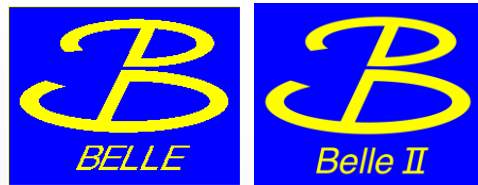


Status and outlook for $R(D^{(*)})$

Koji Hara (KEK)

Sep. 12, 2020

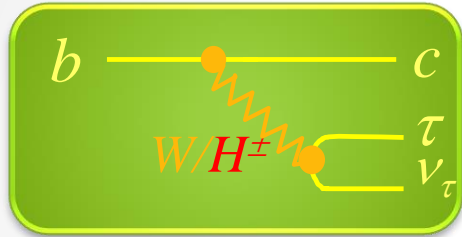
Anomalies 2020



Semi-tauonic B decay: $B \rightarrow D^{(*)} \tau \nu$

- Sensitive to new physics

Ratio of τ to μ, e could be reduced/enhanced



$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)} \quad \text{L=e, } \mu$$

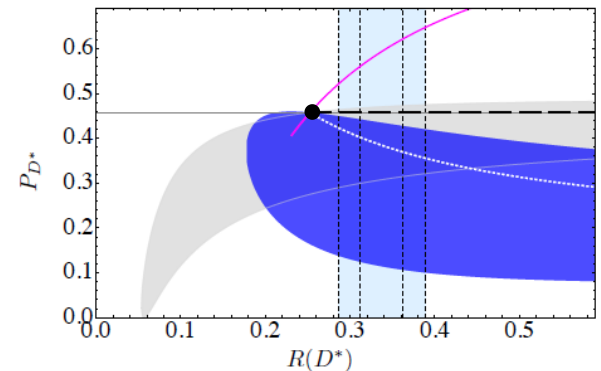
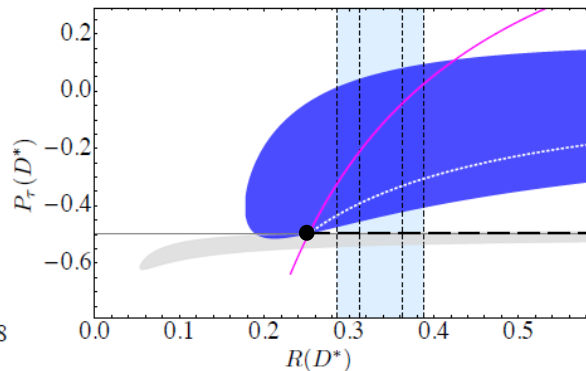
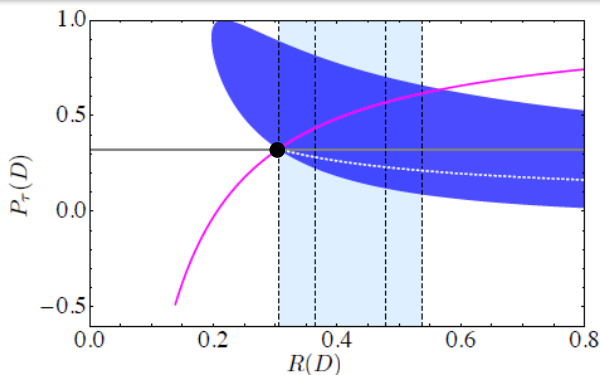
SM $R(D) = 0.299 \pm 0.003$, $R(D^*) = 0.258 \pm 0.005$ [HFLAV2019]

Polarizations of τ and D^* can probe the NP model

$$P_{\tau}(D^{(*)}) = \frac{\Gamma^{+} - \Gamma^{-}}{\Gamma^{+} + \Gamma^{-}} \quad F_L^{D^*} = \frac{\Gamma(D_L^*)}{\Gamma(D_L^*) + \Gamma(D_T^*)}$$

NP type (vector, scalar, tensor) dependence

[M. Tanaka and R. Watanabe PRD 87, 034028 (2013)]



Meas.(2013)

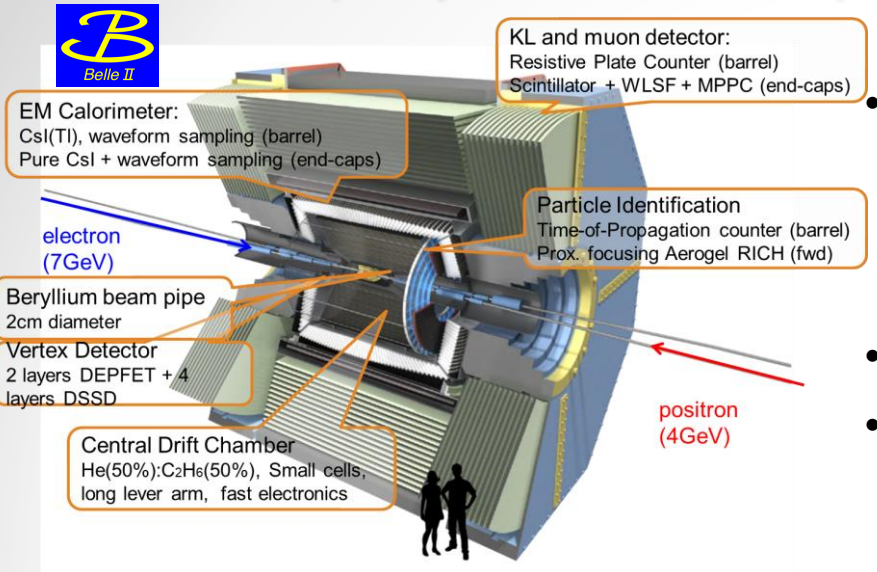
• SM

— Scalar

○ Vector

● Tensor

R(D) and R(D*) Experiments



B factory experiments

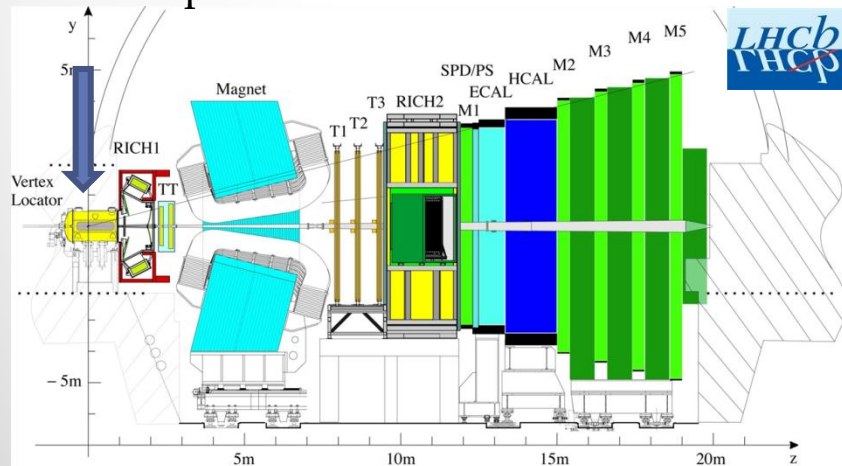
- Produce $B\bar{B}$ pairs via $e^+e^- \rightarrow Y(4s)$
- **Only one $B\bar{B}$ pair in an event**
- **4π detector surrounding the IP**
- **Belle + BaBar** have accumulated $>\sim 1 \text{ ab}^{-1}$
- **Belle II** started physics data taking in 2019 and will accumulate **50 ab^{-1}**

LHCb Detector

LHCb

- Experiment dedicated to B physics at LHC
- **Many b hadrons produced in pp collisions**
- Single arm detector covering the forward region
- **Large boost \rightarrow good separation of vertices: primary vertex, B, D, τ**
- Collected Run 1 + Run 2 $\sim 9 \text{ fb}^{-1}$
- Now in long shutdown for upgrade

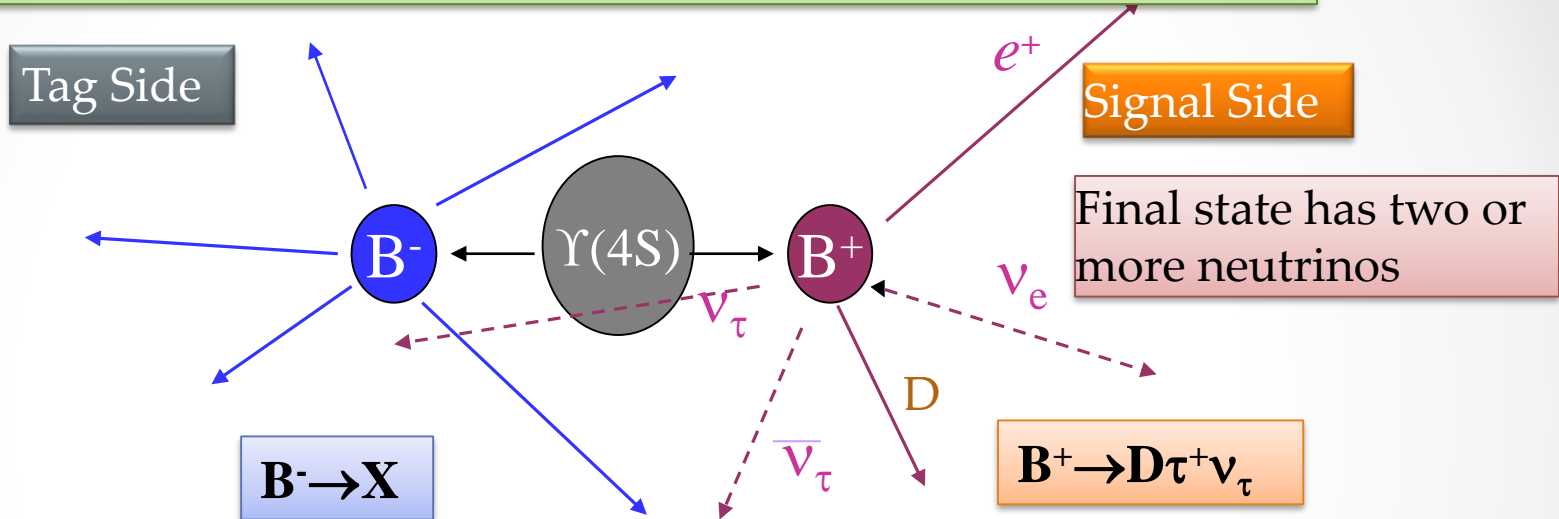
Collision point



These experiments are complementary

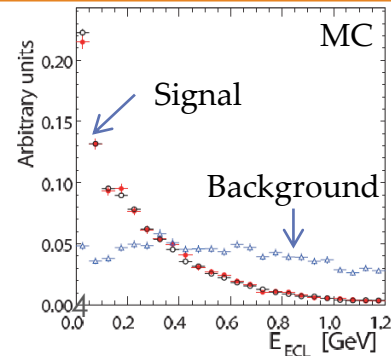
$B \rightarrow D^{(*)} \tau \nu$ Analysis at B factories

Utilize the B factory specific feature :
only one B-meson pair is produced



Tag B pair event by reconstructing one B meson in hadronic or semileptonic B Decay
 → Provide pure single B event

- Require **no** particle remains after removing tagging B and **signal B candidates**
 → Remaining energy in the calorimeter (E_{ECL})
- Multiple missing neutrinos → $(\text{Missing mass})^2 > 0$



Tagging Methods

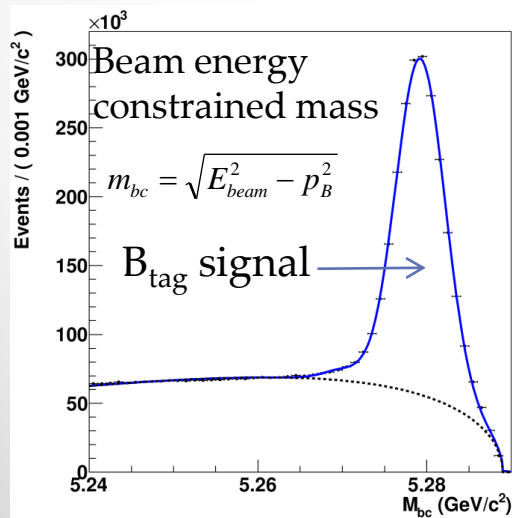
Hadronic Tag

Exclusive tag

- Fully reconstruct in $B \rightarrow DX$ decays
 - ~1100 exclusive decay channels (Belle) [NIM A 654, 432 (2011)]
- Tagging efficiency ~ 0.2 %
- Less background

Inclusive tag

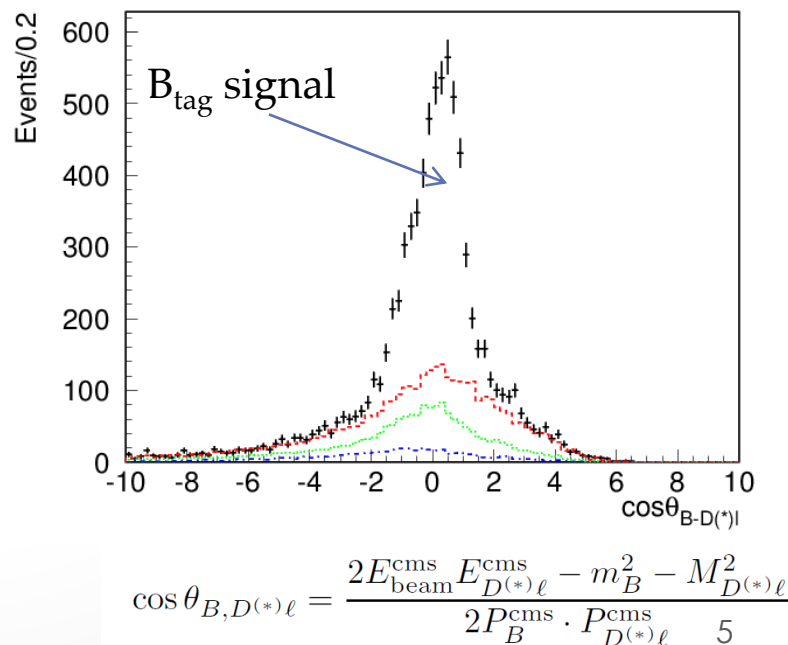
- Reconstruct tag-side B with all particles except signal-side
- Higher efficiency than exclusive tag
- Need clean signal-side final state
- **Used for first observation of $B \rightarrow D^* \tau \nu$ by Belle [PRL99, 191807(2007)]**



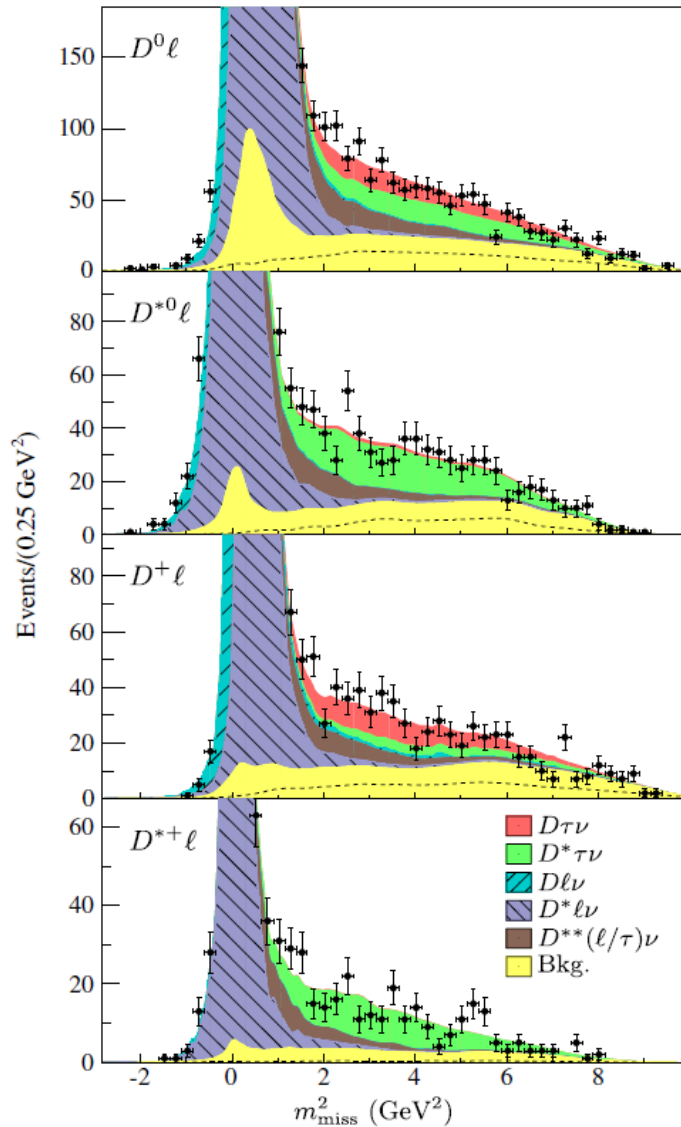
Semileptonic Tag

- Reconstruct $B \rightarrow D^{(*)} l \nu$
 - Partial reconstruction with
 - $E_B = E_{beam}$
 - Undetected neutrino mass ~ 0
- Tagging efficiency ~ 0.5%
- More background

Belle $B \rightarrow \tau \nu$ analysis [PRD 82, 071101(R) (2010)]



Results with Hadronic Tag by BaBar



[PRL109, 101802 (2012)]

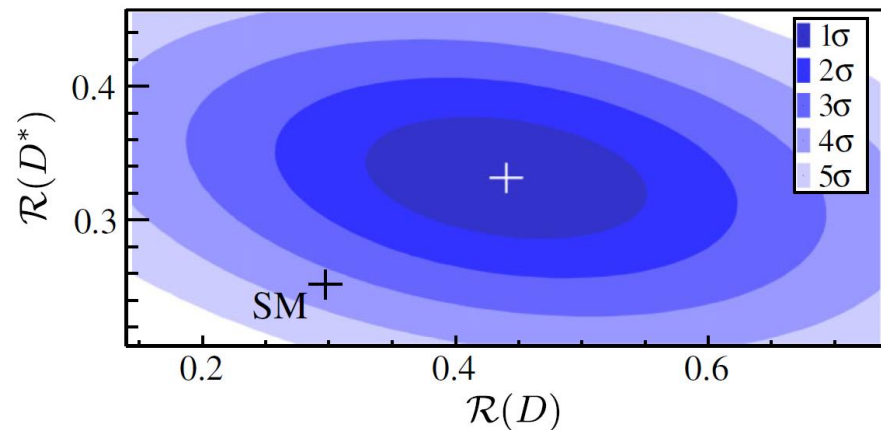
[PRD88, 072012 (2013)]

- 471 M $B\bar{B}$ sample
- Leptonic tau decays are used

$$\mathcal{R}(D) = 0.440 \pm 0.058 \pm 0.042$$

$$\mathcal{R}(D^*) = 0.332 \pm 0.024 \pm 0.018$$

Both are larger than SM expectations

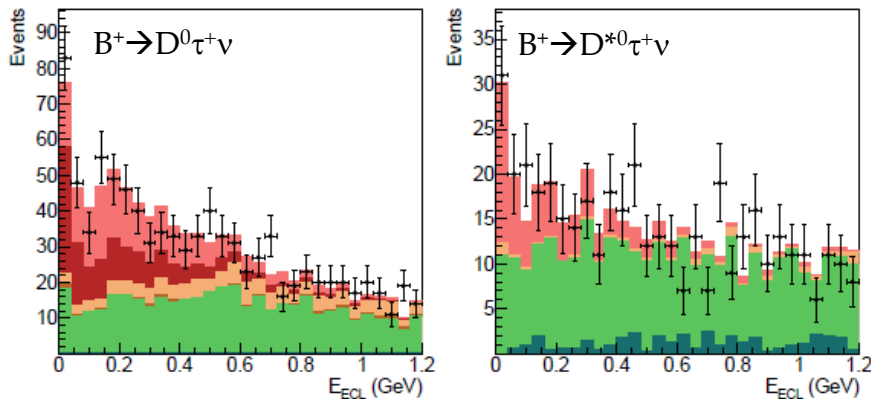
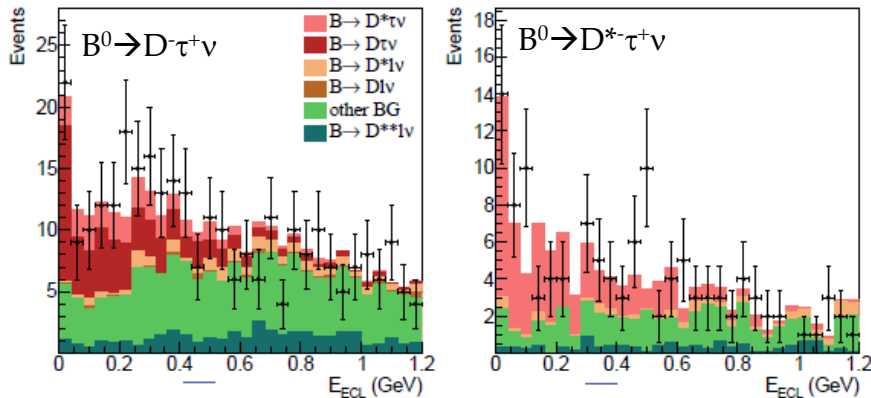


Results with Hadronic Tag by Belle (leptonic τ decays)



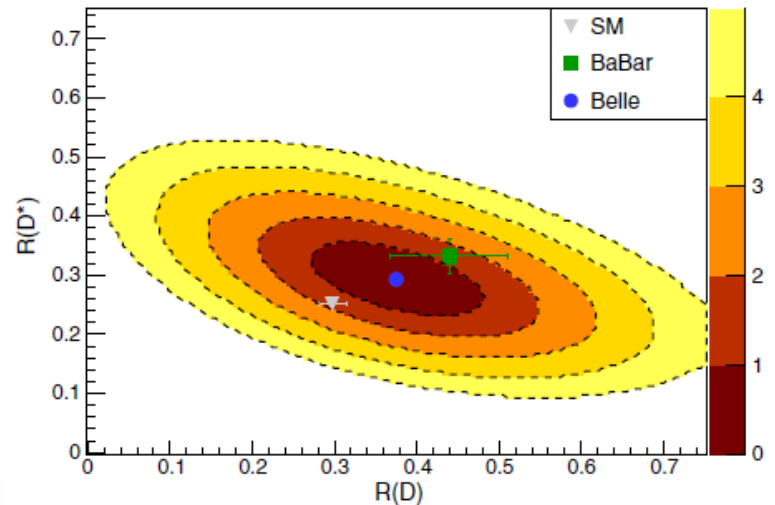
[PRD92,072014(2015)]

- 772 M $B\bar{B}$ sample
- Leptonic tau decays are used



$$R(D) = 0.375 \pm 0.064 \pm 0.026$$

$$R(D^*) = 0.293 \pm 0.038 \pm 0.015$$



Belle $R(D^{(*)})$ Measurement with Semileptonic Tag

- Previous Analysis [PRD94,072007(2016)]

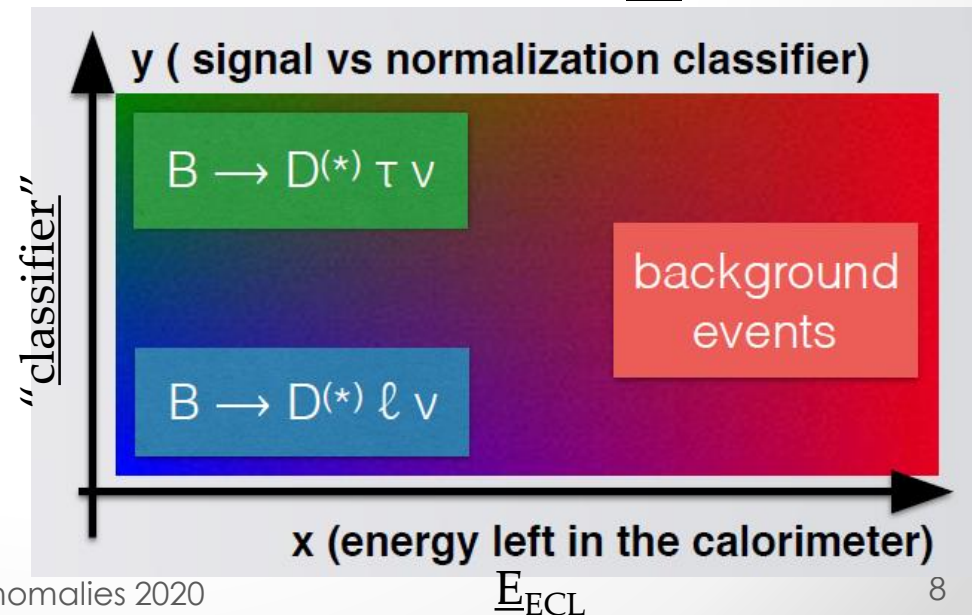
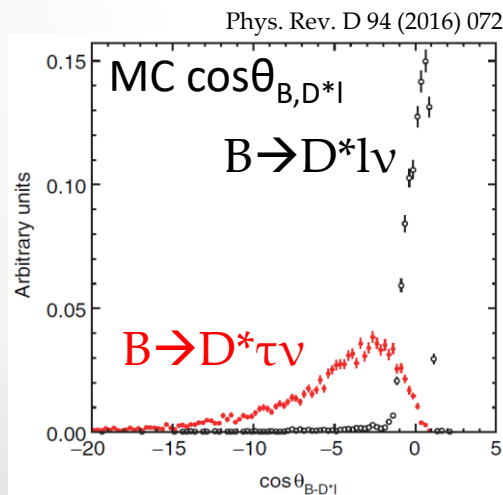
Measure $R(D^{(*)})$ with $B^0 \rightarrow D^{*-} \tau^+ \nu$ (and charge conjugate) decays

- Good signal purity by using clean $D^{*-} \rightarrow D^0 \pi^-$ decays

- **Recent Update [PRL124,161803 (2020)]**

- **Full Event Interpretation (FEI)** tool developed in **BelleII software framework** [Comput. Softw. Big. Sci. (2019) 3:6]
- Multivariate analysis with Boosted-Decision Tree classifier
→ Better efficiency and enable to use more signal decay modes
- **Both $R(D)$ and $R(D^{*})$** with **both B^0 and $B^+ \rightarrow D^{*} \tau \nu$**
- 2D extended maximum-likelihood fit on **“classifier”** and E_{ECL}

Classifier: Boosted decision tree output of $\cos\theta_{B,D^{(*)}}$, M_{miss2} , E_{vis}

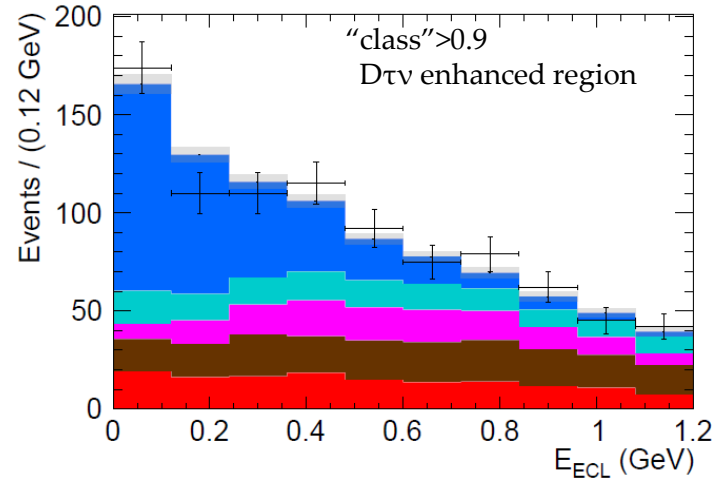
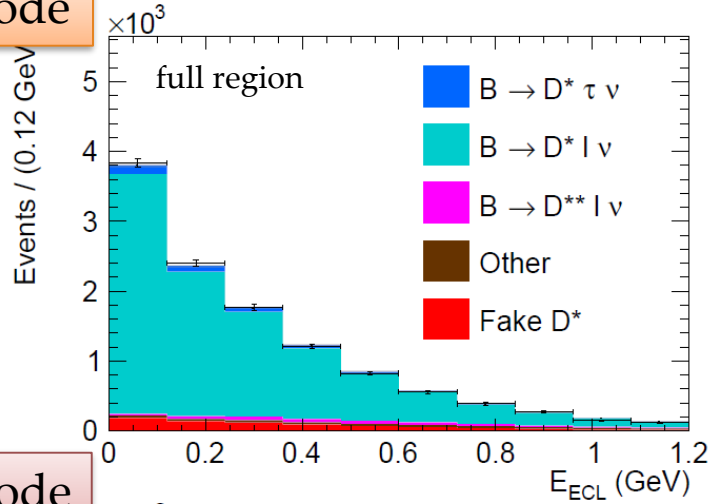


Belle $R(D^*)$ Semileptonic Tag Result

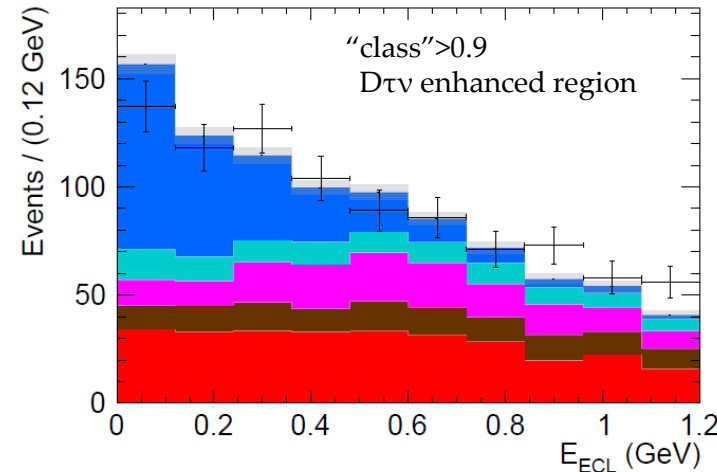
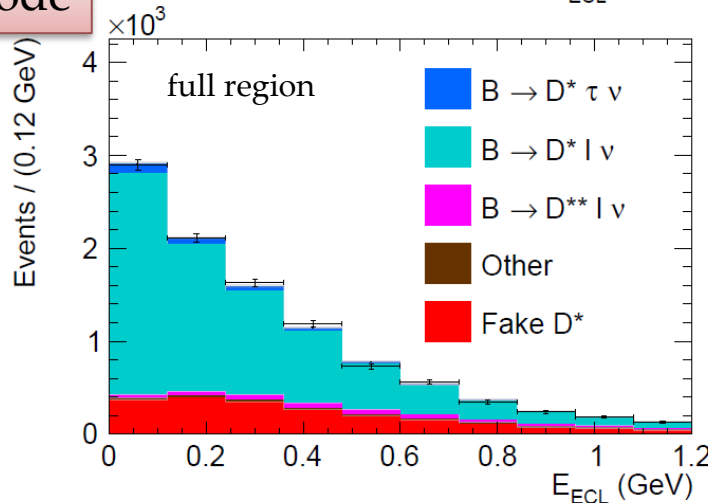


Signal
 $B \rightarrow D^* l \nu$
 $B \rightarrow D \tau \nu$

$D^{*+} l^-$ mode



$D^{*0} l^-$ mode



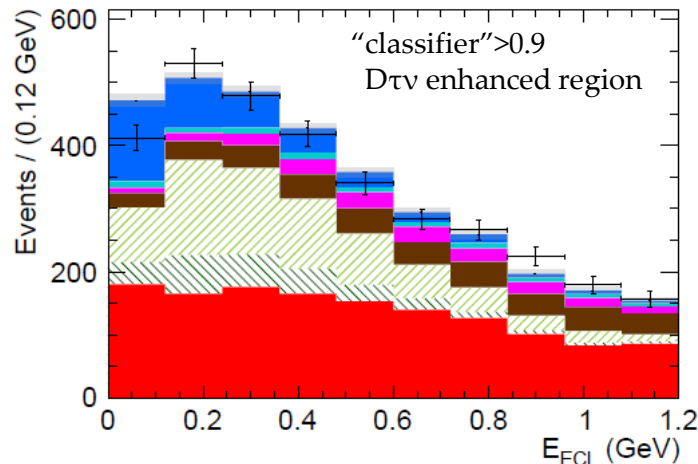
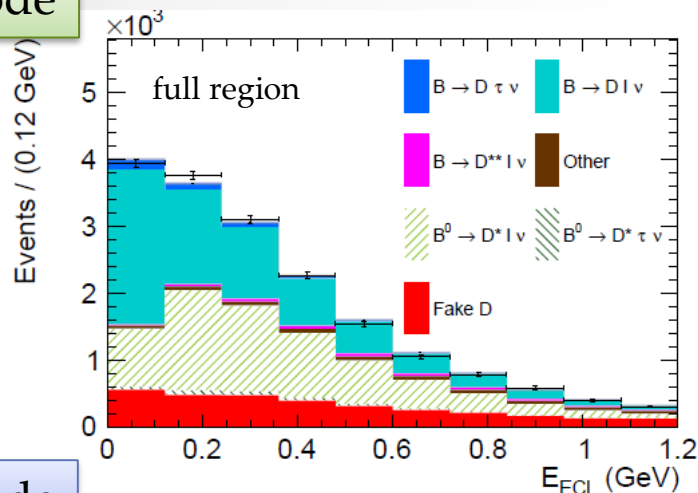
$D^{*+} l^-$	$B \rightarrow D^* \tau \nu$	376 ± 36
	$B \rightarrow D^* l \nu$	9794 ± 109
	$B \rightarrow D^{**} l \nu$	314 ± 65
	Fake D^*	754 ± 39 (Fixed)
	Other	287 ± 13 (Fixed)
$D^{*0} l^-$	$B \rightarrow D^* \tau \nu$	275 ± 29
	$B \rightarrow D^* l \nu$	7148 ± 100
	$B \rightarrow D^{**} l \nu$	406 ± 64
	Fake D^*	1993 ± 122 (Fixed)
	Other	187 ± 7 (Fixed)

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014$$

Belle R(D) Semileptonic Tag Result



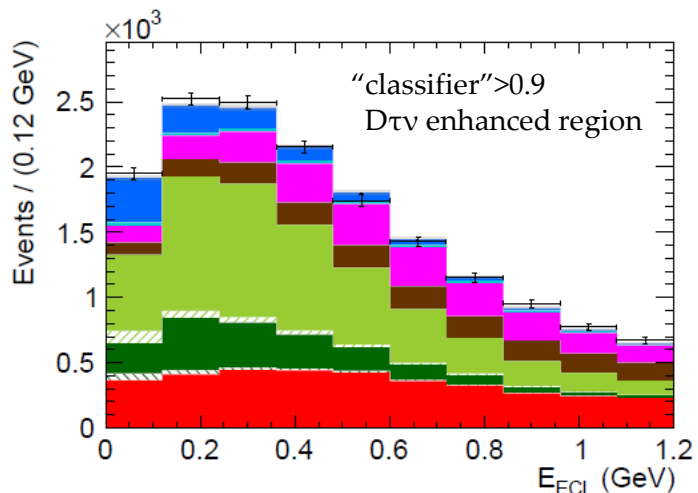
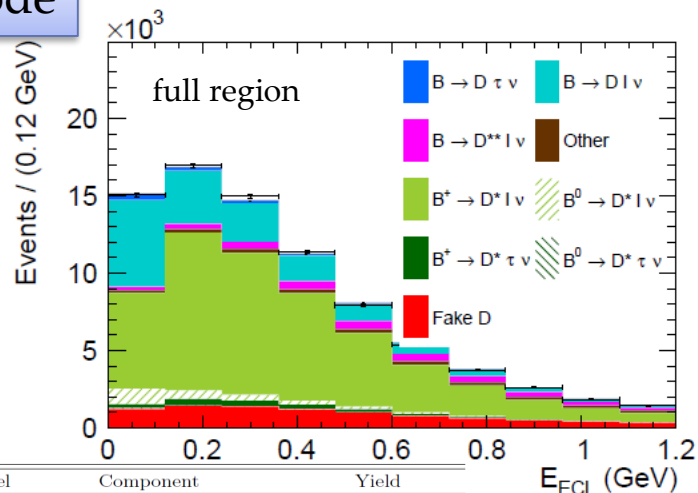
D⁺ mode



Signal

- B → D l ν
- B → D τ ν

D⁰ mode



Channel	Component	Yield
D ⁺ ℓ ⁻	B → Dτν	307 ± 65
	B → Dℓν	6800 ± 179
	B ⁰ → D*ℓν	6370 ± 225
	B ⁰ → D*τν	269 ± 24
	B → D**ℓν	413 ± 110
	Fake D	3072 ± 129 (Fixed)
	Other	506 ± 23 (Fixed)
	D ⁰ ℓ ⁻	B → Dτν
B → Dℓν		16096 ± 436
B ⁺ → D*ℓν		45042 ± 563
B ⁰ → D*ℓν		2302 ± 531
B ⁺ → D*τν		1704 ± 177
B ⁰ → D*τν		123 ± 11
B → D**ℓν		3595 ± 252
Fake D		8708 ± 418 (Fixed)
Other		2131 ± 83 (Fixed)

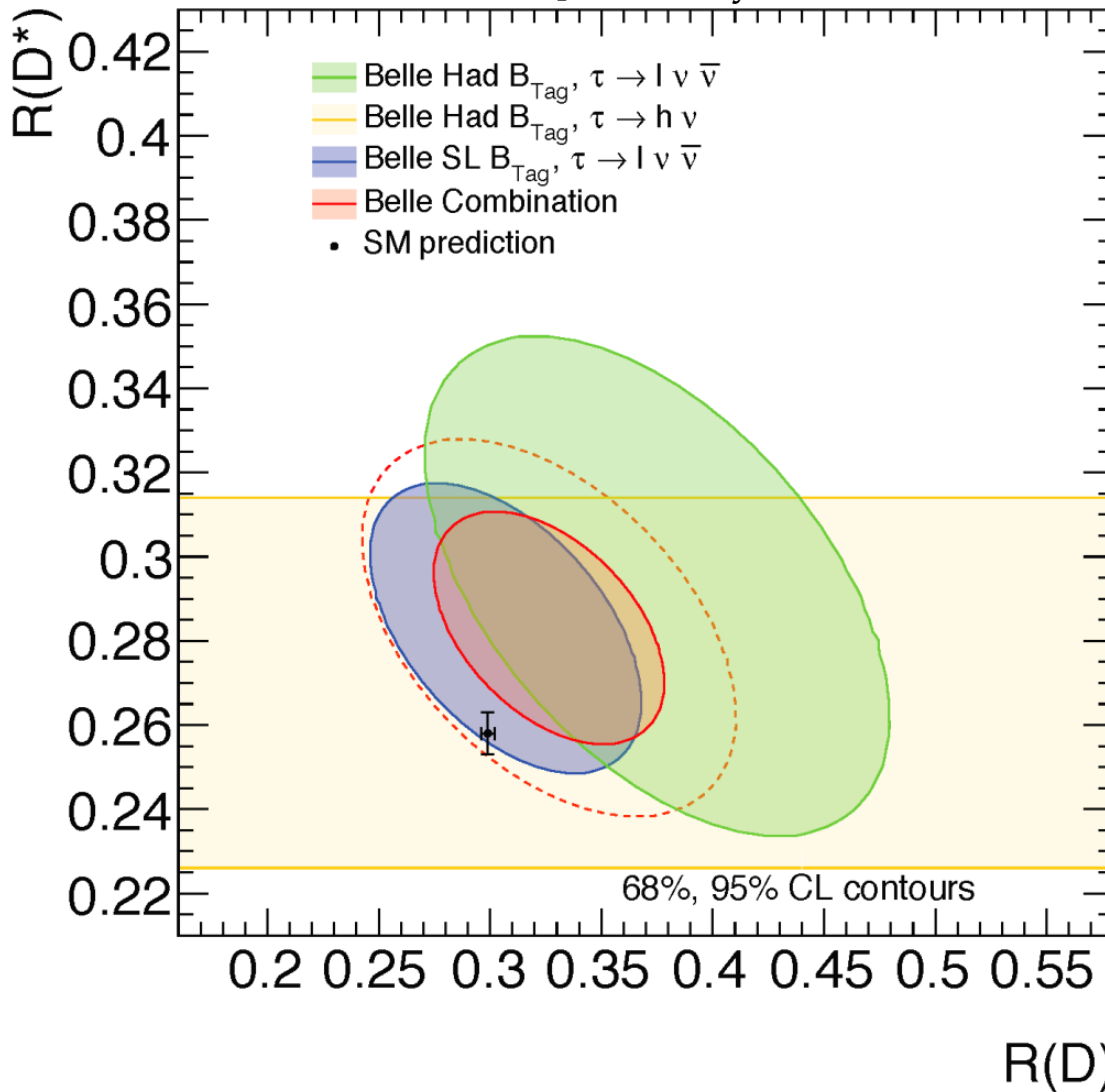
$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$

First R(D) measurement with Semileptonic tag

Belle R(D(*)) Results



[S. Sandilya, talk at FPCP2020]



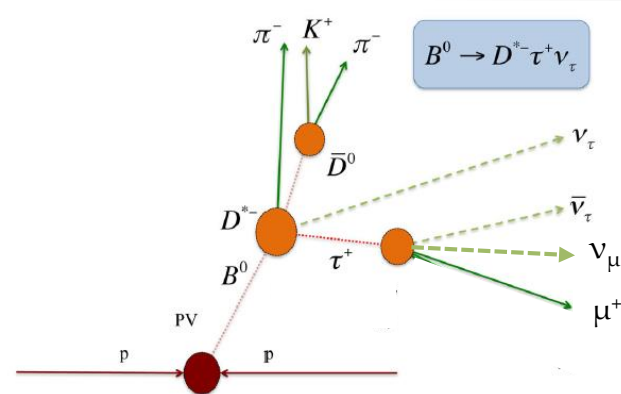
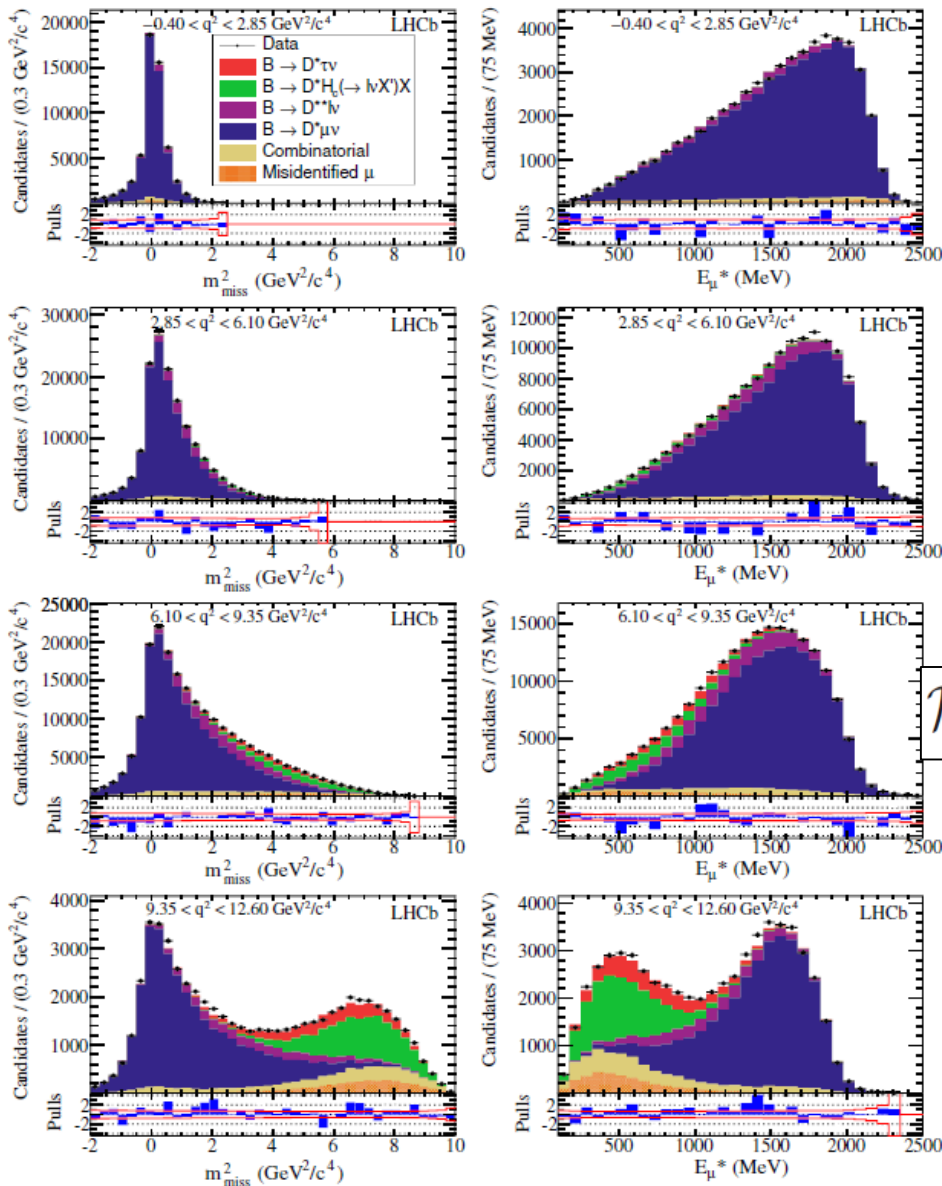
Belle combined result
at about 1.6σ from SM

R(D*) with $\tau \rightarrow \mu \nu \nu$ by LHCb

[PRL 115, 111803 (2015)]

- 3.0 fb⁻¹ Data
- $B^0 \rightarrow D^* \tau \nu$, $\tau \rightarrow \mu \nu \nu$
- 3D Fit to (Missing mass)², E_μ^* , q^2
- Primary and B vertices
→ P_B direction
- $|P_B|$ is approximated by
 $(P_B)_Z = m_B/m_{D^* \mu} (P_{D^* \mu})_Z$

$$\mathcal{R}(D^*) = 0.336 \pm 0.027(\text{stat}) \pm 0.030(\text{syst})$$



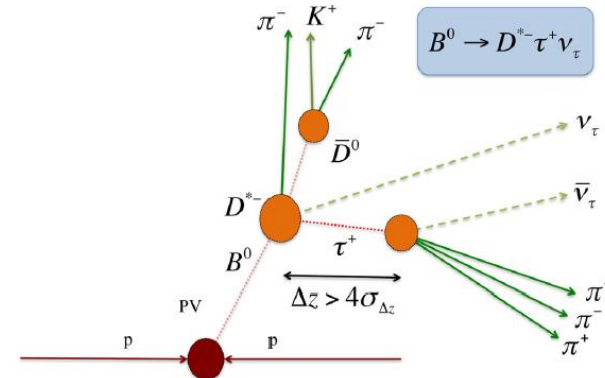
R(D*) with $\tau \rightarrow 3\pi\nu$ by LHCb

[PRD97, 072013 (2018)]

- 3.0 fb⁻¹ Data
- Obtain Ratio

$$\mathcal{K}(D^*) = \text{Br}(B^0 \rightarrow D^* \tau \nu) / \text{Br}(B^0 \rightarrow D^* 3\pi)$$

- **Reconstruct P_T Direction**



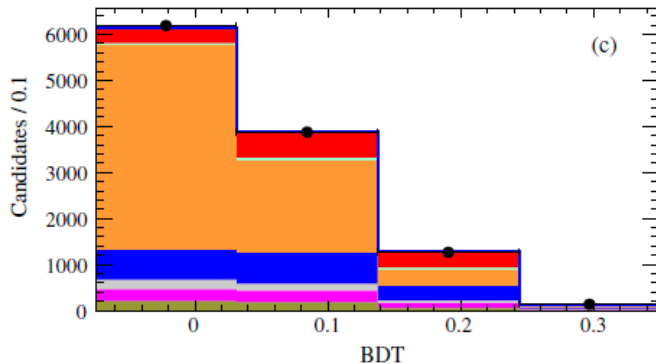
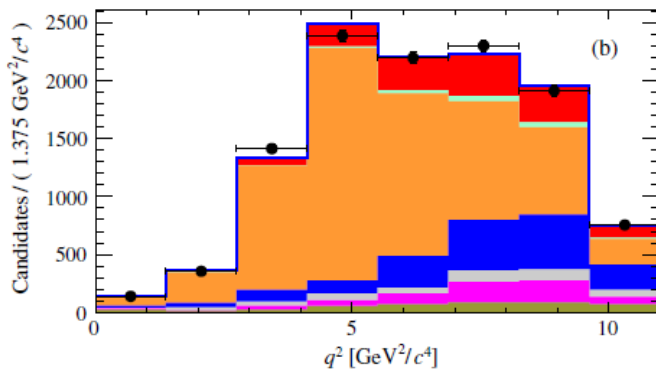
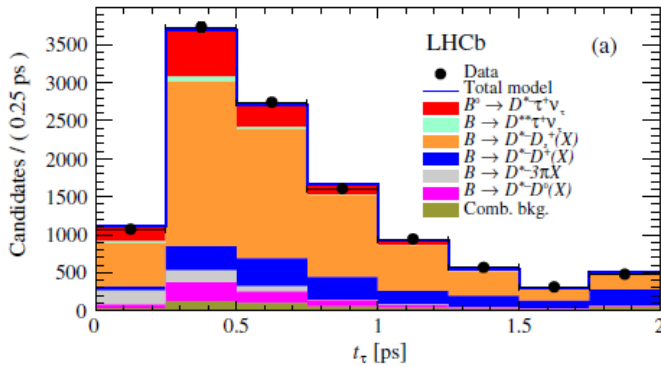
- 3D fit to τ decay time, q^2 , BDT output

$$\mathcal{K}(D^{*-}) = 1.97 \pm 0.13(\text{stat}) \pm 0.18(\text{syst})$$

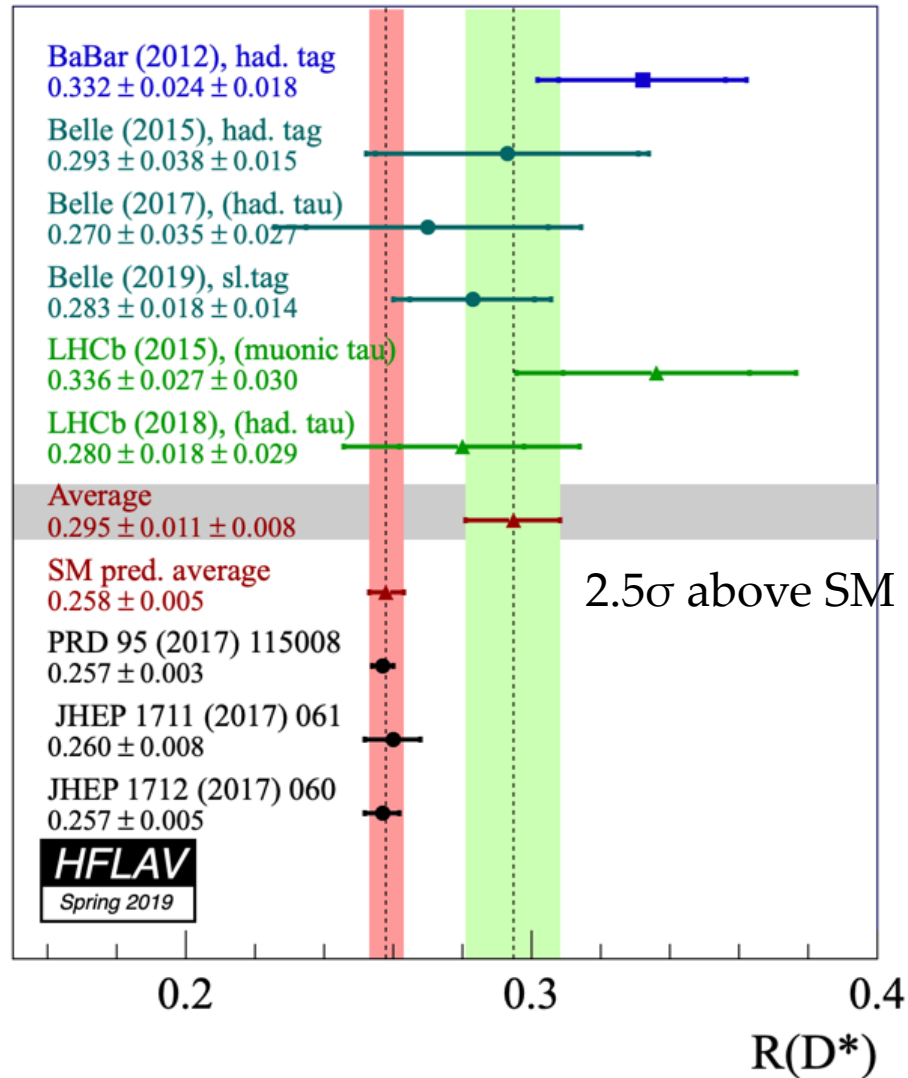
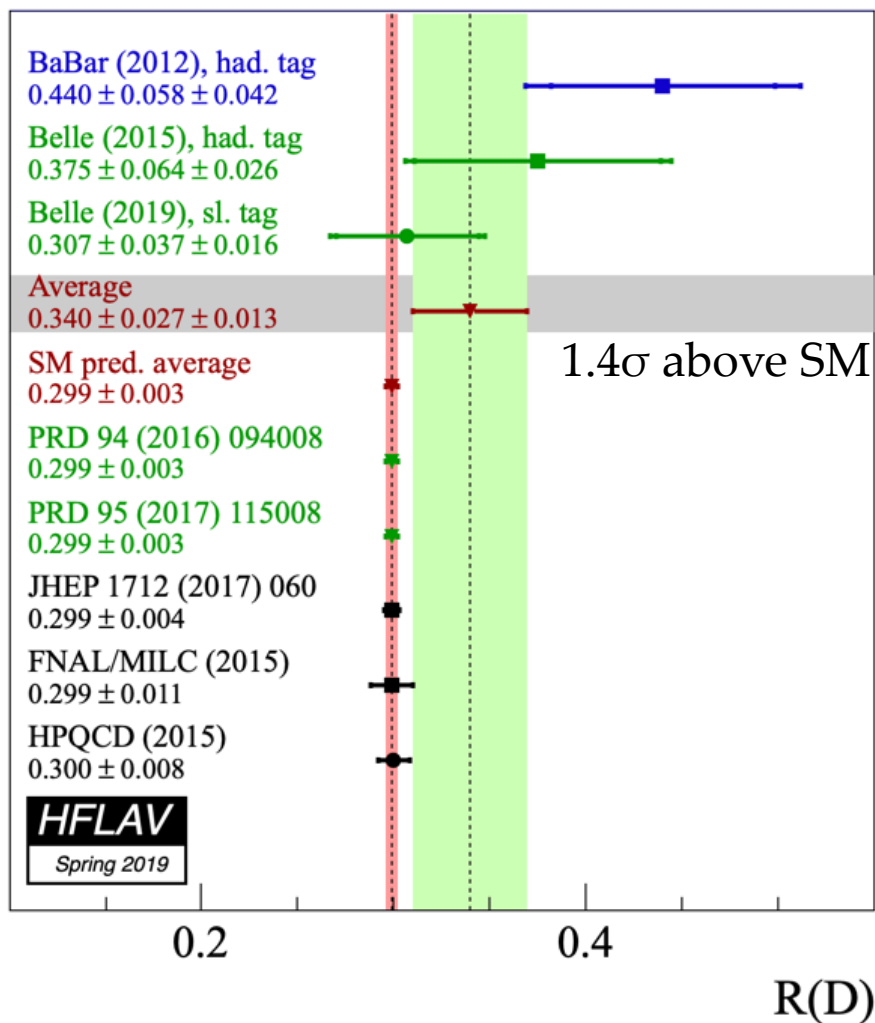
↓ Multiply
 $\text{Br}(B \rightarrow D^* 3\pi) / \text{Br}(B \rightarrow D^* l \nu)$

$$\mathcal{R}(D^*) = 0.280 \pm 0.018(\text{stat}) \pm 0.029(\text{syst})$$

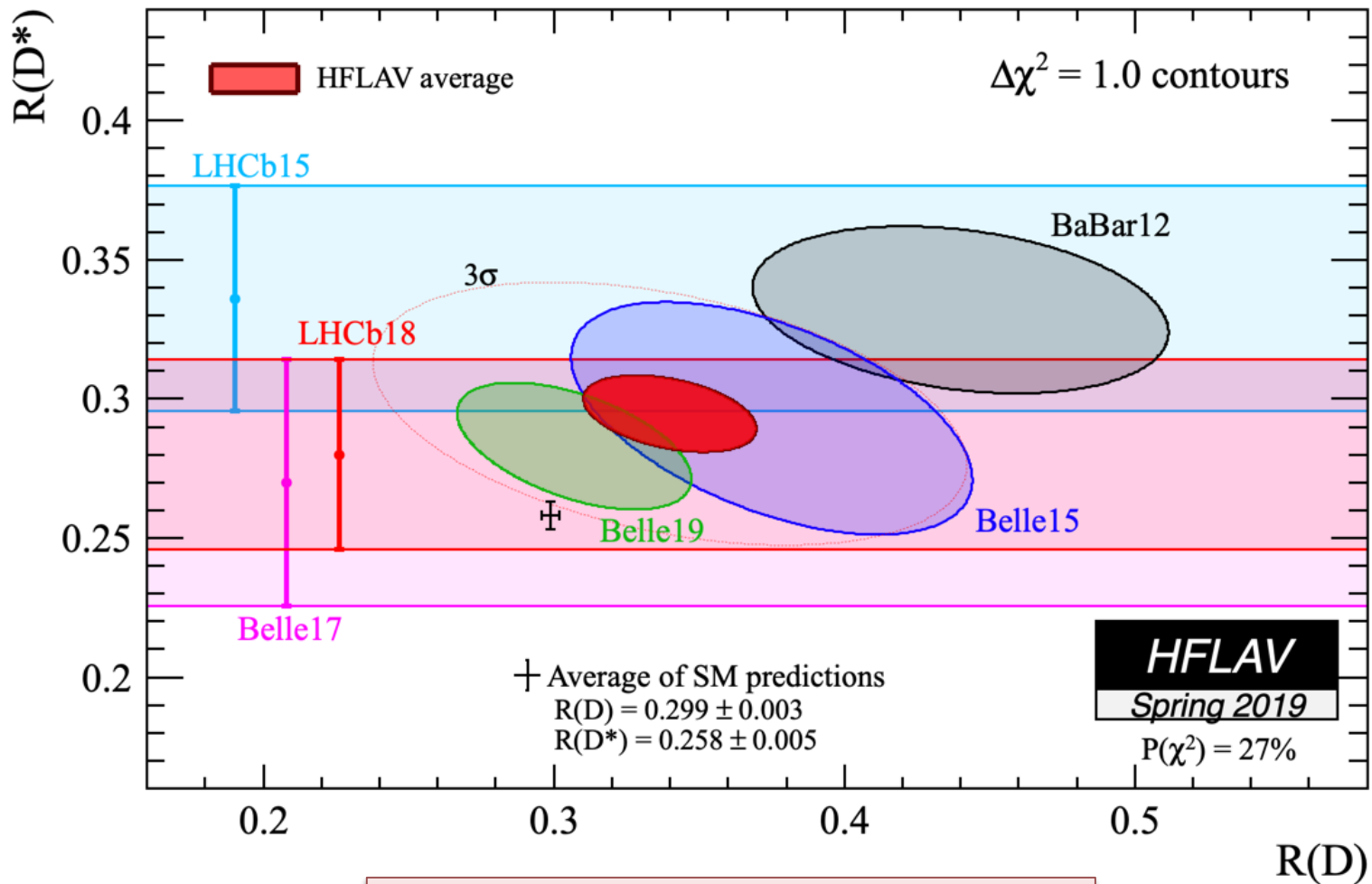
(Update of $\text{Br}(B \rightarrow D^* l \nu)$ by HFLAV2019)



Latest R(D) and R(D*) Situation



Latest R(D)-R(D*) vs SM



Deviation from SM is 3.1σ

More measurements in Addition to $R(D^{(*)})$

- Polarizations
- Other $b \rightarrow c$ hadrons

τ Polarization Measurement at Belle

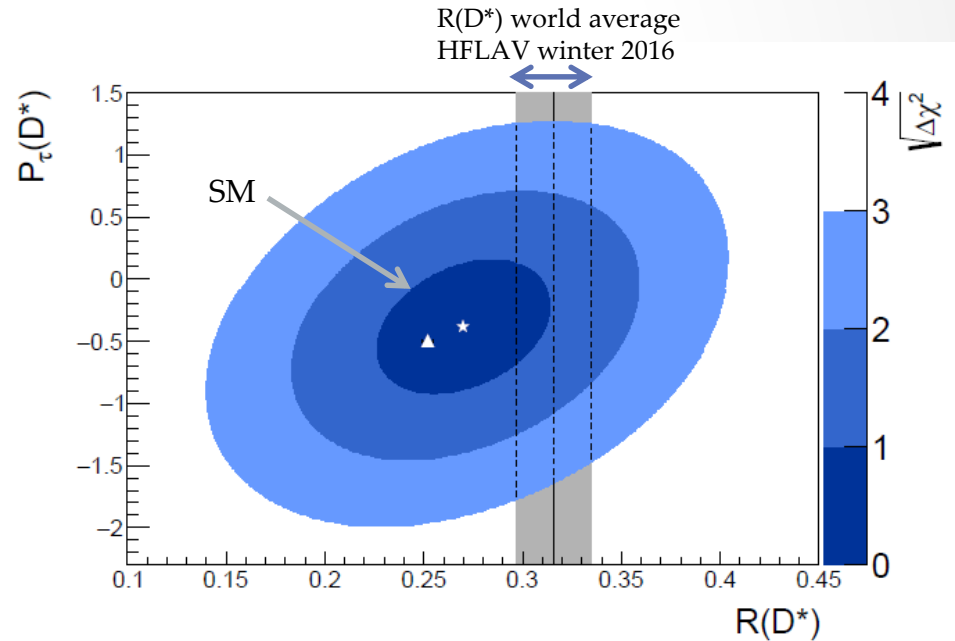
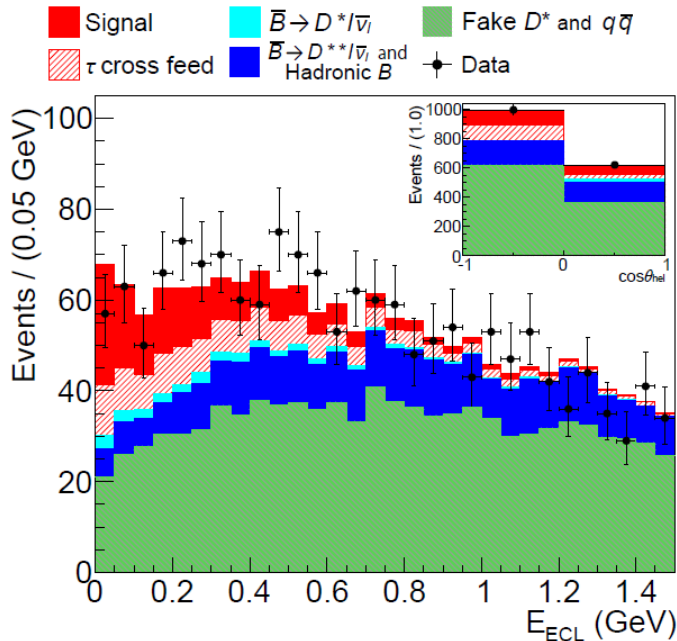
[PRL118, 211801 (2017) PRD97, 012004 (2018)]



- Hadronic tag
- Two body tau decays : $\tau \rightarrow \pi \nu, \rho \nu$
 - Helicity angle sensitive to the tau polarization
- $P_\tau(D^*)_{SM} = -0.497 \pm 0.013$
[Tanaka, Watanabe, PRD 87, 034028 (2013)]

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{hel}} = \frac{1}{2} (1 + \alpha \cdot \mathcal{P}_\tau \cos \theta_{hel})$$

$$\alpha = \begin{cases} 1 & \text{for } \tau \rightarrow \pi^- \nu \\ 0.45 & \text{for } \tau \rightarrow \rho^- \nu \end{cases}$$



$$R(D^*) = 0.270 \pm 0.035(\text{stat})_{-0.025}^{+0.028}(\text{syst}),$$

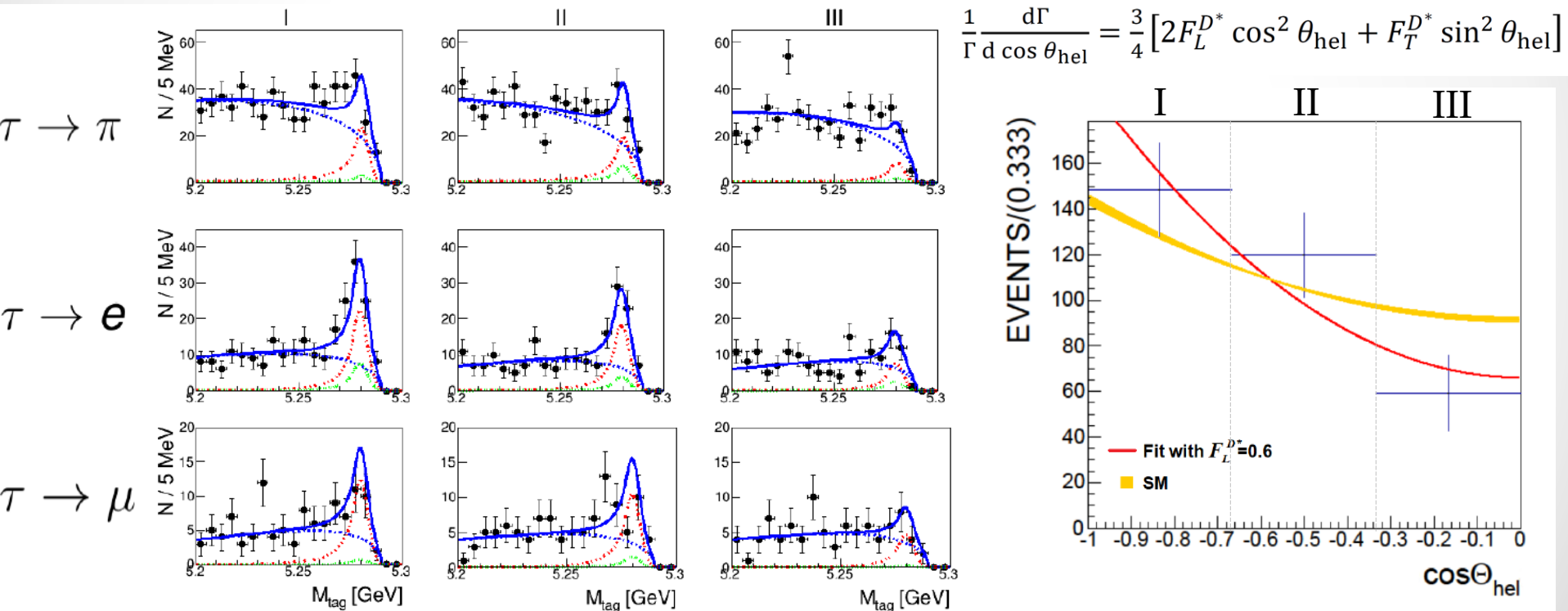
$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat})_{-0.16}^{+0.21}(\text{syst}),$$

($R(D^*)$ included in the HFLAV avg)

D* Polarization Measurement at Belle



- Reconstruct $B^0 \rightarrow D^* \tau \nu$
- Utilized **inclusive tag** method
- Extract signal yield in three $D^* \rightarrow D\pi$ helicity angle regions
- Fit the helicity angle distribution



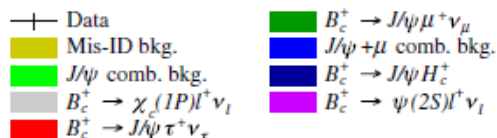
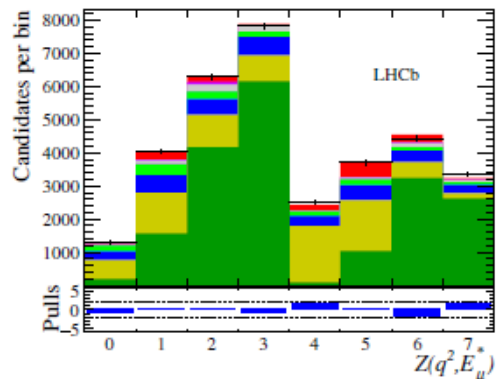
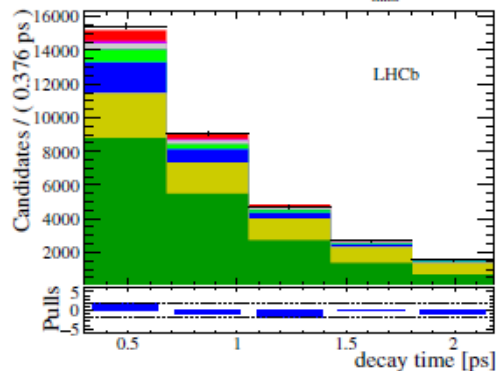
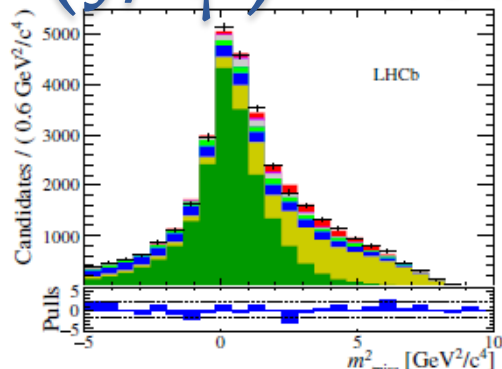
$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{3}{4} [2F_L^{D^*} \cos^2 \theta_{\text{hel}} + F_T^{D^*} \sin^2 \theta_{\text{hel}}]$$

preliminary
[arXiv:1903.03102]

$F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{syst})$
cf. in SM
 - $F_L^{D^*} = 0.46 \pm 0.03$ [PRD95, 115038(2017)]
 - $F_L^{D^*} = 0.441 \pm 0.006$ [arXiv: 1808: 03565]

within 2σ of SM

R(J/ψ) Measurement at LHCb



[PRL120, 121801(2018)]

- 3.0 fb⁻¹ Data
- Measure

$$R(J/\psi) = \frac{Br(B_c^+ \rightarrow J/\psi \tau \nu)}{Br(B_c^+ \rightarrow J/\psi \mu \nu)}$$

- Same method as muonic R(D*) to estimate P_{BC}
- 3D fit to (missing mass)², B_c decay time, category index Z for (q², E_μ^{*}) bins

$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)}$$

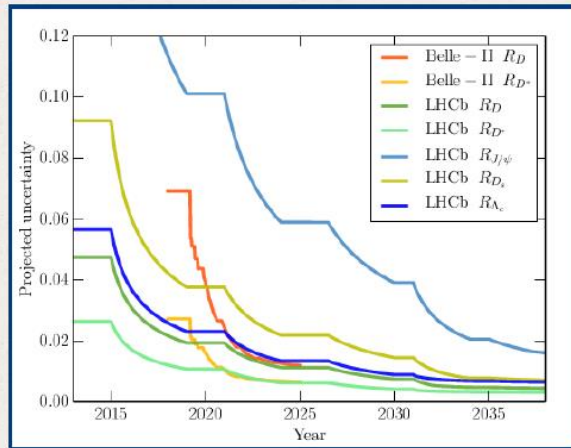
$$= 0.71 \pm 0.17(\text{stat}) \pm 0.18(\text{syst}).$$

2σ from SM expectation 0.25-0.28

LHCb Future Prospect

[Beatriz Garcia Plana, talk at ICHEP2020]

Future prospects



❖ New results are expected from:

- Run 2 updates with a total uncertainty reduction

○ Ongoing analyses:

- $R(D^0): B^+ \rightarrow D^0 \tau \nu$
- $R(D^+): \bar{B}^0 \rightarrow D^+ \tau \nu$
- $R(D_s^{(*)}): B_s \rightarrow D_s^{(*)} \tau \nu$
- $R(D^{**}): B^+ \rightarrow D^{**}(2420)^0 \tau \nu$
- $R(\Lambda_c^{(*)}): \Lambda_b \rightarrow \Lambda_c^{(*)} \tau \nu$
- $R(J/\psi): B_c^+ \rightarrow J/\psi \tau \nu$
- $R(p): \Lambda_b \rightarrow p \tau \nu$
- Combined measurement of $R(D)$ and $R(D^*)$

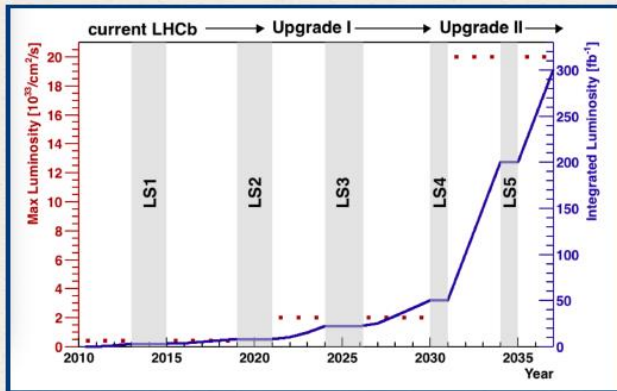
○ Form factor measurements

- $\Lambda_b \rightarrow \Lambda_c l \nu$
- $\Lambda_b \rightarrow \Lambda_c^* l \nu$
- $B_s \rightarrow D_s^{(*)} l \nu$ [arXiv:2003.08453]

○ Angular analyses

❖ In the **Upgrade I**, LHCb will collect $\sim 50 \text{fb}^{-1}$ (luminosity $\times 5$)

[arXiv:1809.06229]



[arXiv:2003.08453]

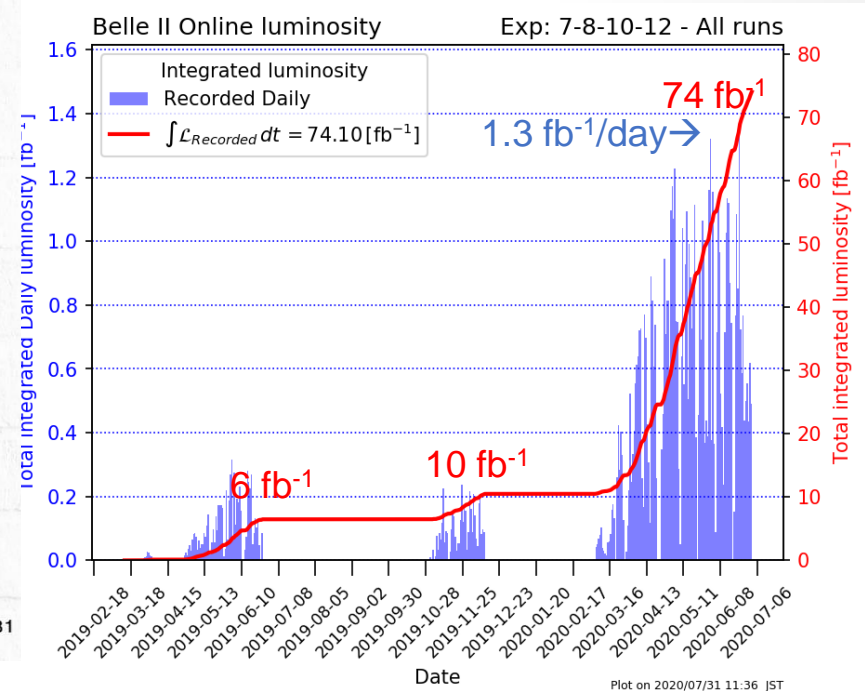
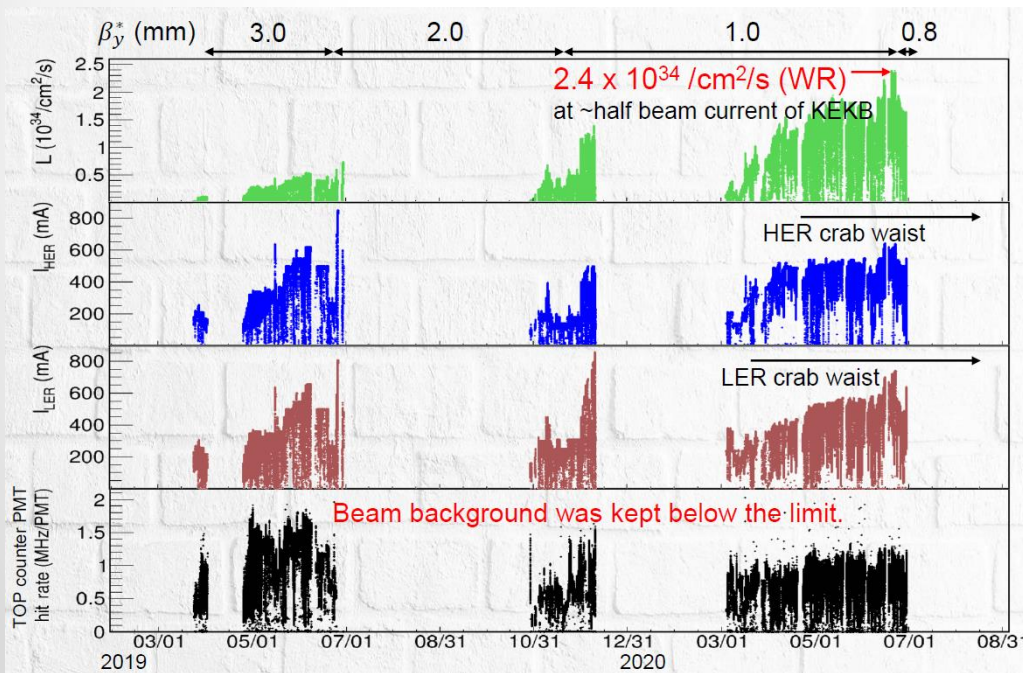
[arXiv:1808.08865]

Belle II Accumulating Physics Data



- Belle II / SuperKEKB started physics data taking with full detectors in 2019
- Peak luminosity $2.4 \times 10^{34} / \text{cm}^2/\text{s}$ (WR) exceeded KEKB
 - About half beam currents of KEKB, with β_y^* squeezed to 1.0 mm ($\beta_y^*=0.3\text{mm}$ is the final target)
 - good achievement as a start up

More details in Gagan's talk



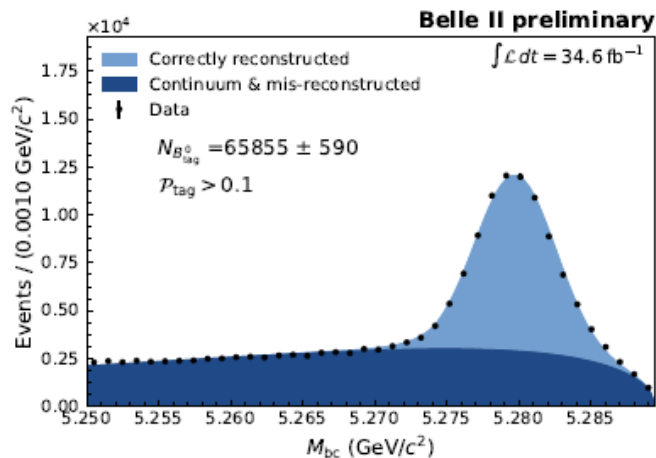
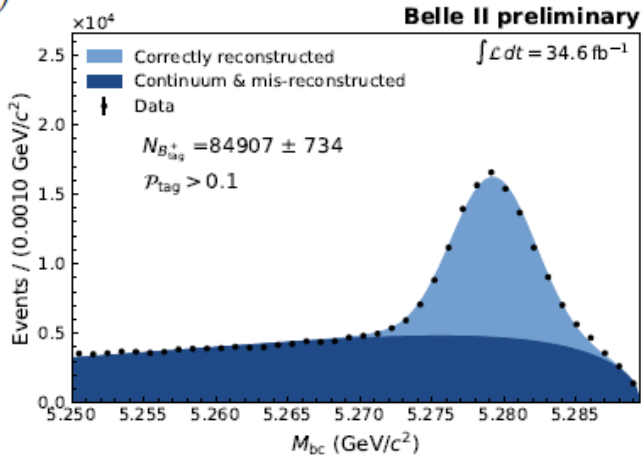
Hadronic Tag in Early BelleII Data



- Belle II analysis software works very well.
- Hadronic tag (Full Event Interpretation) performance calibrated with data

[BELLE2-CONF-PH-2020-005, arXiv: 2008.06096]

(b)

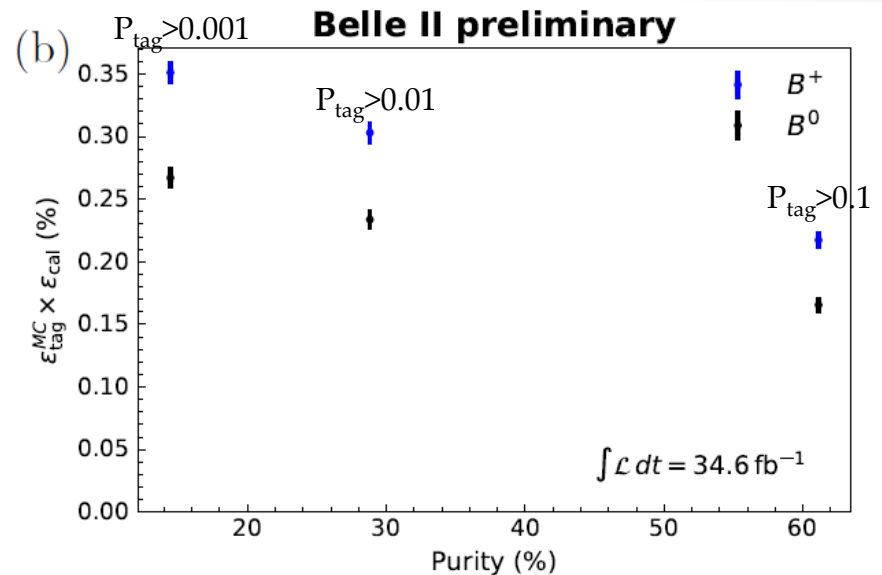


Reconstructed variables:

$$M_{bc} = \sqrt{(E_{\text{beam}}^2 - p_B^2)}$$

P_{tag} : classifier of purity

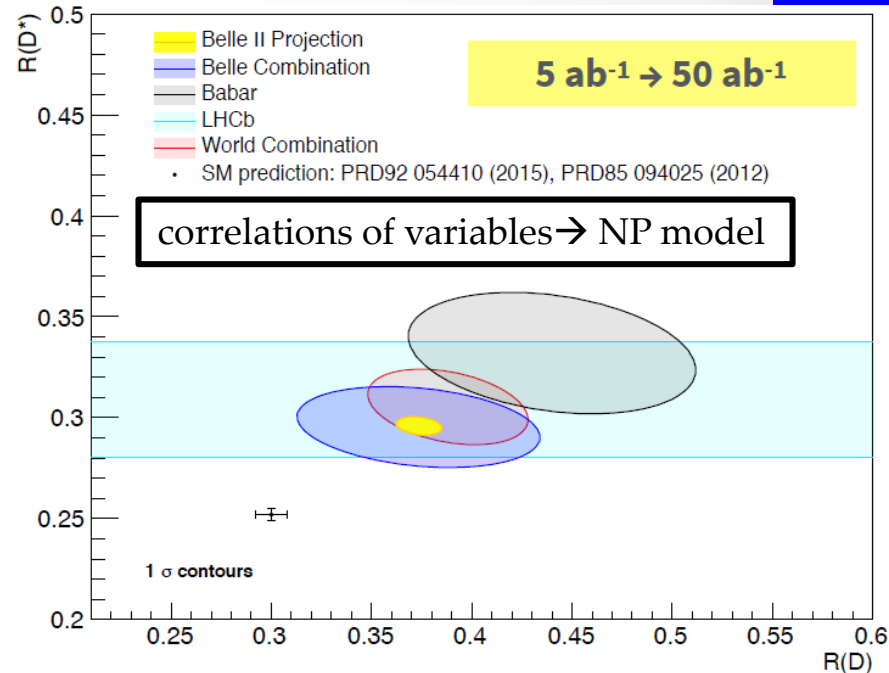
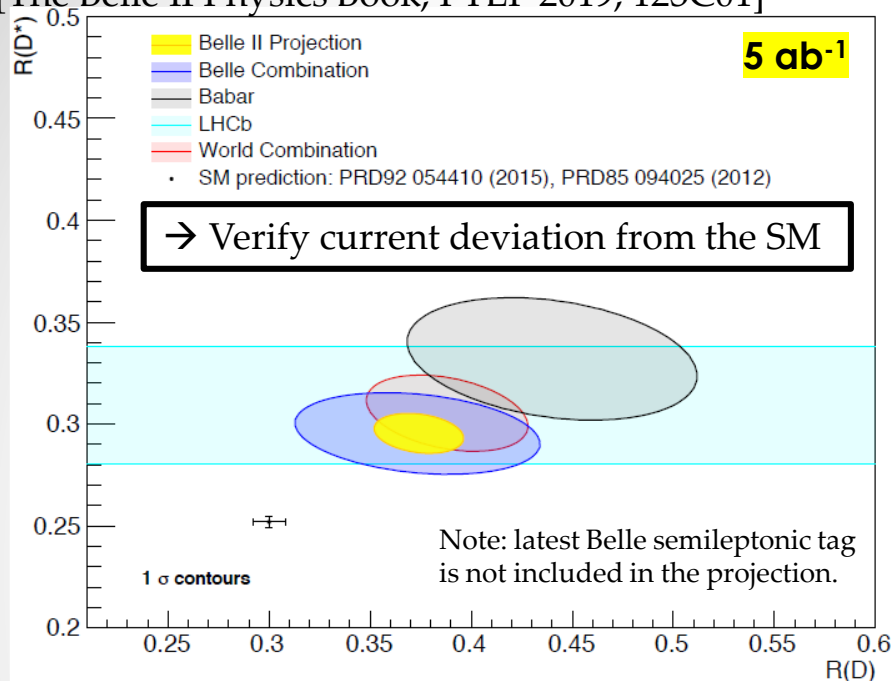
Purity dependent efficiency is calibrated



R(D^{*}) Belle II Prospect



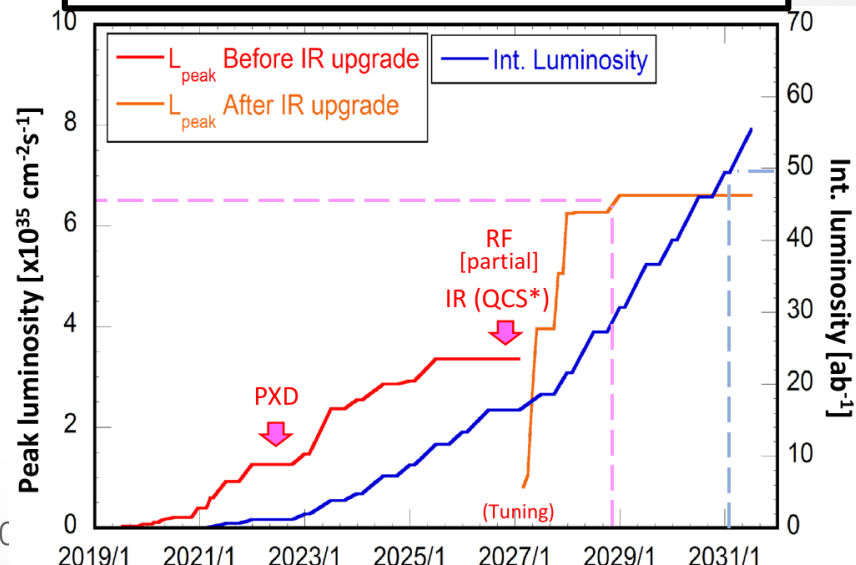
[The Belle II Physics Book, PTEP 2019, 123C01]



Expected Precision at Belle II
for R(D^{*}), τ polarization

	5 ab ⁻¹	50 ab ⁻¹
R_D	(±6.0 ± 3.9)%	(±2.0 ± 2.5)%
R_{D^*}	(±3.0 ± 2.5)%	(±1.0 ± 2.0)%
$P_\tau(D^*)$	±0.18 ± 0.08	±0.06 ± 0.04

Belle II/SuperKEKB Luminosity Prospect



Summary

- $B \rightarrow D^{(*)} \tau \nu$ decays are good probes for New Physics
- Belle, BaBar, LHCb have measured $R(D^{(*)})$ with various methods and sub-decay modes
 - In addition to $R(D^{(*)})$, other variables have been also measured
 - τ , D^* Polarizations
 - $R(J/\psi)$
- ‘Anomaly’ exists between measurements and SM
 - Little bit reduced but still there is 3.1σ difference
- LHCb and Belle II will provide more interesting results in future
 - Verify or reject the current ‘anomaly’
 - Determine the new physics model, if exists

Belle Systematic Errors

Source	Belle (Had, ℓ^-) R_D	Belle (Had, ℓ^-) R_{D^*}	Belle (SL, ℓ^-) R_{D^*}	Belle (Had, h^-) R_{D^*}
MC statistics	4.4%	3.6%	2.5%	+4.0% -2.9%
$B \rightarrow D^{**} \ell \nu_\ell$	4.4%	3.4%	+1.0% -1.7%	2.3%
Hadronic B	0.1%	0.1%	1.1%	+7.3% -6.5%
Other sources	3.4%	1.6%	+1.8% -1.4%	5.0%
Total	7.1%	5.2%	+3.4% -3.5%	+10.0% -9.0%

τ Hadronic decay: $R(D^*)$, τ Polarization

Systematic Errors

TABLE II. The systematic uncertainties in $R(D^*)$ and $P_\tau(D^*)$, where the values for $R(D^*)$ are relative errors. The group “common sources” identifies the common systematic uncertainty sources in the signal and the normalization modes, which cancel to a good extent in the ratio of these samples. The reason for the incomplete cancellation is described in the text.

Source	$R(D^*)$	$P_\tau(D^*)$
Hadronic B composition	+7.7% -6.9%	+0.134 -0.103
MC statistics for PDF shape	+4.0% -2.8%	+0.146 -0.108
Fake D^*	3.4%	0.018
$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$	2.4%	0.048
$\bar{B} \rightarrow D^{**} \tau^- \bar{\nu}_\tau$	1.1%	0.001
$\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$	2.3%	0.007
τ daughter and ℓ^- efficiency	1.9%	0.019
MC statistics for efficiency estimation	1.0%	0.019
$\mathcal{B}(\tau^- \rightarrow \pi^- \nu_\tau, \rho^- \nu_\tau)$	0.3%	0.002
$P_\tau(D^*)$ correction function	0.0%	0.010
Common sources		
Tagging efficiency correction	1.6%	0.018
D^* reconstruction	1.4%	0.006
Branching fractions of the D meson	0.8%	0.007
Number of $B\bar{B}$ and $\mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^-$ or $B^0 \bar{B}^0)$	0.5%	0.006
Total systematic uncertainty	+10.4% -9.4%	+0.21 -0.16

D* Polarization Systematic Errors

TABLE I. Summary of systematic uncertainties

Source		$\Delta F_L^{D^*}$
Monte Carlo statistics	AR shape and peaking background	± 0.032
	CB shape	± 0.010
	Background scale factors	± 0.001
Background modeling	$B \rightarrow D^{**} \ell \nu$	± 0.003
	$B \rightarrow D^{**} \tau \nu$	± 0.011
	$B \rightarrow$ hadrons	± 0.005
	$B \rightarrow \bar{D}^* M$	± 0.004
Signal modeling	Form factors	± 0.002
	$\cos \theta_{\text{hel}}$ resolution	± 0.003
	Acceptance non-uniformity	+0.015 -0.005
Total		+0.039 -0.037