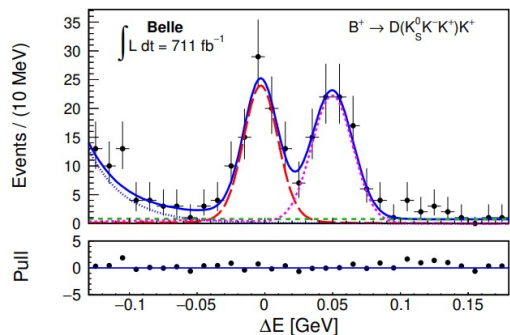
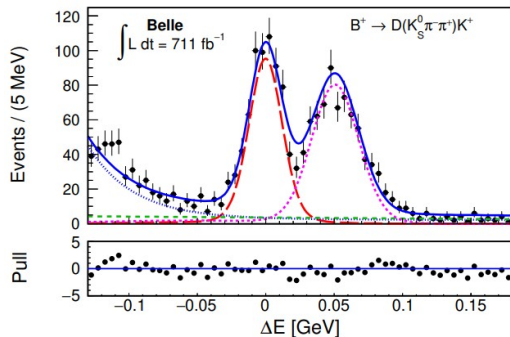
PRD 82, 112006 (2010)



$$d\Gamma_{B^-}(m_+^2, m_-^2) \propto |A_+|^2 + r_B^2 |A_-|^2 + 2r_B |A_+| |A_-| (\cos \delta_D \cos(\delta_B + \phi_3) - \sin \delta_D \sin(\delta_B + \phi_3)) dp$$

ϕ_3 : GGSZ, Belle II prospect

- The latest result with Belle (771 fb⁻¹) + Belle II (128 fb⁻¹):
1st paper with combined data! [JHEP 02 2022, 063 \(2022\)](#)



Belle:

[PRD 85, 112014 \(2012\)](#)

$$\phi_3 = (77.3_{-14.9}^{+15.1} \pm 4.1 \pm 4.3)^\circ$$

Belle + Belle II:

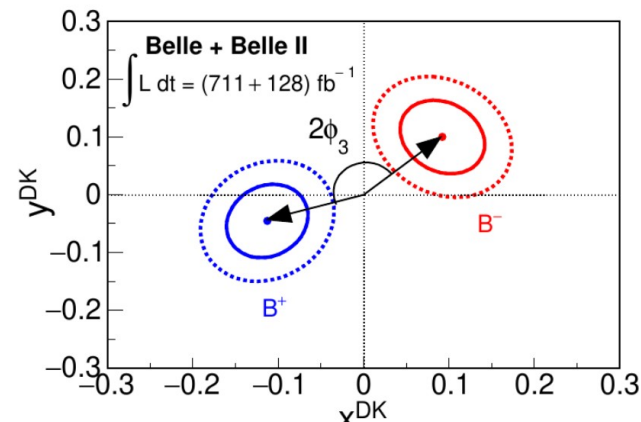
$$\phi_3 = (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ,$$

$$r_B^{DK} = 0.129 \pm 0.024 \pm 0.001 \pm 0.002,$$

$$\delta_B^{DK} = (124.8 \pm 12.9 \pm 0.5 \pm 1.7)^\circ.$$

3rd uncertainty:
ext. input

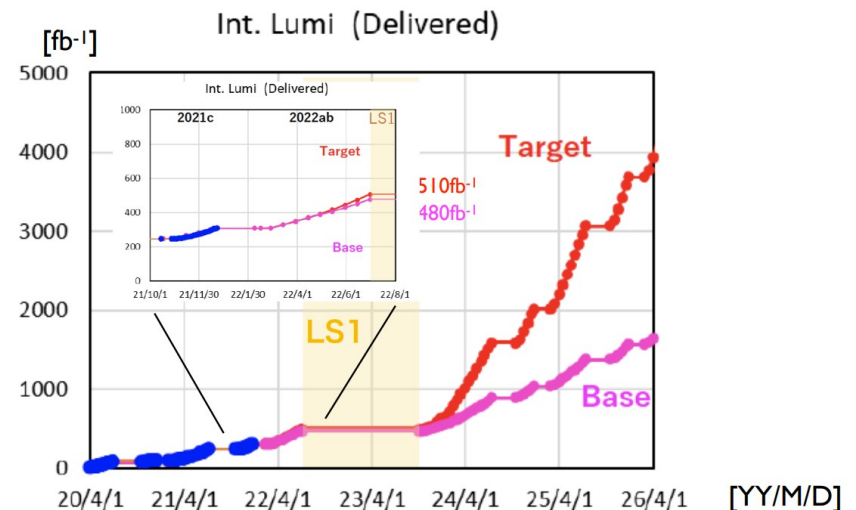
- Belle II prospect:
 - Present precision by LHCb: 4°.
 - Assume 10 fb⁻¹ $\psi(3770)$ data from BES-III:
 $\delta\phi_3(50 \text{ ab}^{-1}) = 3^\circ$ using GGSZ
 $\delta\phi_3(50 \text{ ab}^{-1}) = 1.6^\circ$ with other D decay modes.



$$(x_{\pm}, y_{\pm}) = r_B(\cos(\delta_B \pm \phi_3), \sin(\delta_B \pm \phi_3))$$

Summary

- Measurements on CKM matrix elements offer a good probe for SM precision test and NP search in flavor sector.
- Belle II will play a key role in it.
 - Much larger data set.
 - Improvements on software, methodologies, and systematics.
 - Unique sensitivity and capability of most decay modes.
 - Preliminary studies with Belle II early data have been performed for each.
- Stay tuned with us to look forward to more results from Belle II.



LS1: Full pixel detector installation, readout upgrade for DAQ, etc.

Other Belle II talks with new results @ JPS Spring 2022

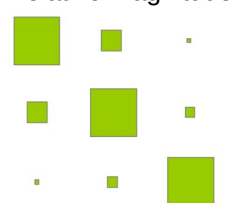
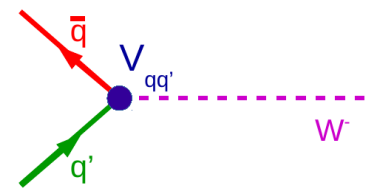
- 15aA561
 - 10. 伊藤慎太郎 「 Belle-II 実験における heavy QCD axion を伴った $B^+ \rightarrow K^+ a$ 崩壊の探索」
- 16pA573
 - 8. 植松祐真 「 Belle II 実験における $B^0 \rightarrow K_S^0 \pi^0 \gamma$ 過程の時間依存 CP 非対称度の解析に向けた研究」
 - 9. 杉浦亮平 「 Belle II 実験における $B^0 \rightarrow K^+ K^- K_S^0$ 崩壊過程の時間依存 CP 非対称度の解析に向けた研究」
 - 10. 古賀太一朗 「 BelleII 実験における $B \rightarrow D^* \lnu$ 崩壊分岐比と CKM 行列要素 $|V_{cb}|$ の測定」
 - 11. 裴漢郁 「 Belle II 実験における $B^0 \rightarrow \eta' K_S$ 崩壊過程での時間依存 CP 対称性破れ測定の研究」
 - 12. 楠戸愛美 「 Belle II 実験における $B^0 \rightarrow J/\psi K^{*0} (\rightarrow K^+ \pi^-)$ モードによるフレーバー識別の較正と Δt 分解能の評価」
 - 13. 谷川輝 「 Belle II 実験における $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ 過程の時間依存 CP 非対称度の測定」
- 19pS06
 - 4. 大強度ビームと標的技術が拓く素粒子・原子核実験の新展開
吉原圭亮 「高ルミノシティマシンで探す新たな物理法則」

Backup

CKM matrix

- Cabibbo-Kobayashi-Maskawa (CKM) matrix
 - Describes mixing of quarks via weak interaction in Standard Model (SM).

Relative magnitude

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



The complex phase represents the source of CV violation in SM.

$$= \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \quad \text{Wolfenstein parameterization}$$

- Unitarity:

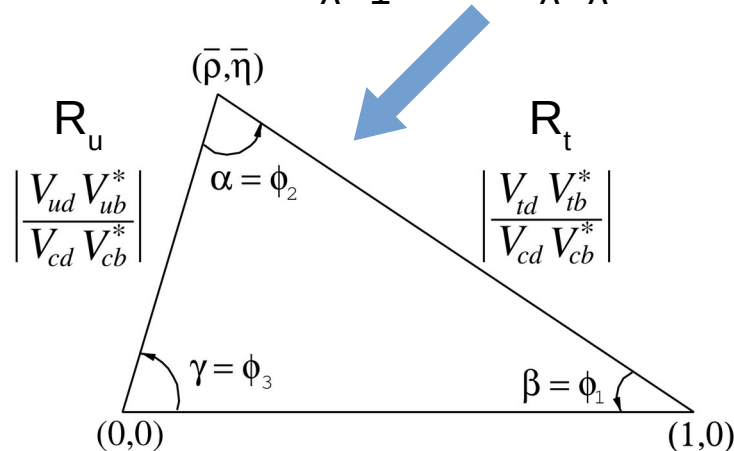
$$V^\dagger V = 1 \quad \longrightarrow \quad \boxed{V_{ud} V_{ub}^*} + V_{cd} V_{cb}^* + \boxed{V_{td} V_{tb}^*} = 0$$

$\lambda^3 * 1$ $\lambda^2 * \lambda$ $1 * \lambda^3$

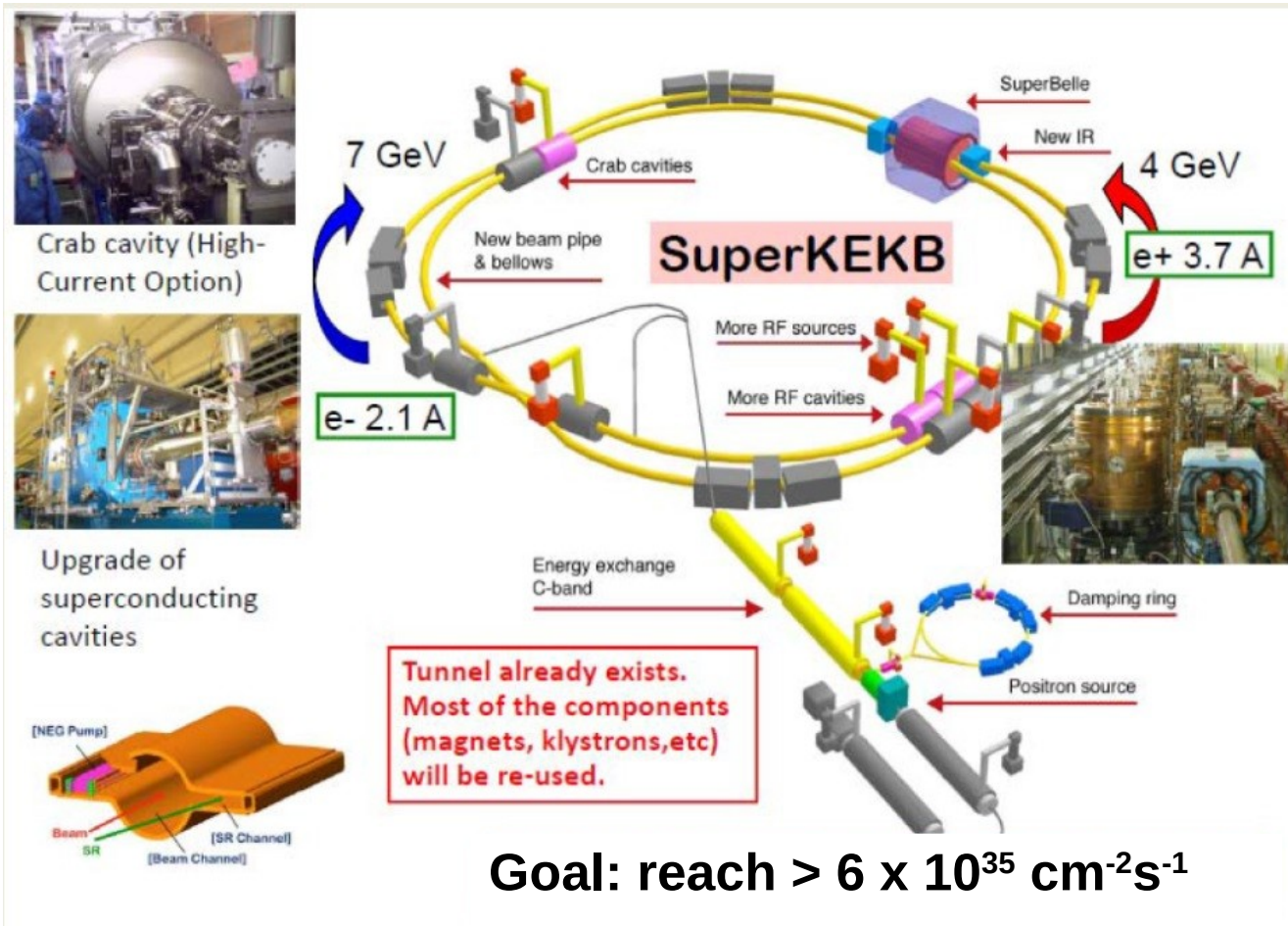
$$\beta = \phi_1 = \arg \left(- \frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right)$$

$$\alpha = \phi_2 = \arg \left(- \frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right)$$

$$\gamma = \phi_3 = \arg \left(- \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$



SuperKEKB



UT angles

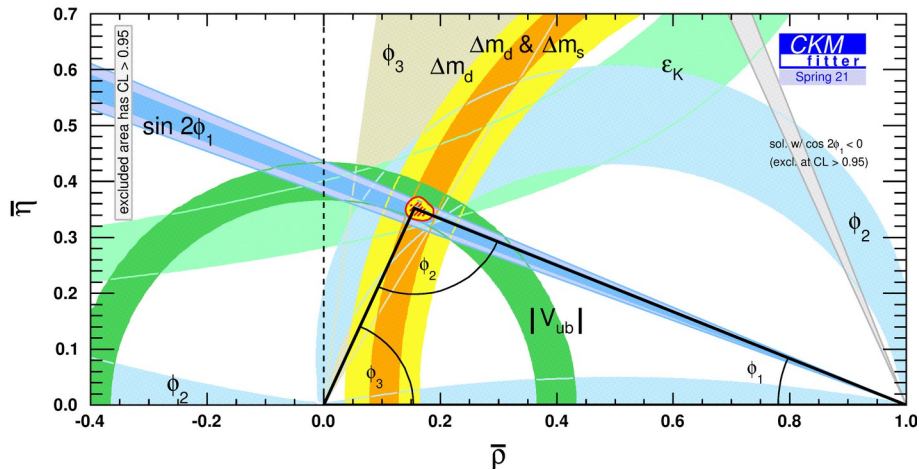
- Current results:

Global fit by CKM fitter

$$\beta = \varphi_1 = (23.7^{+1.3}_{-1.2})^\circ$$

$$\alpha = \varphi_2 = (91.8^{+2.7}_{-2.1})^\circ$$

$$\gamma = \varphi_3 = (65.6^{+0.9}_{-2.6})^\circ$$

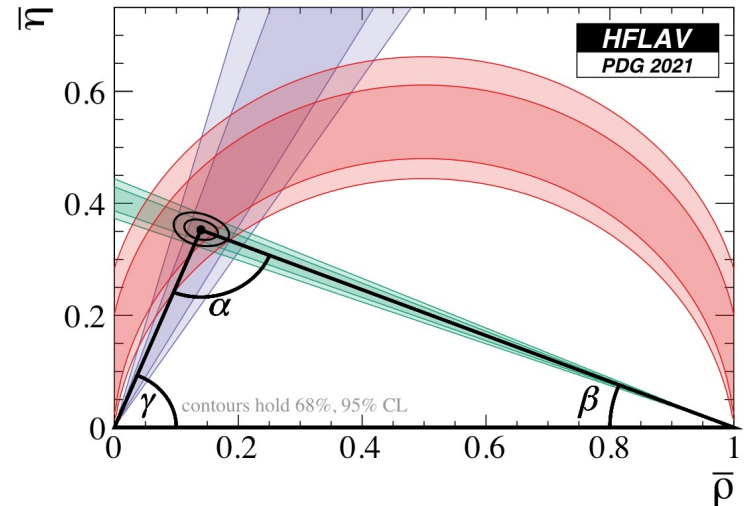


World average by HFLAV

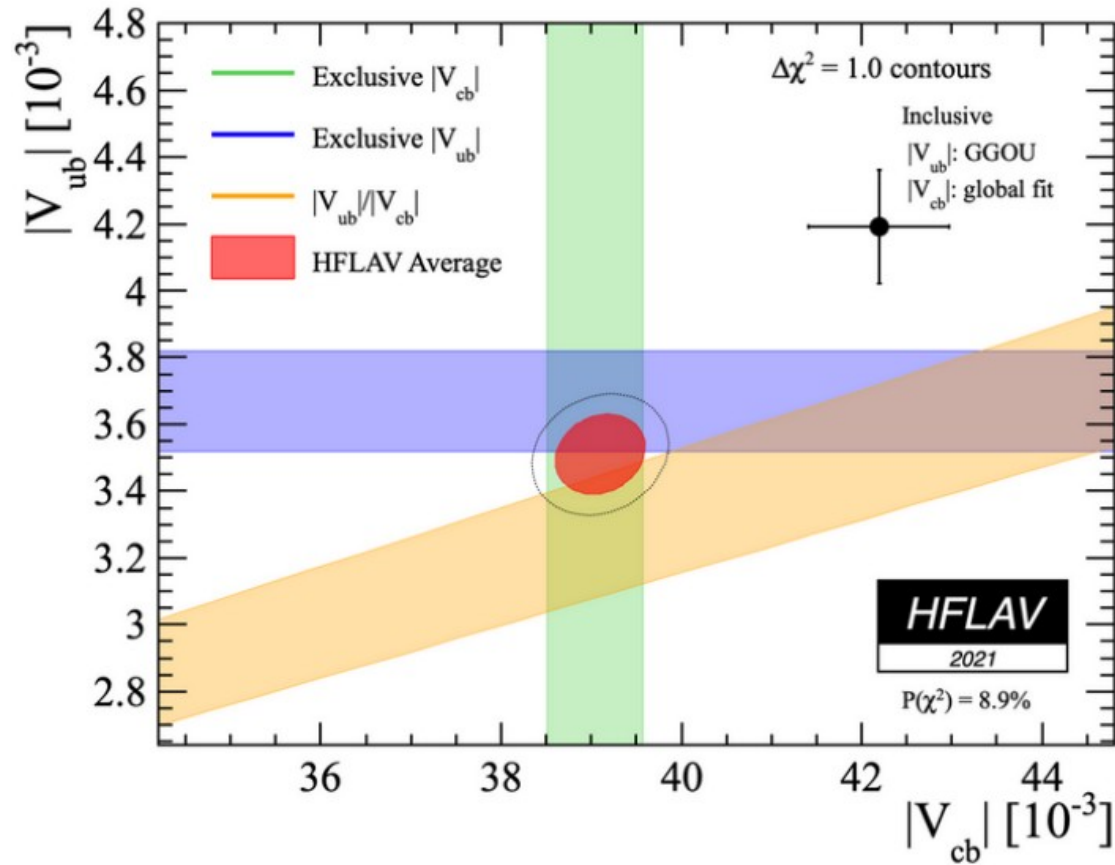
$$\beta = \varphi_1 = (22.2 \pm 0.7)^\circ$$

$$\alpha = \varphi_2 = (85.2^{+4.8}_{-4.3})^\circ$$

$$\gamma = \varphi_3 = (66.2^{+3.4}_{-3.6})^\circ$$



- Current results:



$|V_{cb}|$ exclusive determination

- dBF of $B \rightarrow D^{(*)} | \nu$ as a function of w :

Prog. Theor. Phys. 49, 652
Phys. Rept. 245, 259

Nucl. Phys. B 196 (1982) 83-92
PRD 79 (2009) 014506
Nucl. Phys. B 530 (1998) 153-181

- η_{EW} is electroweak correction: 1.006

$$\frac{d\Gamma}{dw} = \frac{\eta_{EW}^2 G_F^2}{48\pi^3} m_{D^*}^3 (m_B - m_{D^*})^2 g(w) F^2(w) |V_{cb}|^2$$

$$w = \frac{P_B \cdot P_{D^*}}{m_B m_{D^*}} = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

$$g(w) F^2(w) = h_{A_1}^2(w) \sqrt{w^2 - 1} (w + 1)^2 \left\{ 2 \left[\frac{1 - 2wr + r^2}{(1 - r)^2} \right] \right. \\ \left. \times \left[1 + R_1^2(w) \frac{w - 1}{w + 1} \right] + \left[1 + (1 - R_2(w)) \frac{w - 1}{1 - r} \right]^2 \right\}$$

$$r = \frac{m_{D^*}}{m_B}$$

- $h_{A_1}(w)$, $R_1(w)$, $R_2(w)$: form factors,

CLN parameterization:

$$h_{A_1}(w) = h_{A_1}(1) [1 - 8\rho^2 z + (53\rho^2 - 15)z^2 - (231\rho^2 - 91)z^3]$$

$$R_1(w) = R_1(1) - 0.12(w - 1) + 0.05(w - 1)^2$$

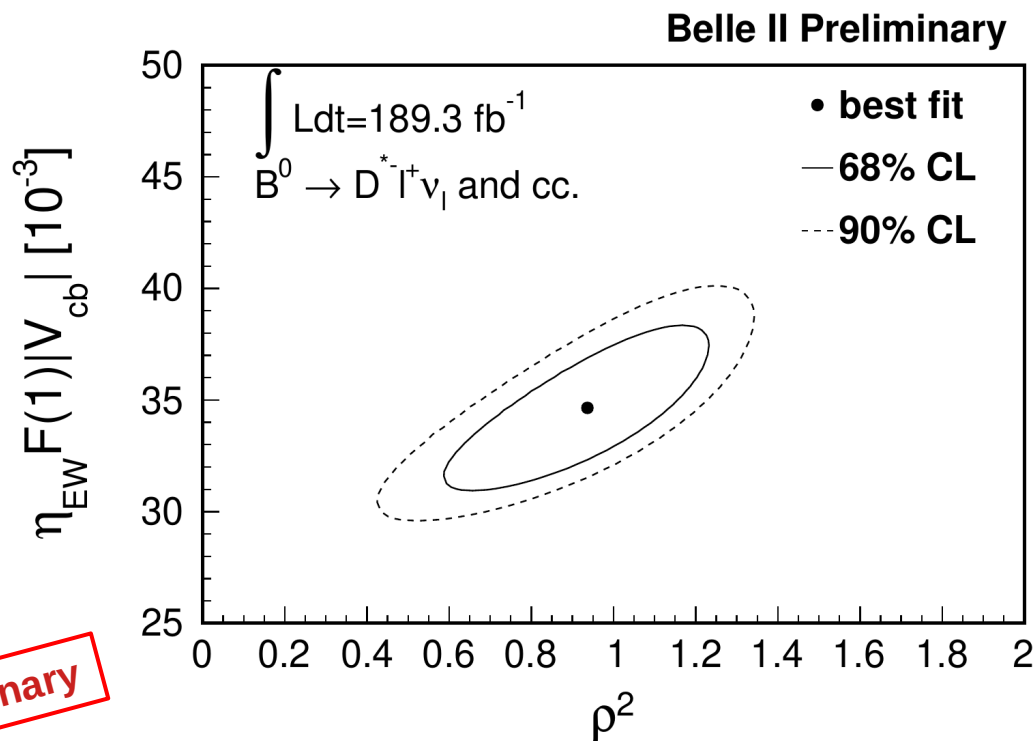
- ρ , $h_{A_1}(1)$, $R_1(1)$, $R_2(1)$:

$$R_2(w) = R_2(1) - 0.11(w - 1) - 0.06(w - 1)^2$$

form factor constants.

$$z = \frac{\sqrt{w + 1} - \sqrt{2}}{\sqrt{w + 1} + \sqrt{2}}$$

$|V_{cb}|$ exclusive determination



Preliminary

$$\eta_{EW} F(1) |V_{cb}| (B^- \rightarrow D^{*0} l^- \bar{\nu}_l) = 0.0351 \pm 0.0030 (stat. + syst.)$$

$$\rho^2 (B^- \rightarrow D^{*0} l^- \bar{\nu}_l) = 1.03 \pm 0.27 (stat. + syst.)$$

$$\eta_{EW} F(1) |V_{cb}| (B^0 \rightarrow D^{*-} l^+ \nu_l) = 0.0352 \pm 0.0028 (stat. + syst.)$$

$$\rho^2 (B^0 \rightarrow D^{*-} l^+ \nu_l) = 1.04 \pm 0.22 (stat. + syst.)$$

	Statistical	Systematic (reducible, irreducible)	Total Exp	Theory	Total
$ V_{ub} $ exclusive (had. tagged)					
711 fb ⁻¹	3.0	(2.3, 1.0)	3.8	7.0	8.0
5 ab ⁻¹	1.1	(0.9, 1.0)	1.8	1.7	3.2
50 ab ⁻¹	0.4	(0.3, 1.0)	1.2	0.9	1.7
$ V_{ub} $ exclusive (untagged)					
605 fb ⁻¹	1.4	(2.1, 0.8)	2.7	7.0	7.5
5 ab ⁻¹	1.0	(0.8, 0.8)	1.2	1.7	2.1
50 ab ⁻¹	0.3	(0.3, 0.8)	0.9	0.9	1.3
$ V_{ub} $ inclusive					
605 fb ⁻¹ (old B tag)	4.5	(3.7, 1.6)	6.0	2.5–4.5	6.5–7.5
5 ab ⁻¹	1.1	(1.3, 1.6)	2.3	2.5–4.5	3.4–5.1
50 ab ⁻¹	0.4	(0.4, 1.6)	1.7	2.5–4.5	3.0–4.8
$ V_{ub} $ $B \rightarrow \tau\nu$ (had. tagged)					
711 fb ⁻¹	18.0	(7.1, 2.2)	19.5	2.5	19.6
5 ab ⁻¹	6.5	(2.7, 2.2)	7.3	1.5	7.5
50 ab ⁻¹	2.1	(0.8, 2.2)	3.1	1.0	3.2
$ V_{ub} $ $B \rightarrow \tau\nu$ (SL tagged)					
711 fb ⁻¹	11.3	(10.4, 1.9)	15.4	2.5	15.6
5 ab ⁻¹	4.2	(4.4, 1.9)	6.1	1.5	6.3
50 ab ⁻¹	1.3	(2.3, 1.9)	2.6	1.0	2.8

$\phi_1: b \rightarrow c\bar{c}s, \text{ Belle II prospect}$

- $B^0 \rightarrow J/\psi K_S^0$ @ 50 ab^{-1} : Systematic uncertainty dominates.
- Penguin pollution is not negligible @ 50 ab^{-1} : constraint from $b \rightarrow c\bar{c}d$ such as $B^0 \rightarrow J/\psi \pi^0$ or other SU(3) related modes.

Belle $B^0 \rightarrow J/\psi K_S^0$ [PRL, 108, 171802 \(2012\)](#)

$$S_{J/\psi K_S^0} = +0.670 \pm 0.029(\text{stat}) \pm 0.013(\text{syst}), \quad \sin(2\phi_1) = 0.699 \pm 0.017 \text{ (world average)}$$

$$A_{J/\psi K_S^0} = -0.015 \pm 0.021(\text{stat}) \begin{matrix} + 0.045 \\ - 0.023 \end{matrix}(\text{syst}).$$

**Ultimate sensitivity
by Belle II
on $B^0 \rightarrow J/\psi K_S^0$
@50 ab^{-1}**

	Refer to Belle		Assume 50% improvement on vertexing related syst,	use only leptonic categories in flavor tagging
	No improvement	Vertex improvement	Vertex improvement	Leptonic categories
$S_{J/\psi K_S^0}$ (50 ab^{-1})				
stat.	0.0035	0.0035	0.0035	0.0060
syst. reducible	0.0012	0.0012	0.0012	0.0012
syst. irreducible	0.0082	0.0044	0.0044	0.0040
$A_{J/\psi K_S^0}$ (50 ab^{-1})				
stat.	0.0025	0.0025	0.0025	0.0043
syst. reducible	0.0007	0.0007	0.0007	0.0007
syst. irreducible	+0.043 -0.022	+0.042 -0.011	+0.042 -0.011	0.011

Belle II Physics Book PTEP 2019, 123C01

$\varphi_1: b \rightarrow c\bar{c}q$, Belle II prospect (cont'd)

- $b \rightarrow c\bar{c}s$ @ 50 ab^{-1} .
- ξ_f (CP eigenstate) = -1 : $B^0 \rightarrow J/\psi K_S^0$, $B^0 \rightarrow \psi(2S) K_S^0$, $B^0 \rightarrow \chi_{c1} K_S^0$.
 ξ_f (CP eigenstate) = +1 : $B^0 \rightarrow J/\psi K_L^0$
- Other $b \rightarrow c\bar{c}X$ modes: $B^0 \rightarrow \psi(X) K_S^0$, $B^0 \rightarrow J/\psi V$, $B^0 \rightarrow D^{(*)+}D^{(*)-}$.

Belle all $b \rightarrow c\bar{c}s$

$$S_{c\bar{c}s} = 0.667 \pm 0.023(\text{stat}) \pm 0.012(\text{syst}), \quad \sin(2\varphi_1) = 0.699 \pm 0.017 \text{ (world average)}$$

$$A_{c\bar{c}s} = 0.006 \pm 0.016(\text{stat}) \pm 0.012(\text{syst}),$$

Assume 50%
improvement on
vertexing related
syst,

use only leptonic
categories in flavor
tagging

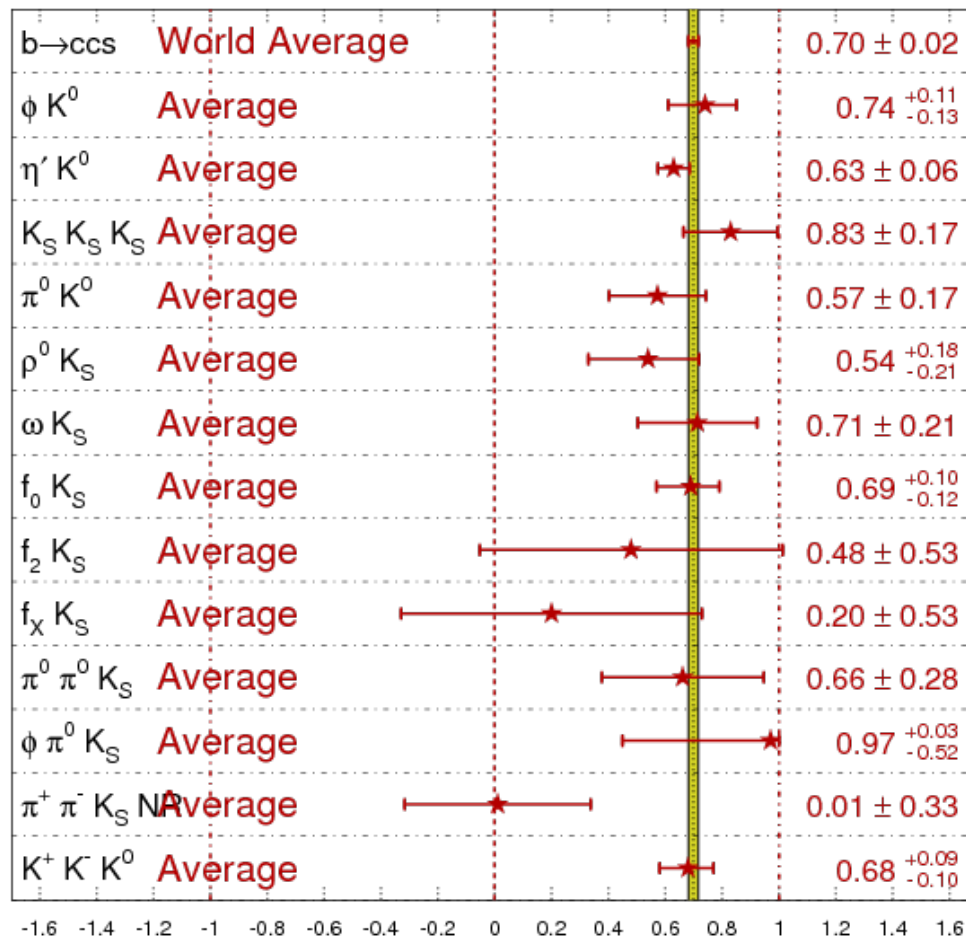
Belle II sensitivity on all $b \rightarrow c\bar{c}s$ @50 ab^{-1}

	Refer to Belle	Assume 50% improvement on vertexing related syst,	use only leptonic categories in flavor tagging
	No	Vertex	Leptonic
	improvement	improvement	categories
$S_{c\bar{c}s}$ (50 ab^{-1})			
stat.	0.0027	0.0027	0.0048
syst. reducible	0.0026	0.0026	0.0026
syst. irreducible	0.0070	0.0036	0.0035
$A_{c\bar{c}s}$ (50 ab^{-1})			
stat.	0.0019	0.0019	0.0033
syst. reducible	0.0014	0.0014	0.0014
syst. irreducible	0.0106	0.0087	0.0035

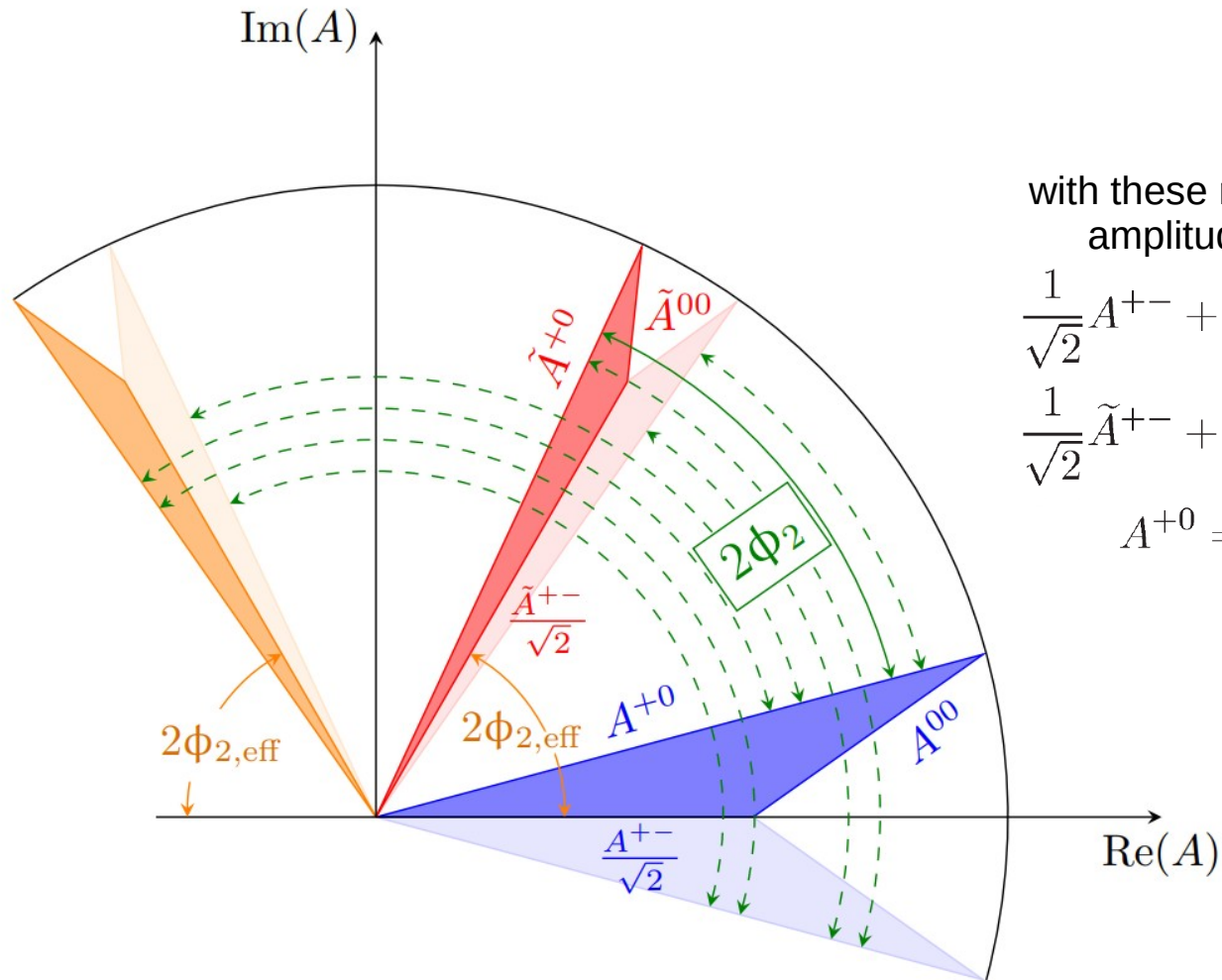
$\sin(2\phi_1^{\text{eff}})$ for $b \rightarrow sq\bar{q}$ penguin

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

HFLAV
Moriond 2021
PRELIMINARY



ϕ_2 : Isospin analysis



with these relations on amplitudes hold:

$$\frac{1}{\sqrt{2}}A^{+-} + A^{00} = A^{+0}$$

$$\frac{1}{\sqrt{2}}\tilde{A}^{+-} + \tilde{A}^{00} = \tilde{A}^{+0}$$

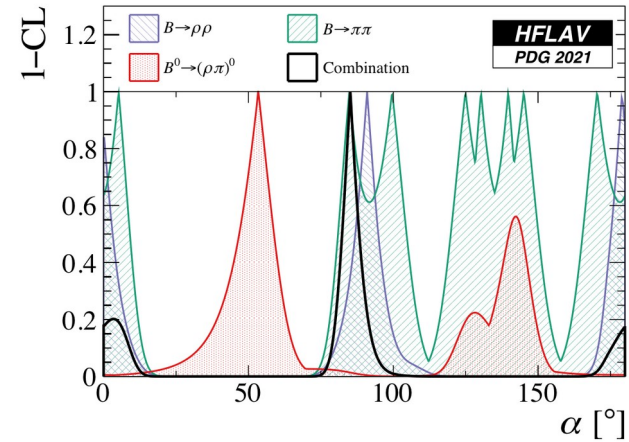
$$A^{+0} = \tilde{A}^{+0}$$

ϕ_2 : Belle II Prospect

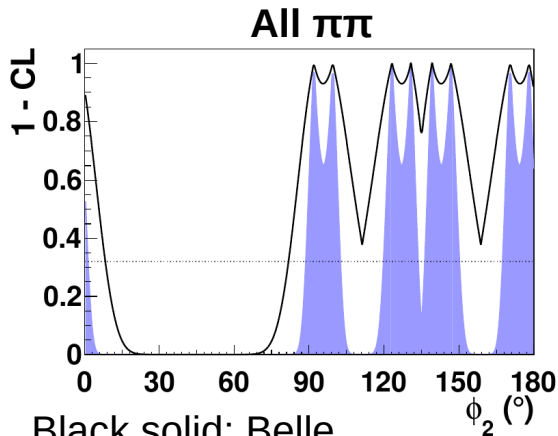
- $S(\pi^0\pi^0)$ would reduce the ambiguity in ϕ_2 determination by a factor of 2 or 4, depending on the measured central value.

- $(85.2^{+4.8}_{-4.3})^\circ$ by World average (HFLAV)
- $(91.8^{+2.7}_{-1.0})^\circ$ by Global fit (CKM fitter)

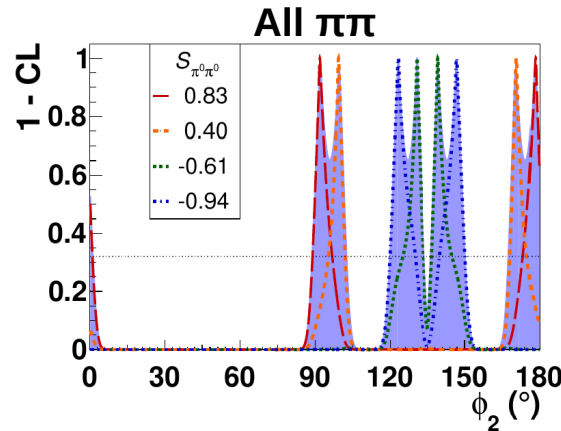
- Belle II combining all $\rho\rho + \pi\pi + S(\pi^0\pi^0)$:
 - ϕ_2 sensitivity $\sim 0.6^\circ$ @50 ab^{-1}



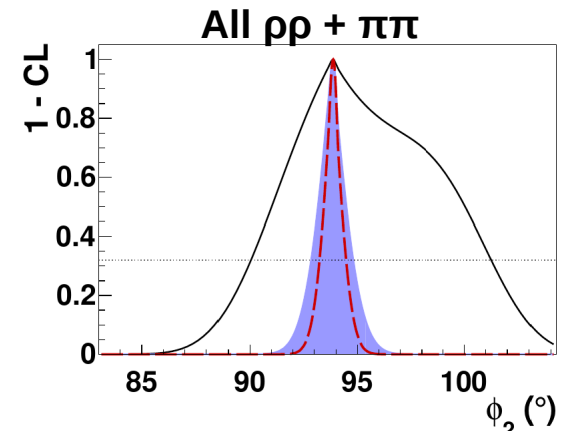
- Other prospect: All $B \rightarrow \rho\pi$ by $B \rightarrow \pi\pi\pi$ amplitude analysis. [Phys. Rev. D 48, 2139 \(1993\)](#)



Black solid: Belle
Blue filled: Belle II @ 50 ab^{-1} extrapolated from Belle's.



Dashed: Belle II + $S(\pi^0\pi^0)$ @ 50 ab^{-1}



Dashed: Belle II, $S(\pi^0\pi^0) = 0.75$, $S(\rho^0\rho^0) = -0.14$ @ 50 ab^{-1}

- Main methods based on different D decay modes:
 - CP eigenstates (GLW):
 K^+K^- , $\pi^+\pi^-$ (CP-even), $K_S^0\pi^0$, $K_S^0\eta$ (CP-odd). [PLB 253, 483 \(1991\)](#)
[PLB 265, 172 \(1991\)](#)
 - Cabibbo-favored and doubly-Cabibbo-suppressed decays (ADS):
 $K^+ + n\pi$ [PRD 63, 036005 \(2001\)](#)
 - **Self-conjugate three-body decays (GGSZ):** [PRD 68, 054018 \(2003\)](#)
 $K_S^0 h^+h^-$ with amplitude analysis
Golden mode for Belle II
 - Singly-Cabibbo-suppressed decays (GLS): [PRD 67 071301 \(2003\)](#)
 $K_S^0 K^+\pi^-$

ϕ_3 : Belle II prospect

- Current limit:
 - $(78^{+15}_{-16})^\circ$ by Belle
 - $(69^{+17}_{-16})^\circ$ by BaBar [PRD 87 052015 \(2013\)](#)
 - $(67 \pm 4)^\circ$ by LHCb [LHCb-CONF-2018-002](#)
[LHCb-CONF-2020-003](#)
 - $(66.2^{+3.4}_{-3.6})^\circ$ by World average (HFLAV)
 - $(65.6^{+0.9}_{-2.6})^\circ$ by Global fit (CKM fitter)

- Belle II prospect:
 - Neutral reconstruction:
More D decay modes at Belle II.
 - Strong phase: external input from BES-III.
 - Assume $10 \text{ fb}^{-1} \psi(3770)$ data from BES-III, expected by Belle II:
 $\delta\phi_3(50 \text{ ab}^{-1}) = 3^\circ$ using GGSZ
 $\delta\phi_3(50 \text{ ab}^{-1}) = 1.6^\circ$ with other D decay modes.

