

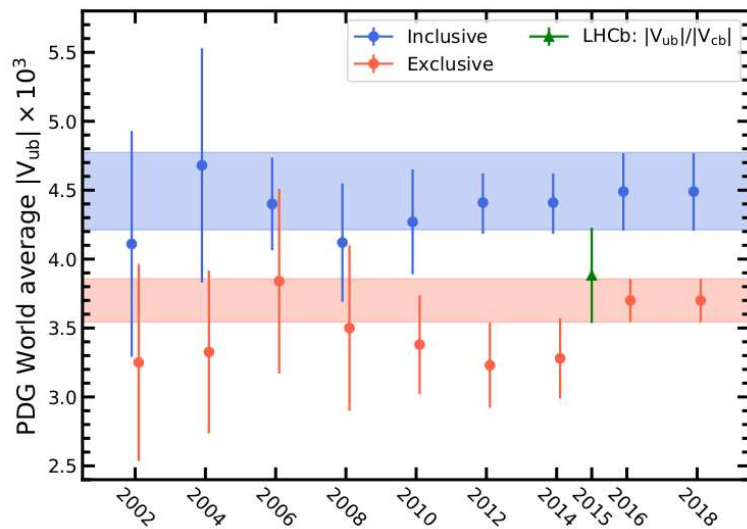
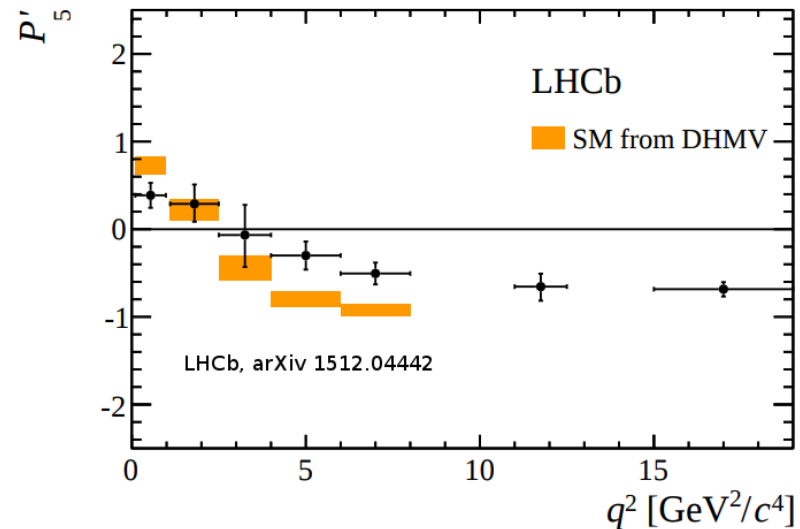
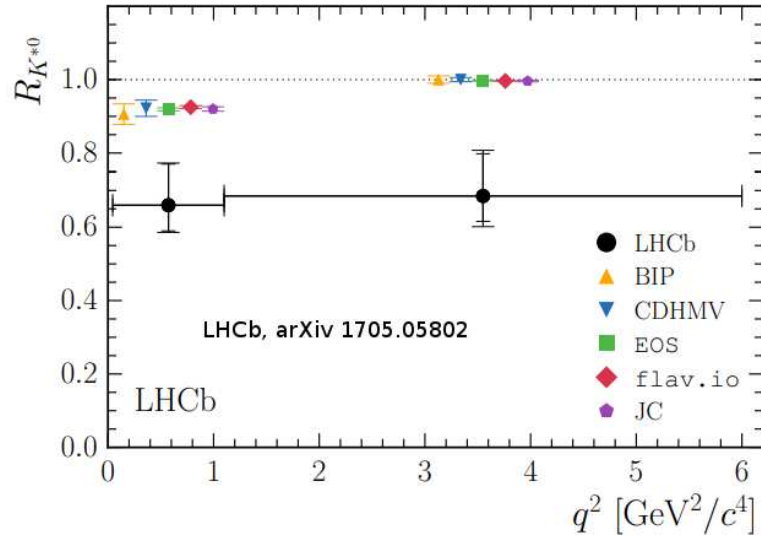


Anomalies in B (semi)leptonic decays at B factories

S. Glazov on behalf of Belle II collaboration

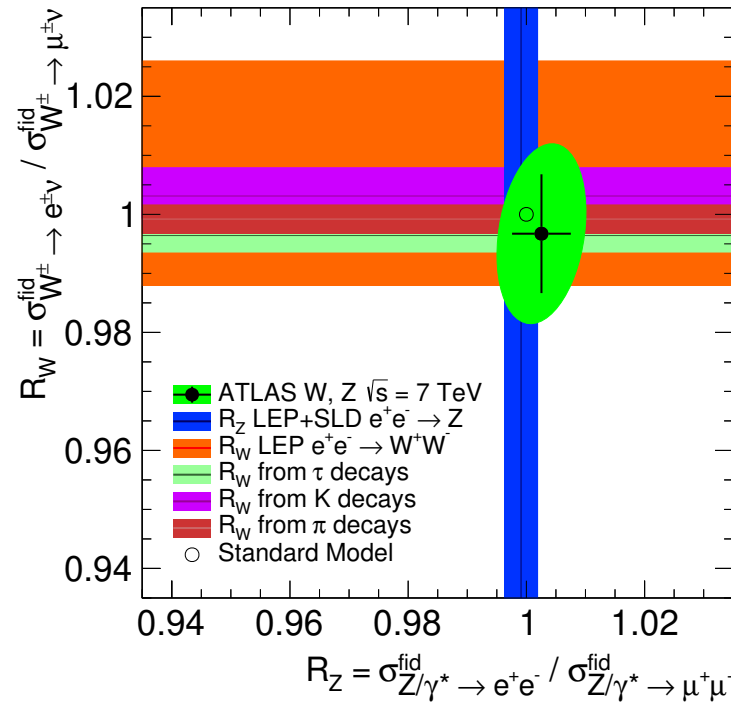
KAON2019, Perugia, 11 September 2019.

Signatures of B anomalies



- Deviation from expected branching fractions
- Lepton flavour universality violation: $R_D, R_{D^*}, R_K, R_{K^*}$
- Anomalies in angular distributions
- Inconsistencies in $|V_{cb}|, |V_{ub}|$ determination for inclusive vs exclusive methods.

Experimental data on LFU

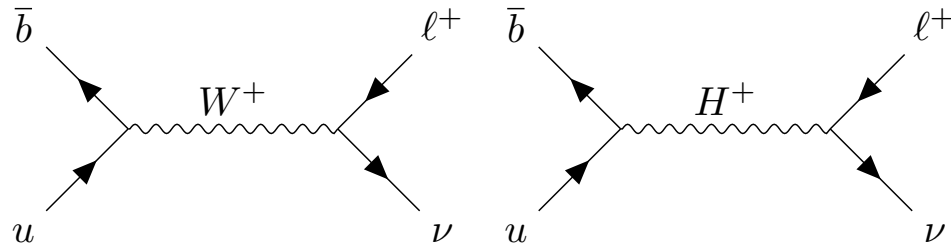


ATLAS EPJC 77 (2017) 367;
 LEP+SLD, PR 427 (2006) 257;
 HFAG arXiv:1412.7515;
 KTEV PRD70 (2004) 092007;
 NA62 PLB 719 (2013) 326;
 PIENU PRL 115 (2015) 071801.

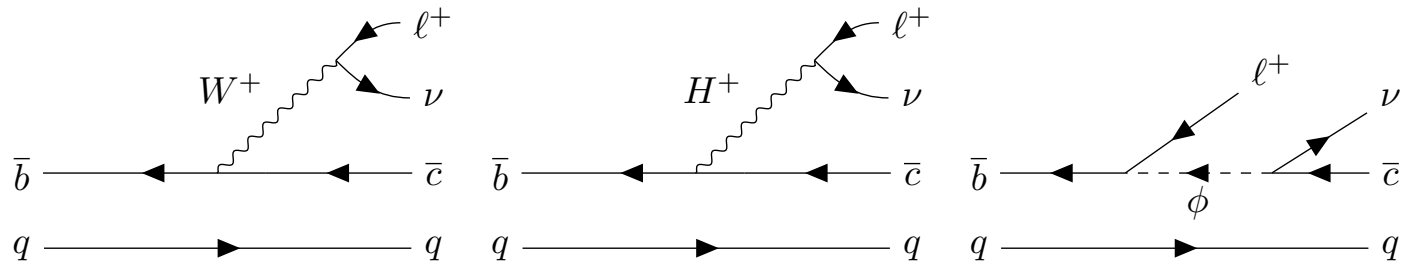
- Lepton flavour violation probed to 10^{-12} level in μ decays.
- Lepton universality for $Z \rightarrow \ell\ell$ probed to per mille accuracy at LEP, including $\Gamma_{Z \rightarrow \tau\tau} / \Gamma_{Z \rightarrow \ell\ell} = 1.0019 \pm 0.0032$.
- Lepton universality for $W \rightarrow e\nu$ and $W \rightarrow \mu\nu$ decays measured directly, controlled with high precision using π , K and τ decays. Some tension for $W \rightarrow \tau\nu$ from LEP: $(\Gamma(\tau\nu) / \Gamma(e\nu)) = 1.063 \pm 0.027$, $\Gamma(\tau\nu) / \Gamma(\mu\nu) = 1.070 \pm 0.026$.

B decays and LFV/LFU

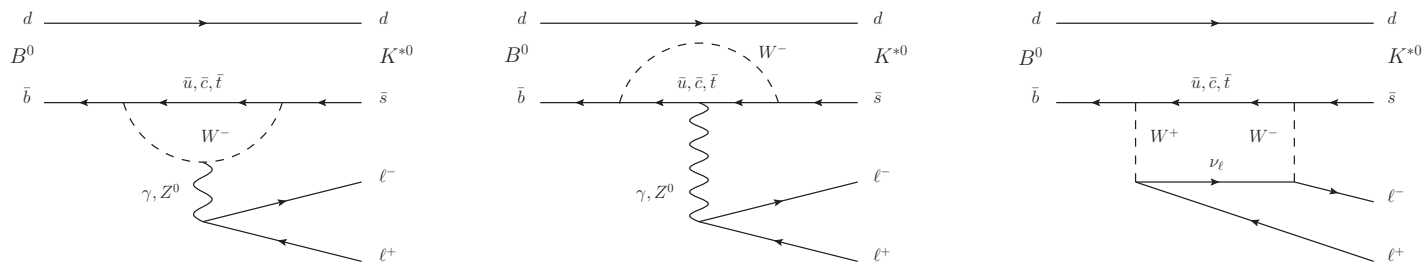
- Leptonic decays $B^\pm \rightarrow \ell^\pm \nu$, $B^0 \rightarrow \ell \ell'$.



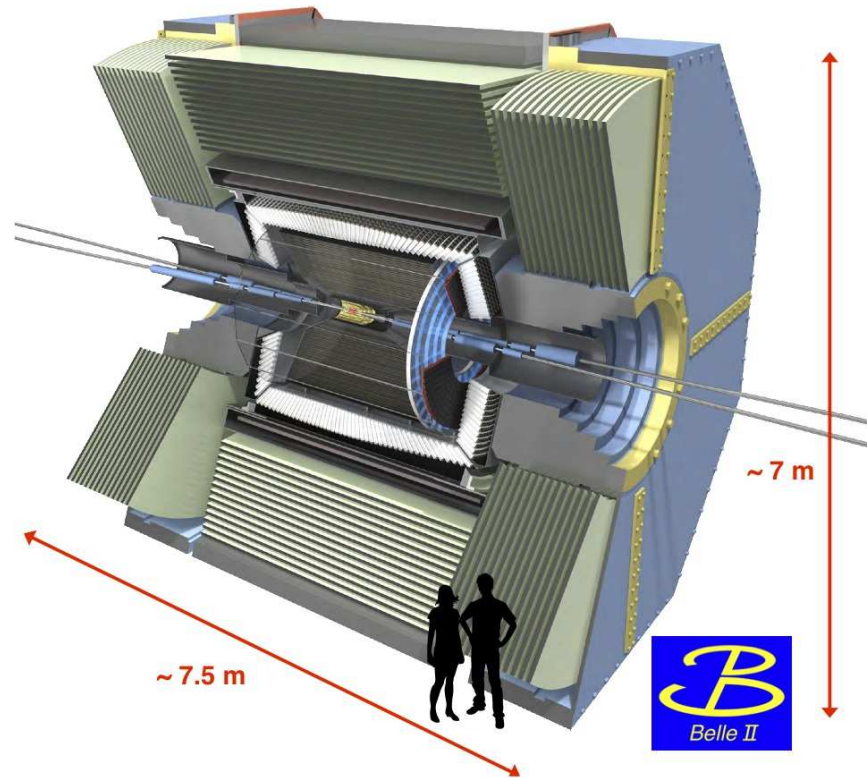
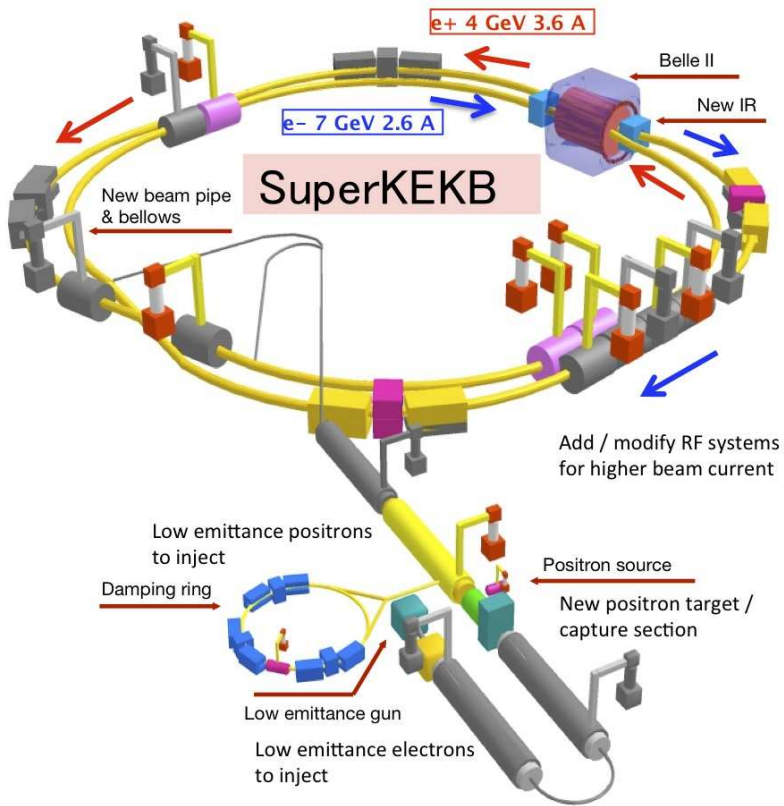
- Semileptonic decays $B \rightarrow X \ell \nu$



- FCNC processes $B \rightarrow X_{s(d)} \ell^+ \ell^-$.

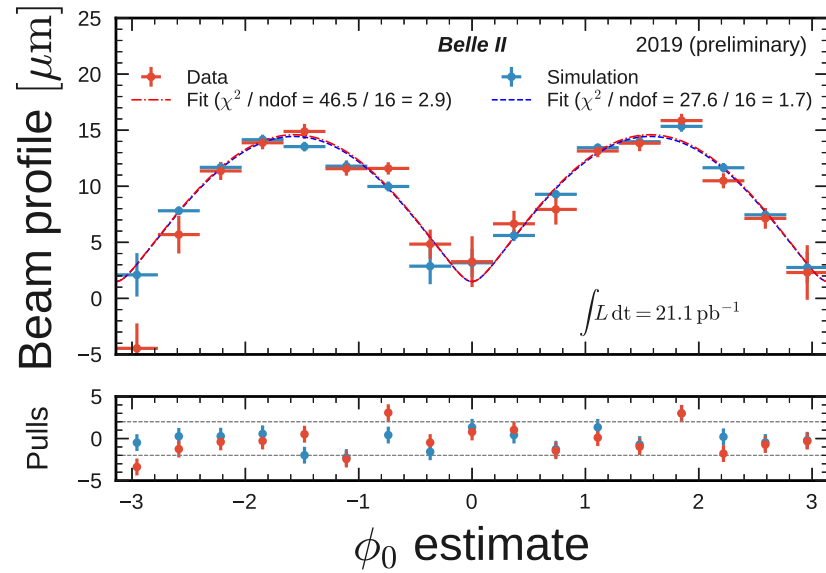
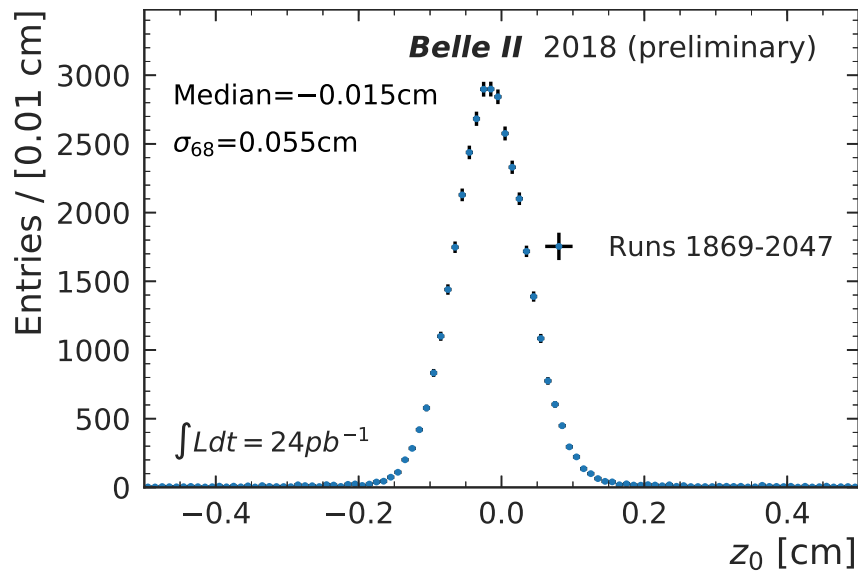


SuperKEKB and Belle II



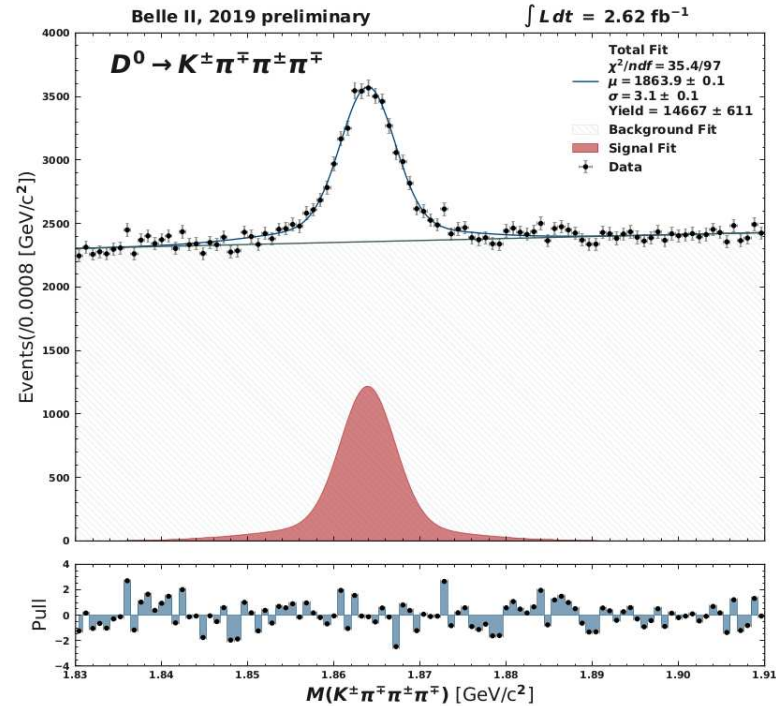
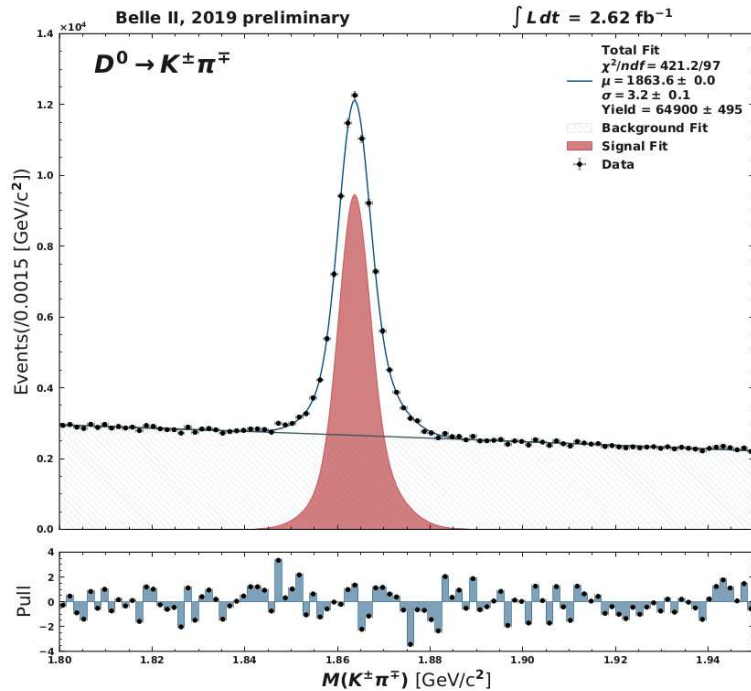
→ First physics data in 2018, 2019 runs.

Status of Belle II



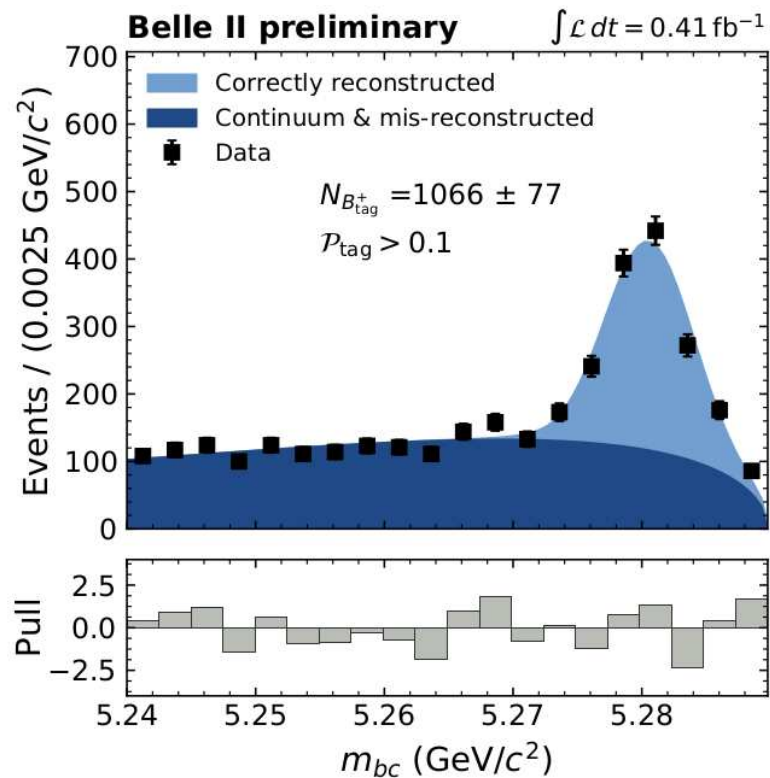
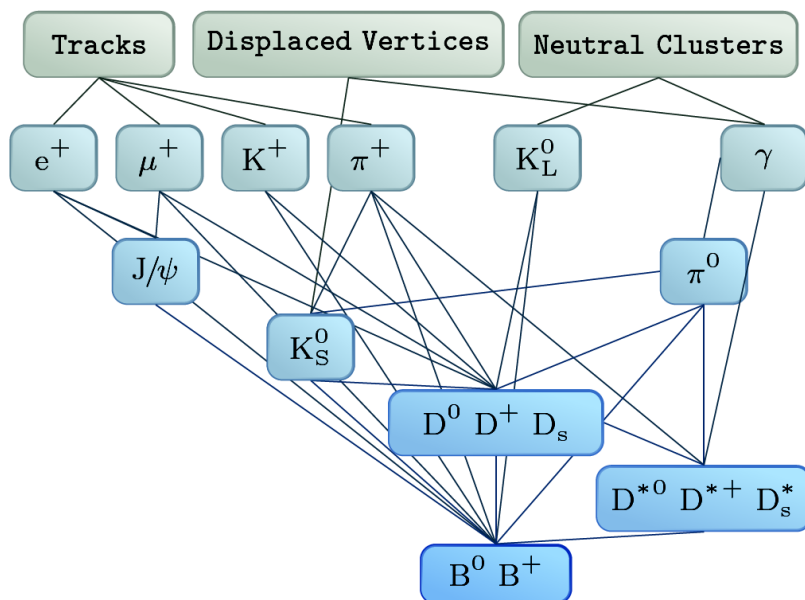
- z -vertex spread at **0.5 mm** level (vs **1 cm** at Belle-I): strong focusing, large crossing angle, towards nano-beam scheme.
- Transverse impact parameter resolution of **$12\ \mu\text{m}$** (vs **$10\ \mu\text{m}$** expected) thanks to PXD, about twice better vs Belle-I.
- However many challenges remain, including high background, requiring further machine and detector tuning.

D-meson reconstruction



- D^* mesons are reconstructed from $D^{*0} \rightarrow D^0 \gamma, D^0 \pi^0$ and $D^{*+} \rightarrow D^+ \pi^0, D^0 \pi^+$ while D are from $D^0 \rightarrow K_S^0 \pi^0, \pi^+ \pi^-, K^- \pi^+, K^+ K^-, K^- \pi^+ \pi^0, K_S^0 \pi^+ \pi^-, K_S^0 \pi^+ \pi^- \pi^0, K^- \pi^+ \pi^+ \pi^-, D^+ \rightarrow K_S^0 \pi^+, K_S^0 K^+, K_S^0 \pi^+ \pi^0, K^- \pi^+ \pi^+, K^+ K^- \pi^+, K^- \pi^+ \pi^+ \pi^0, K_S^0 \pi^+ \pi^+ \pi^-$
- Many of the channels are “rediscovered” at Belle II.
- With increased statistics, different channels provide important systematic check.

B-tagging: full event interpretation



- Hierarchical approach using several stages to construct full decay chains of B^0, B^+ mesons.
- Heavy use of ML methods (BDT) leads to improvement vs previous methods.
- Can be used for hadronic as well as semileptonic tagging. For B^\pm Hadronic / semileptonic tag efficiency is 0.61% / 1.45%, about twice better vs Belle.
- Tested on early Belle-II data.

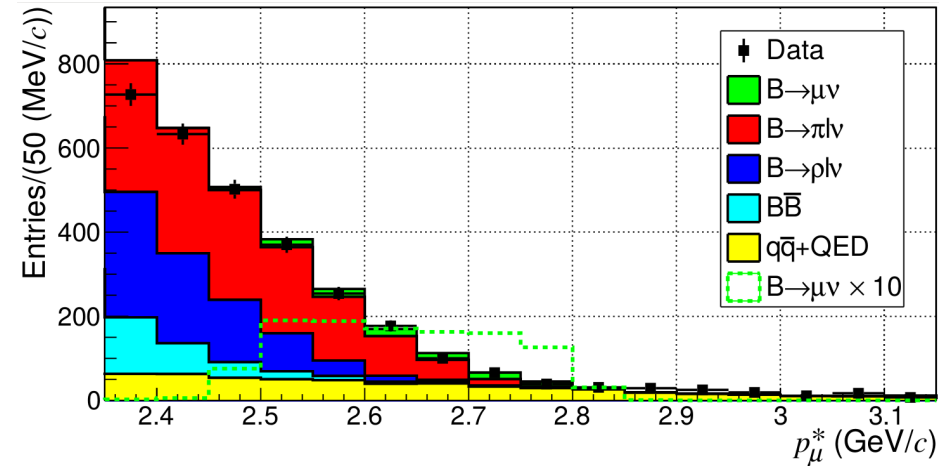
arXiv:1807.0868

Leptonic decays

Expected branching fraction and yield at Belle:

ℓ	B_{SM}	N_{SM}^{Belle}
τ	$(8.45 \pm 0.70) \times 10^{-5}$	$(670 \pm 57) \times 10^2$
μ	$(3.80 \pm 0.31) \times 10^{-7}$	301 ± 25
e	$(8.89 \pm 0.73) \times 10^{-12}$	0.0071 ± 0.0006

PRL 121, 031801 (2018)



$$B(B^- \rightarrow \ell^- \bar{\nu}_\ell) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B,$$

- With decay constant from FLAG $f_B = 0.186 \pm 0.004$, interesting alternative for $|V_{ub}|$ determination.
- Analysis using 2D fit to p_μ^* and NN estimator.
- Signal branching fraction is determined using $R = N_{B \rightarrow \mu \bar{\nu}_\mu} / N_{N \rightarrow \pi \mu \bar{\nu}_\mu}$ to be $B(B \rightarrow \mu \bar{\nu}_\mu) = (6.46 \pm 2.22 \pm 1.60) \times 10^{-7}$, consistent with SM expectations.

PRL 121, 031801 (2018)

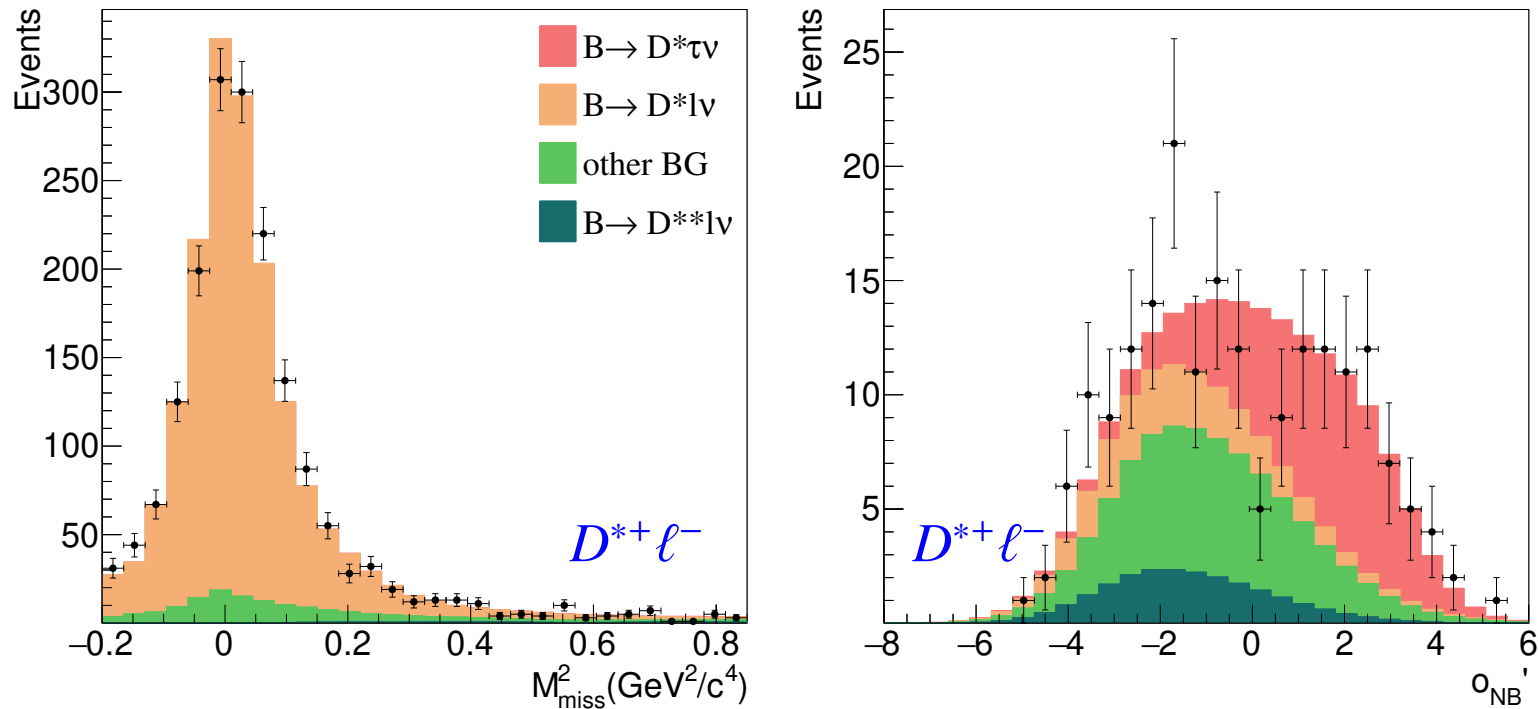
Semileptonic decays: R_D and R_{D^*}

Exp.	Tag method	τ^- decays	Observables	Fit variables
Belle PRL 99, 191807 (2007)	Untagged	$e^- \nu_\tau \bar{\nu}_e, \pi \nu_\tau$	$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau)$	M_{bc}^{comp}
Belle PRD 82, 072005 (2010)	Untagged	$\ell^- \nu_\tau \bar{\nu}_\ell, \pi \nu_\tau$	$\mathcal{B}(B^- \rightarrow D^{(*)0} \tau^- \bar{\nu}_\tau)$	M_{bc}^{comp} and p_{D^0}
Belle PRD 92, 072014 (2015)	Hadronic	$\ell^- \nu_\tau \bar{\nu}_\ell$	$R_D, R_{D^*}, q^2, p_\ell^* $	M_{miss}^2 and \mathcal{O}_{NB}^\dagger
Belle PRL 118, 211801 (2017)	Hadronic	$h^- \nu_\tau$	$R_{D^*}, P_\tau(D^*)$	E_{ECL} and $\cos \theta_{\text{hel}}$
Belle PRD 94, 072007 (2016)	Semileptonic	$\ell^- \nu_\tau \bar{\nu}_\ell$	$R_{D^*}, p_\ell^* p_{D^*}^* $	E_{ECL} and $\mathcal{O}'_{NB} \ddagger$
Belle preliminary conf-1902	Semileptonic FEI	$\ell^- \nu_\tau \bar{\nu}_\ell$	R_D, R_{D^*}	E_{ECL} and \mathcal{O}_{BDT}

Several methods to reconstruct $B \rightarrow D^{(*)} \tau \ell \nu$:

- Untagged early measurements used for observation of the decay
- Hadronically tagged for simultaneous fit of R_D, R_{D^*} and determination of differential distributions (semileptonic τ decays).
- Hadronically tagged with hadronic τ decays, for τ polarisation measurements.
- Semileptonically tagged, with semileptonic τ decays for R_{D^*}, R_D

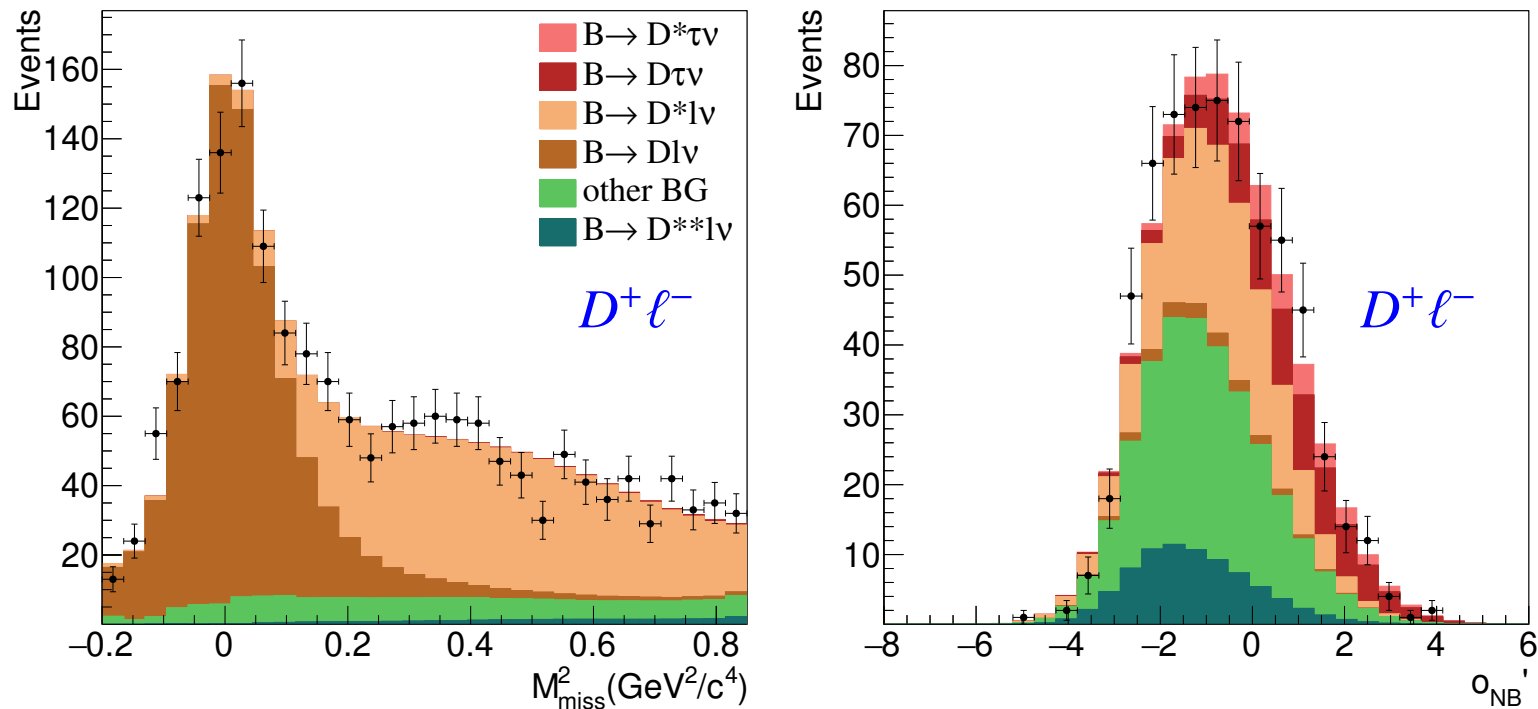
Measurement of R_{D^*} with hadronic tag at Belle



$$M_{\text{miss}}^2 = (p_{e^+e^-} - p_{\text{tag}} - p_{D^{(*)}} - p_{\ell})^2.$$

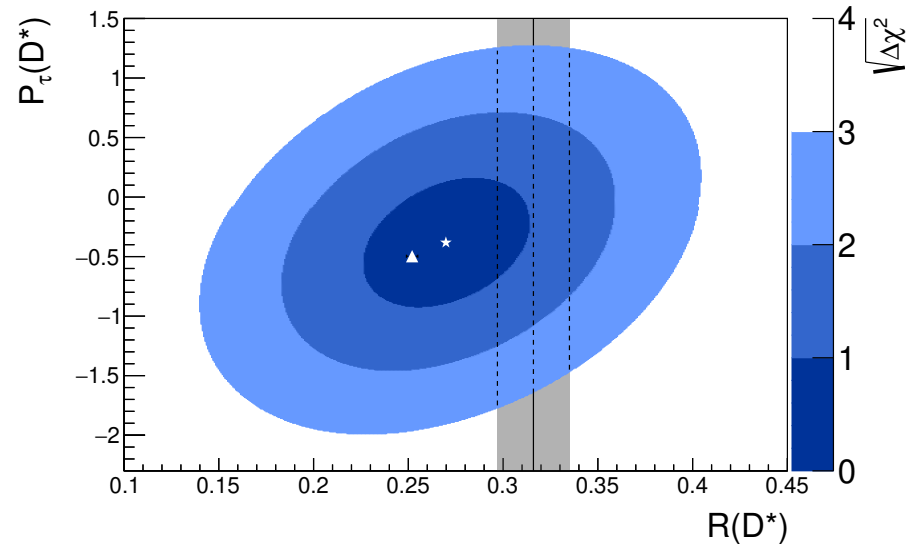
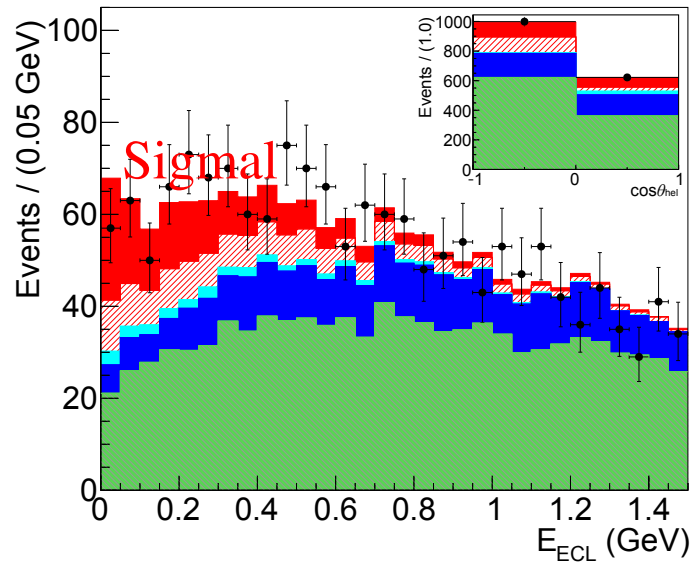
- Use reconstructed hadronically tagged B and $D^{(*)} + \ell$ with $\ell = \mu, e$ to determine M_{miss}^2 .
- Low $M_{\text{miss}}^2 < 0.85 \text{ GeV}$ is used to determine normalization $B \rightarrow D^{(*)} \ell \nu$, high $M_{\text{miss}}^2 > 0.85 \text{ GeV}$ — to fit NN output to determine $B \rightarrow D^{(*)} \tau \nu$. For NN, E_{ECL} is the main discriminating variable.

Measurement of R_D with hadronic tag at Belle



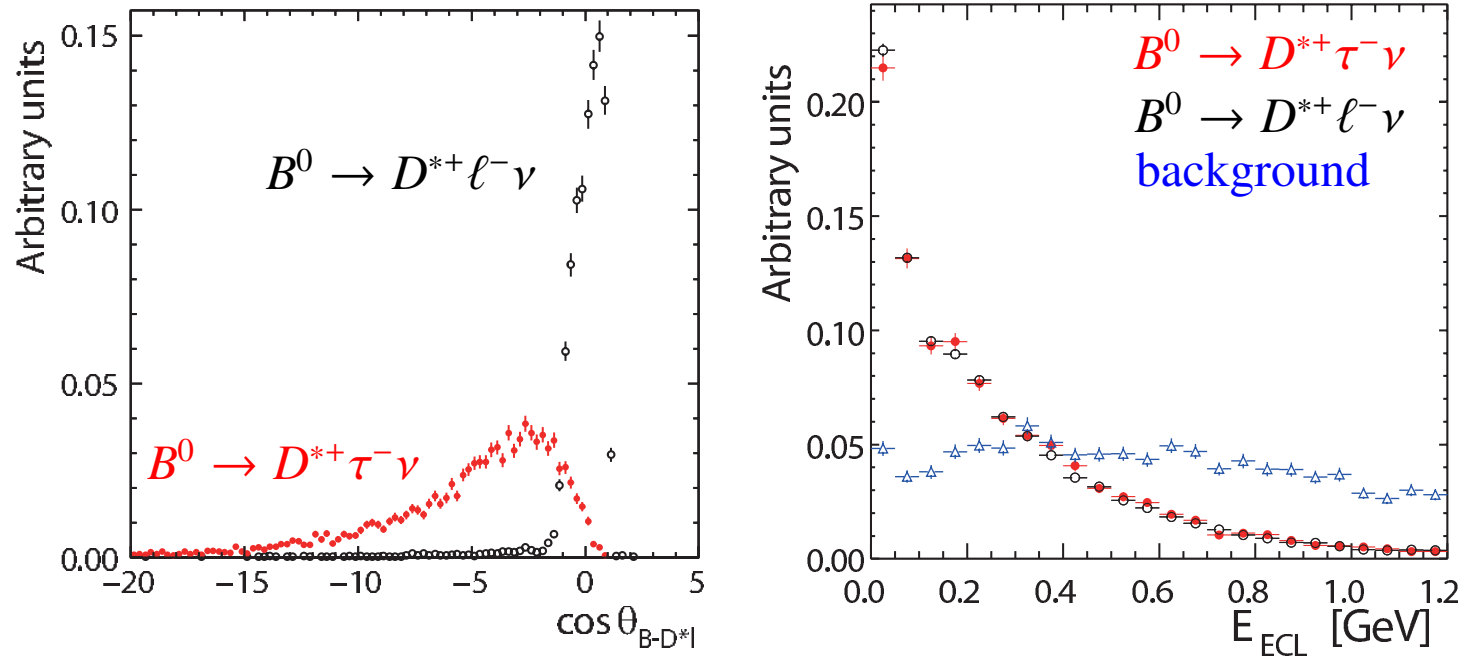
- Simultaneous fit of ℓ normalization, τ signal for D and D^* samples together with some of background sources while others are fixed to MC expectations.
- Significant backgrounds are $D^{**} \ell$ (fitted) and for $D \ell$ cross-feed from $D^* \ell$ (fitted).

R_{D^*} and τ polarisation measurements



- SM predictions for τ polarisation are very accurate: $P_\tau(D^*) = -0.497 \pm 0.013$, while BSM allows for larger variations.
- Polarisation is measured in two-body hadronic $\tau^- \rightarrow \pi^- \nu$ and $\tau^- \rightarrow \rho^- \nu$ ($\rho^- \rightarrow \pi^- \pi^0$) decays.
- Significant backgrounds from misreconstructed D^* candidates, hadronic B decays.

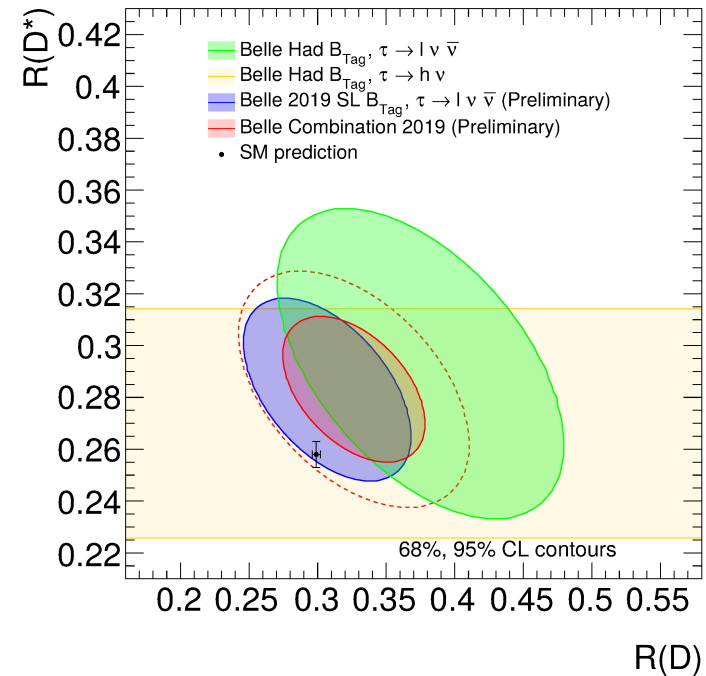
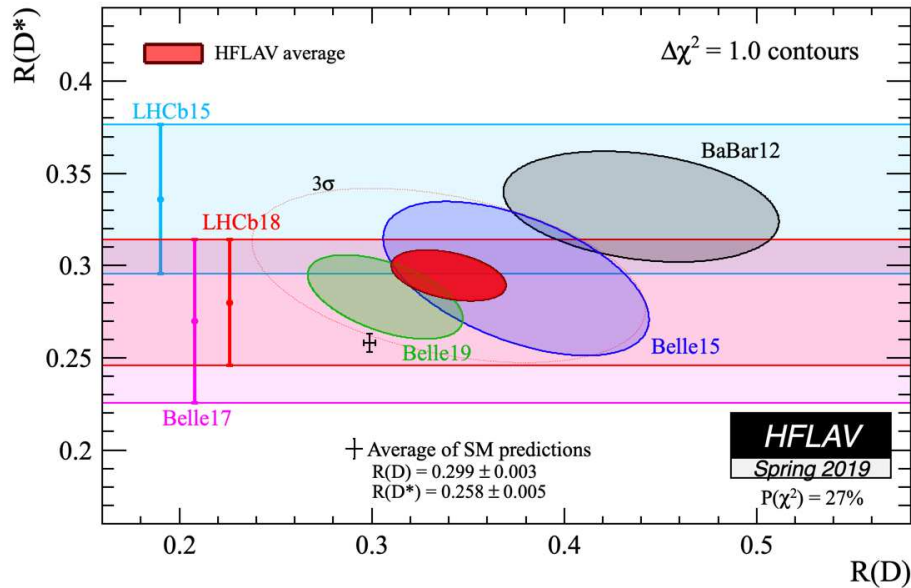
Measurement of $R_{D^{*+}}$ with semileptonic tag at Belle



$$\cos \theta_{B-D^{*+}\ell} \equiv \frac{2E_{\text{beam}}E_{D^{*+}\ell} - m_B^2 - M_{D^{*+}\ell}^2}{2|\vec{p}_B| \cdot |\vec{p}_{D^{*+}\ell}|},$$

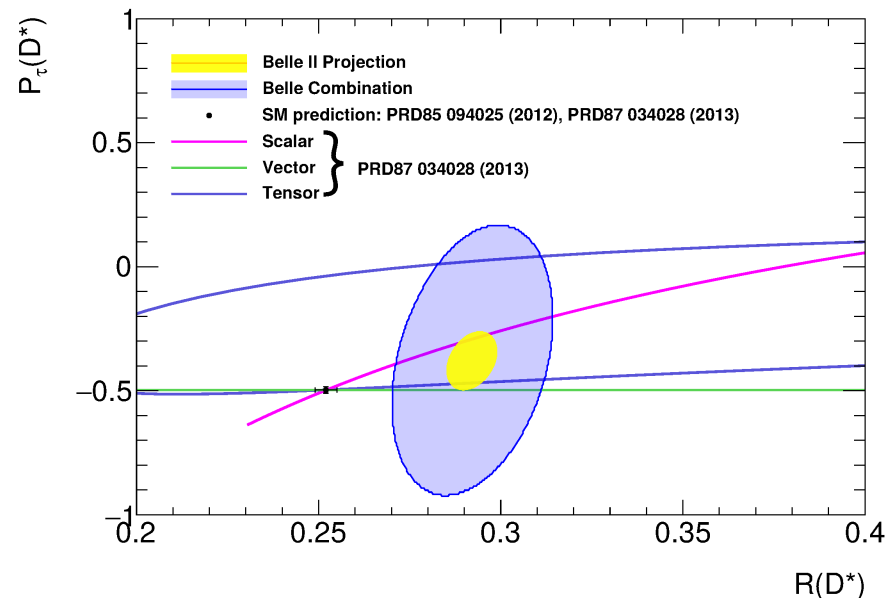
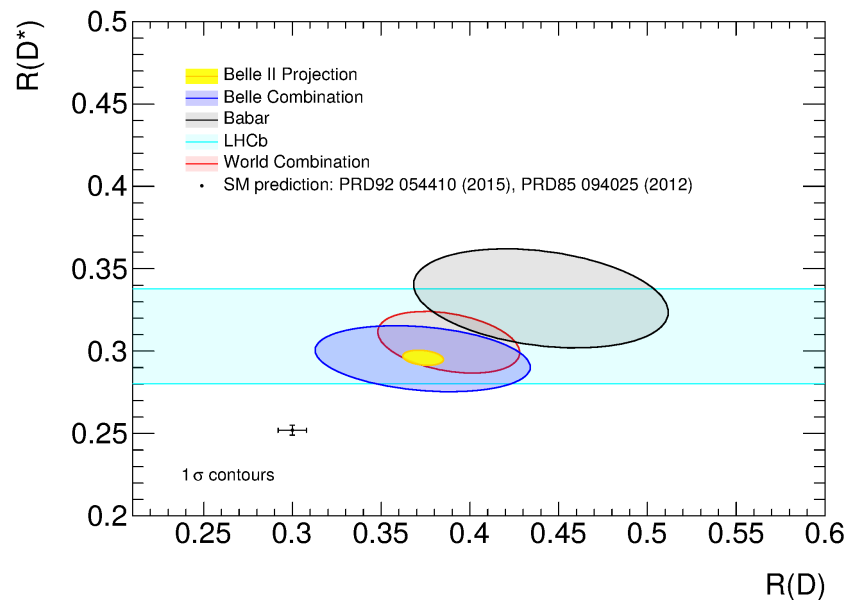
- Use leptonic $\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau$ decays to reconstruct τ ; require two leptons of opposite charge, missing energy and D/D^* .
- Combine lepton of opposite charge with D^{*+} , compute $\cos \theta_{B-D^{*+}\ell}$.
- E_{ECL} — sum of energies of extra neutrals in calorimeter — useful to separate background

Summary of R_D, R_{D^*} measurements



- New preliminary semileptonic tag based measurement of R_D, R_{D^*} is consistent with the old result, more precise.
- Recent measurements from Belle and LHCb reduce tensions with SM
- Combined Belle result is consistent with SM at 2σ level

$R_{D^{(*)}}$ and polarisation measurement projections for Belle II



	5 ab^{-1}	50 ab^{-1}
R_D	$(\pm 6.0 \pm 3.9)\%$	$(\pm 2.0 \pm 2.5)\%$
R_{D^*}	$(\pm 3.0 \pm 2.5)\%$	$(\pm 1.0 \pm 2.0)\%$
$P_\tau(D^*)$	$\pm 0.18 \pm 0.08$	$\pm 0.06 \pm 0.04$

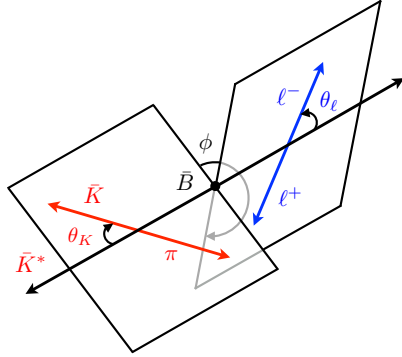
- Projections for 5 and 50 ab^{-1} . For 50 ab^{-1} systematics start to play important role.
- $P_\tau(D^*)$ as well as the double ratio of R_{D^*}/R_D provide extra information on the nature of NP (if deviation remains).

arXiv:1808.10567

FCNC: $B \rightarrow K^* \ell \ell$ differential rate

Angular decomposition for the differential rate:

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d \cos \theta_\ell d \cos \theta_K d\phi dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \right. \\ \left. + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right],$$



Redefinition of parameters: $P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$

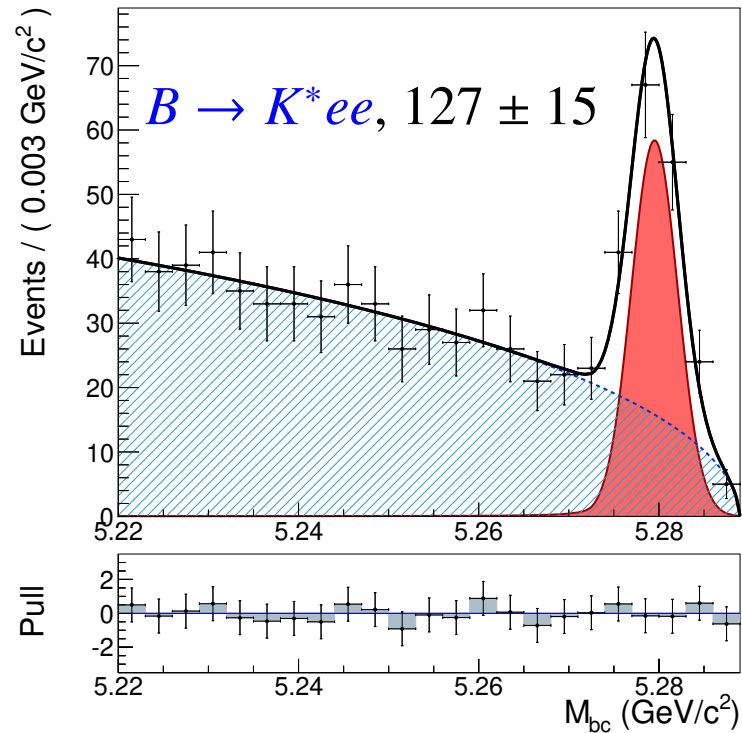
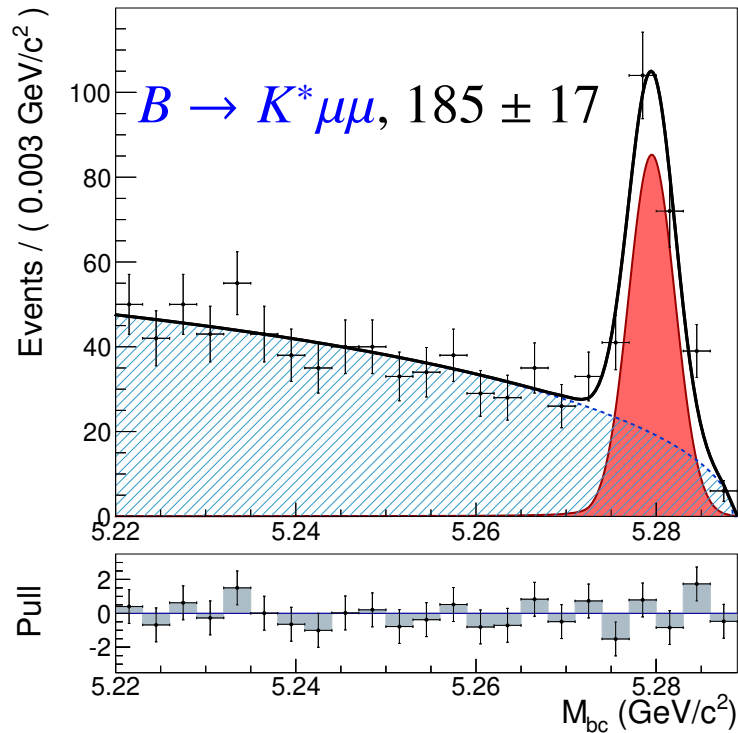
Folding of variables:

$$P'_4, S_4 : \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \phi \rightarrow \pi - \phi & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases} \quad P'_5, S_5 : \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2. \end{cases}$$

For small q^2 , P'_5 is connected to semi-leptonic operators Q_9 and Q_{10} .

$$P'_5 \simeq \frac{\text{Re}(C_{10}^* C_{9,\perp} + C_{9,\parallel}^* C_{10})}{\sqrt{(|C_{9,\perp}|^2 + |C_{10}|^2)(|C_{9,\parallel}|^2 + |C_{10}|^2)}},$$

$B \rightarrow K^{(*)}\mu\mu$ and $B \rightarrow K^{(*)}ee$ at Belle



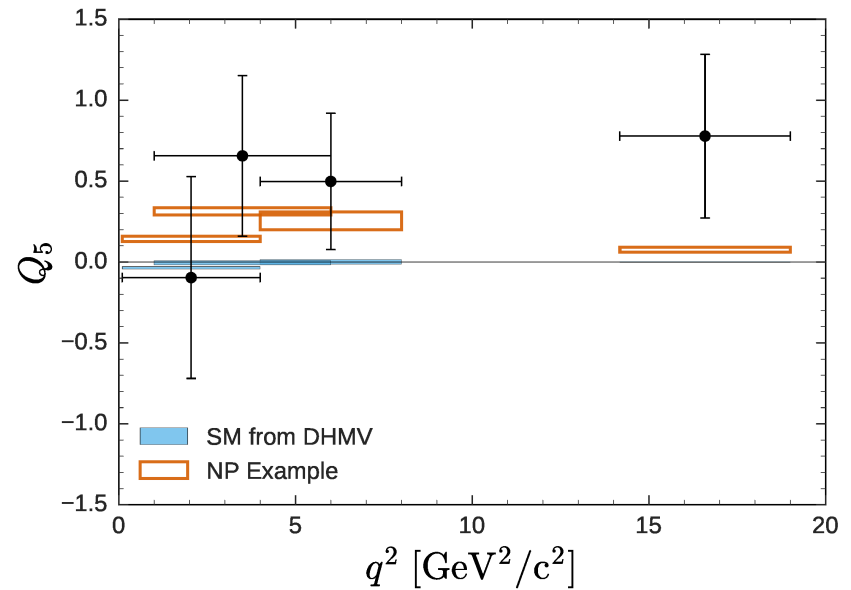
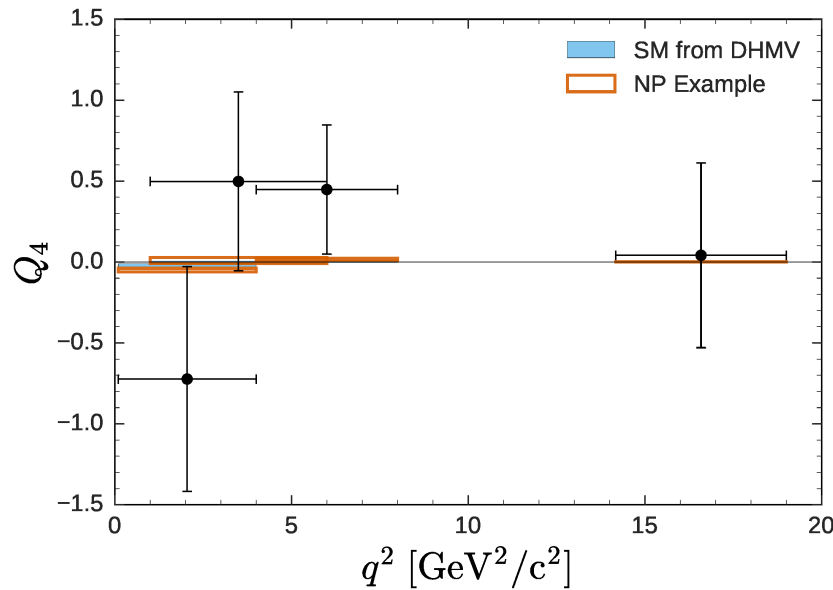
- Fit to beam constrained mass distribution,

$$M_{bc} = \sqrt{E_{beam}^2 - |\vec{p}_B|^2}.$$

- Similar quality for $K^*\mu\mu$ and K^*ee reconstruction: reduced systematics for R_{K^*} .

PRL118, 111801 (2017).

Differential LFU tests for $B \rightarrow K^{(*)}\ell\ell$

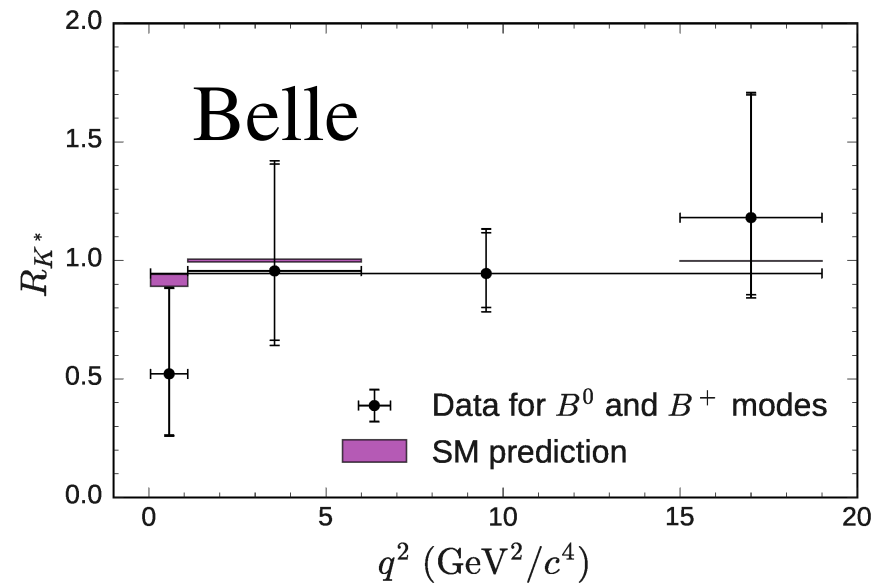
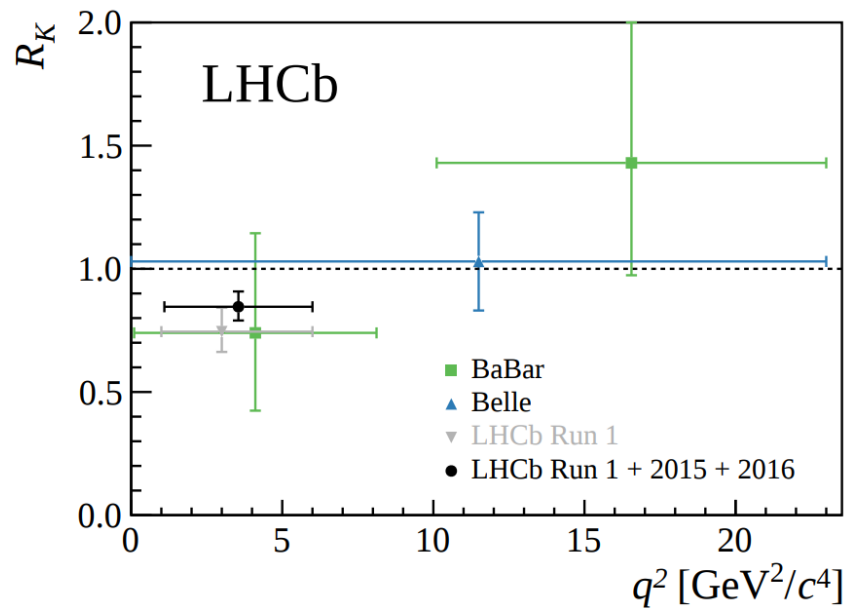


- Determine flavour dependent angular coefficient difference:
 $Q_i = P'_{i,\mu} - P'_{i,e}$.
- Sensitivity to NP in Q_5 , errors dominated by statistics.
- Modeling of QED radiation / bin-to-bin migrations may start play a role with improved stats.

(Note that the measurement is presented for two different binning schemes, the measurement for the $1 < q^2 < 6 \text{ GeV}^2$ bin is correlated with measurements in the overlapping bins.)

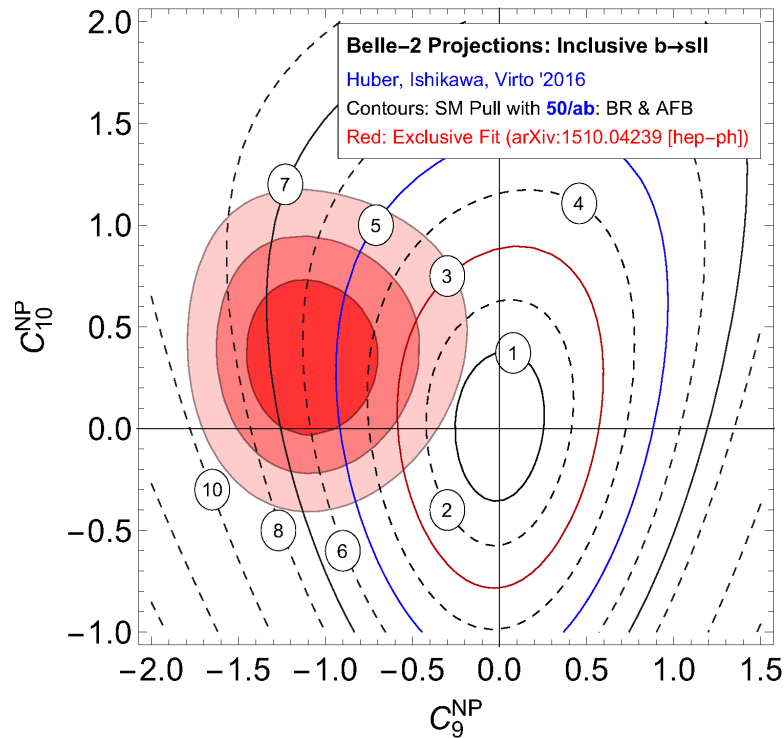
PRL118, 111801 (2017).

Recent R_K and R_{K^*} results



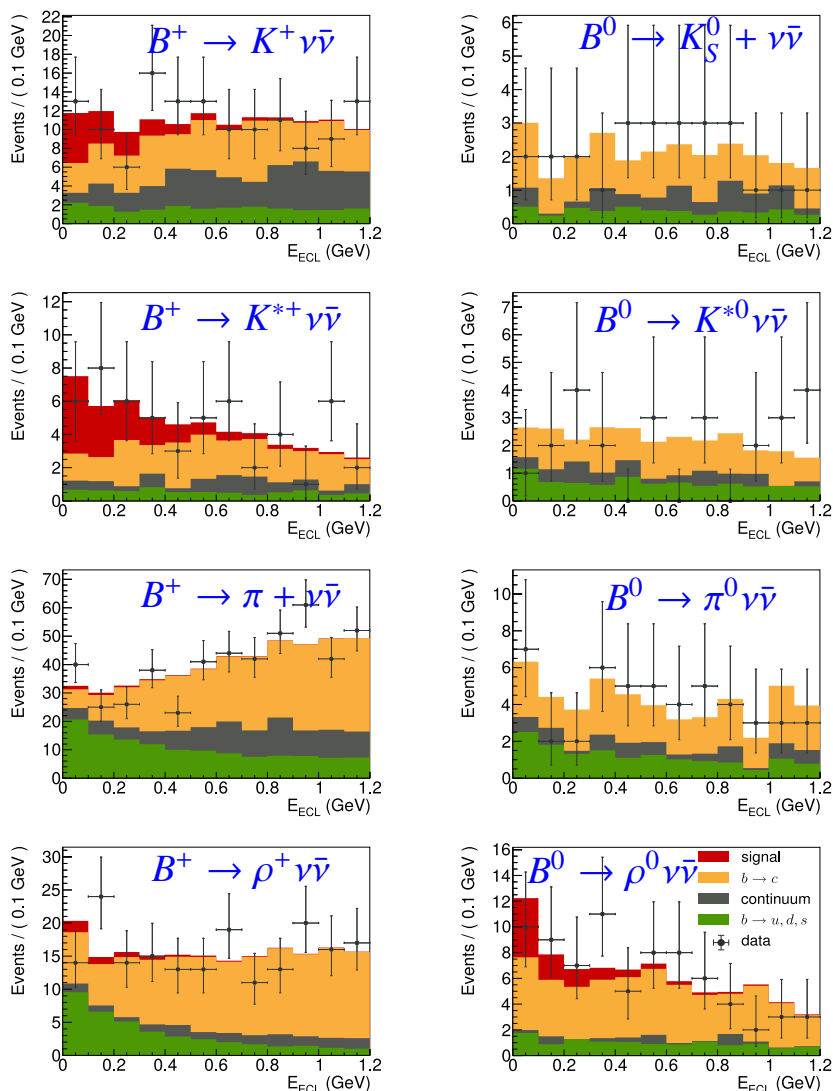
- Recent update on R_K from LHCb ([PRL 122 \(2019\) 191801](#)) and preliminary result from Belle on R_{K^*} .
- New measurements are closer to the SM predictions.

Perspective for inclusive $B \rightarrow X_s \ell \ell$ decays at Belle-II



- Initial measurements sum over exclusive method with $M_{X_s} \lesssim 1.8 \text{ GeV}$, eventually: fully inclusive recoil method.
- Theoretical uncertainties from M_{X_s} cut, resolved photon contribution, charmonium resonances.
- Can be performed for $X_s e e$ and $X_s \mu \mu$ separately.

$B \rightarrow h\nu\bar{\nu}$ study from Belle (semileptonic tag)

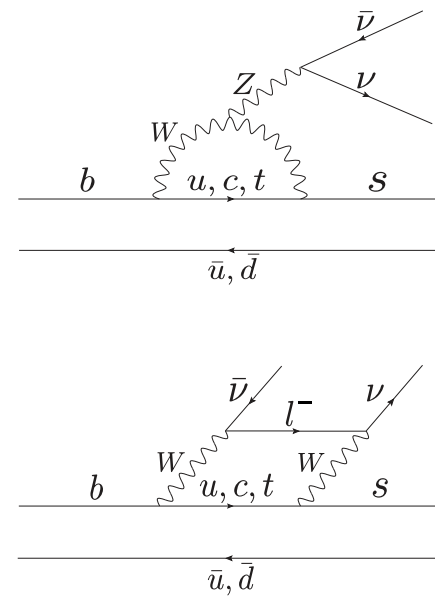
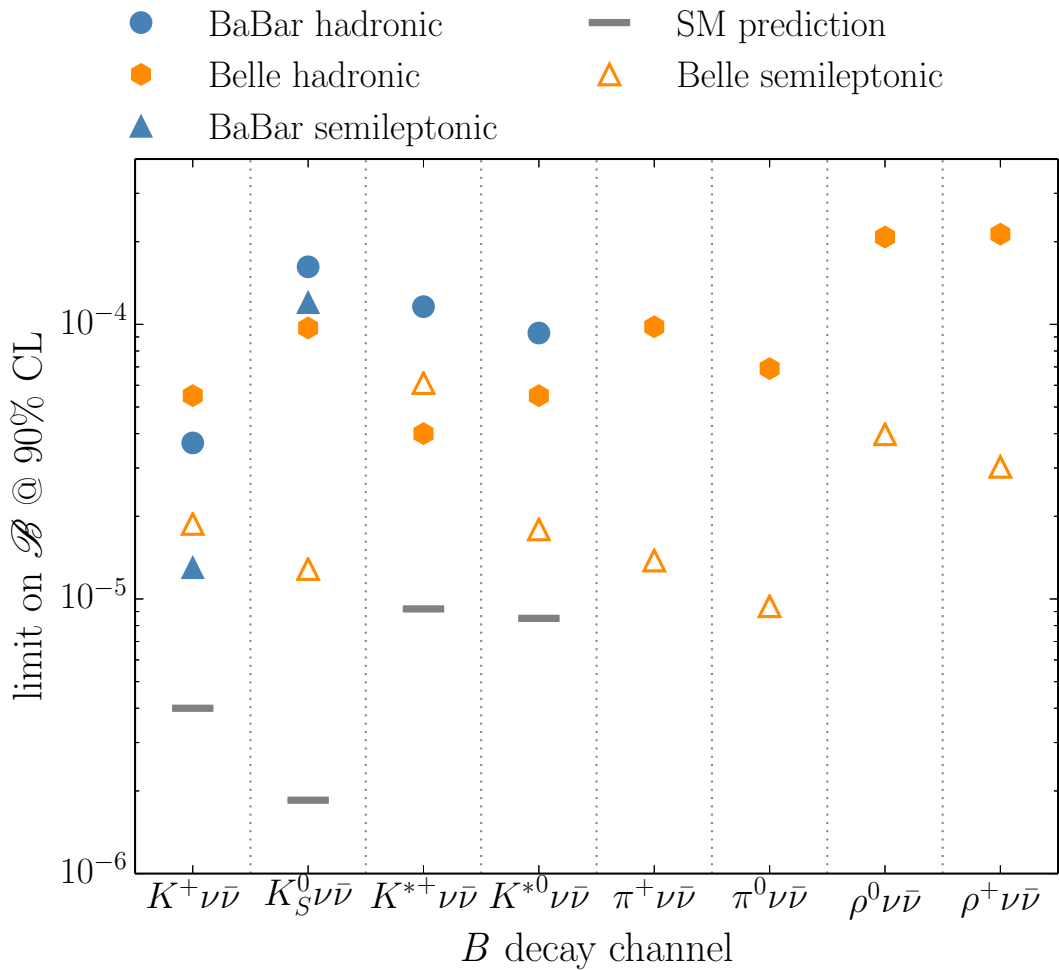


- Simultaneous analysis of $B \rightarrow s, d\nu\bar{\nu}$ transition in several modes
- Presence of LFV may affect these modes
- Relative background fractions are fixed to MC expectations
- No significant signal yield:

Channel	Expected limit	Observed limit
$K^+ \nu\bar{\nu}$	0.8×10^{-5}	1.9×10^{-5}
$K_S^0 \nu\bar{\nu}$	1.2×10^{-5}	1.3×10^{-5}
$K^{*+} \nu\bar{\nu}$	2.4×10^{-5}	6.1×10^{-5}
$K^{*0} \nu\bar{\nu}$	2.4×10^{-5}	1.8×10^{-5}
$\pi^+ \nu\bar{\nu}$	1.3×10^{-5}	1.4×10^{-5}
$\pi^0 \nu\bar{\nu}$	1.0×10^{-5}	0.9×10^{-5}
$\rho^+ \nu\bar{\nu}$	2.5×10^{-5}	3.0×10^{-5}
$\rho^0 \nu\bar{\nu}$	2.2×10^{-5}	4.0×10^{-5}

PRD 96, 091101 (2017)

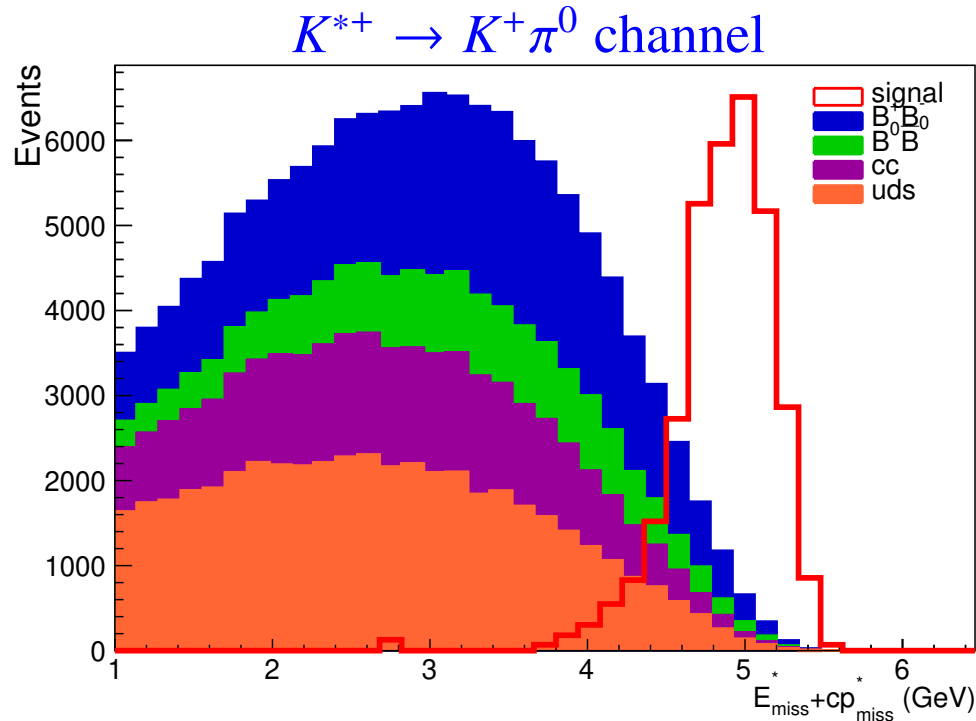
B → hνν̄ limits from Belle



- Best upper limits at the time
- Golden channel for Belle-II

PRD 96, 091101 (2017)

Perspectives for $B \rightarrow K^* \nu \bar{\nu}$ at Belle II



- Study based on hadronic tag, using FEI.
- Good discrimination vs background using $E_{\text{miss}} + p_{\text{miss}}$ variable with low correlation to $m_{\nu \bar{\nu}}$
- Expected observation with 4 ab^{-1} , 10% accuracy with 50 ab^{-1} .
- Measurement of K^* longitudinal polarisation fraction to 0.08 (SM accuracy 0.03).

arXiv:1808.10567

Perspectives for $B \rightarrow K^* \tau \tau$

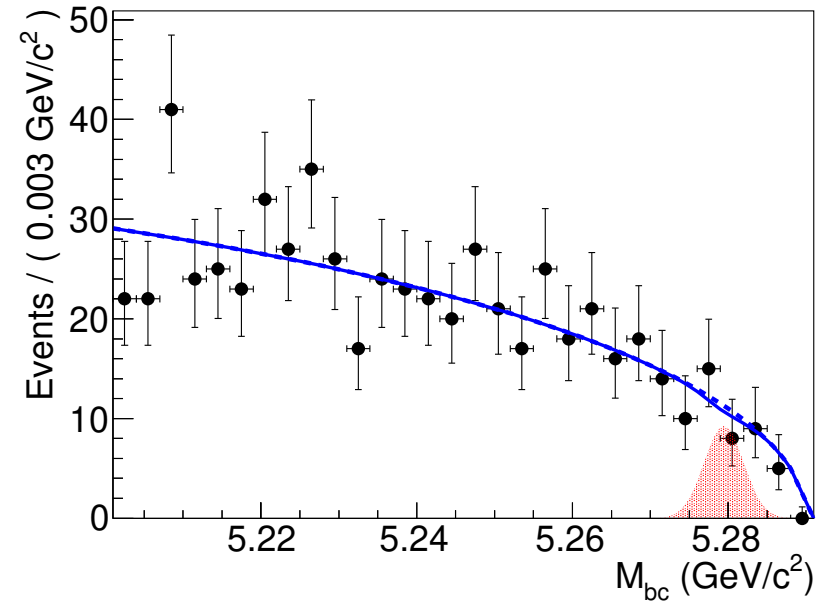
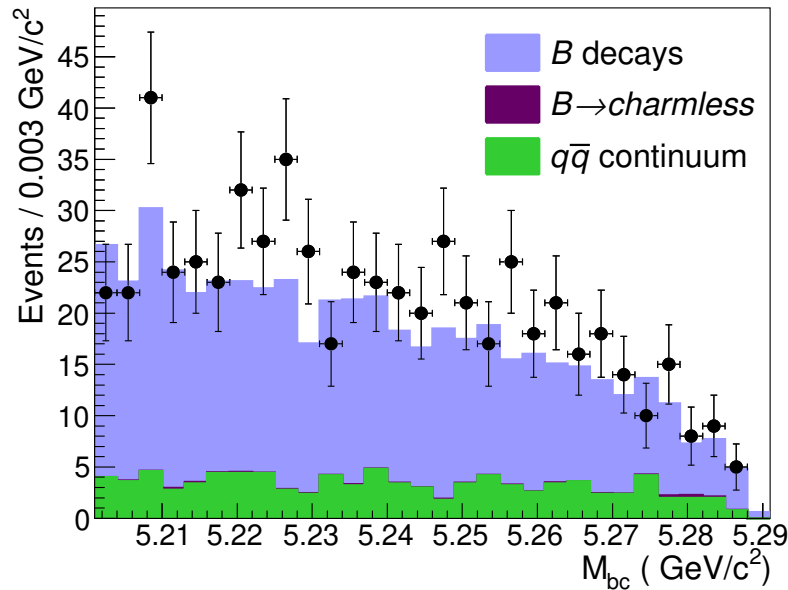
Observables	Belle II 5 ab^{-1}	Belle II 50 ab^{-1}
$\text{Br}(B^+ \rightarrow K^+ \tau^+ \tau^-) \cdot 10^5$	< 6.5	< 2.0
$\text{Br}(B^0 \rightarrow \tau^+ \tau^-) \cdot 10^5$	< 30	< 9.6
$\text{Br}(B_s^0 \rightarrow \tau^+ \tau^-) \cdot 10^4$	< 8.1	–
$\text{Br}(B^+ \rightarrow K^+ \tau^\pm e^\mp) \cdot 10^6$	–	< 2.1
$\text{Br}(B^+ \rightarrow K^+ \tau^\pm \mu^\mp) \cdot 10^6$	–	< 3.3
$\text{Br}(B^0 \rightarrow \tau^\pm e^\mp) \cdot 10^5$	–	< 1.6
$\text{Br}(B^0 \rightarrow \tau^\pm \mu^\mp) \cdot 10^5$	–	< 1.3

- Standard Model $B \rightarrow K \tau \tau$ is difficult at Belle II even with full luminosity.
- Lepton flavour violating processes, such a $B \rightarrow K \tau \mu$, are easier to get to better limits.

→ perhaps some room for CepC/FCCee to do flavour physics.

arXiv:1808.10567

Belle search for $B \rightarrow K^{*0} \mu e$



- Selection on beam-constrained mass M_{bc} and the energy difference $\Delta E = E_B - E_{\text{beam}}$, continuum suppression using NN (kinematics, flavour tagging).
- Main remaining background from (a) both B decay semileptonically, (b) $B \rightarrow \bar{D}^{(*)} X \ell^+ \nu$, $\bar{D}^* \rightarrow X \ell^- \bar{\nu}$, (c) lepton mis-ID. Suppressed by NN using vertex, ECL information.
- $B(B^0 \rightarrow K^{*0} \mu^+ e^-) < 1.2 \times 10^{-7}$, $B(B^0 \rightarrow K^{*0} \mu^- e^+) < 1.6 \times 10^{-7}$,
 $B(B^0 \rightarrow K^{*0} \mu^\pm e^\mp) < 1.8 \times 10^{-7}$

PRD 98, 071101 (2018)

Summary

- Anomalies in leptonic B decays are reduced with the recent data, however remain significant.
- Belle-II is an excellent detector for lepton universality studies, especially for the channels involving **missing energy**, but also for ee vs $\mu\mu$ channels, due to similar reconstruction efficiency.
- Most of the channels at Belle-II are statistics limited, however for $R_{D^{(*)}}$ better modeling of $B \rightarrow D^{**} \ell \nu$ and hadronic B decays is needed.
- ML-based full event interpretation tagging method improves B -meson tagging compared to Belle-I. Further improvements are possible, with better modelling of B decays used for the training.

The Belle II Physics Book: [arXiv:1808.10567](https://arxiv.org/abs/1808.10567)

B-factories vs *pp*

- Pros:
 - Nearly 4π reconstruction (however, not so good for K_L)
 - Hadronic/semileptonic tagging, full event interpretation (FEI), reliable reconstruction of missing energy
 - Excellent reconstruction of both muons and electrons.
- Cons:
 - Lower rates
 - Lower energies, larger multiple scattering effects, reduced tracking efficiency.
 - Stronger dependence of final state topologies on Q^2

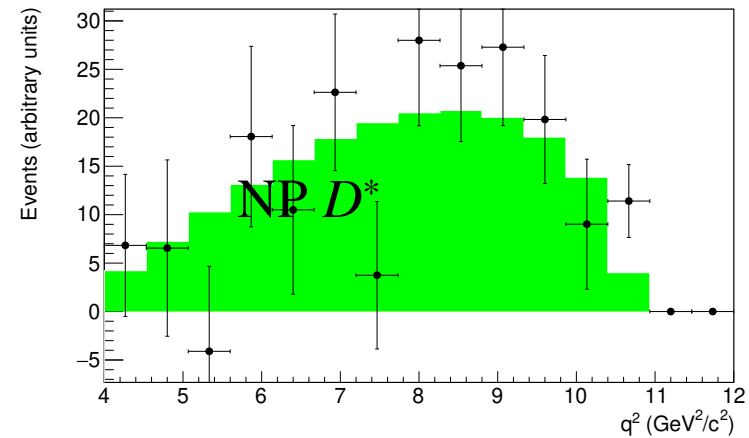
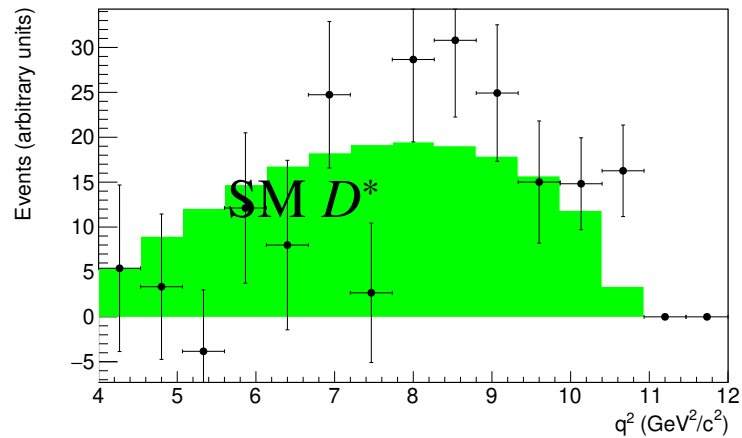
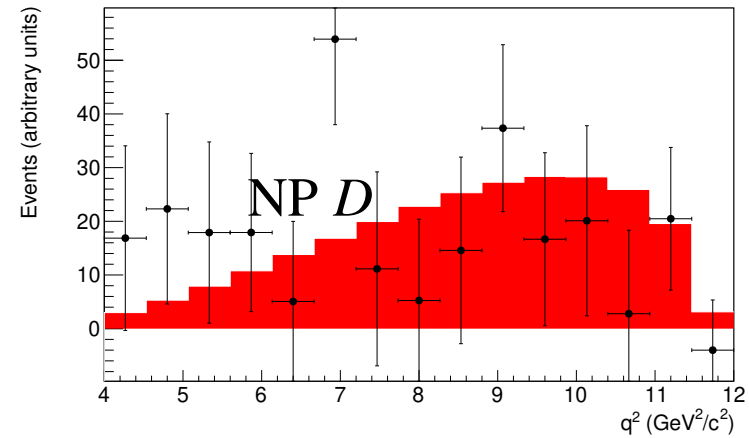
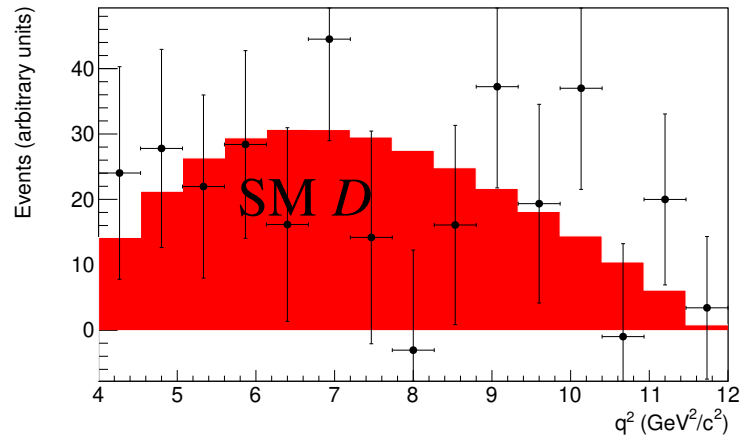
$R_{D^{(*)}}$ measurements: systematic uncertainties

Source	Belle (Had, ℓ^-) R_D	Belle (Had, ℓ^-) R_{D^*}	Belle (SL, ℓ^-) R_{D^*}	Belle (Had, h^-) R_{D^*}
MC statistics	4.4%	3.6%	2.5%	+4.0% -2.9%
$B \rightarrow D^{**} \ell \nu_\ell$	4.4%	3.4%	+1.0% -1.7%	2.3%
Hadronic B	0.1%	0.1%	1.1%	+7.3% -6.5%
Other sources	3.4%	1.6%	+1.8% -1.4%	5.0%
Total	7.1%	5.2%	+3.4% -3.5%	+10.0% -9.0%

- Leading systematic sources:
 - $B \rightarrow D^{**} \ell \nu$ for analyses with leptonic τ decays;
 - Hadronic B decays for $\tau \rightarrow h \nu_\tau$ analysis
- Other significant sources are form factors of $B \rightarrow D^{(*)} \ell / \tau \nu$ decays, background from $B \rightarrow X_c D^{(*)}$ and cross-feed from $B \rightarrow D^* \ell / \tau \nu$ to $B \rightarrow \ell / \tau \nu$.

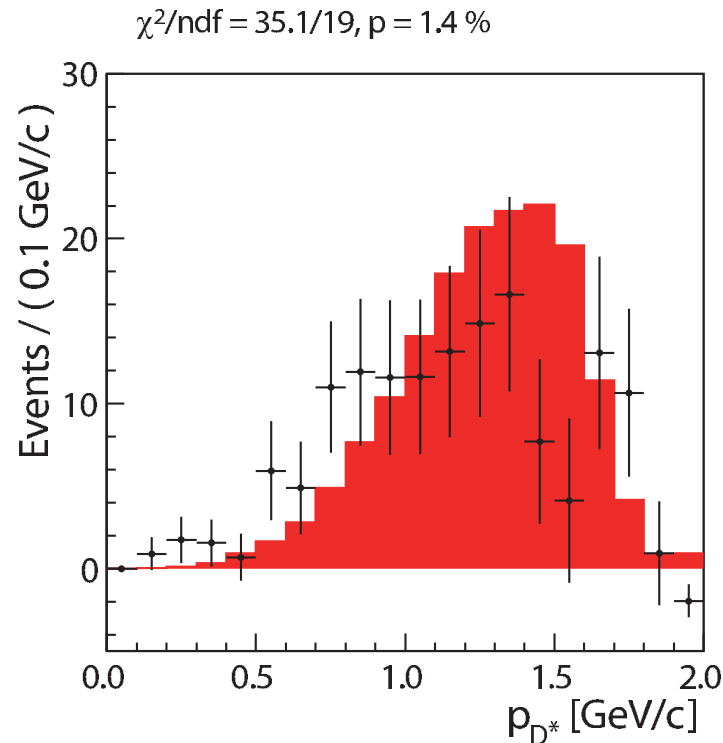
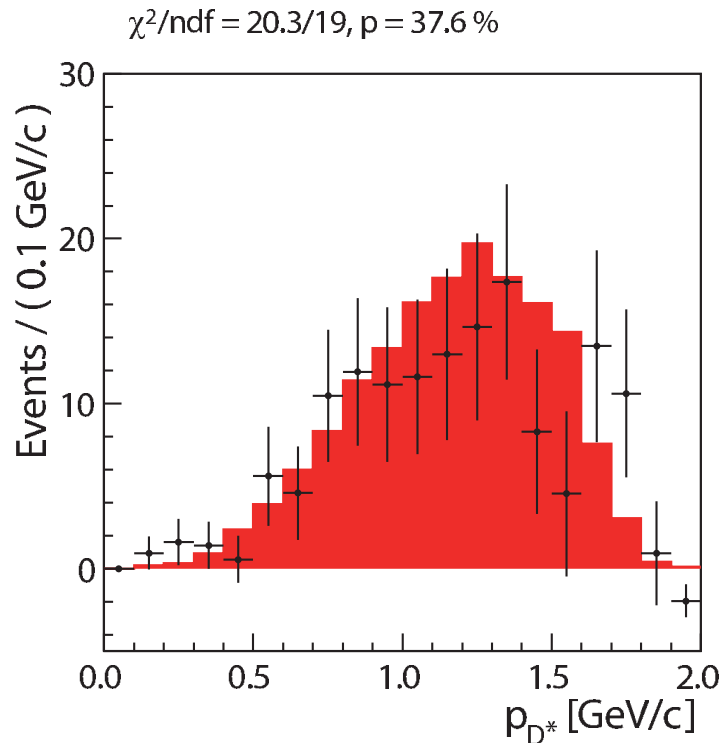
→ dedicated measurements of $B \rightarrow D^{**} \ell \nu$; direct constrain on $B \rightarrow D^{**} \tau \nu_\tau$.

Differential $R_{D^{(*)}}$ measurements (hadronic tag)



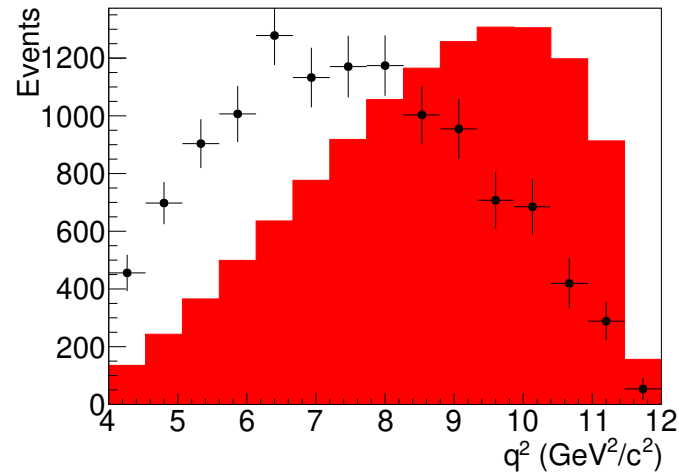
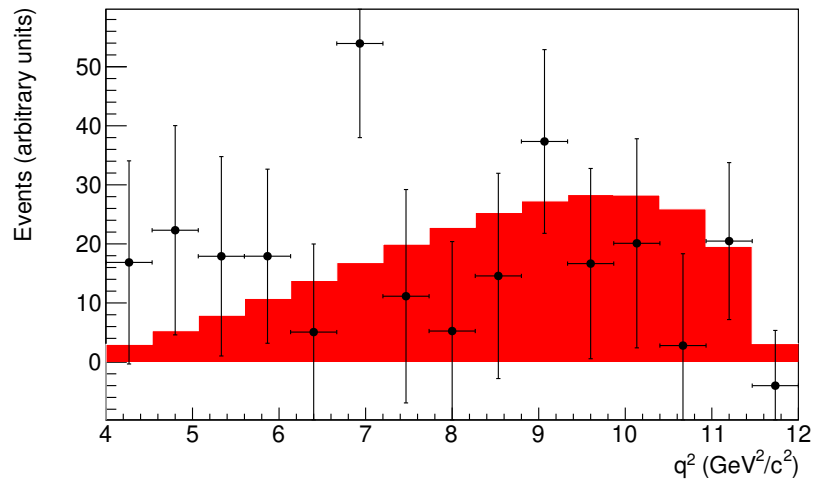
- Compare $q^2 = (P_B - p_{D^{(*)}})^2$ distributions vs SM and NP scenarios.
- Significant discriminating power in the q^2 distribution, different for $B \rightarrow D^* \tau \nu$ vs $B \rightarrow D \tau \nu$.

Differential $R_{D^{(*)}}$ measurements (semileptonic tag)



- For semileptonic tag, q^2 can not be determined directly, use P_{D^*} instead.
- Some additional discrimination between SM and R_2 -type leptoquark model.

Differential measurements: Belle-II projections



$$M_{\text{NP}} \sim (2\sqrt{2}G_F V_{cb} C_X)^{-1/2} \sim 5 - 10 \text{ TeV}$$

- Hadron-tag based analysis for published Belle vs Belle II estimated using 50 ab^{-1} .
- Strong discriminating power vs 2HDM of type II model.
- Discrimination vs other models with scalar or tensor mediators.

[arXiv:1808.10567](https://arxiv.org/abs/1808.10567)