

# $b \rightarrow c\tau\nu$ overview and Belle II prospects

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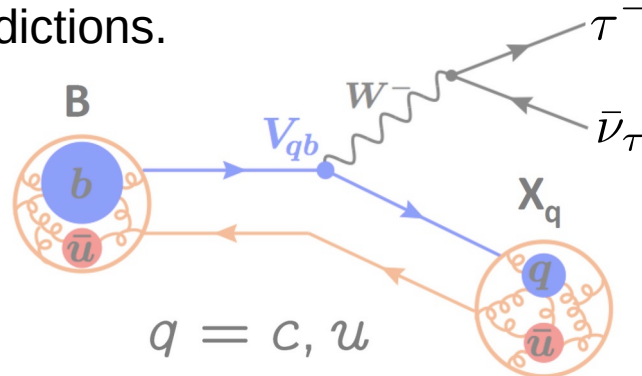
On behalf of the Belle II collaboration

Anomalies and Precision in the Belle II era

Vienna, 6-8.9. 2021

## Introduction

- semi-tauonic  $b \rightarrow c\tau\nu$  decays provide powerful probes of the Standard Model (SM)
  - NP contributions typically less constrained than in  $b \rightarrow c\ell\nu$  ( $\ell = e, \mu$ )
  - rich spectrum of kinematic observables accessible
  - complementary sensitivities of different modes to various SM extensions
  - far from fully explored, experimentally very challenging
  - in the last decade several measurements indicating enhanced rates of  $b \rightarrow c\tau\nu$  compared with the SM predictions.



## Observables

Lepton flavor universality tests:  $\mathcal{R}(H_c) = \frac{\text{signal } \mathcal{B}(B \rightarrow H_c \tau \bar{\nu}_\tau)}{\text{normalization } \mathcal{B}(B \rightarrow H_c \ell \bar{\nu}_\ell)}$   $H_C = D^{(*)}, J/\psi$   
 $(\ell = e, \mu)$

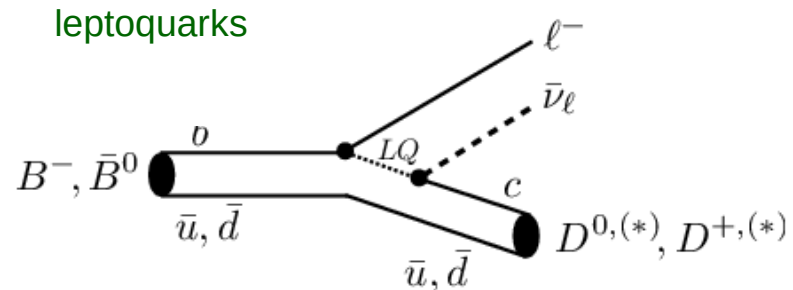
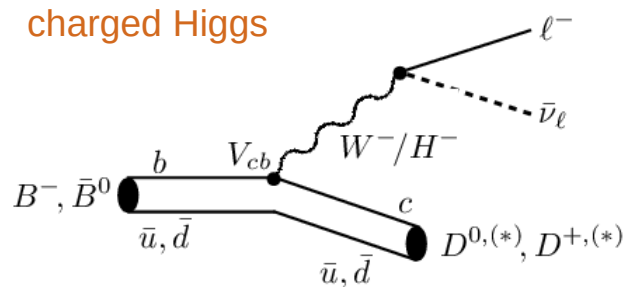
→ experimentally and theoretically convenient due to cancellation of several uncertainties in the ratio

Kinematic variables: e.g.  $q^2 = (p_B - p_{D^*})^2$  distributions

Polarization fractions:  $\tau$  polarization,  $D^{*-}$  longitudinal polarization

Uncertainties of the SM predictions for  $\mathcal{R}(H_c)$  range from 1% to 3%

→ sensitivity to NP contributions



## Measurement basics

- relatively large branching fractions
- but multiple neutrinos in the final state → challenging decay reconstruction
  - determination of initial B momentum allows for evaluation of

$$q^2 = (p_B - p_{D^*})^2$$

momentum transfer to leptons

$$m_{\text{miss}}^2 = (p_B - p_{D^{(*)}} - p_\ell)^2$$

missing mass

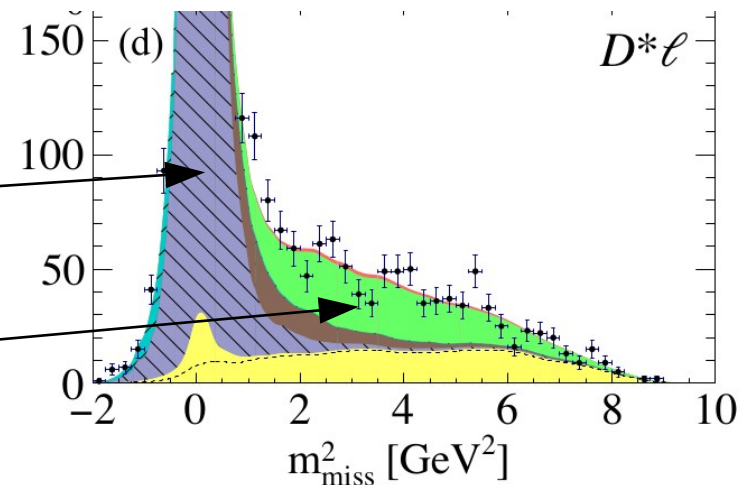
$$E_\ell^* = (p_\ell \cdot p_B) / m_B$$

charged lepton energy in B frame

→ basis for signal / normalization mode separation

single neutrino  
 $B \rightarrow D^* \ell \bar{\nu}_\ell$

multiple neutrinos  
 $B \rightarrow D^* \tau \bar{\nu}_\tau$

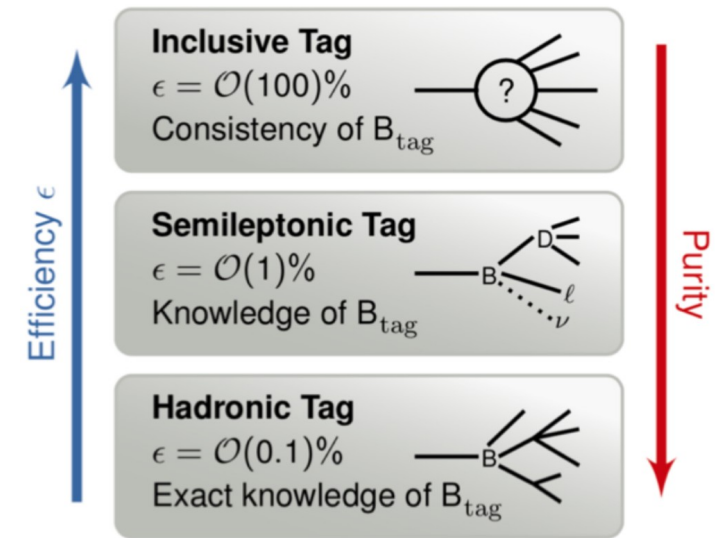
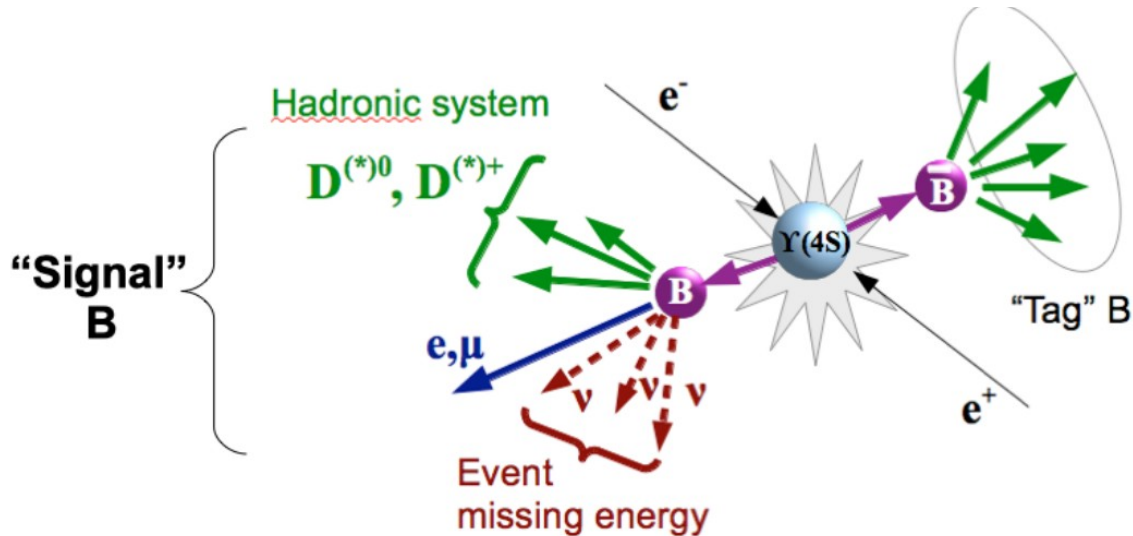


- accessible to **B factories** and **LHCb**

## Measurement basics - B factories

$$- e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

- fully known initial state + hermetic detector ( $4\pi$ )  $\rightarrow$  **tagging techniques**



$\rightarrow$  in signal/normalization events all particles in an event assigned (to  $B_{\text{sig}}$  or  $B_{\text{tag}}$ )

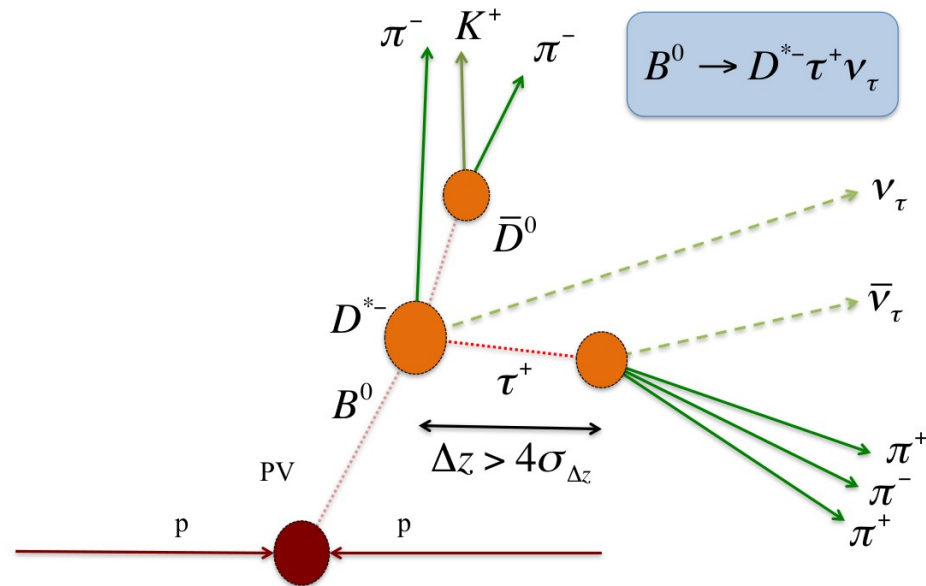
background events: larger  $E_{\text{ECL}}$

extra energy in EM calorimeter

signal vs. normalization:  $m_{\text{miss}}^2$  + kinematics

## Measurement basics - LHCb

- tagging not available
- but very large sample of b-hadrons + large Lorentz boost + excellent vertexing
- well separated vertices in the decay chain



- if  $\tau$  decay vertex can be reconstructed (e.g.  $\tau \rightarrow (3\pi)\nu$ )
  - $B$  momentum determined up to discrete ambiguity
- for  $\tau \rightarrow \mu\nu\bar{\nu}$  vertex not available

→ rest frame approximation:

$$(p_B)_z = \frac{m_B}{m_{reco}} (p_{reco})_z$$

$\downarrow$   
 $D^* \mu$

## Summary of existing B-factory measurements

Hadronic tag with  $\tau \rightarrow \ell\nu\bar{\nu}$

BaBar: Phys. Rev. Lett. 109, 101802, [arXiv:1205.5442](https://arxiv.org/abs/1205.5442)

Belle: Phys. Rev. D 92, 072014, [arXiv:1507.03233](https://arxiv.org/abs/1507.03233)

Result	BABAR	Belle
$\mathcal{R}(D)$	$0.440 \pm 0.058 \pm 0.042$	$0.375 \pm 0.064 \pm 0.026$
$\mathcal{R}(D^*)$	$0.332 \pm 0.024 \pm 0.018$	$0.293 \pm 0.038 \pm 0.015$

Semi-leptonic tag with  $\tau \rightarrow \ell\nu\bar{\nu}$

Belle: Phys. Rev. Lett. 124, 161803, [arXiv:1910.05864](https://arxiv.org/abs/1910.05864)

$$\mathcal{R}(D) = 0.307 \pm 0.037 (\text{stat}) \pm 0.016 (\text{syst})$$

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 (\text{stat}) \pm 0.014 (\text{syst})$$

Hadronic tag with  $\tau \rightarrow \pi\nu, \tau \rightarrow \rho\nu$   
Belle  $\tau$  polarization measurement

Phys. Rev. D 97 (1), 012004, [arXiv:1709.00129](https://arxiv.org/abs/1709.00129)

$$R(D^*) = 0.270 \pm 0.035 (\text{stat})_{-0.025}^{+0.028} (\text{syst})$$

$$P_\tau(D^*) = -0.38 \pm 0.51 (\text{stat})_{-0.16}^{+0.21} (\text{syst})$$

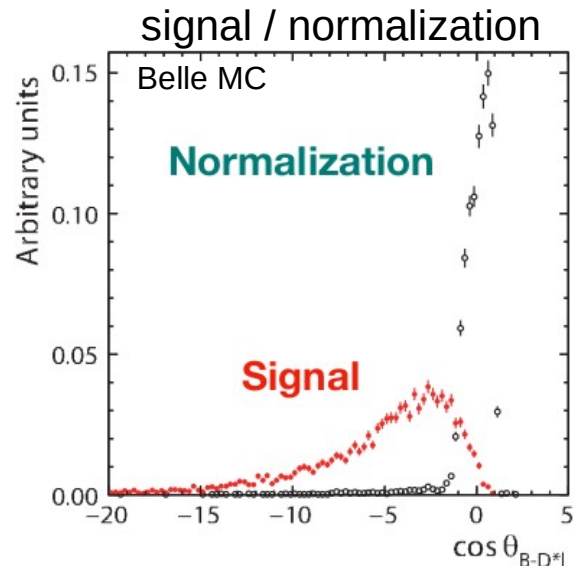
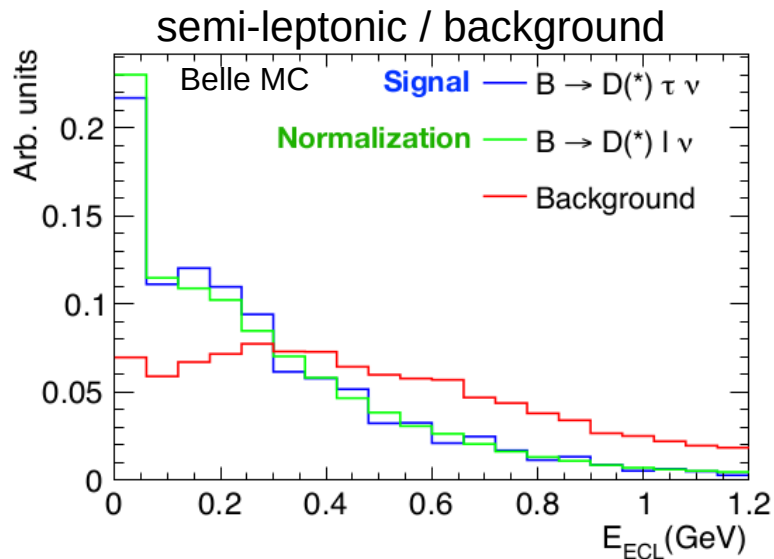
Inclusive tag with  $\tau \rightarrow \pi\nu, \tau \rightarrow \ell\nu\bar{\nu}$   
Belle  $D^{*-}$  polarization measurement  
[arXiv:1903.03102](https://arxiv.org/abs/1903.03102)

$$F_{L,\tau}(D^*) = 0.60 \pm 0.08 (\text{stat}) \pm 0.04 (\text{syst})$$

## Example: Latest $\mathcal{R}(D^{(*)})$ from Belle – Semi-leptonic tag

Phys. Rev. Lett. 124, 161803, [arXiv:1910.05864](https://arxiv.org/abs/1910.05864)

- using FEI (full event interpretation) for the tag-side  $B \rightarrow D^{(*)} l \bar{\nu}_l$  reconstruction
- reconstructed signal modes:  $D^+ \ell^-$ ,  $D^0 \ell^-$ ,  $D^{*+} \ell^-$ ,  $D^{*0} \ell^-$  ( $\ell = e, \mu$ )
- combine kinematic variables using BDT:  $(\cos \theta_{B, D^{(*)} l}, m_{\text{miss}}^2, E_{\text{vis}}) \rightarrow \mathcal{O}_{\text{sig}}$





- $E_{ECL} - \mathcal{O}_{sig}$  distributions of all samples are fit simultaneously, constraining  $\mathcal{R}(D^{(*)0}) = \mathcal{R}(D^{(*)+})$
- free parameters: signal yields, normalization yields,  $B \rightarrow D^{**} l \nu$  yield, feed-down  $D^{(*)}$

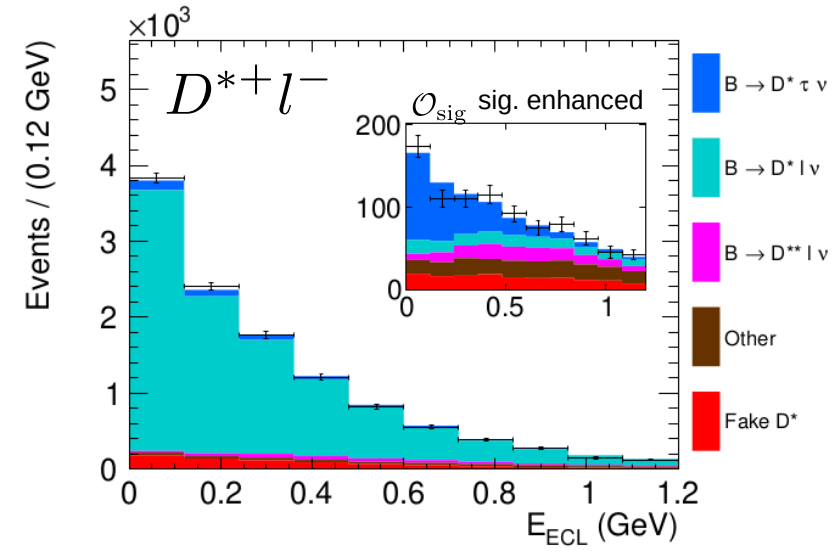
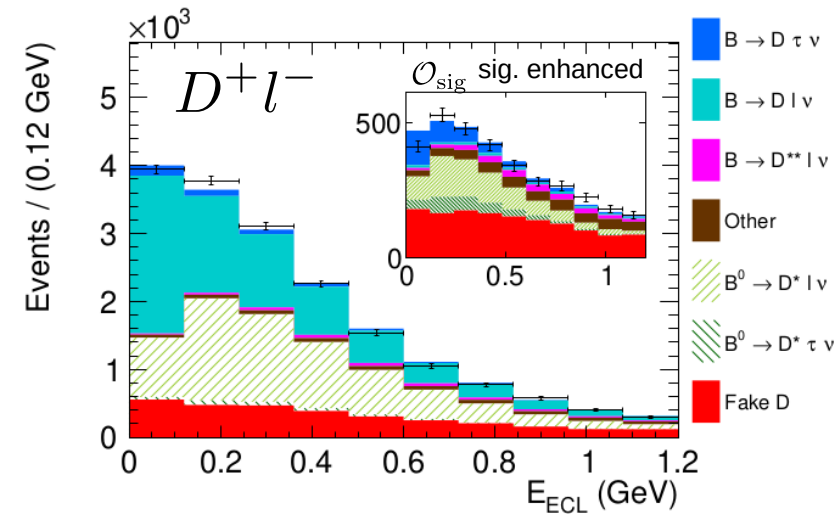
$$\mathcal{R}(D) = 0.307 \pm 0.037 \text{ (stat)} \pm 0.016 \text{ (syst)}$$

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \text{ (stat)} \pm 0.014 \text{ (syst)}$$

Most precise values to date!

### Main systematic uncertainties

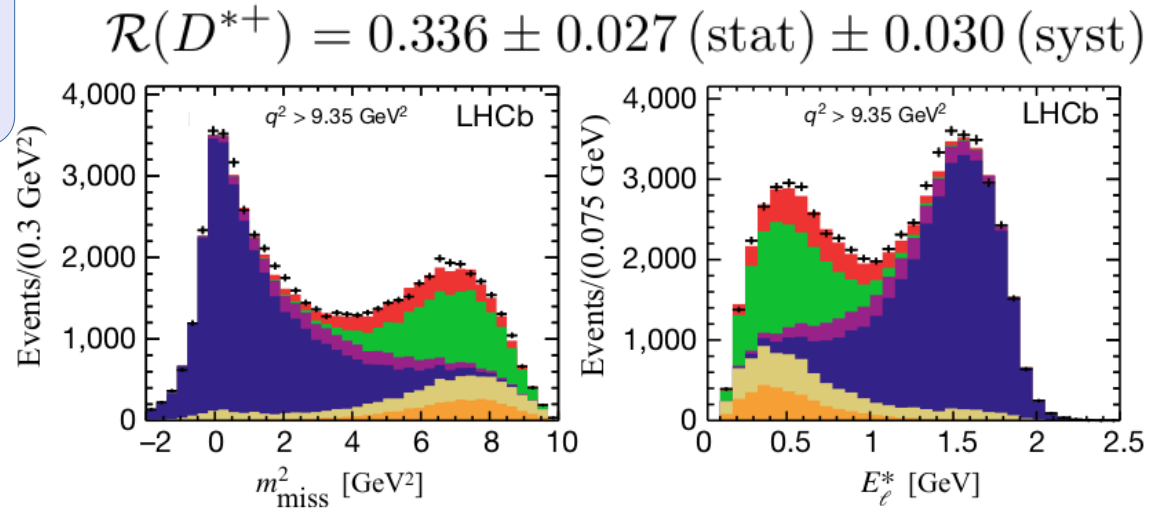
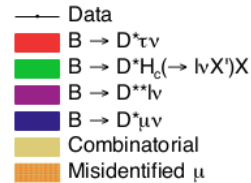
Source	$\Delta\mathcal{R}(D)$ (%)	$\Delta\mathcal{R}(D^*)$ (%)
$D^{**}$ composition	0.76	1.41
PDF shapes	4.39	2.25
Feed-down factors	1.69	0.44
Efficiency factors	1.93	4.12



## Summary of existing LHCb measurements

$$\mathcal{R}(D^{*+}) \text{ with } \tau \rightarrow \mu\nu\bar{\nu}$$

Phys. Rev. Lett. 120 (12), 121801, [arXiv:1711.05623](https://arxiv.org/abs/1711.05623)



$$\mathcal{R}(D^{*+}) \text{ with } \tau \rightarrow \pi^- \pi^+ \pi^- \nu$$

Phys. Rev. D 97 (7), 072013, [arXiv:1711.02505](https://arxiv.org/abs/1711.02505)

$$\mathcal{R}(D^{*+}) = 0.291 \pm 0.019 \pm 0.026 \pm 0.013$$

$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c \rightarrow J/\psi \tau \bar{\nu}_\tau)}{\mathcal{B}(B_c \rightarrow J/\psi l \bar{\nu}_l)}$$

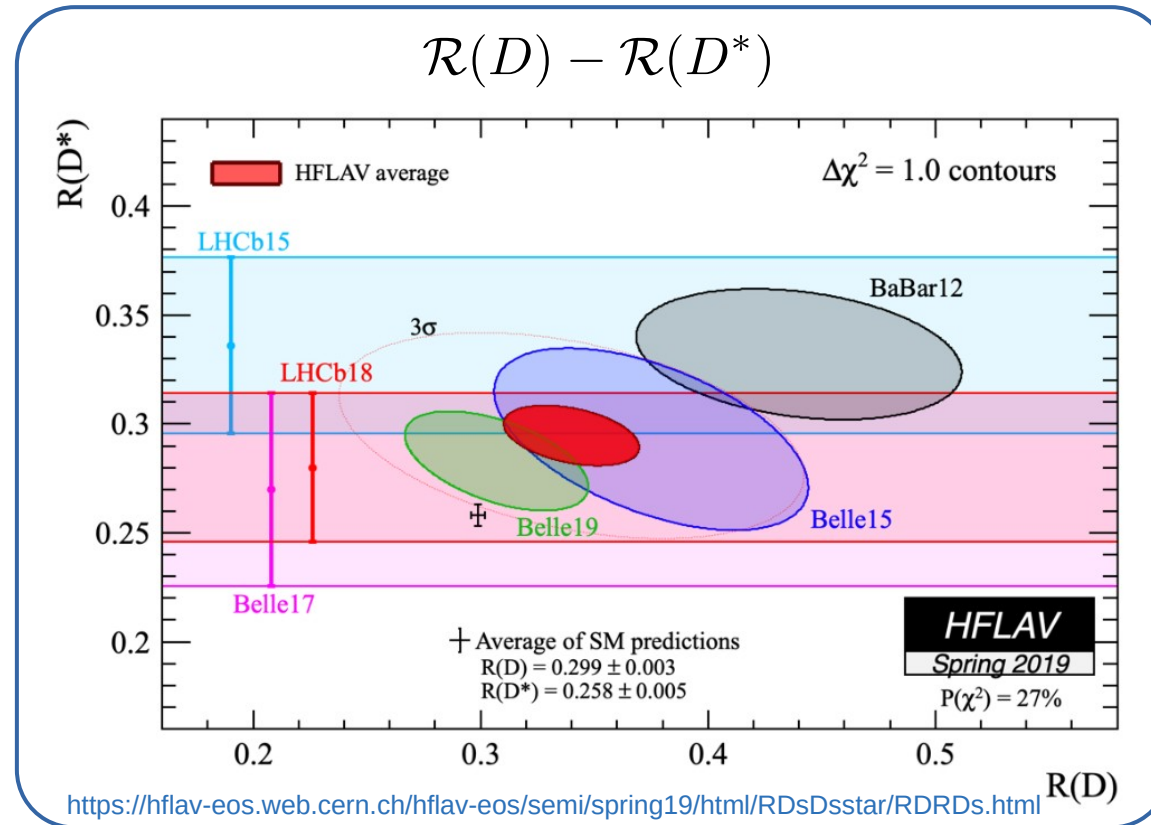
Phys. Rev. Lett. 120 (12), 121801, [arXiv:1711.05623](https://arxiv.org/abs/1711.05623)

$$\mathcal{R}(J/\psi) = 0.71 \pm 0.17 \text{ (stat)} \pm 0.18 \text{ (syst)}$$

$$\mathcal{R}(J/\psi)^{SM} = 0.2582 \pm 0.0038 \implies \sim 2\sigma \text{ deviation}$$

- so far  $\mathcal{R}(D)$  not measured: lower  $\mathcal{B}$ , no  $D^*$  mass constraint, significant  $D^*$  feed-down

## Consistency with the SM predictions

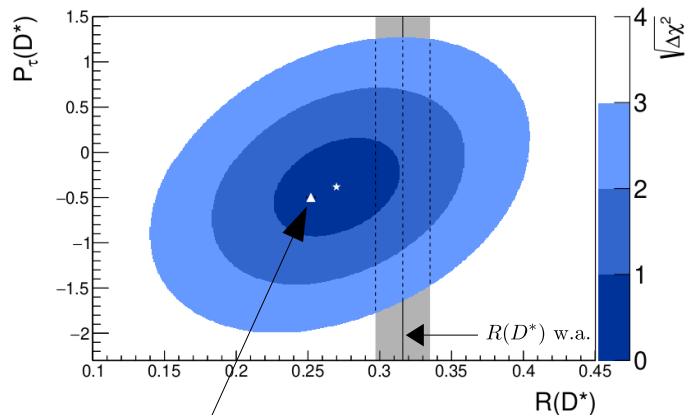


→ present world average of  $\mathcal{R}(D) - \mathcal{R}(D^*)$  deviates from the SM with significance of  $\sim 3.1\sigma$

## Belle $\tau$ polarization measurement

Phys. Rev. D 97 (1), 012004, [arXiv:1709.00129](https://arxiv.org/abs/1709.00129)

$$P_\tau(D^{(*)}) = \frac{\Gamma^+ - \Gamma^-}{\Gamma^+ + \Gamma^-} \quad \Gamma^\pm - \tau \text{ helicity}$$

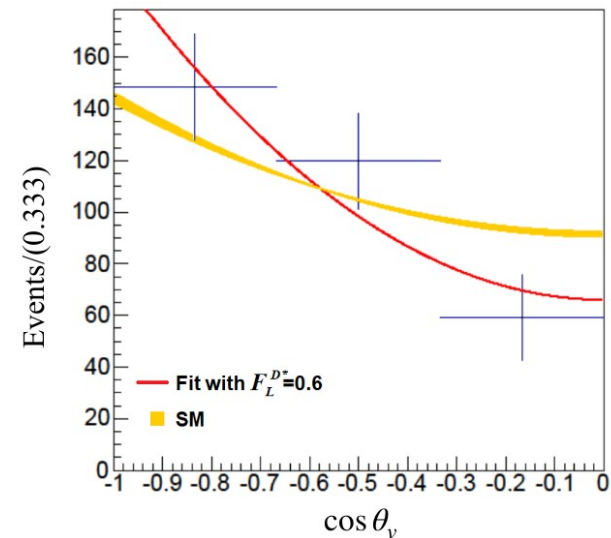


SM expectation

Phys. Rev. D 88, 094012 (2013) [arXiv:1309.0301](https://arxiv.org/abs/1309.0301)

## Belle $D^{*-}$ longitudinal polarization fraction

[arXiv:1903.03102](https://arxiv.org/abs/1903.03102)



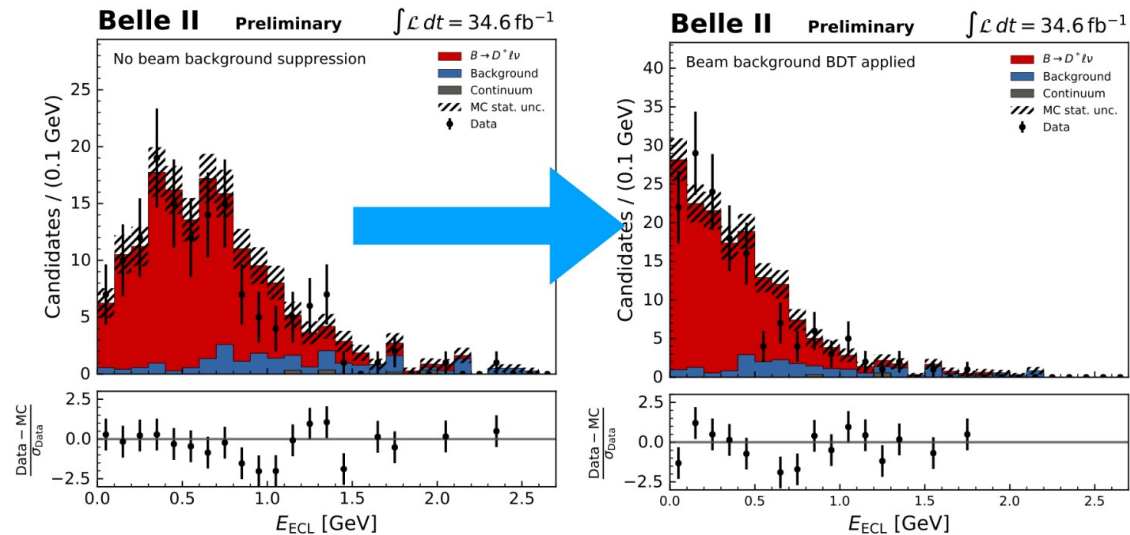
Phys. Rev. D 98, 095018 (2018) [arXiv:1808.03565](https://arxiv.org/abs/1808.03565)

consistent with the SM at  $1.6\sigma$

## Prospects @ Belle II

- uncertainty in existing B-factory measurements largely statistically dominated
- but increased luminosity at Belle II with higher beam background levels will provide very challenging environment → novel methods
- relevant input to  $\mathcal{R}(D^{(*)})$  anomaly already with  $\sim 0.5 \text{ ab}^{-1}$  (summer 2022)

fight beam backgrounds with ML methods



expected sensitivity ( $\pm \text{stat} \pm \text{syst}$ )

	$5 \text{ ab}^{-1}$	$50 \text{ ab}^{-1}$
$R_D$	$(\pm 6.0 \pm 3.9)\%$	$(\pm 2.0 \pm 2.5)\%$
$R_{D^*}$	$(\pm 3.0 \pm 2.5)\%$	$(\pm 1.0 \pm 2.0)\%$

PTEP 2019 (12), 123C01, [arXiv:1808.10567](https://arxiv.org/abs/1808.10567)

## $\mathcal{R}(D^{(*)})$ systematic uncertainty considerations

Main systematics in existing Belle measurements

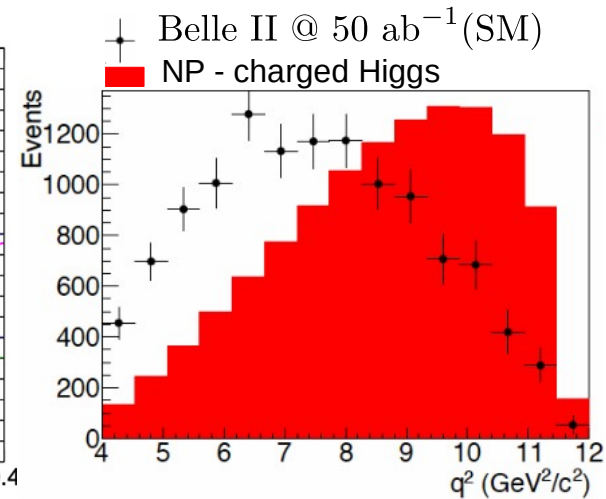
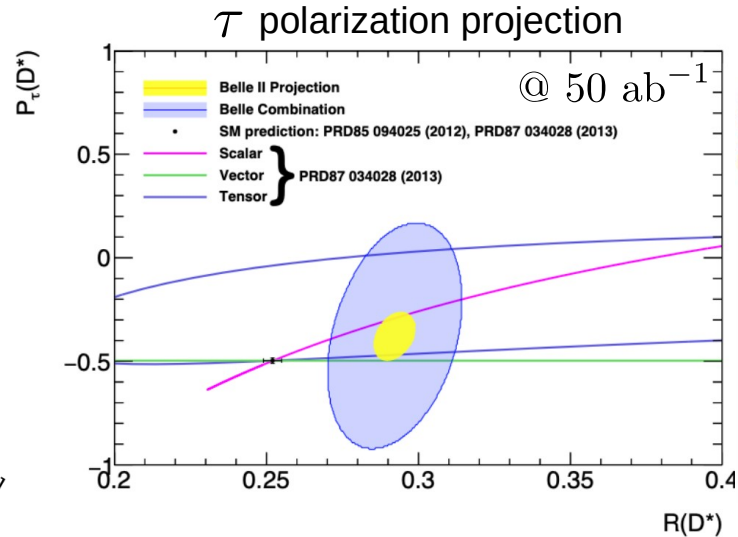
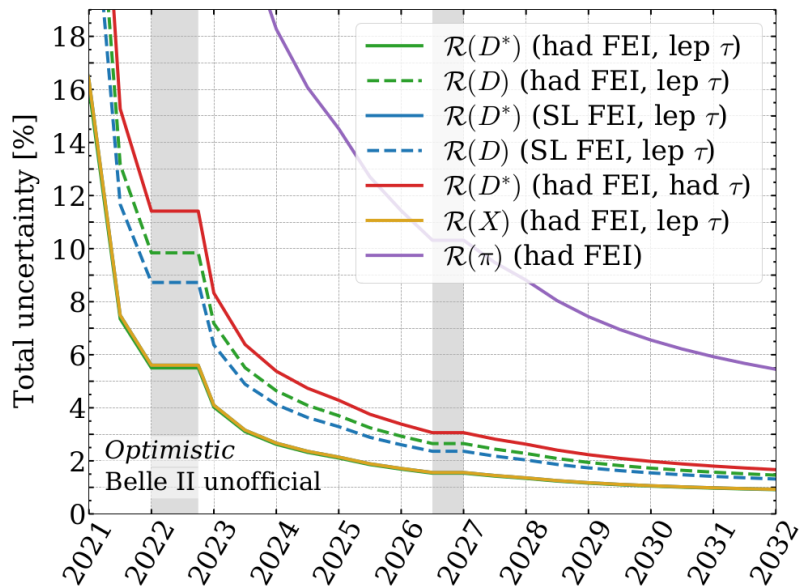
Source	Belle (Had, $\ell^-$ )	Belle (Had, $\ell^-$ )	Belle (SL, $\ell^-$ )	Belle (Had, $h^-$ )
	$R_D$	$R_{D^*}$	$R_{D^*}$	$R_{D^*}$
MC statistics	4.4%	3.6%	2.5%	+4.0% -2.9%
$B \rightarrow D^{**} \ell \nu_\ell$	4.4%	3.4%	+1.0% -1.7%	2.3%
Hadronic $B$	0.1%	0.1%	1.1%	+7.3% -6.5%
Other sources	3.4%	1.6%	+1.8% -1.4%	5.0%
Total	7.1%	5.2%	+3.4% -3.5%	+10.0% -9.0%

PDF templates, efficiencies → reducible with larger MC samples

dedicated measurements of  $B \rightarrow D^{**} \ell \nu_\ell$  and exclusive hadronic B decays (e.g.  $B \rightarrow D^* \pi^+ X$ )

improved modeling of  $B \rightarrow D^{(*)} \ell / \tau \nu$  form factors, lepton id. efficiencies, etc.

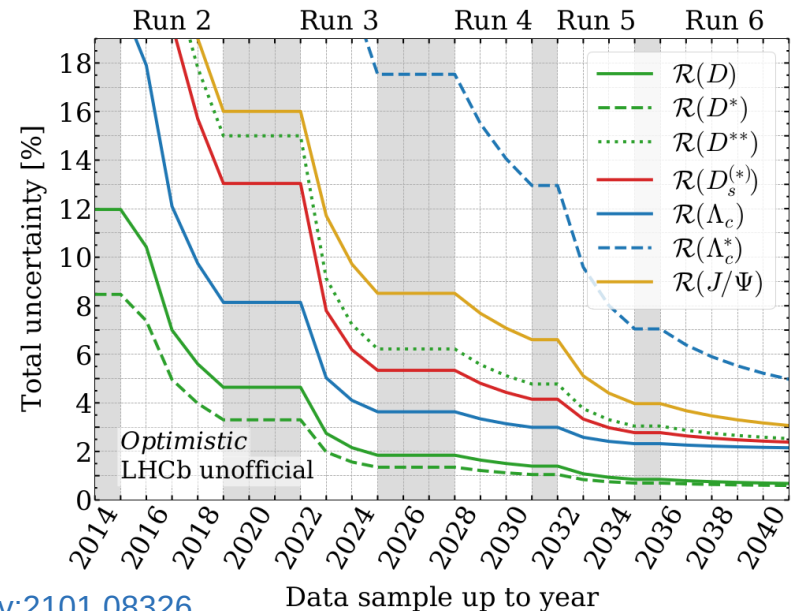
- with hadronic tagging Belle II will also have access to  $\mathcal{R}(X_c)$ 
  - hadronic model independent test of LFU
- with more data other observables will become increasingly important
  - angular correlations, polarizations, asymmetries
  - many of these much easier accessible at Belle II w.r.t LHCb



## Prospects @ LHCb

- all existing LHCb measurements use Run 1 data only (3 fb<sup>-1</sup>)
- statistical uncertainties already at the level of systematic uncertainties  
→ many contributions will get reduced with larger data samples
- many updates (+ 6 fb<sup>-1</sup> of Run 2 data) + new analyses in progress

- $\mathcal{R}(D^+)$
- $\mathcal{R}(D^*)$  - (electron - muon)
- Combined measurement  
 $\mathcal{R}(D^*) - \mathcal{R}(D^0)$
- $\mathcal{R}(D^{**})$
- $\mathcal{R}(D_s^*)$
- $\mathcal{R}(J/\Psi)$
- $\mathcal{R}(\Lambda_c^*)$





## Summary

- semi-tauonic  $b \rightarrow c\tau\nu$  decays provide powerful probes of the Standard Model (SM)
- many possible observable  $\rightarrow$  but experimentally challenging
- in the last decade several measurements indicating enhanced rates of  $b \rightarrow c\tau\nu$  compared with the SM predictions.
- complementary contributions from B factories and LHCb
- Belle II will provide important contributions to resolution of present anomalies already with  $\sim 0.5 \text{ ab}^{-1}$  of collected data (summer 2022)

