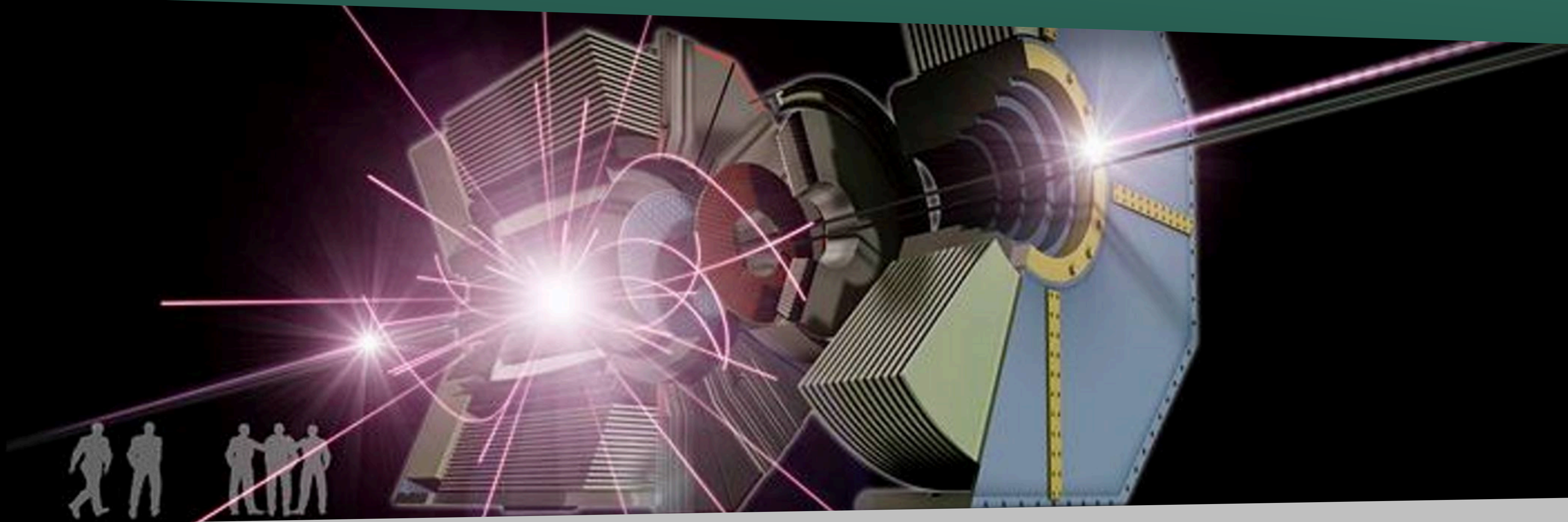


# B-Decays with Missing Energy at Belle II



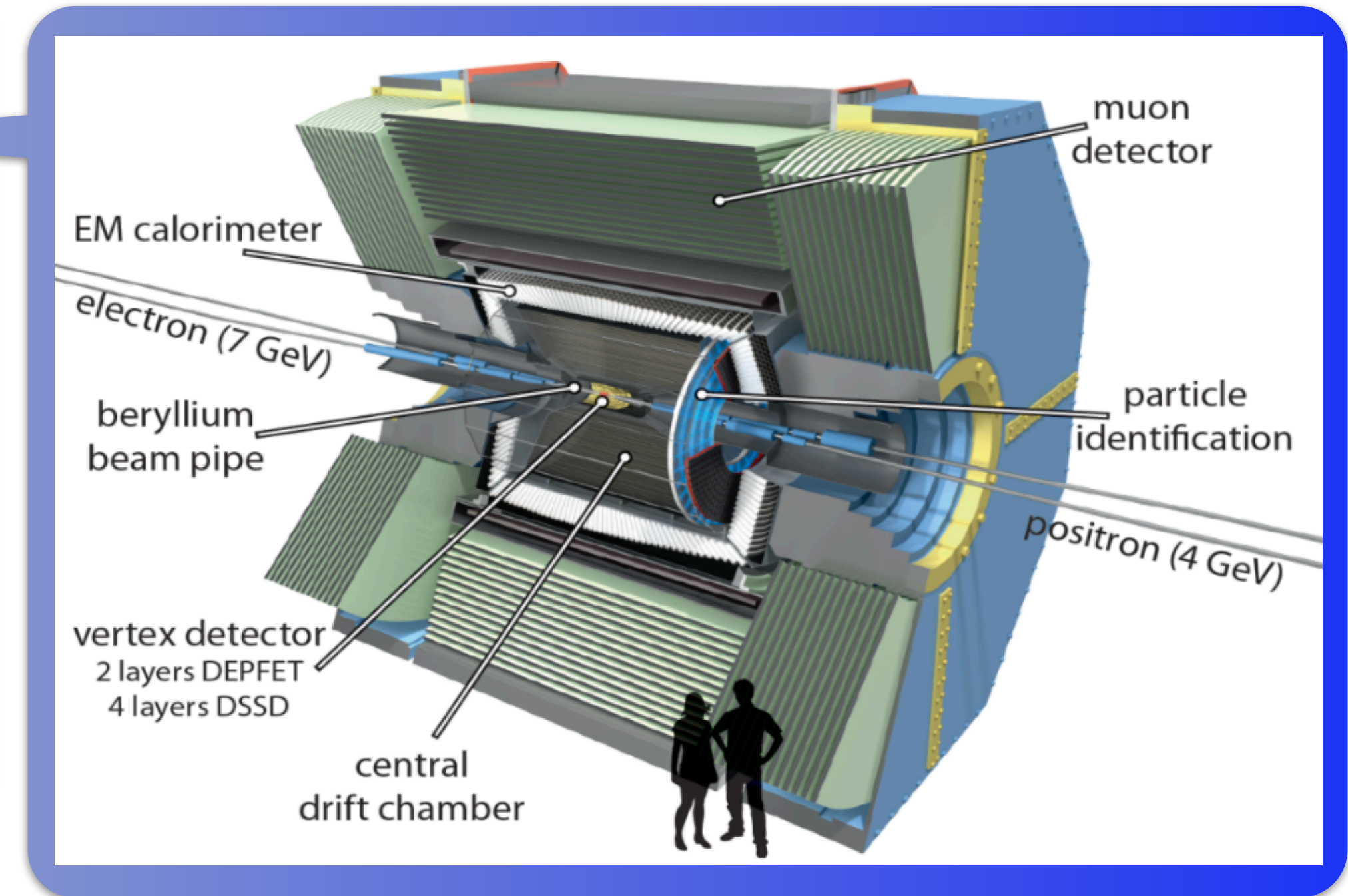
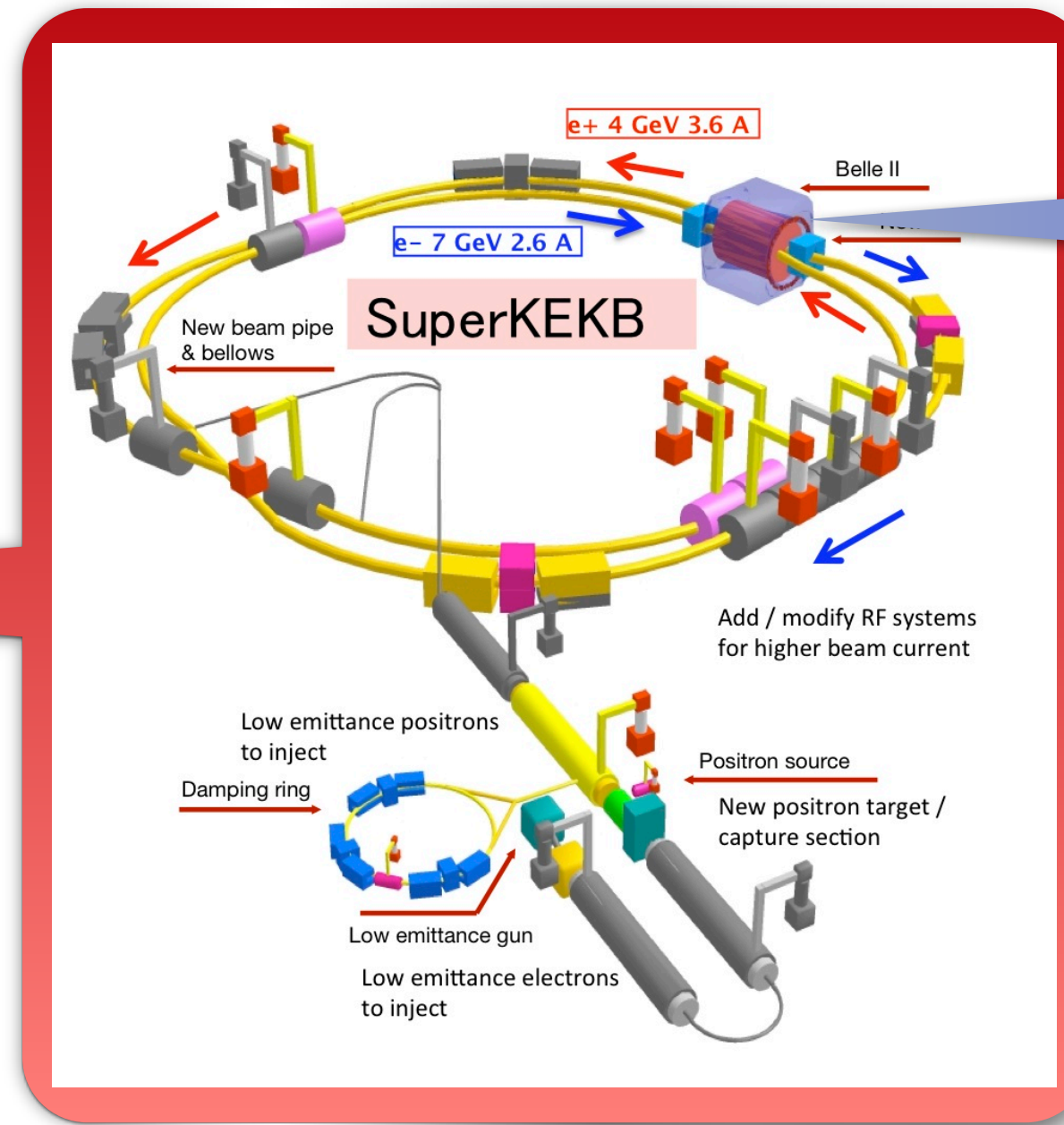
**Lu Cao**

for the Belle II Collaboration

31 Jan. 2019 @ MITP, Mainz



# Belle II Experiment



- 40 times higher instantaneous luminosity from KEKB to SuperKEKB:  $8 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$
- Detector upgraded for intenser particle multiplicity and tracking capacity
- Physics data taking with full detector will start soon

# SuperKEKB/Belle II Schedule

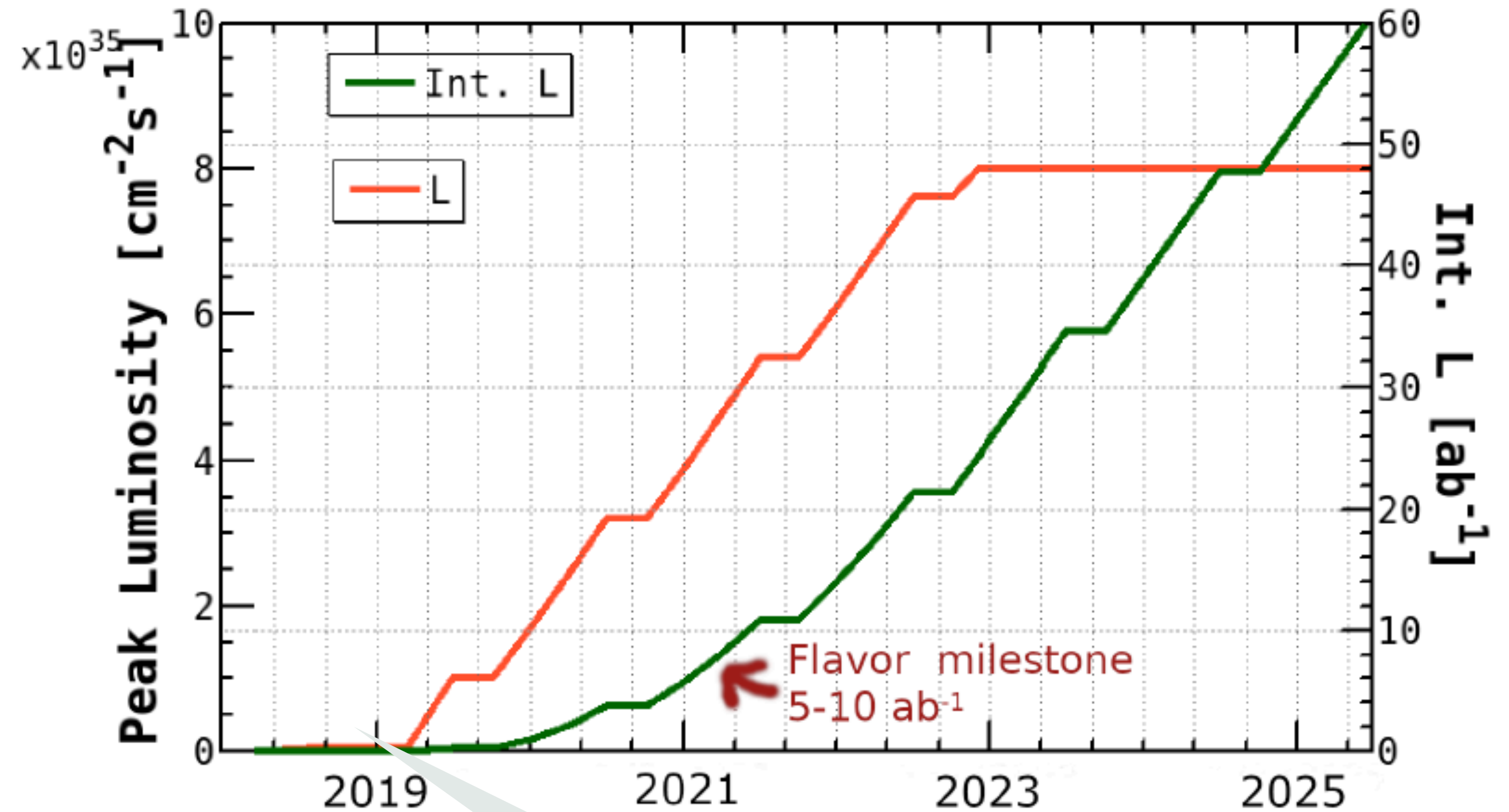
**Phase 1: Bean operation run (2016)** ✓

**Phase 2: Commissioning run (2018)** ✓

- With partial vertex detector
- Collected int.  $L = 0.5\text{fb}^{-1}$

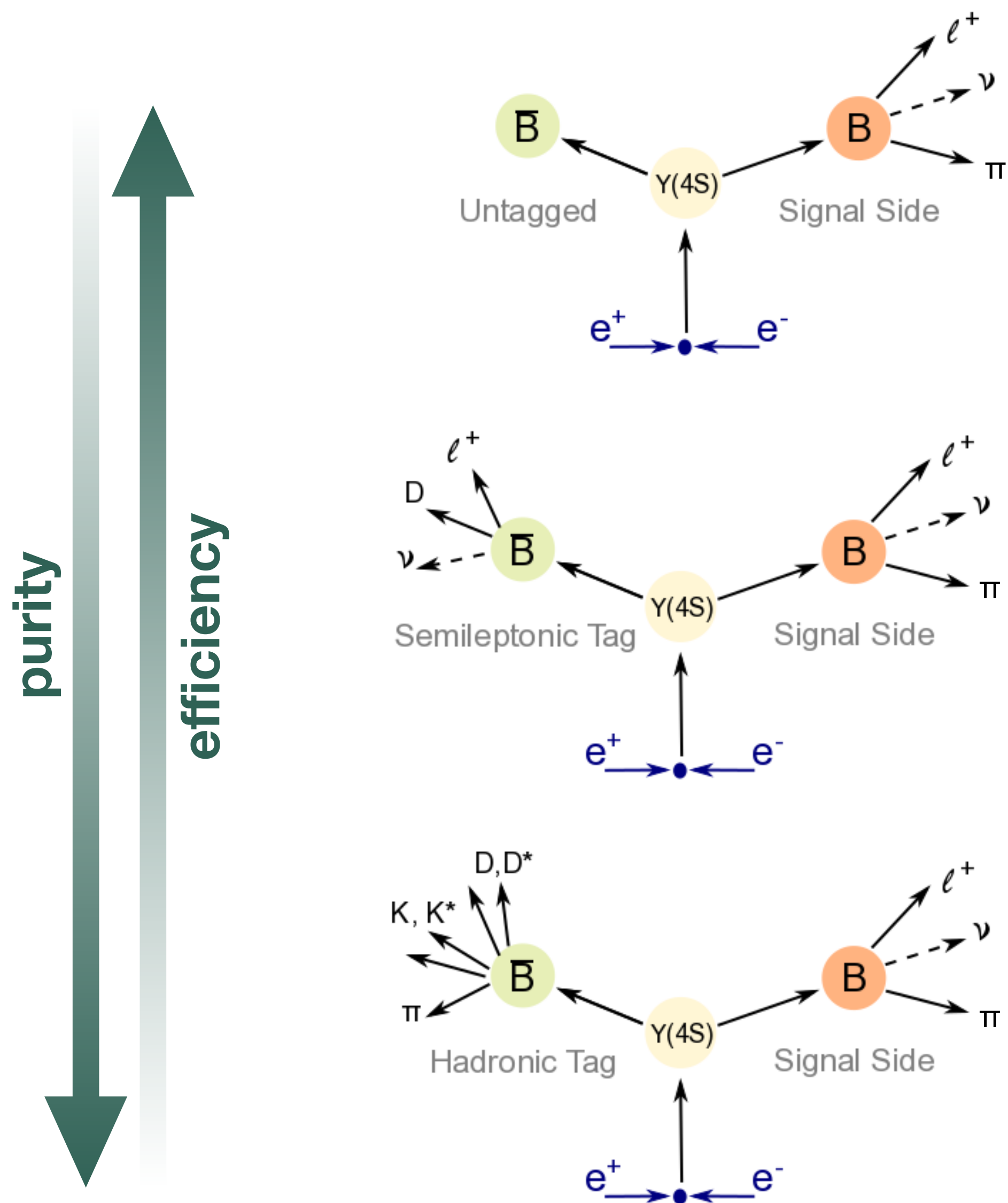
**Phase 3: Physics run** ⇐

- Will start in **March 2019**
- 9 months/year operation
- Will reach “**flavor milestone**” in two years
- will record integrated luminosity  **$50\text{ab}^{-1}$  by 2025**



**Physics data is coming!!**

# Event Reconstruction with Tagging Techniques



- **Untagged**

- Loose constraints on signal
- Very large statistics, but also very large background
- Efficiency  $\epsilon \approx \mathcal{O}(100\%)$

- **Semileptonic tag**

- Mid-range reconstruction efficiency  $\epsilon \approx \mathcal{O}(1\%)$
- Due to multiple neutrinos, less information about  $B_{\text{tag}}$

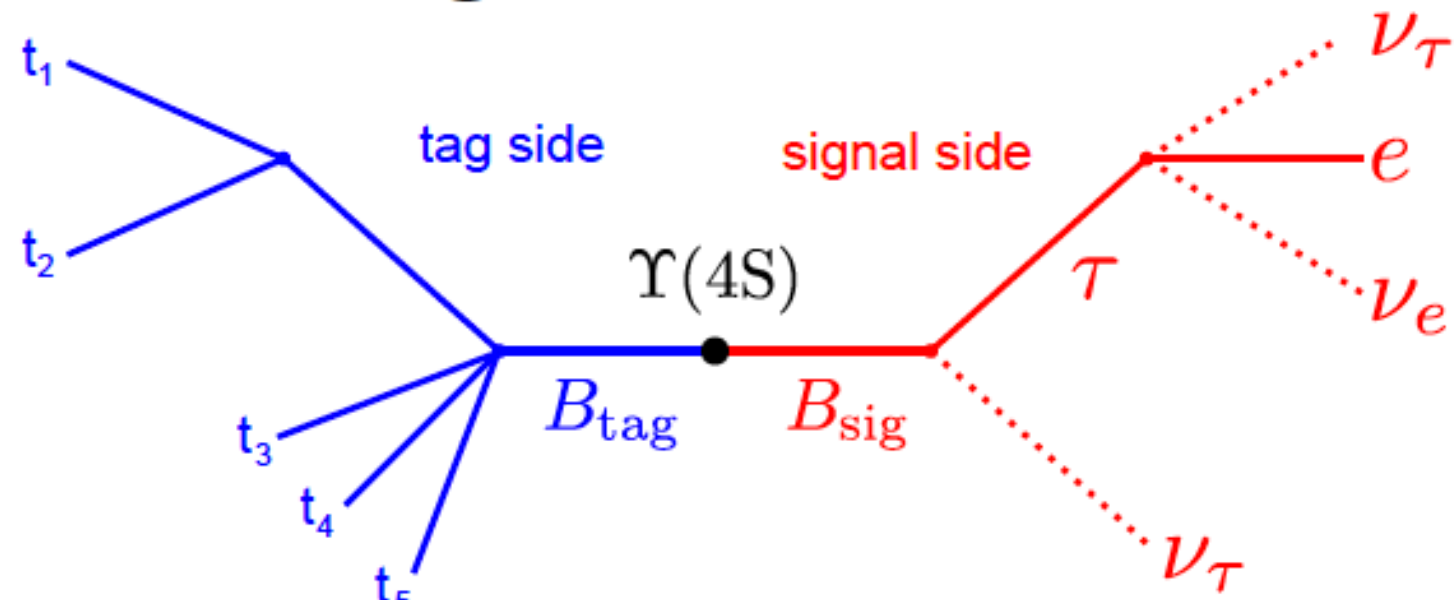
- **Hadronic tag**

- Cleaner sample
- Knowledge of  $p(B_{\text{sig}})$
- Low tag-side efficiency  $\epsilon \approx \mathcal{O}(0.1\%)$

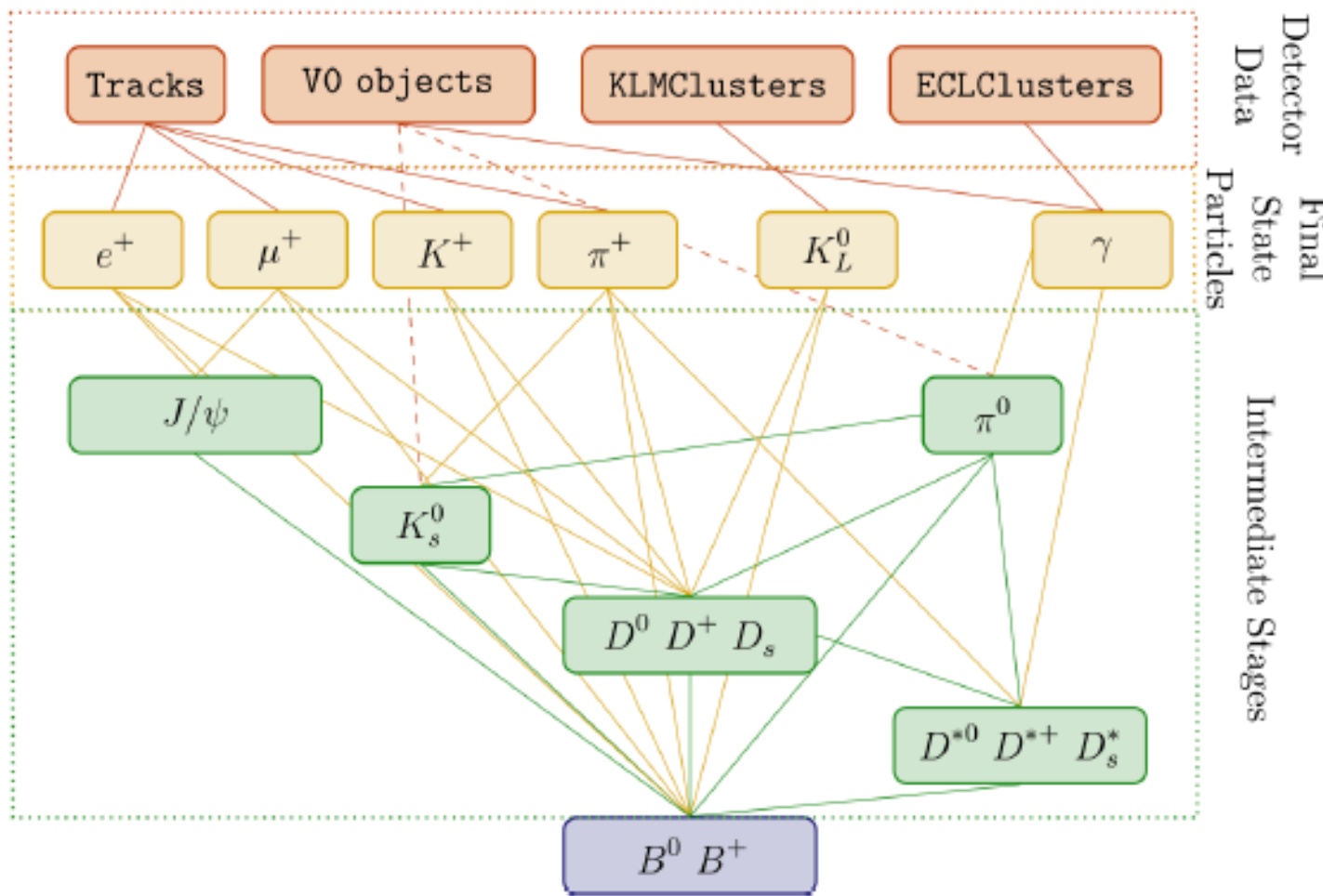
# Improved Tagging Algorithms

Courtesy of W. Sutcliffe

## New Full Event Interpretation (FEI) algorithm for tag-side reconstruction



>5000 B decays modes

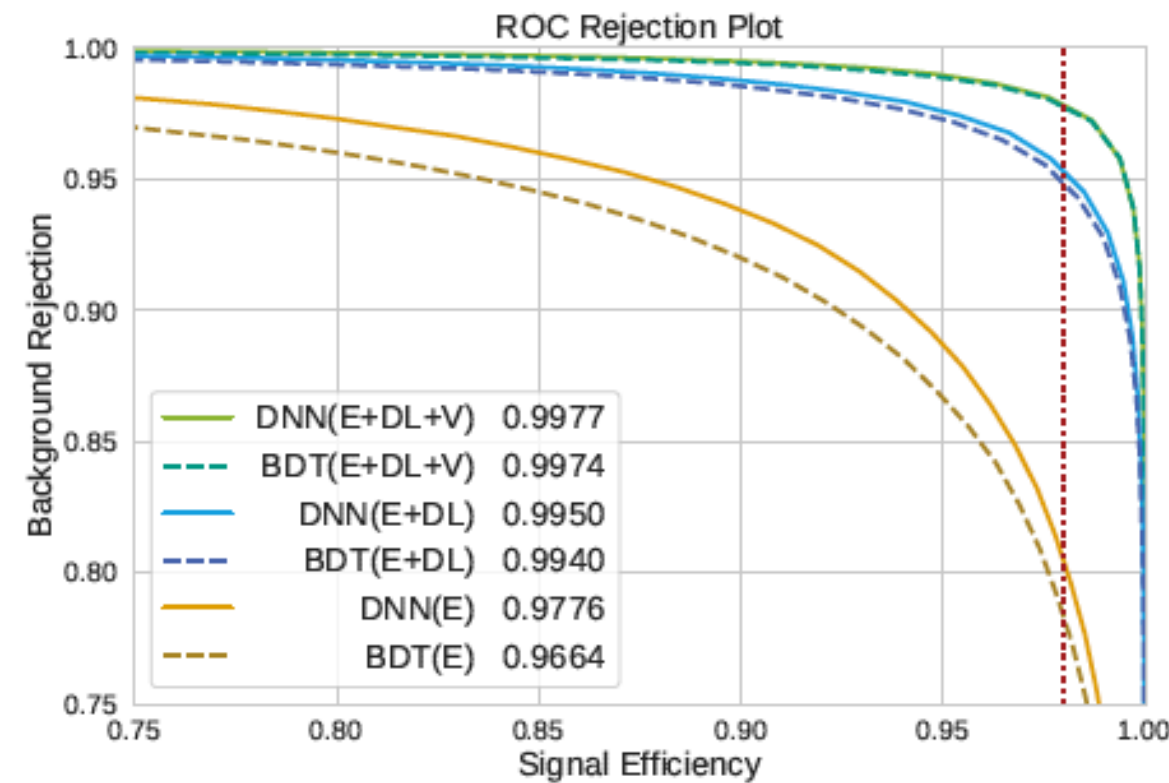


Tagging  $\epsilon$  on MC

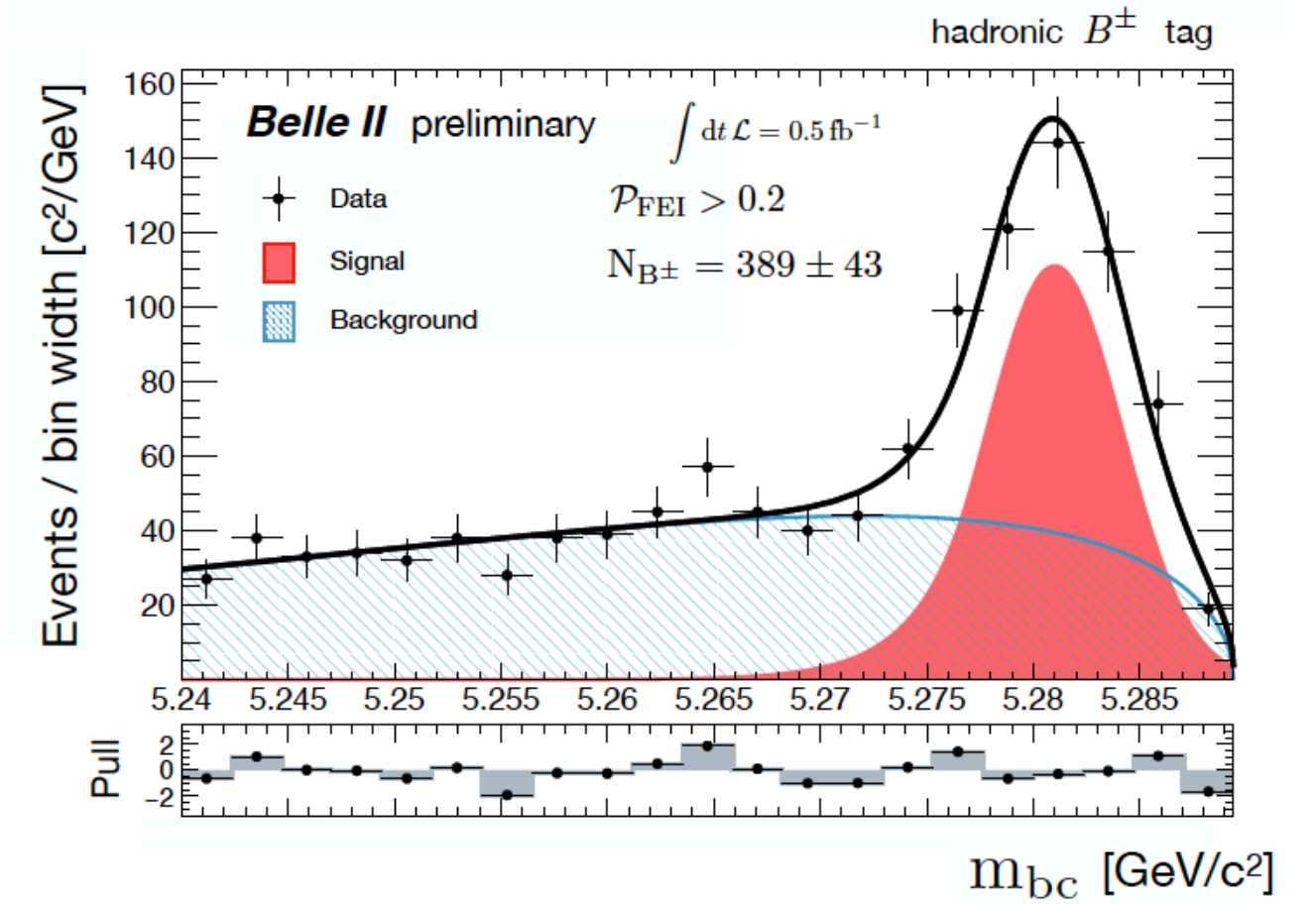
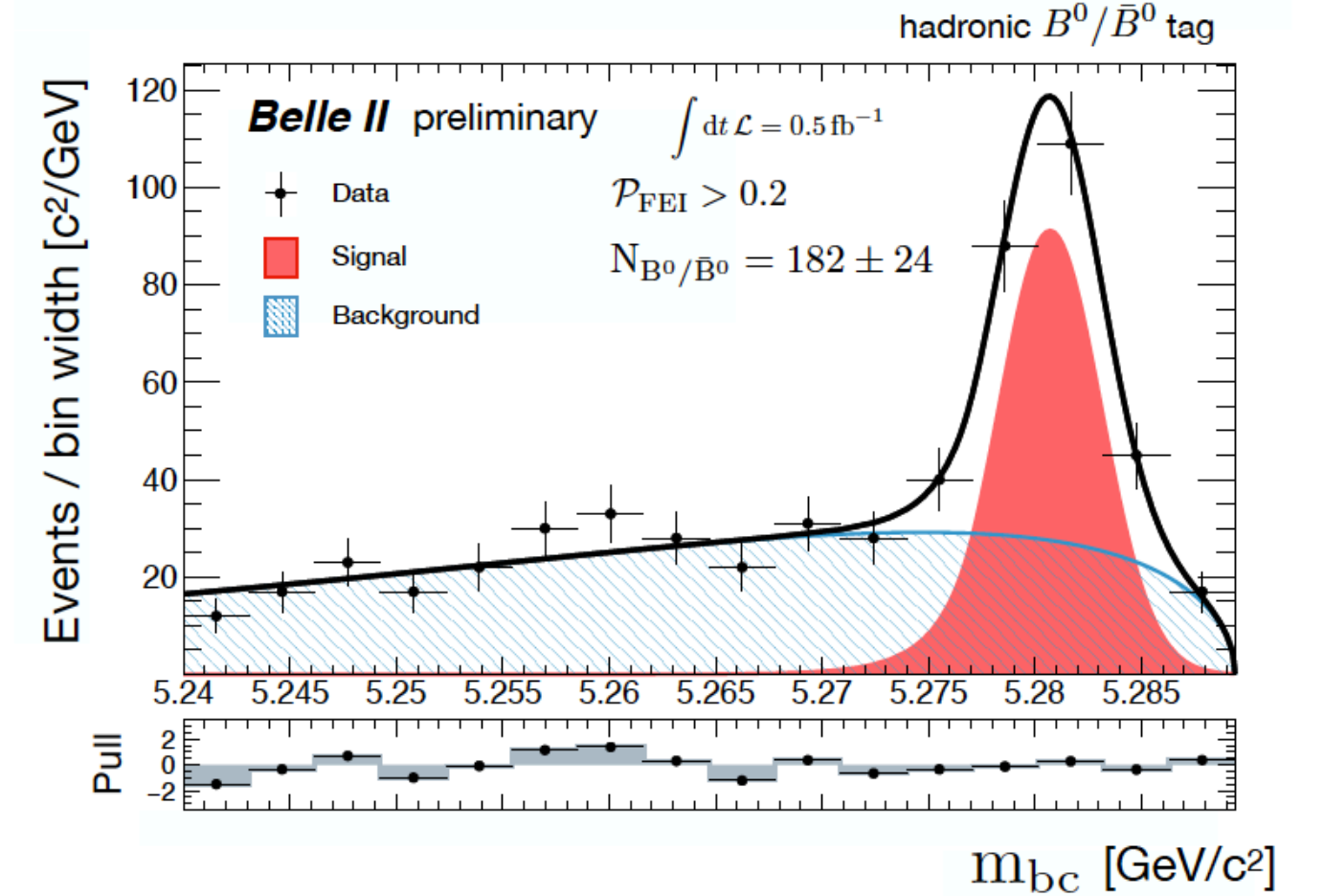
Tag	FR <sup>1</sup>	FEI Belle	FEI Belle II
Hadronic $B^+$	0.28%	0.76%	0.66%
SL $B^+$	0.67%	1.80%	1.45%
Hadronic $B^0$	0.18%	0.46%	0.38%
SL $B^0$	0.63%	2.04%	1.94%

<sup>1</sup>Belle Full Reconstruction algorithm.

## Deep NN based $e^+e^- \rightarrow q\bar{q}$ background suppression



## Phase 2 data

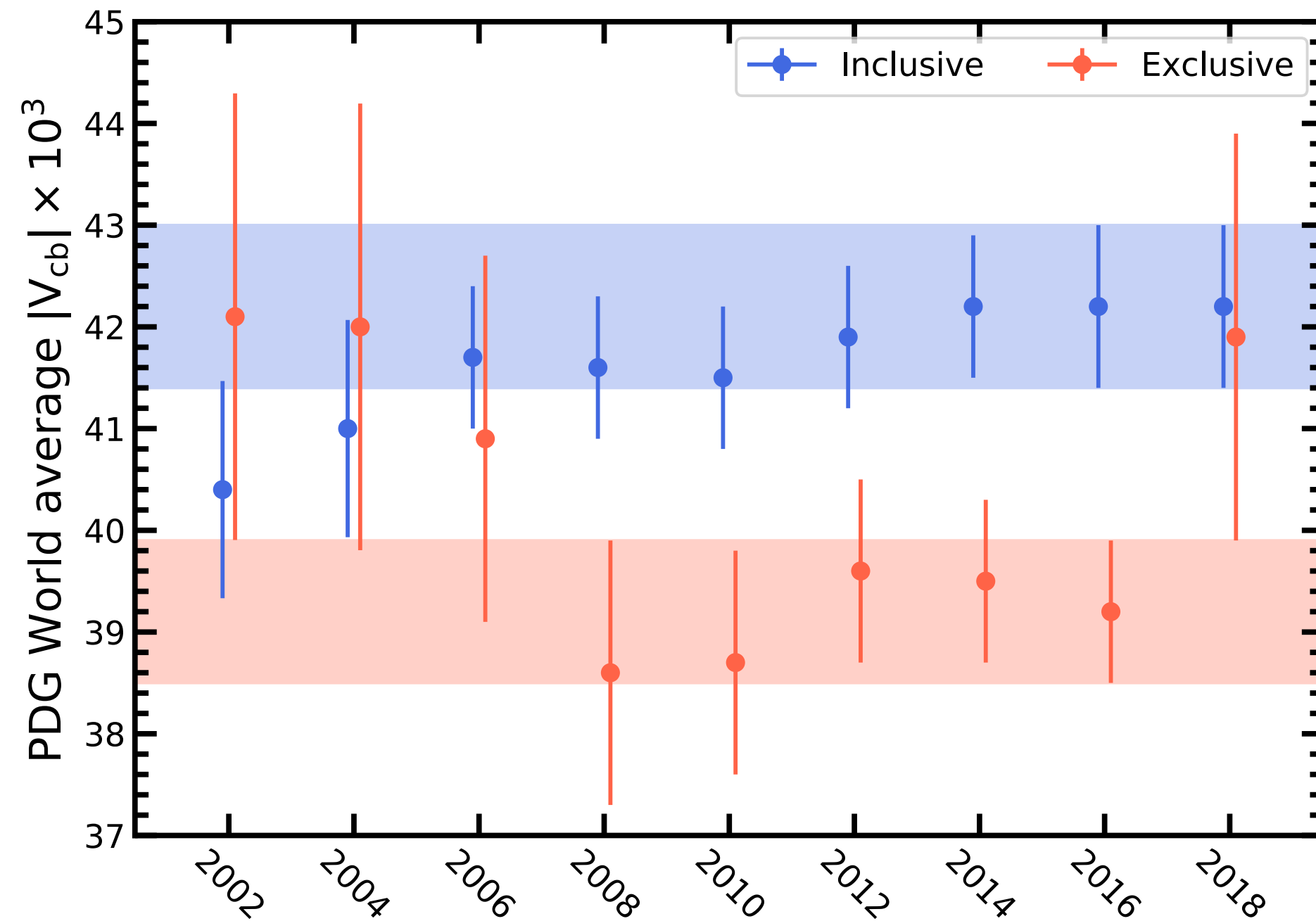


<sup>1</sup> T. Keck; <sup>2</sup> J. Gemmler; <sup>2</sup> D. Weyland

$$M_{bc} = \sqrt{(\sqrt{s}/2)^2 - \vec{p}_{B_{tag}}^2}$$

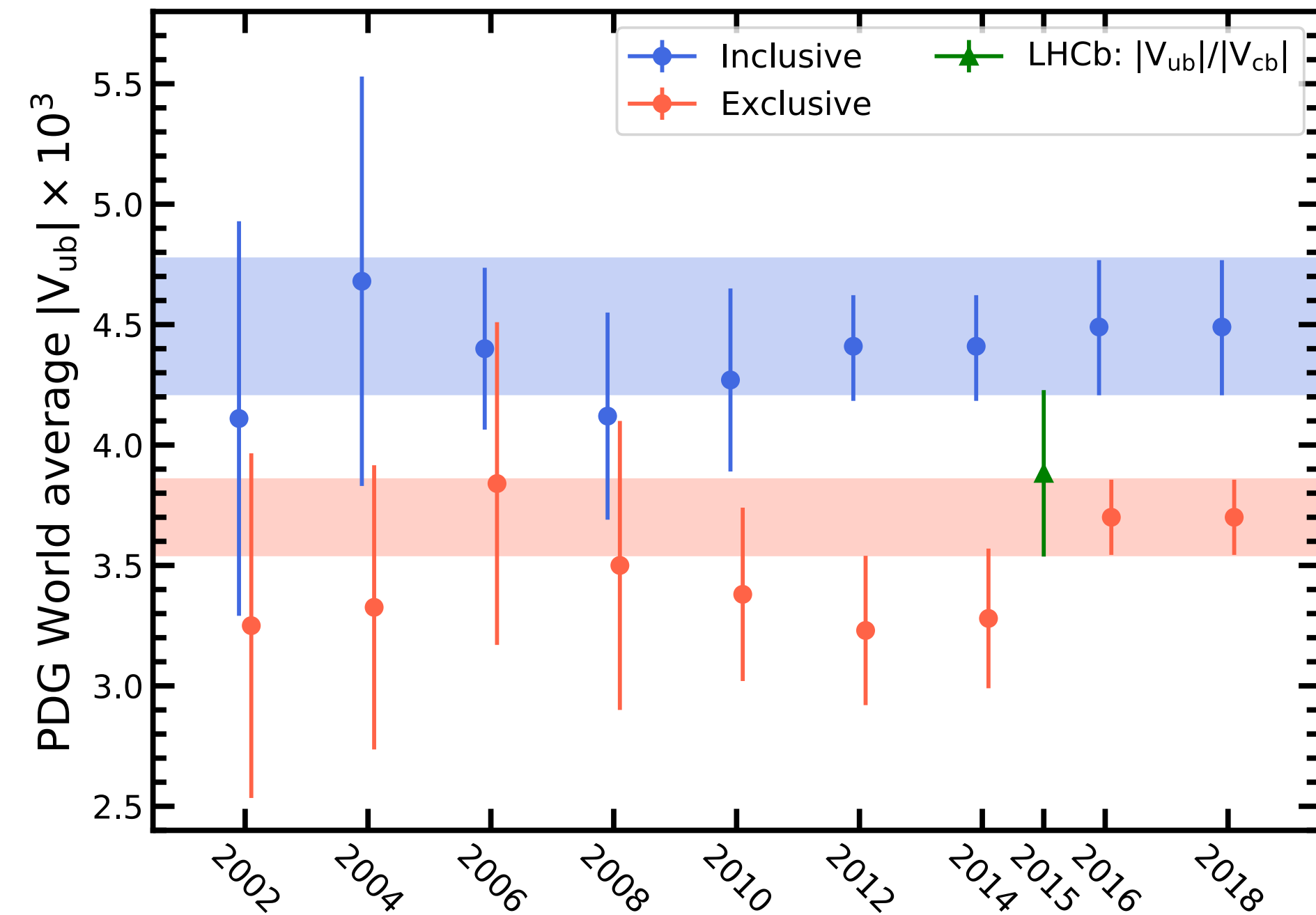
# Long-Standing Puzzle: Inclusive vs. Exclusive $|V_{cb}|$ & $|V_{ub}|$

$V_{cb}$



- $3\sigma$  deviation between excl. vs. incl.
- PDG2018 exclusive value based on only measured unfolded differential decay rates in  $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}_\ell$  from Belle using BGL parameterisation [1702.01521](#)
- More unfolded results needed

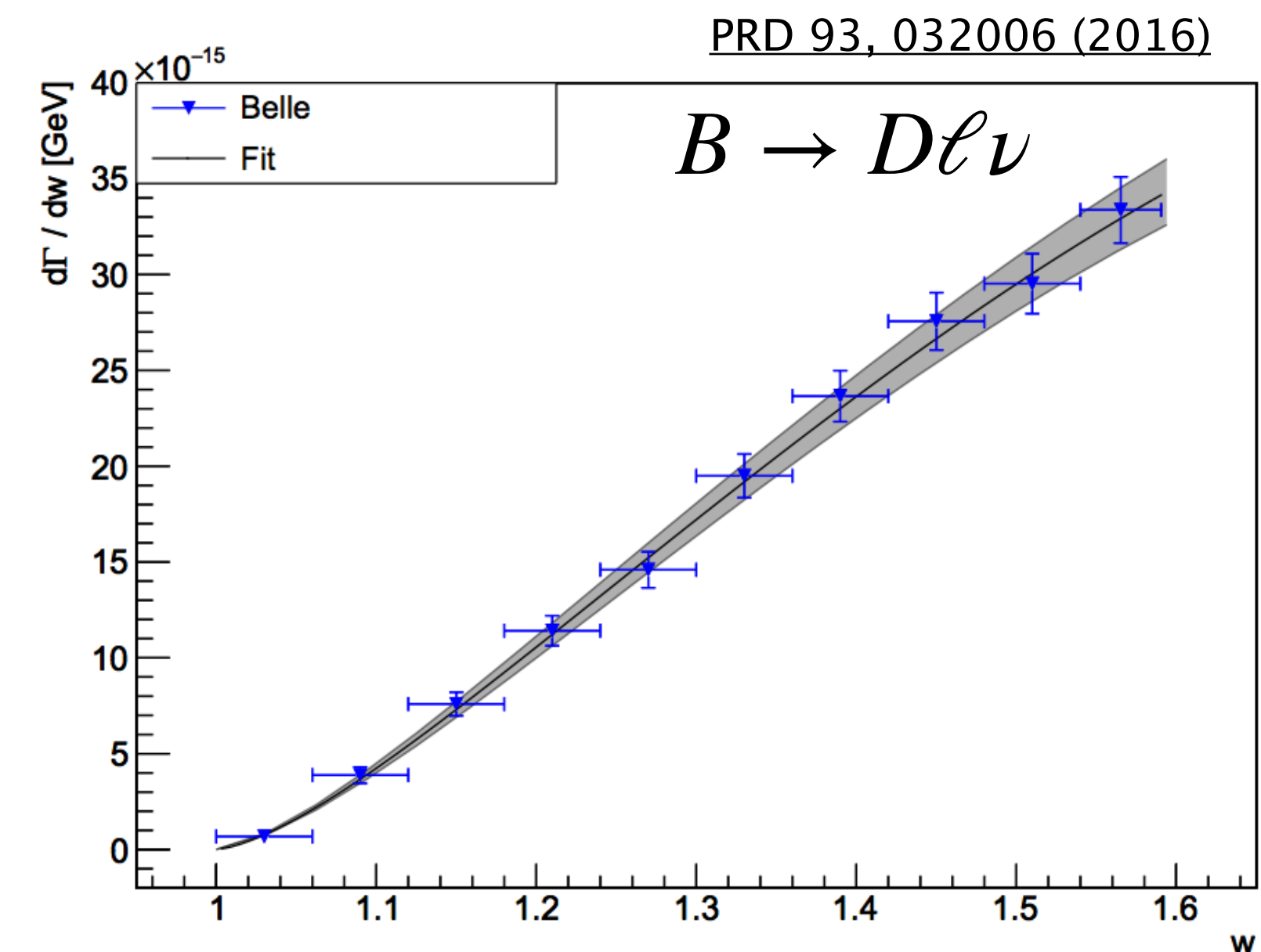
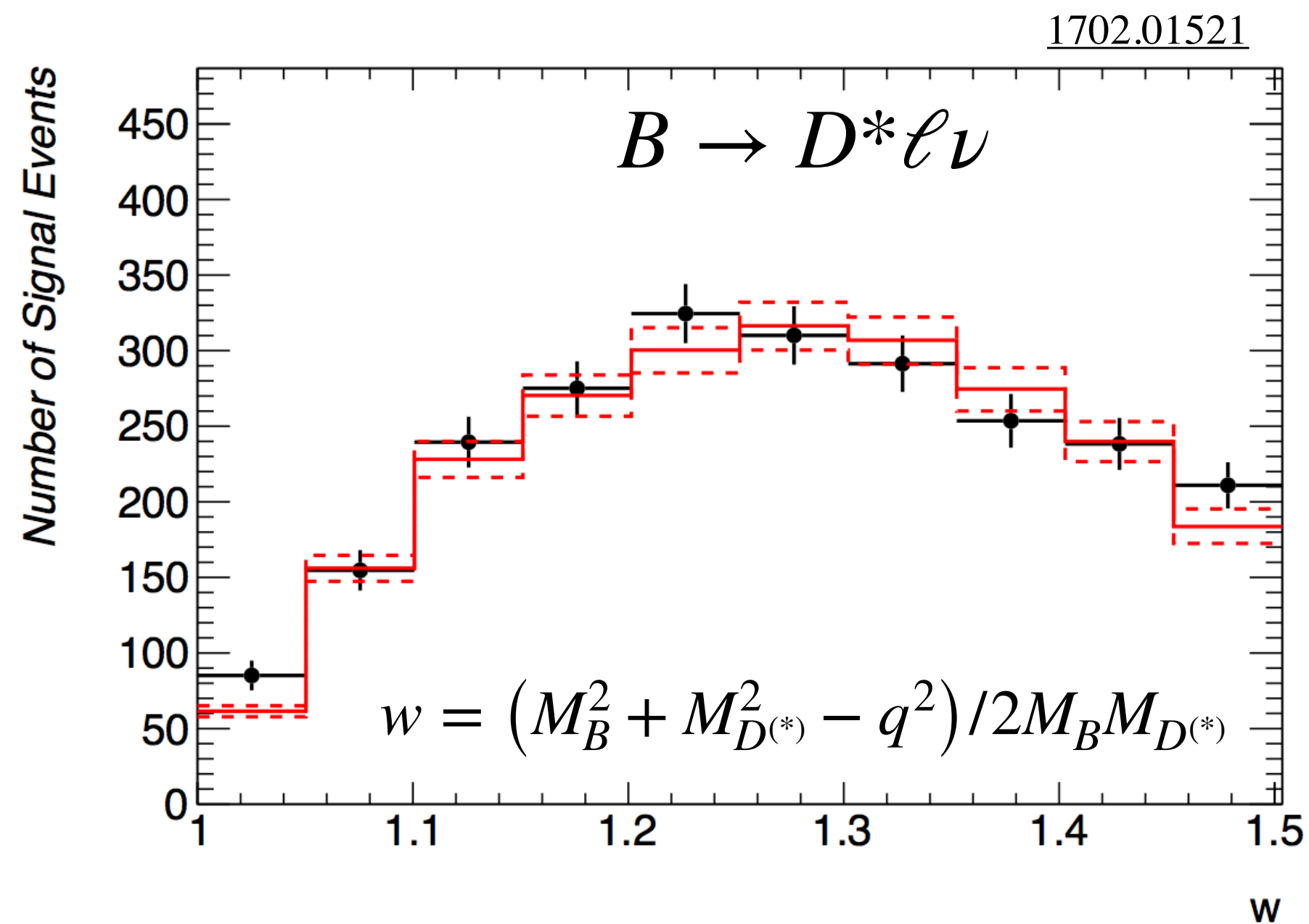
$V_{ub}$



- $3.5\sigma$  discrepancy between excl. vs. incl.
- LHCb provided ratio with baryonic b-decays ([NP 2015](#))
- Leptonic measurements not precise enough, favours inclusive results
- More precise leptonic measurements needed

# Exclusive $|V_{cb}|$ in $B \rightarrow D^{(*)}\ell\nu$

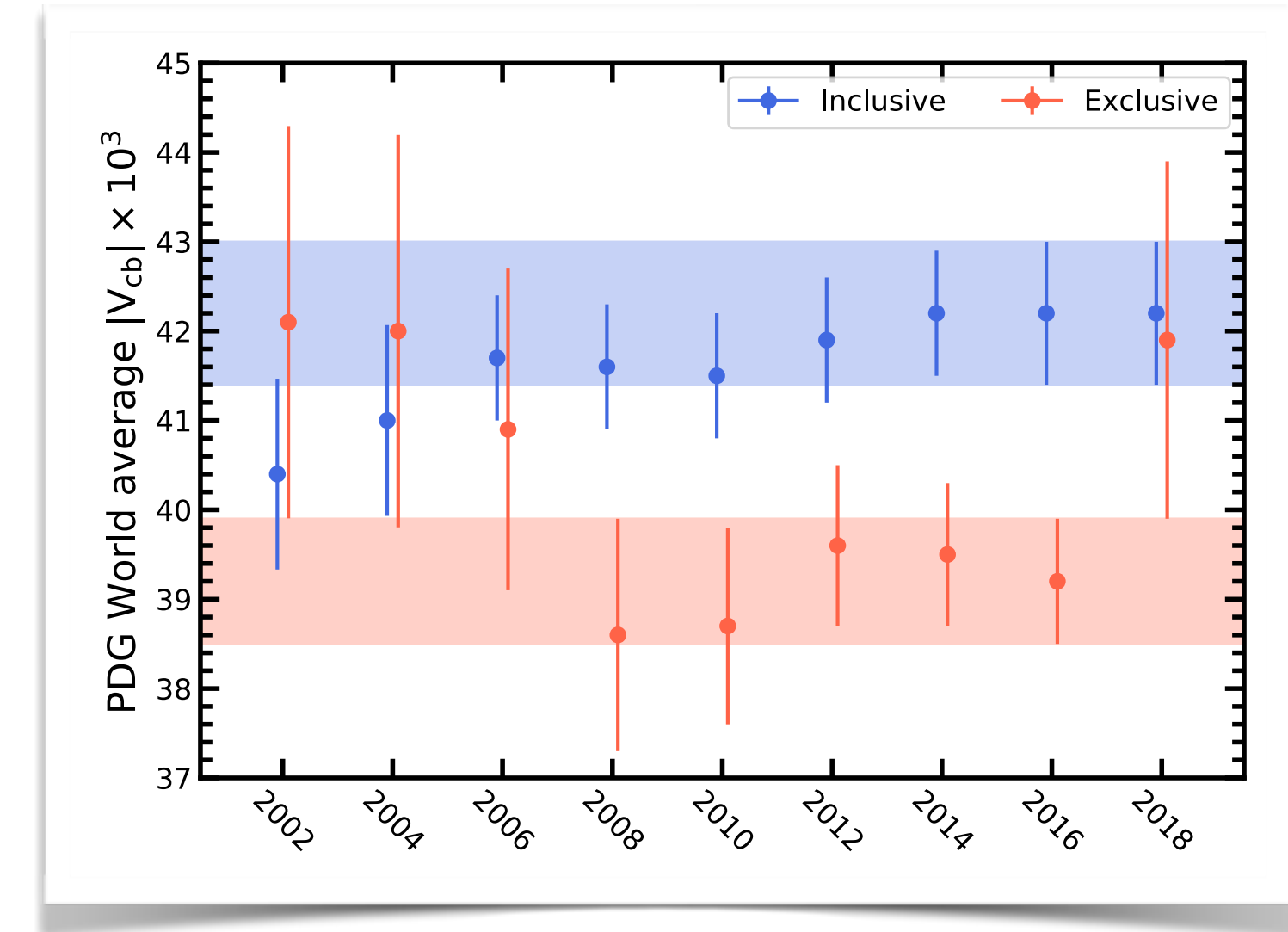
- Recent two measurements from Belle (both provide unfolded differential decay rate)
- Hadronic tagging allows missing mass constraint on signal side  $M_{\text{miss}}^2 = (p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^{(*)}} - p_{\ell})^2$
- Leading systematic uncertainty is from hadronic tag calibration (can be improved with FEI for Belle II)
- Extract  $|V_{cb}|$  requires **form factor** parametrisation and LQCD input as normalisation
- Bonus: separating electron-muon to test lepton flavor universality via  $R_{e/\mu}$



# Form Factor: CLN or BGL ?

Courtesy of F. Bernlochner

- Change from CLN to BGL lead to 10% discrepancy in  $|V_{cb}|$  determination
- Might resolve inclusive vs. exclusive puzzle
- Full kinematic dependence of  $B \rightarrow D^* \ell \nu$  f.f. from LQCD is underway



$D^*$  unfolded distributions analyzed by three groups

Includes additional measurement & beyond zero recoil lattice constraints

1703.06124, 1703.08170

BGL	$D^*$
$ V_{cb}  \times 10^3$	$41.9 \pm 1.9$

BGL: Phys. Rev. Lett. 74, 4603 (1995)

1703.05330

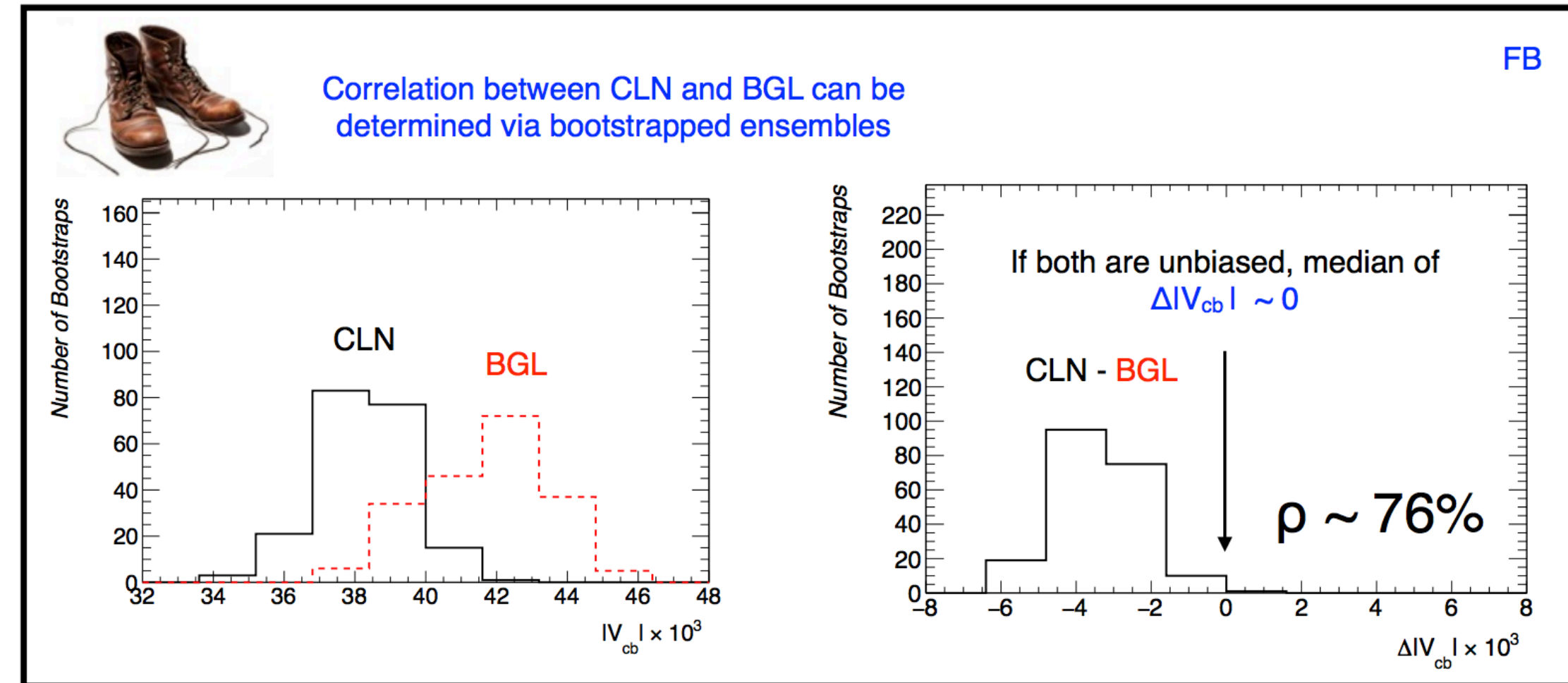
CLN'	$D + D^*$
$ V_{cb}  \times 10^3$	$39.3 \pm 1.0$

$$\bar{B} \rightarrow D^* \ell \bar{\nu}_\ell$$

CLN	$D^*$
$ V_{cb}  \times 10^3$	$38.2 \pm 1.5$

CLN: Phys. Lett. B380, 376 (1996)

From unfolded data, slightly higher than 'folded' result of previous slide



Similar results seen in [PRL 109, 071802\(2012\)](#) [PRD 92\(5\), 054510\(2015\)](#)  
[PRD 94, 094008\(2016\)](#) [PLB 769, 441\(2017\)](#)

CLN  $\longleftrightarrow$  BGL  
 $\sim 3\sigma$

Naive estimate with  $\rho = 100\%$  correlation gives a  $\sim 9\sigma$  tension

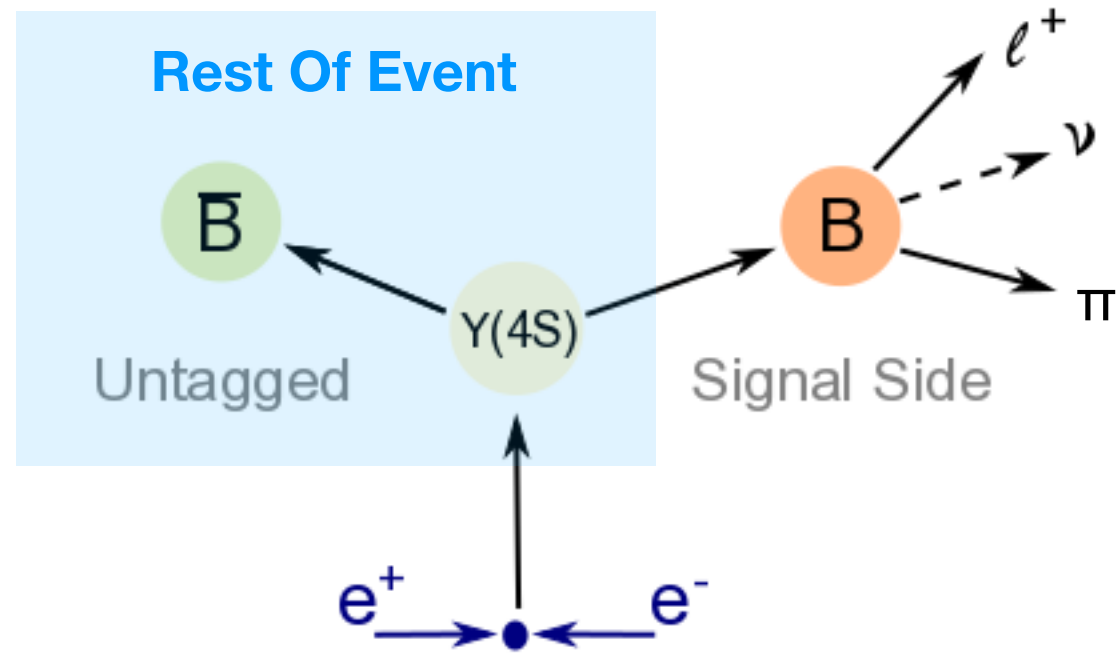


# Inclusive $B \rightarrow X_c l \nu$

$$\Gamma = \frac{G_F^2 m_b^5}{192\pi^3} |V_{cb}|^2 \left( 1 + \frac{c_5(\mu)\langle O_5 \rangle(\mu)}{m_b^2} + \frac{c_6(\mu)\langle O_6 \rangle(\mu)}{m_b^3} + \mathcal{O}\left(\frac{1}{m_b^4}\right) \right)$$

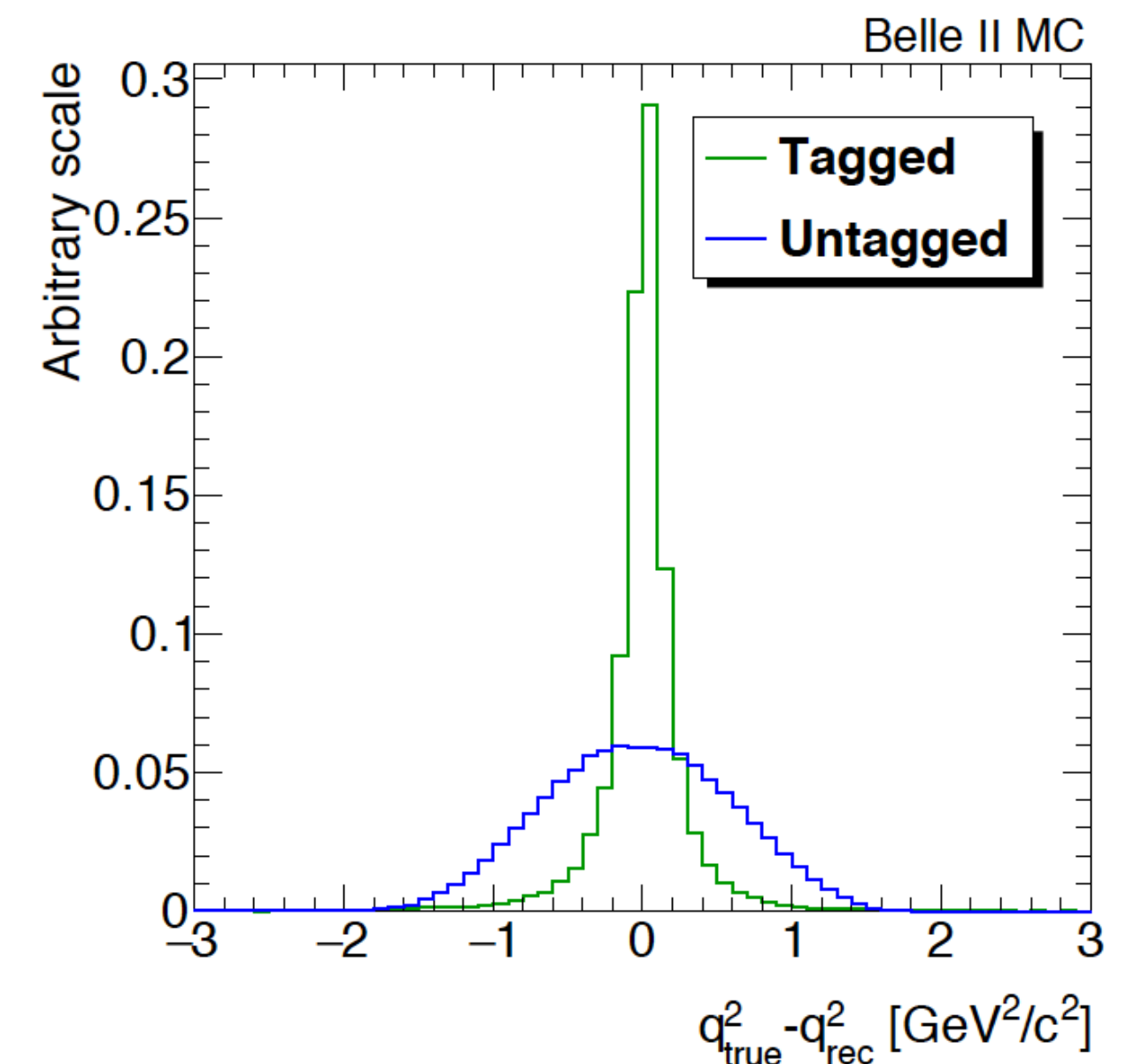
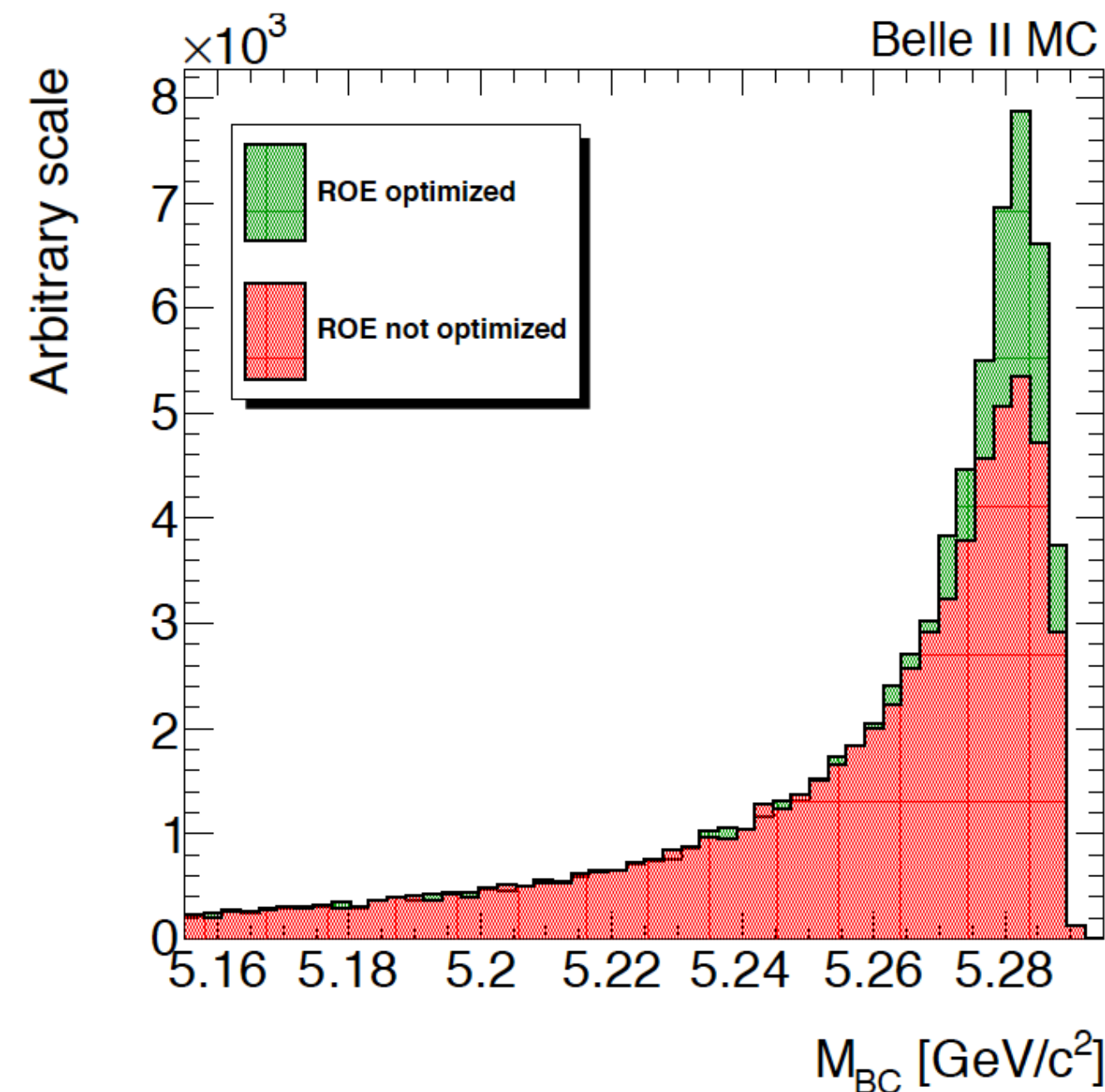
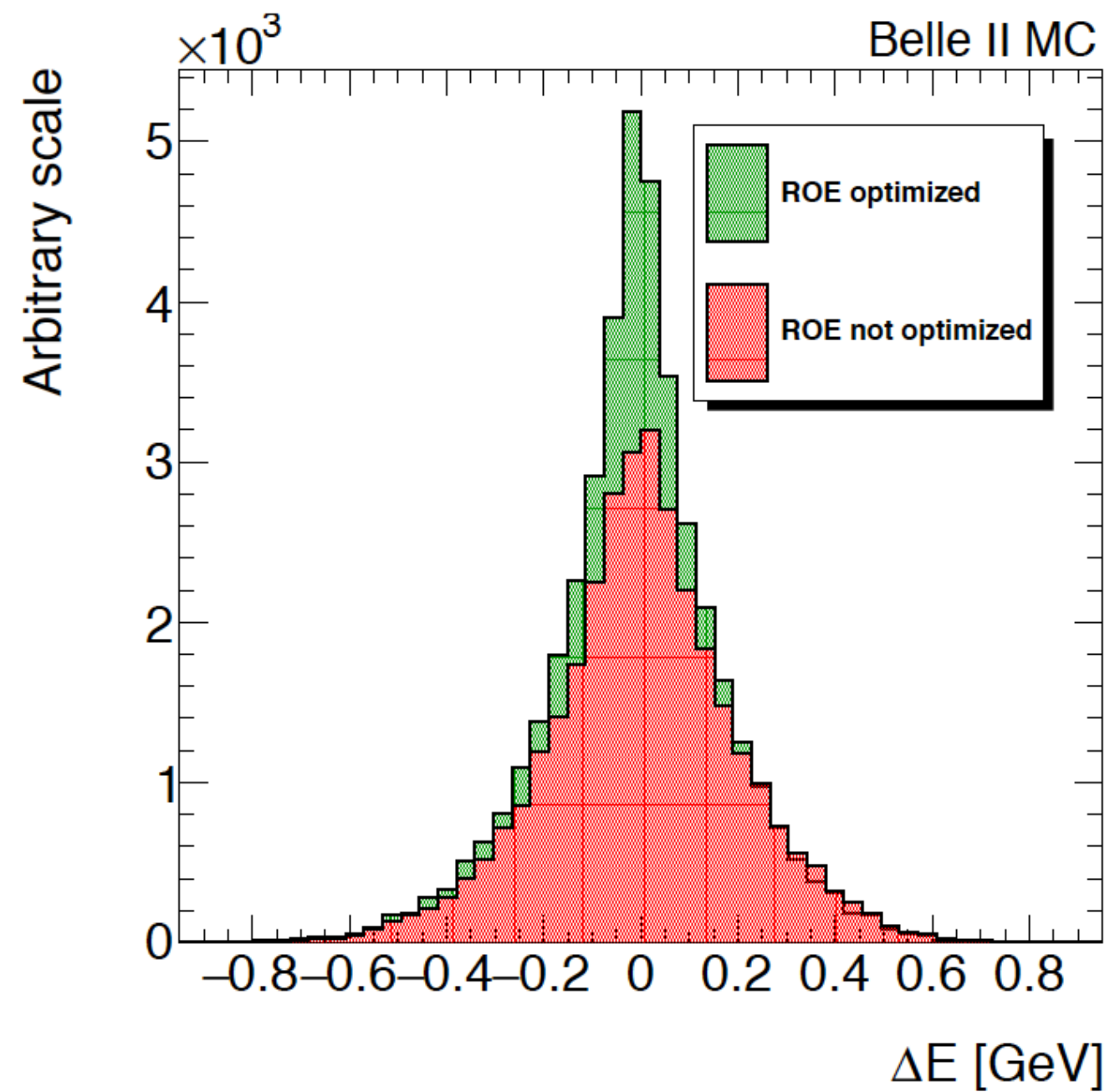
- Latest measurement is from the year 2010!
- Current global fit based on measured moments of  $E_l, M_X^2$
- 2% tot. uncertainty limited by theoretical uncertainty (1.2%~1.4% at Belle II 50ab<sup>-1</sup>)
- New method using  $q^2$  moments has been proposed [1812.07472](#)

# Untagged $B \rightarrow \pi l \nu$ @ Belle II MC

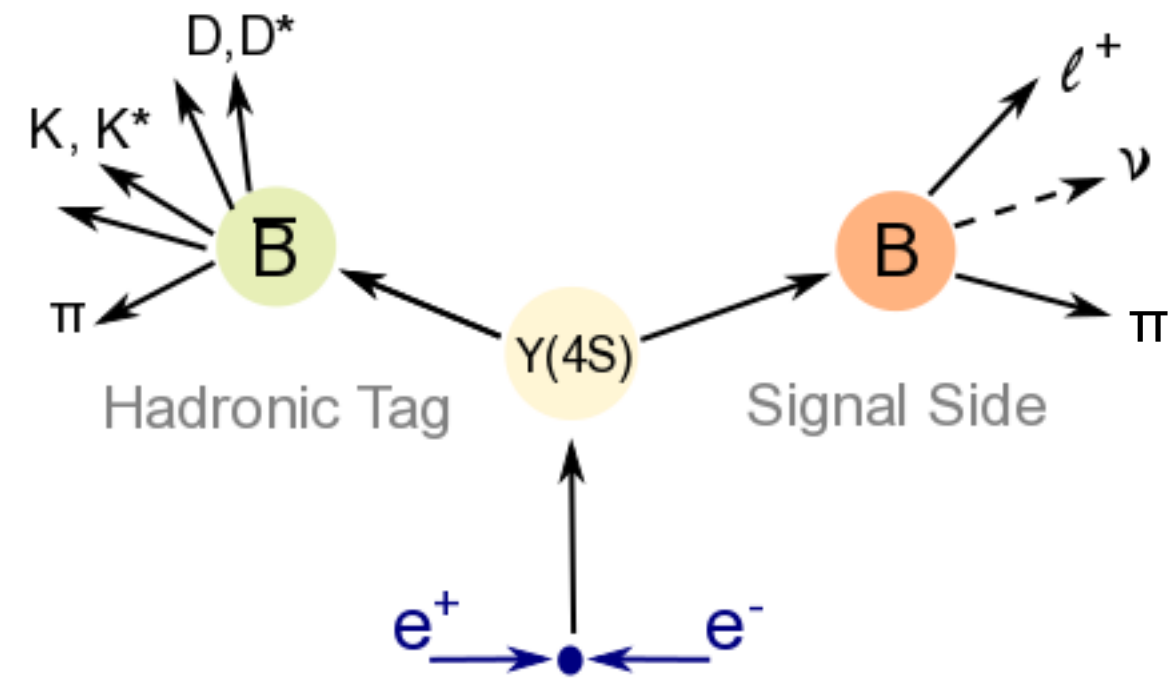


- Select good pion and lepton ( $>1$  GeV/c)
- Assuming neutrino is the only missing particle
- Optimized BDT selection in ROE
- Background suppressed by  $M_{miss}^2, \cos \theta_{BY}, M_{bc}, \Delta E$

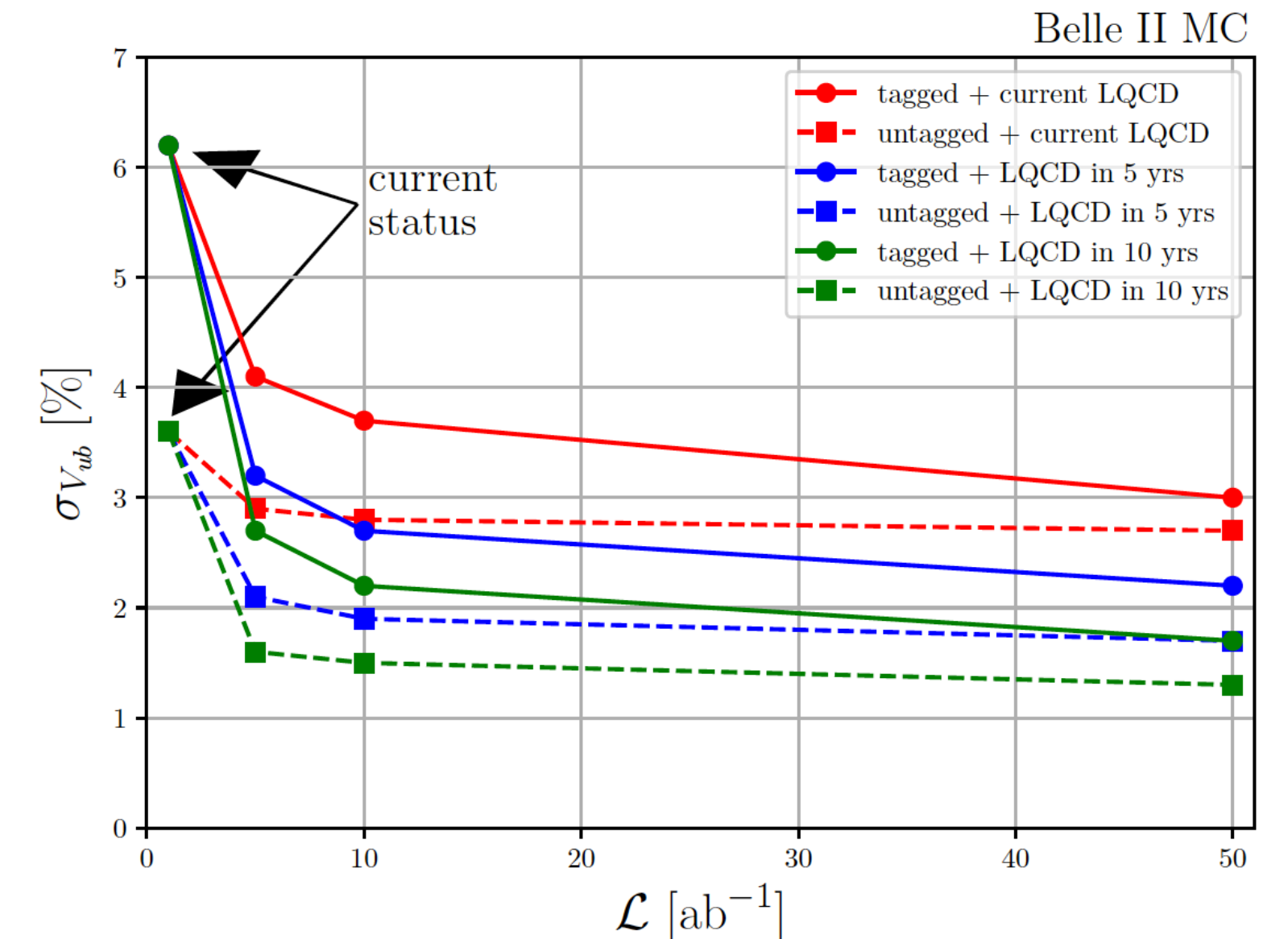
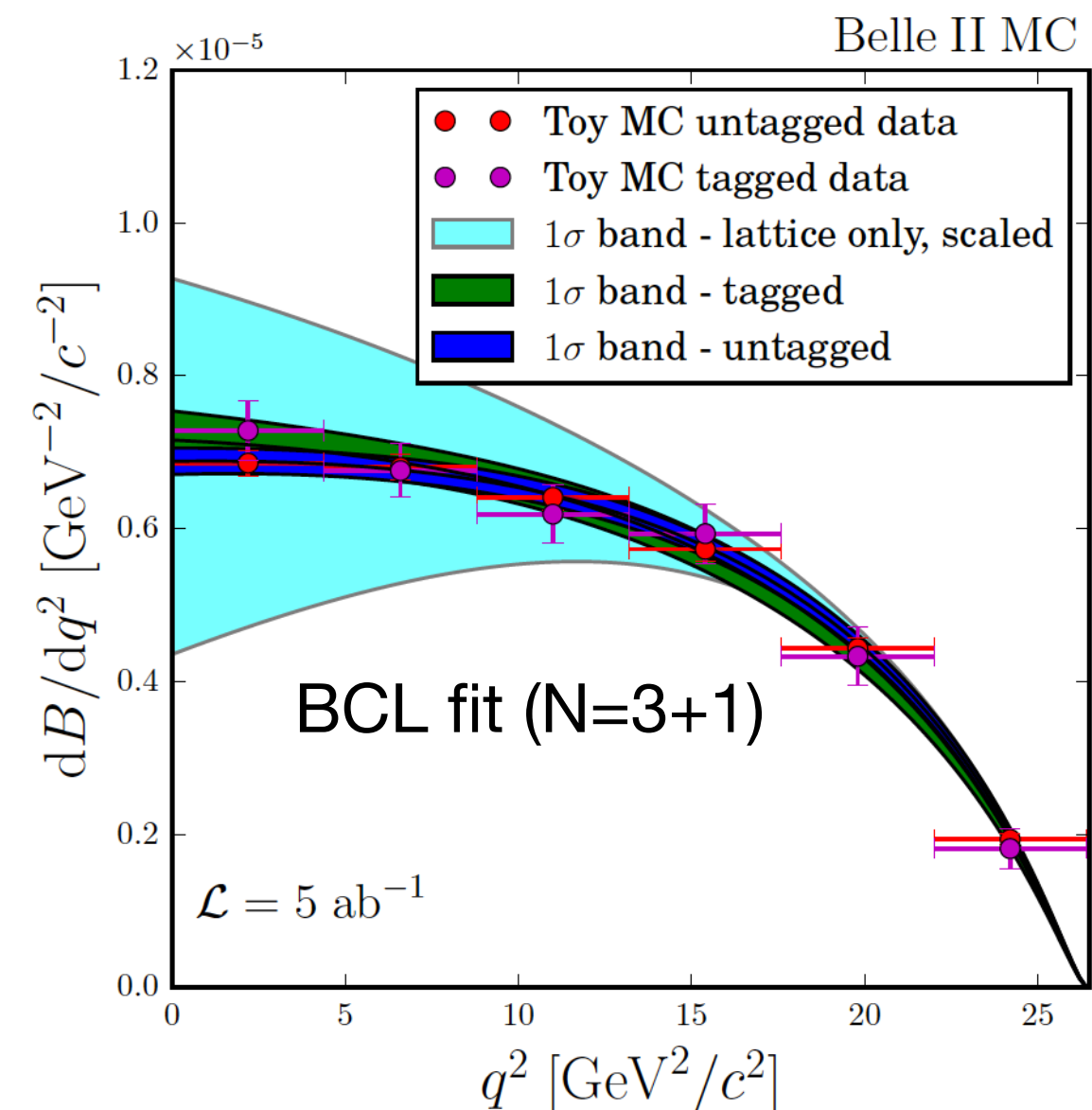
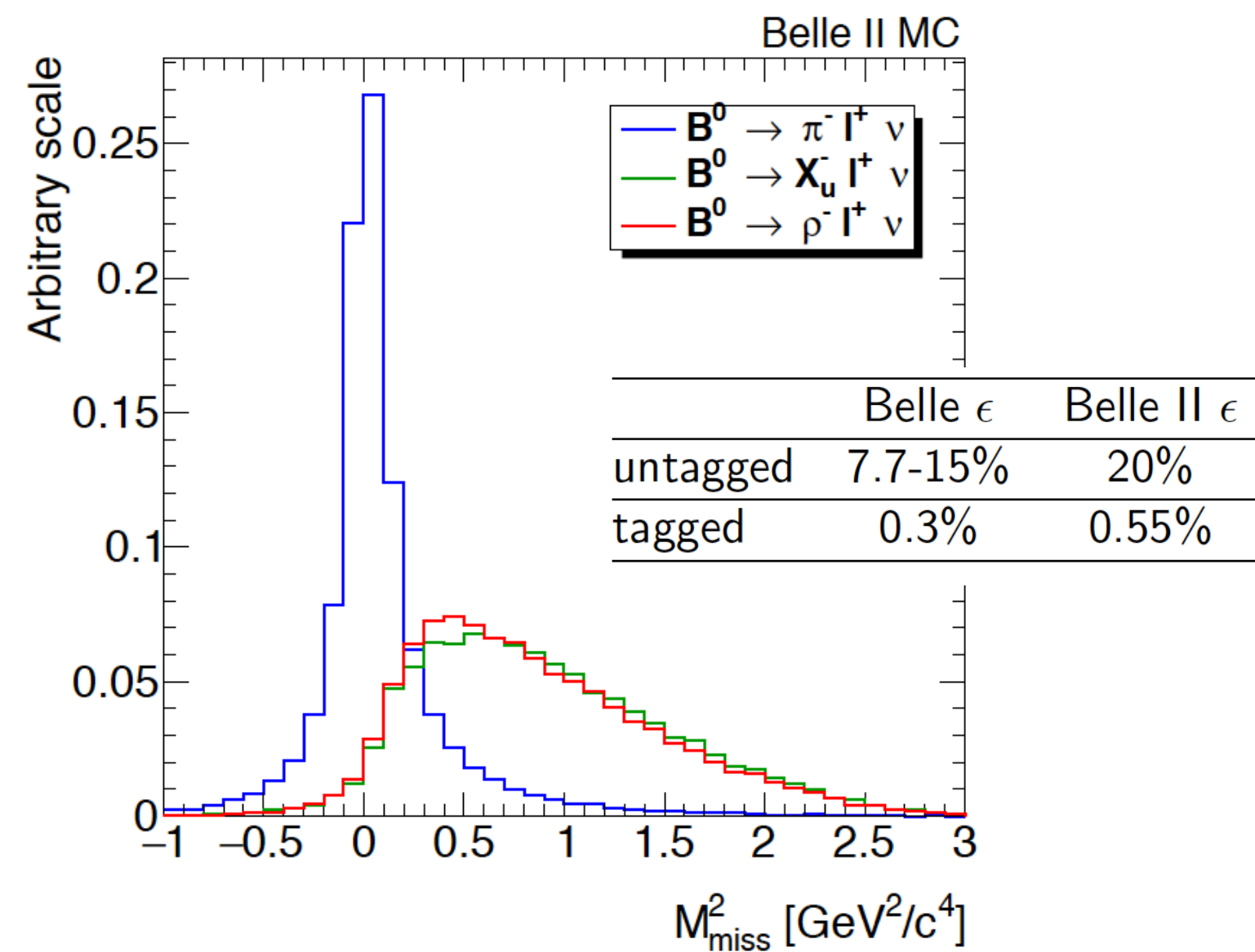
$$M_{miss}^2 = (p_{e^+e^-} - p_{\pi} - p_l - p_{ROE})^2 \quad \cos \theta_{BY} = \frac{2E_B^* E_Y^* - M_B^2 - M_Y^2}{2p_B^* p_Y^*} \quad M_{bc} = \sqrt{\frac{(s/2 + p_B \cdot p_{e^+e^-})^2}{E_{e^+e^-}^2} - p_B^2} \quad \Delta E = \frac{p_B \cdot p_{e^+e^-} - s/2}{\sqrt{s}}$$



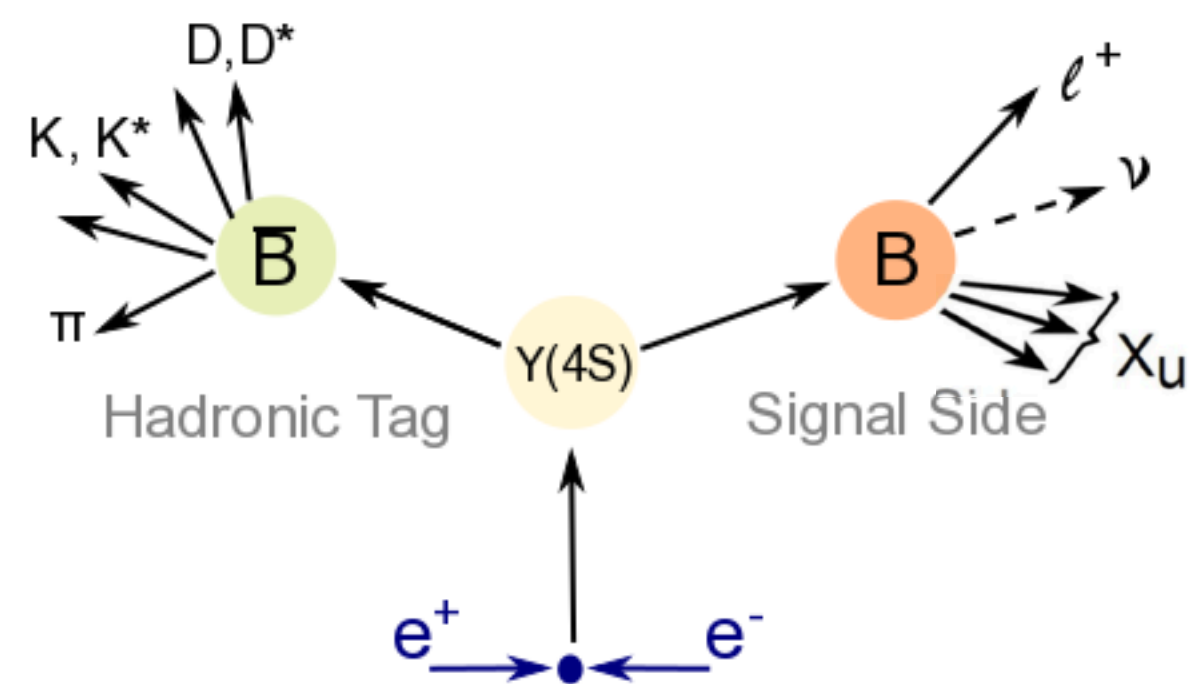
# Tagged $B \rightarrow \pi l \nu$ @ Belle II MC



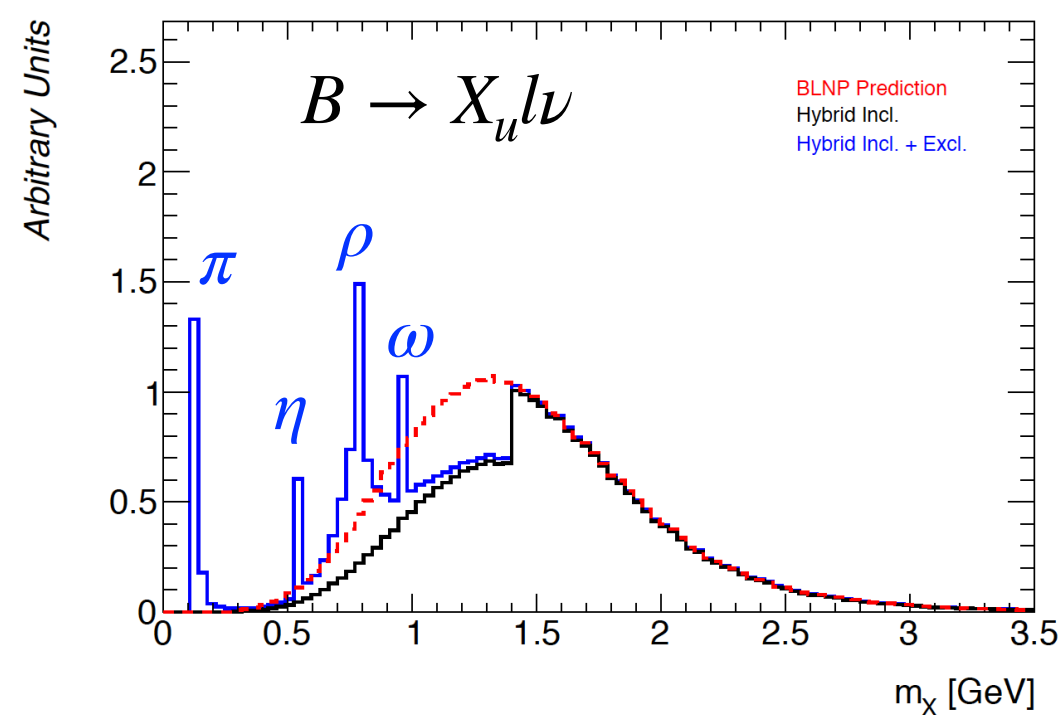
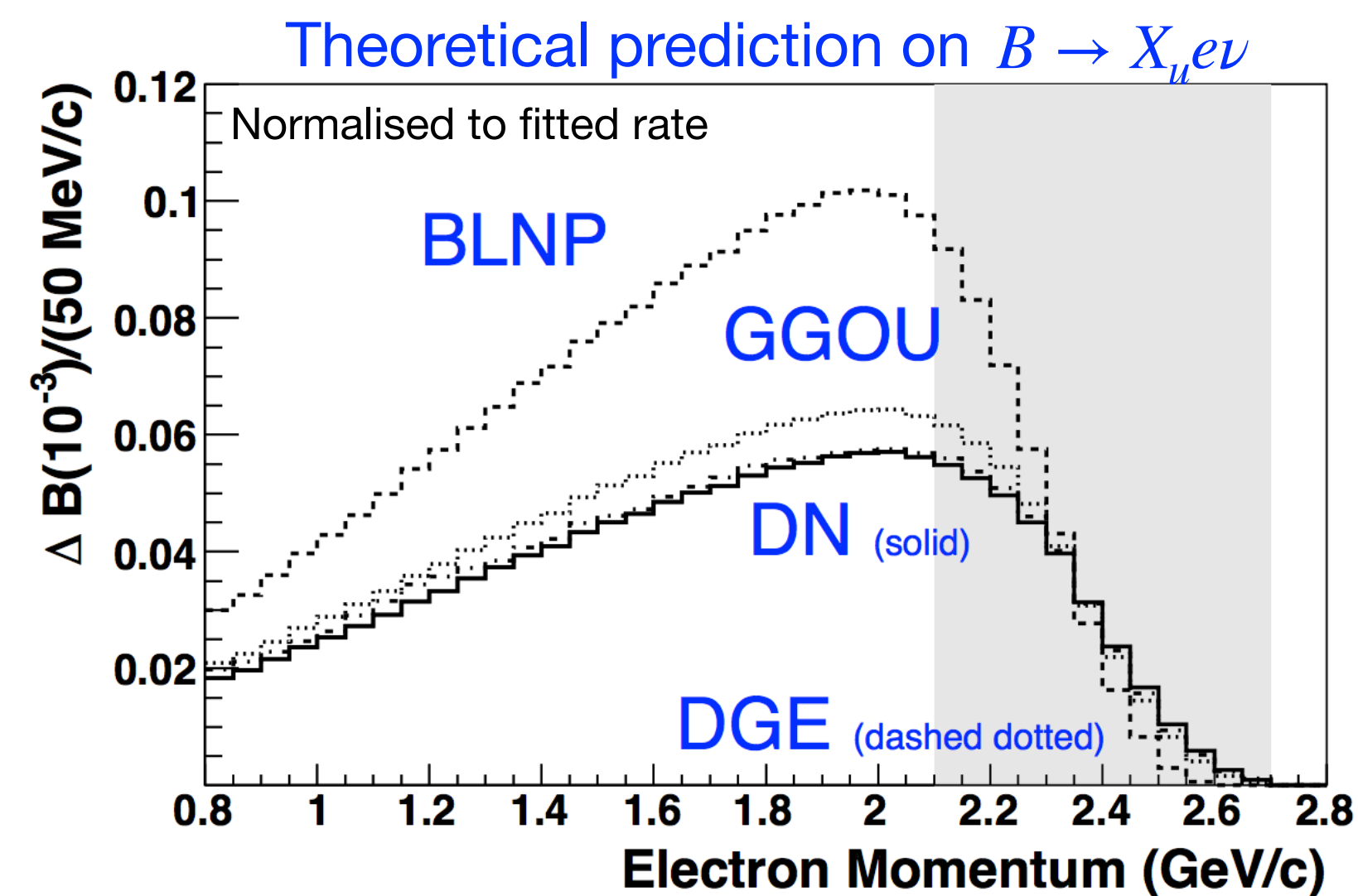
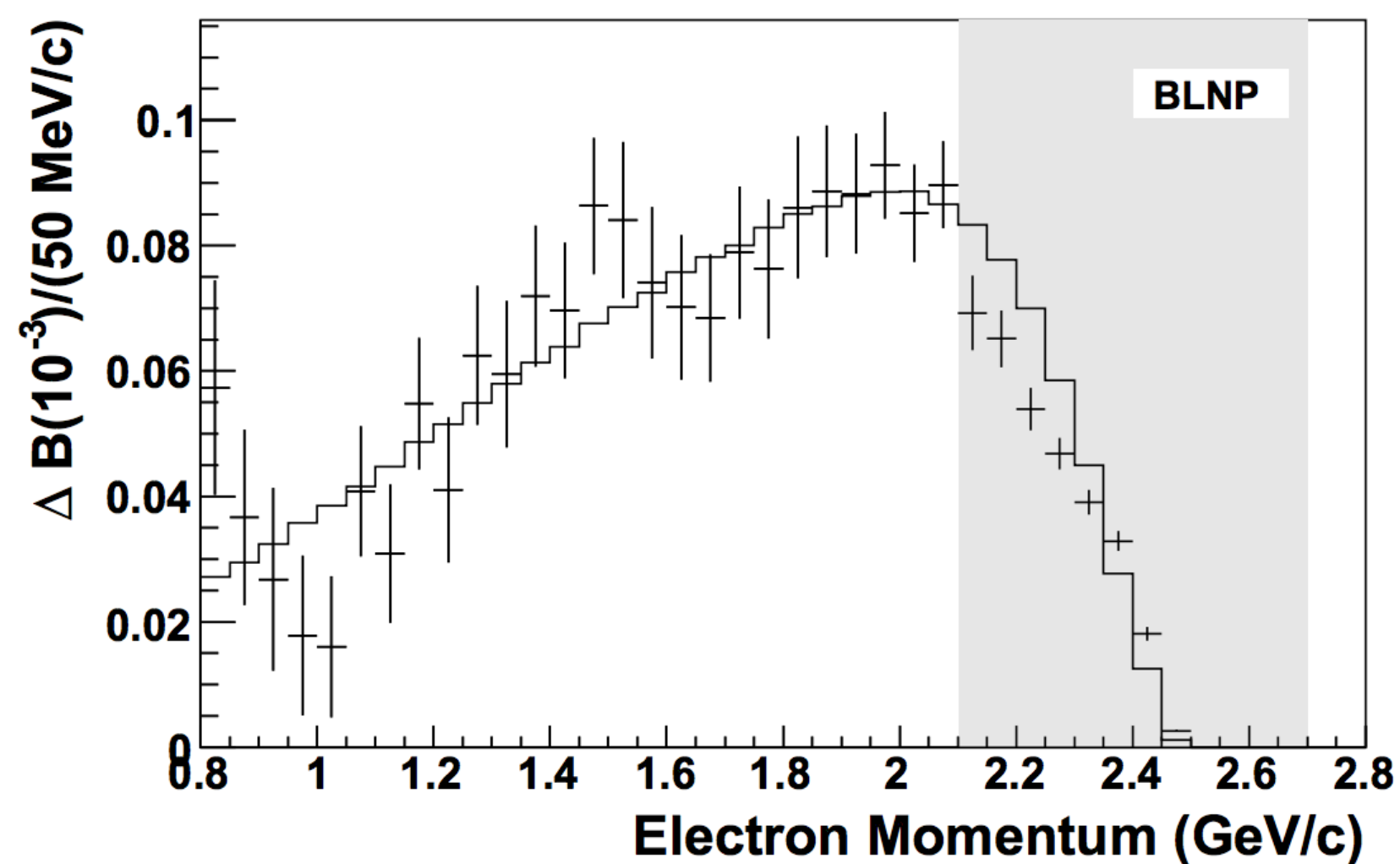
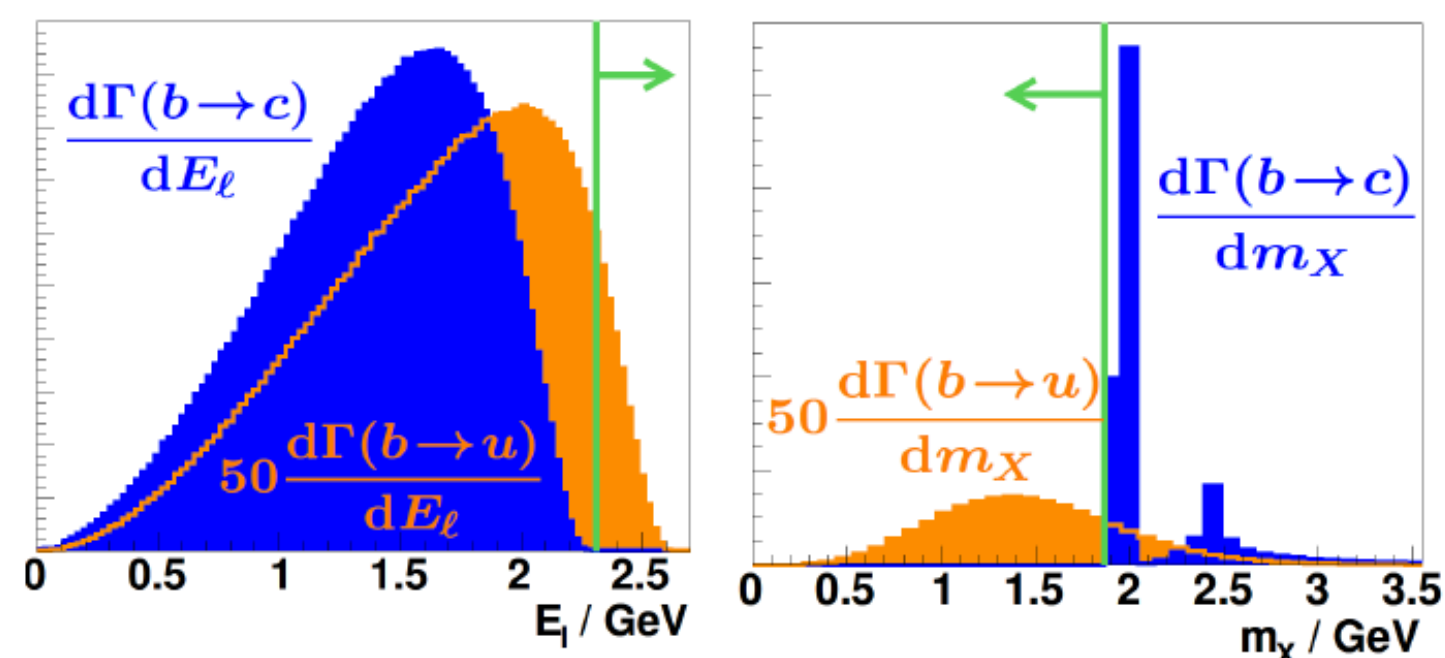
- Select good pion and lepton ( $>1$  GeV/c)
- With new tagging algorithm FEI
- Precise tag knowledge  $M_{\text{miss}}^2 = (p_{e^+e^-} - p_{\text{tag}} - p_{\pi} - p_l)^2$
- Belle II aims at excl.  $|V_{ub}|$  exp.  $\sigma \sim 4\%$  (now 5%)



# Inclusive $B \rightarrow X_u l \nu$



- Challenge in high  $b \rightarrow c$  background
- Inclusive + exclusive hybrid modelling
- Large theoretical uncertainty close to end point
- Belle II aims at inclu.  $|V_{ub}|$  exp.  $\sigma \sim 3\%$  @ $50\text{fb}^{-1}$  (now 5%)
- Latest measurement based on electron energy spectrum fit [BaBar 2017](#)

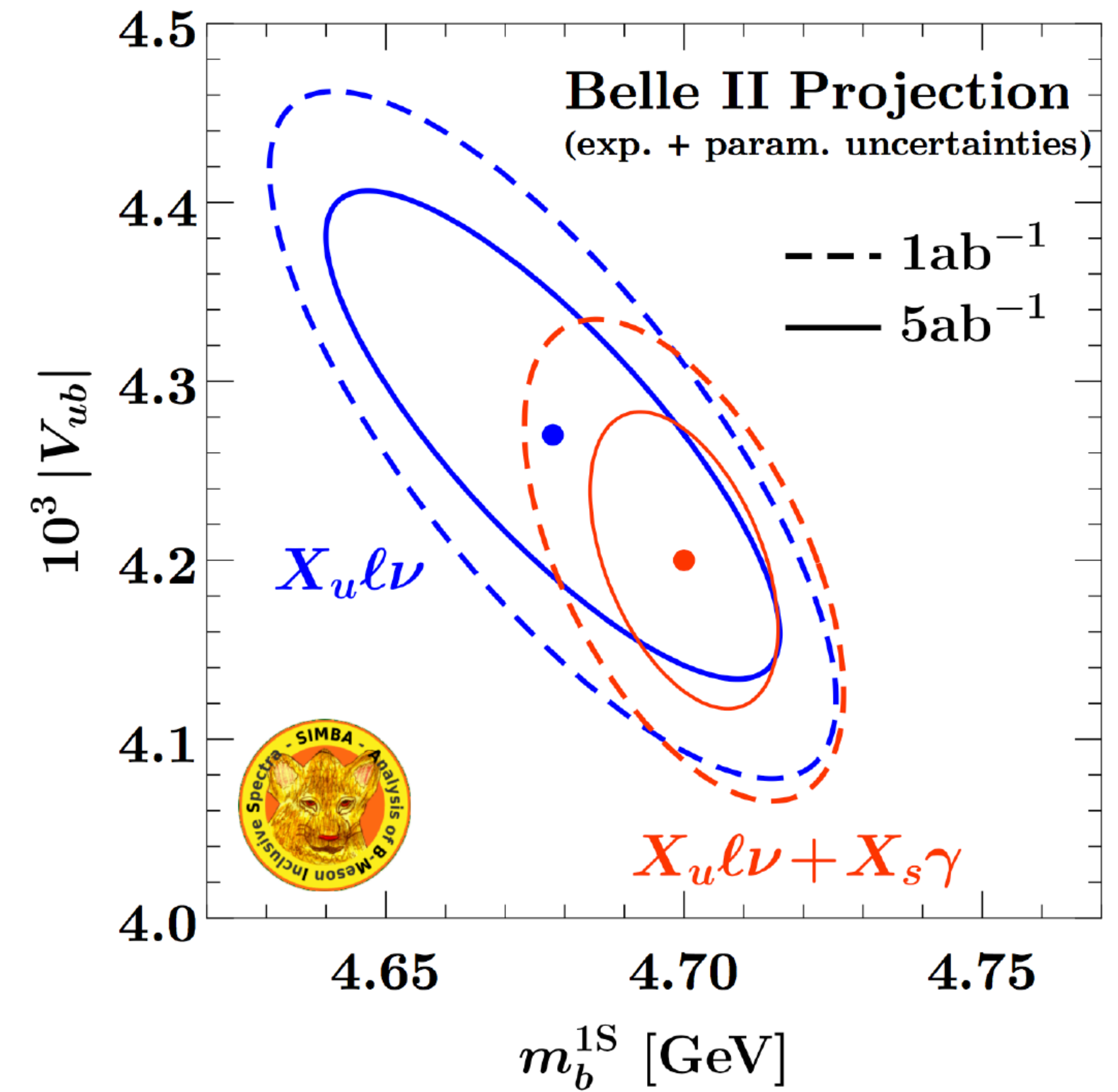
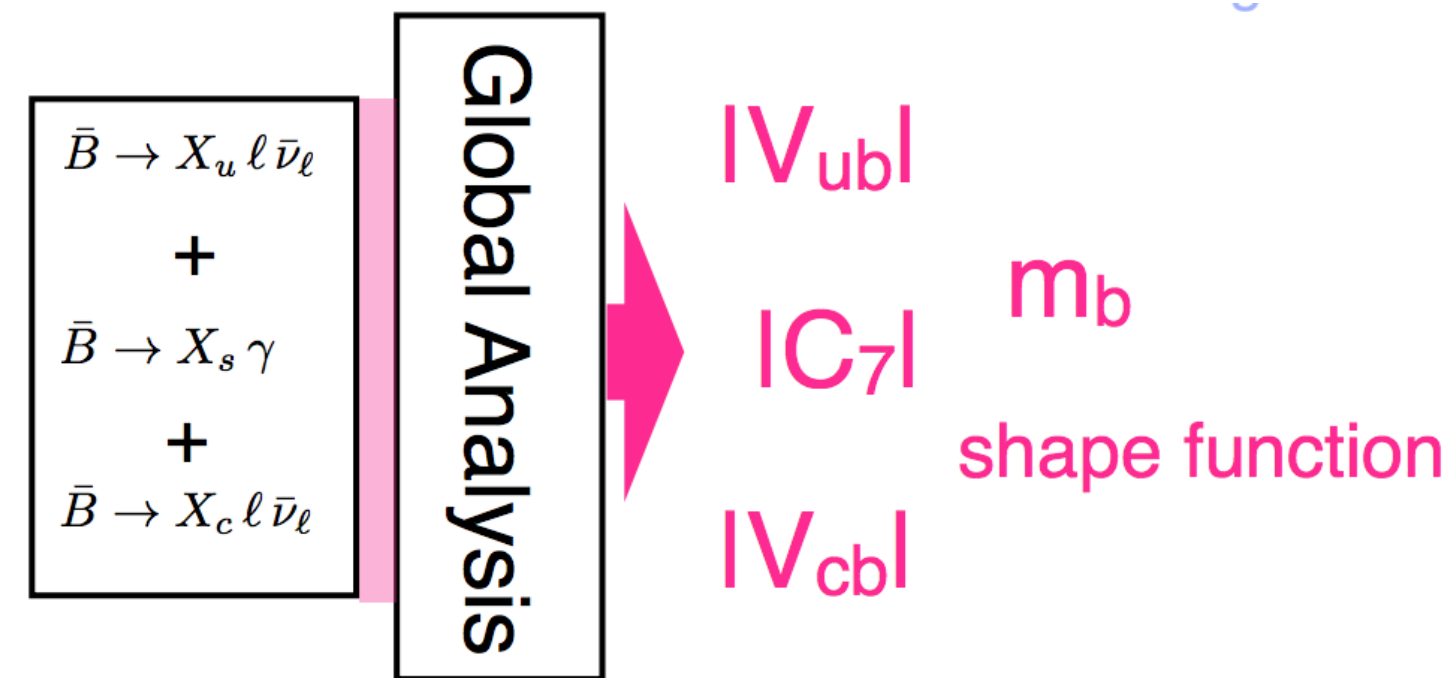
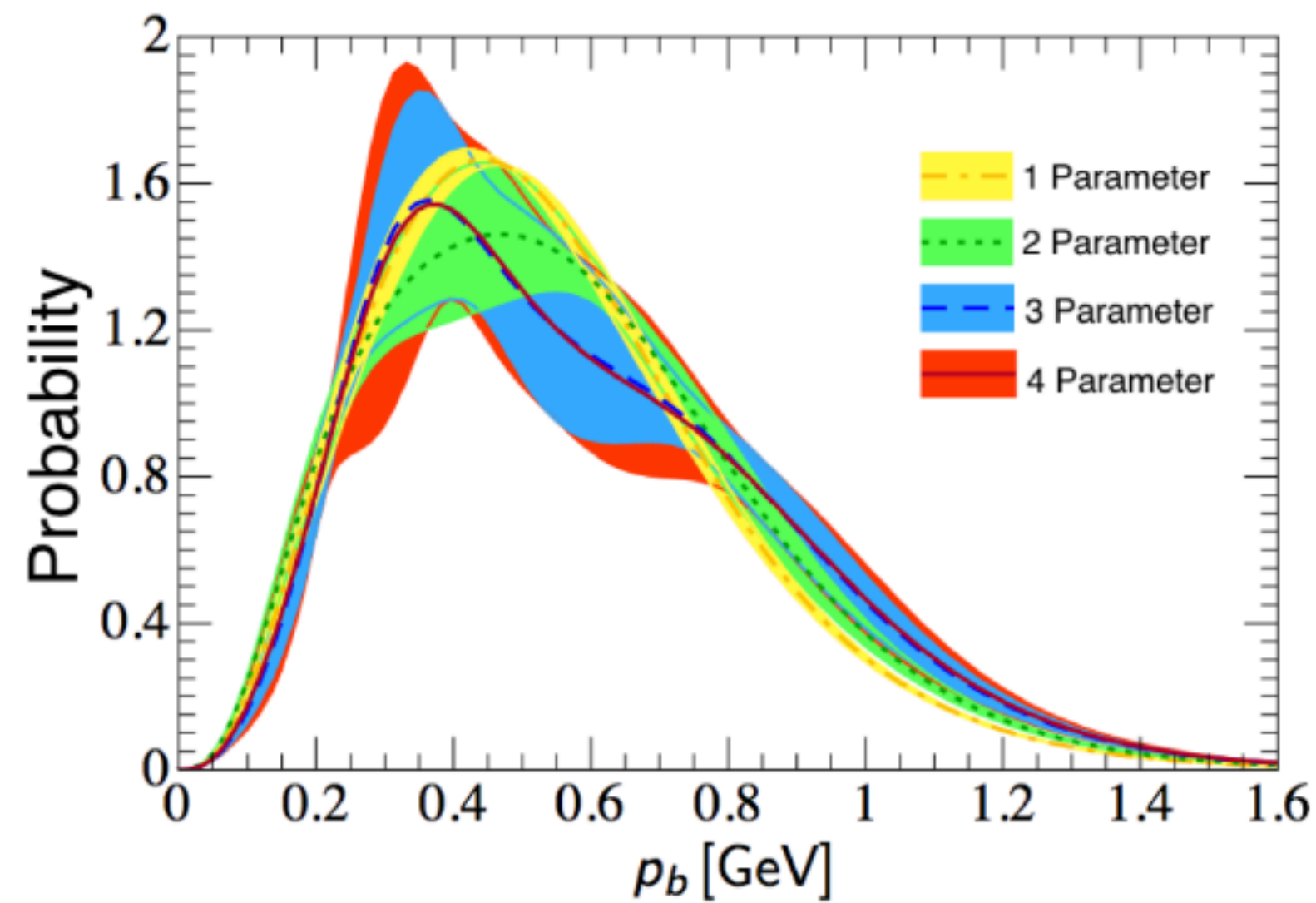


	<i>BLNP</i>	<i>GGOU</i>	<i>DN</i>	<i>DGE</i>
$ V_{ub}  \times 10^3$	$4.6 \pm 0.3$	$4.0 \pm 0.3$	$3.8 \pm 0.3$	$3.8 \pm 0.1$

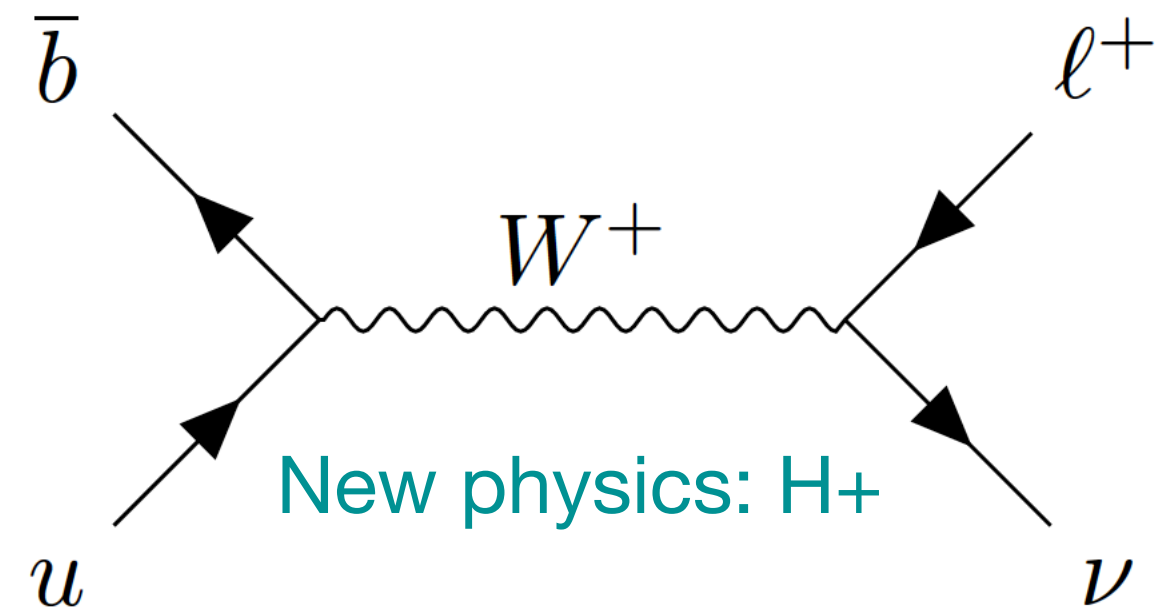
# A Global Fit Approach to Inclusive $|V_{ub}|$

- Global model-independent fits for B meson shape function [1303.0958](#)

$$F(k) = \sum_n (c_n f_n(k))^2$$



# Leptonic: $B \rightarrow l\nu$ ( $l = \mu, \tau$ )



$$\mathcal{B} (B^- \rightarrow l^- \bar{\nu}_l) = \frac{G_F^2 m_B m_l^2}{8\pi} \left( 1 - \frac{m_l^2}{m_B^2} f_B^2 \right) |V_{ub}|^2 \tau_B$$

Expected data set

$l$	$\mathcal{B}_{\text{SM}}$	711 fb $^{-1}$	5 ab $^{-1}$	50 ab $^{-1}$
$\tau$	$(7.71 \pm 0.62) \times 10^{-5}$	$61200 \pm 5000$	$430000 \pm 35000$	$4300000 \pm 350000$
$\mu$	$(3.46 \pm 0.28) \times 10^{-7}$	$275 \pm 23$	$1930 \pm 160$	$19300 \pm 1600$
$e$	$(0.811 \pm 0.065) \times 10^{-11}$	$0.0064 \pm 0.0005$	$0.0453 \pm 0.0037$	$0.453 \pm 0.037$

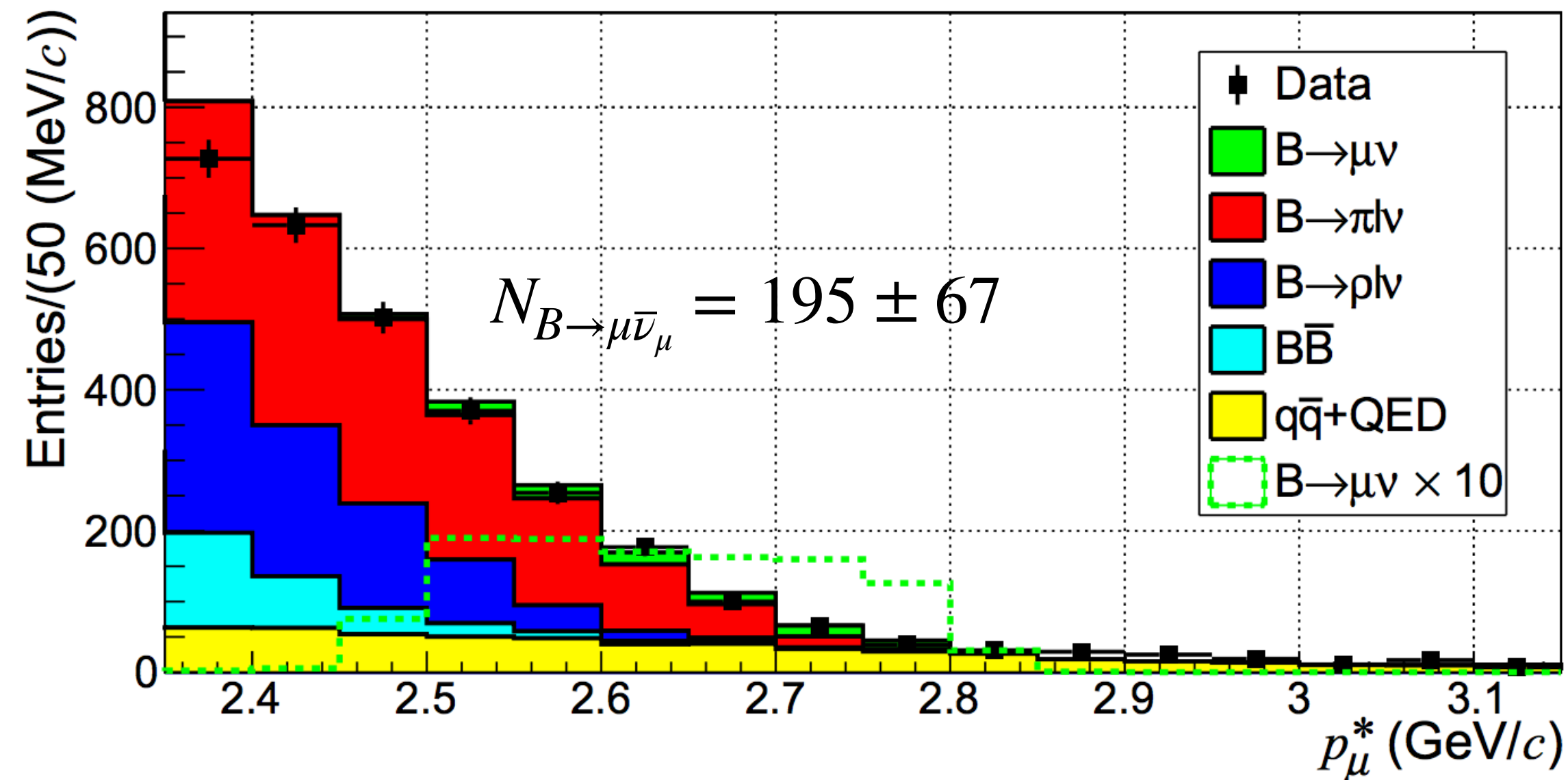
- Branching fractions are hierarchical with lepton mass due to helicity suppression
- Precise theoretical prediction in the SM
- Clean  $|V_{ub}|$  measurement
- Probe of LFU and new physics

- Latest measurement from Belle untagged analysis

Experiment	Upper limit @ 90% C.L.	Comment
Belle	$2.7 \times 10^{-6}$	Fully reconstructed hadronic tag, $711 \text{ fb}^{-1}$
Belle	$1.7 \times 10^{-6}$	Untagged analysis, $253 \text{ fb}^{-1}$
BaBar	$1.0 \times 10^{-6}$	Untagged analysis, $468 \times 10^6 B\bar{B}$ pairs
Belle	$2.9 \times 10^{-7}$	Untagged analysis, $711 \text{ fb}^{-1}$

$$\mathcal{B} \left( B^- \rightarrow \mu^- \bar{\nu}_\mu \right) \in [2.9, 10.7] \times 10^{-7}$$

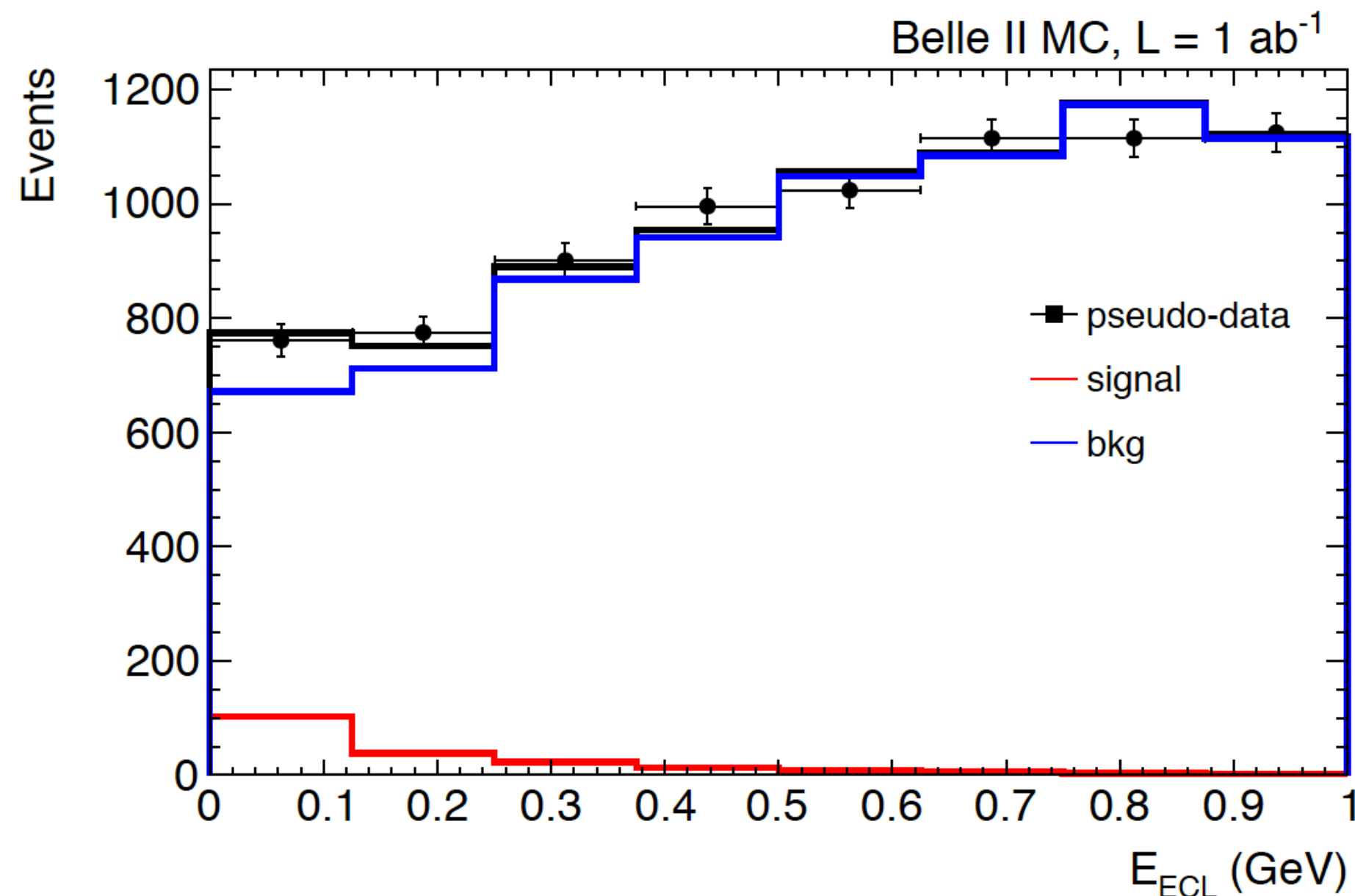
@ 90% C.L. , agree with SM



$$\mathcal{B}_{\text{SM}} \left( B^- \rightarrow \mu^- \bar{\nu}_\mu \right) = (3.80 \pm 0.31) \times 10^{-7}$$

	Expected uncertainty			
	$50 \text{ ab}^{-1}$	$\mathcal{B}_{\text{Stat.}}$	$\mathcal{B}_{\text{Syst.}}$	$ V_{ub} $
Belle II Untagged	$\sim 5\%$	$\sim 5\%$	-	3-4%
Belle II tagged	$\sim 13\%$	-	-	-

- Reconstruct  $B_{\text{tag}}$  hadronically or semileptonic
- Due to tauon decay  $e^- \nu_\tau \bar{\nu}_e, \mu^- \nu_\tau \bar{\nu}_\mu, \pi^- \bar{\nu}_\tau, \rho^- \bar{\nu}_\tau$ , final  $N_\nu \geq 1$
- Fit remaining energy on EM calorimeter ( $E_{\text{ECL}}$ )
- Expect to reach  $5\sigma$  significancy with  $2.6\text{ab}^{-1}$



Expected yields @1 ab<sup>-1</sup>

$E_{\text{ECL}}$		< 1 GeV	< 0.25 GeV
without background	Background yield [events]	12835	2062
	Signal yield [events]	332	238
	Signal efficiency (‰)	3.8	2.7
with background	Background yield [events]	7420	1348
	Signal yield [events]	188	136
	Signal efficiency (‰)	2.2	1.6

Expected uncertainty

	Integrated Luminosity (ab <sup>-1</sup> )	1	5	50
hadronic tag	statistical uncertainty (%)	29	13	4
	systematic uncertainty (%)	13	7	5
	total uncertainty (%)	32	15	6
semileptonic tag	statistical uncertainty (%)	19	8	3
	systematic uncertainty (%)	18	9	5
	total uncertainty (%)	26	12	5



# Summary of $|V_{ub}|$ Projections

	Statistical	Systematic (reducible, irreducible)	Total Exp	Theory	Total
$ V_{ub} $ exclusive (had. tagged)					
711 fb <sup>-1</sup>	3.0	(2.3, 1.0)	3.8	7.0	8.0
5 ab <sup>-1</sup>	1.1	(0.9, 1.0)	1.8	1.7	3.2
50 ab <sup>-1</sup>	0.4	(0.3, 1.0)	1.2	0.9	1.7
$ V_{ub} $ exclusive (untagged)					
605 fb <sup>-1</sup>	1.4	(2.1, 0.8)	2.7	7.0	7.5
5 ab <sup>-1</sup>	1.0	(0.8, 0.8)	1.2	1.7	2.1
50 ab <sup>-1</sup>	0.3	(0.3, 0.8)	0.9	0.9	1.3
$ V_{ub} $ inclusive					
605 fb <sup>-1</sup> (old $B$ tag)	4.5	(3.7, 1.6)	6.0	2.5–4.5	6.5–7.5
5 ab <sup>-1</sup>	1.1	(1.3, 1.6)	2.3	2.5–4.5	3.4–5.1
50 ab <sup>-1</sup>	0.4	(0.4, 1.6)	1.7	2.5–4.5	3.0–4.8
$ V_{ub} $ $B \rightarrow \tau\nu$ (had. tagged)					
711 fb <sup>-1</sup>	18.0	(7.1, 2.2)	19.5	2.5	19.6
5 ab <sup>-1</sup>	6.5	(2.7, 2.2)	7.3	1.5	7.5
50 ab <sup>-1</sup>	2.1	(0.8, 2.2)	3.1	1.0	3.2
$ V_{ub} $ $B \rightarrow \tau\nu$ (SL tagged)					
711 fb <sup>-1</sup>	11.3	(10.4, 1.9)	15.4	2.5	15.6
5 ab <sup>-1</sup>	4.2	(4.4, 1.9)	6.1	1.5	6.3
50 ab <sup>-1</sup>	1.3	(2.3, 1.9)	2.6	1.0	2.8

$|V_{ub}|$  uncertainty @ Belle II

**exclusive ~1.5%**

**inclusive ~ 4%**

**leptonic ~ 3%**

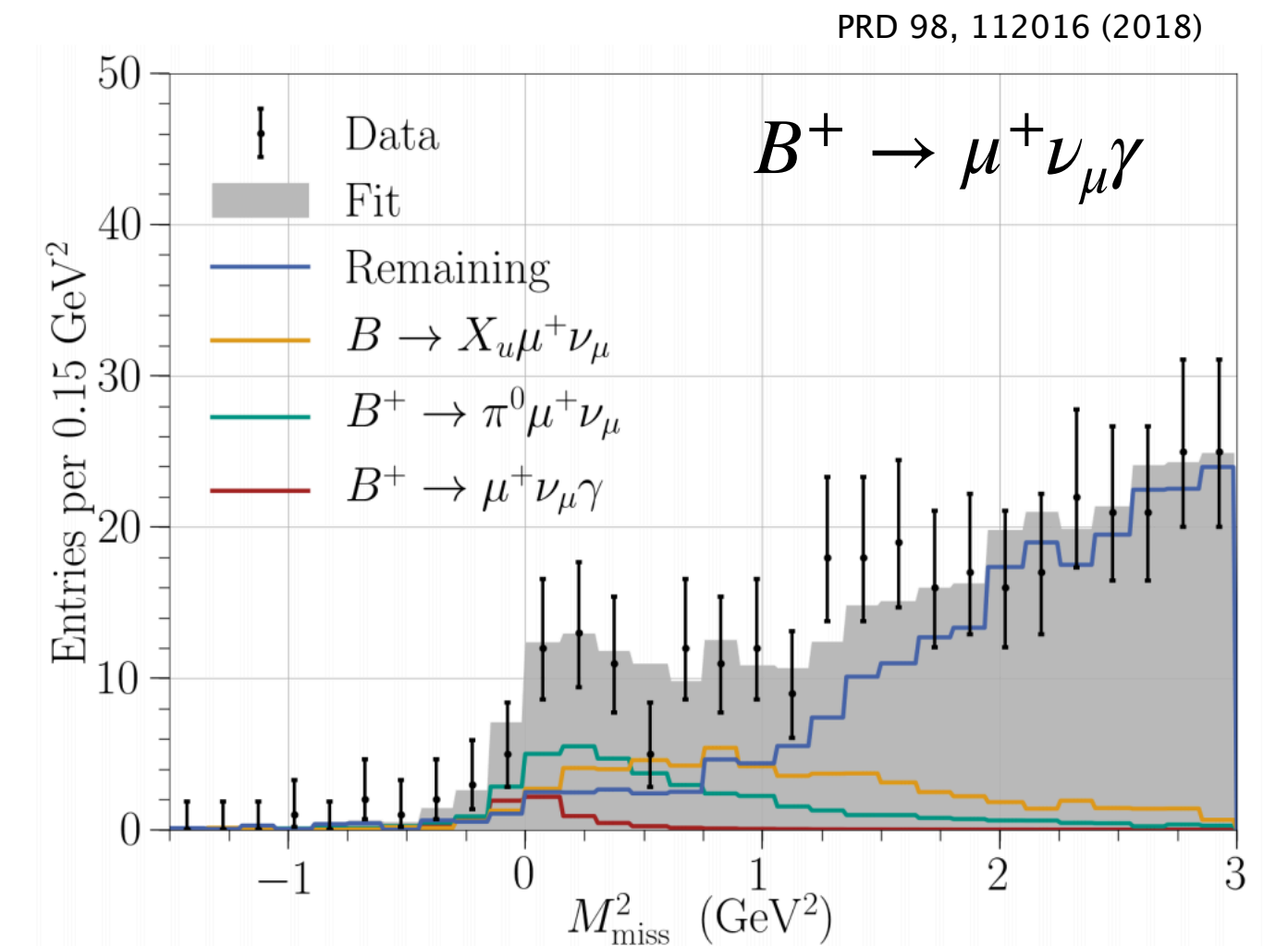
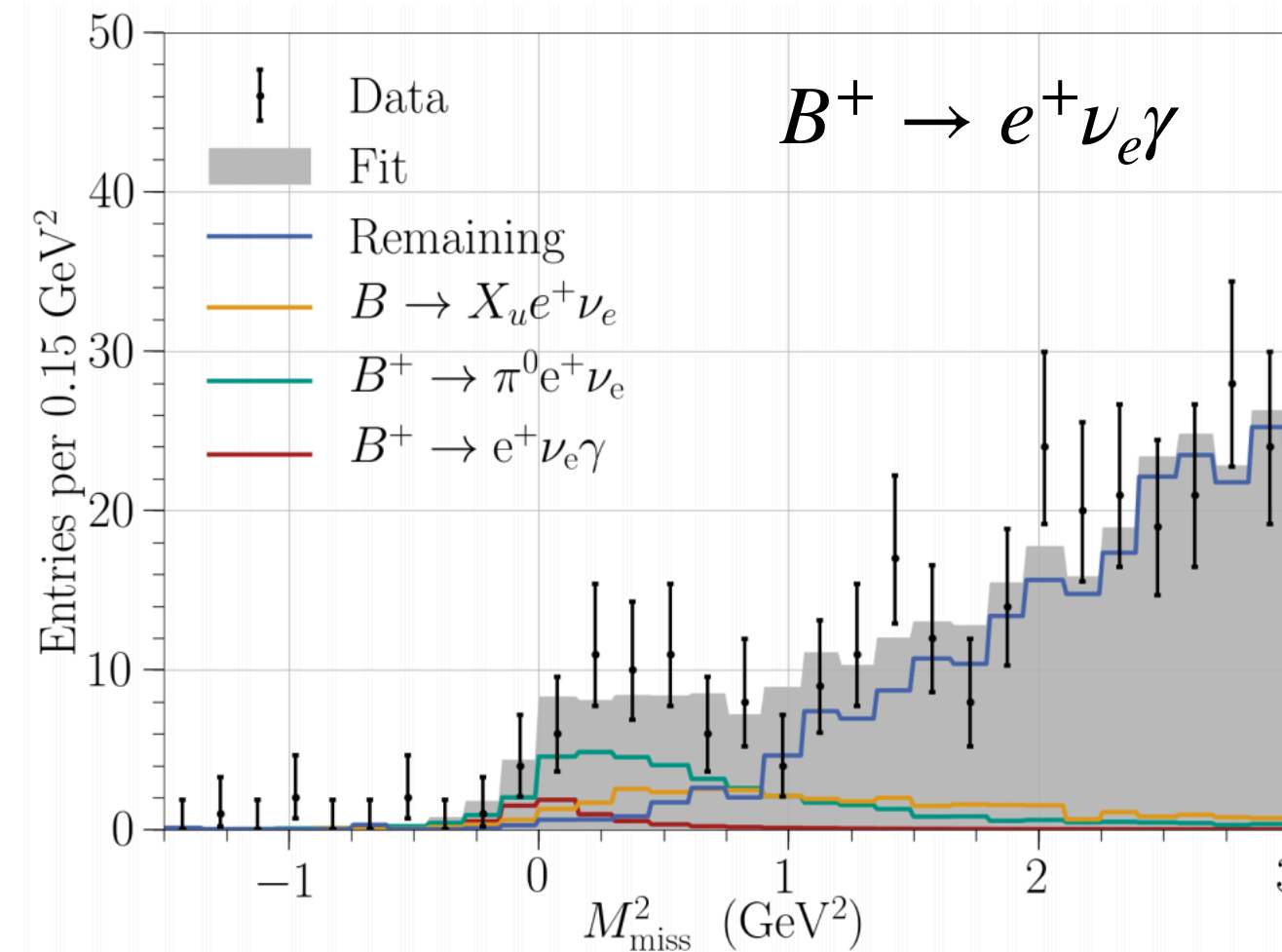
# Radiative Leptonic: $B^+ \rightarrow \ell^+ \nu_\ell \gamma$

- Belle full data set  $711\text{fb}^{-1}$  with new tagging algorithm (FEI)
- Photon energy selection above 1 GeV
- Measured upper limit of  $\Delta B$  and the first inverse moment  $\lambda_B$

$$\frac{d\Gamma(B^+ \rightarrow \ell^+ \nu_\ell \gamma)}{dE_\gamma} = \frac{\alpha_{\text{em}} G_F^2 |V_{ub}|^2}{6\pi^2} m_B E_\gamma^3 \left(1 - \frac{2E_\gamma}{m_B}\right) \times \left( |F_V|^2 + \left|F_A + \frac{e_\ell f_B}{E_\gamma}\right|^2 \right)$$

$$\Delta\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell \gamma) = \tau_B \int_{\text{Selection}} dE_\gamma \frac{d\Gamma}{dE_\gamma}$$

$\ell$	$\Delta\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell \gamma)$ limit ( $10^{-6}$ )		
	BaBar 2009	Belle 2015	Belle 2018
$e$	-	$< 6.1$	$< 4.3$
$\mu$	-	$< 3.4$	$< 3.4$
$e, \mu$	$< 14$	$< 3.5$	$< 3.0$



Expected signal yields assuming  $\Delta\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell \gamma) = 5.0 \times 10^{-6}$

	$B^+ \rightarrow e^+ \nu_e \gamma$	$B^+ \rightarrow \mu^+ \nu_\mu \gamma$	Combined
$N_{\text{New}}$	24.8	25.7	50.5
$N_{\text{Published}}$	8.0	8.7	16.5

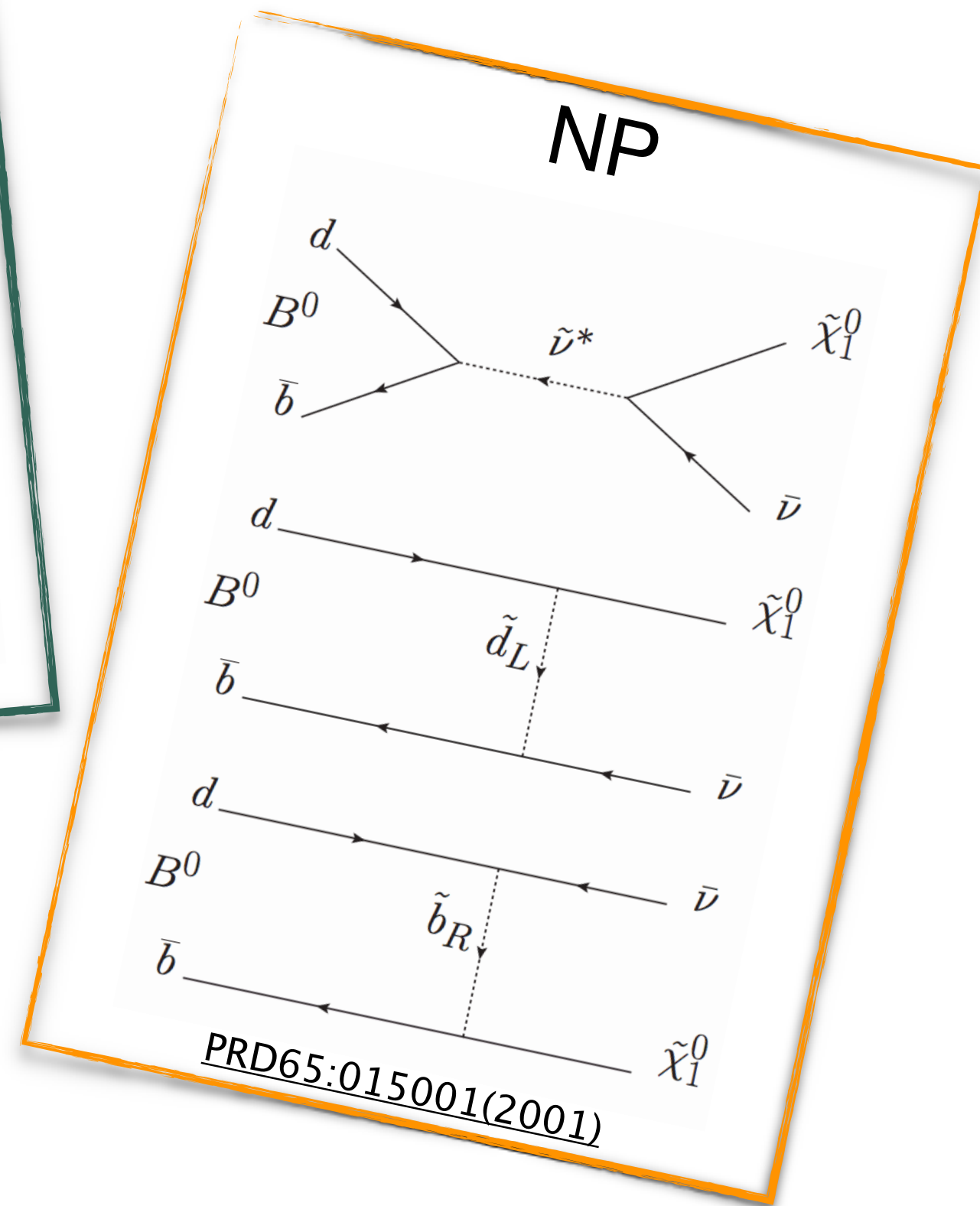
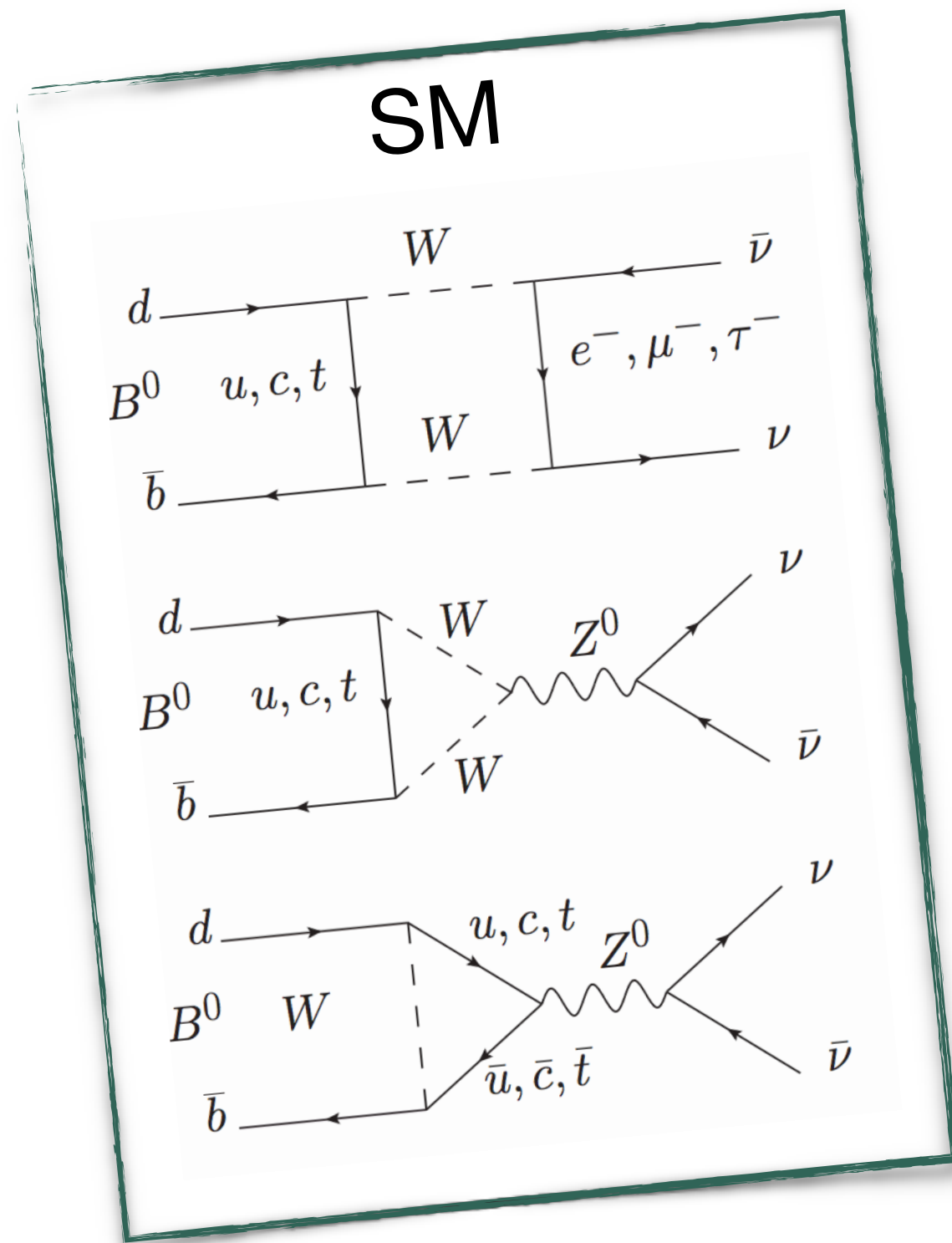
Expected statistical error

	Belle	Belle II	Belle II
New analysis		$5\text{ ab}^{-1}$	$50\text{ ab}^{-1}$
	+1.48	+0.56	+0.18
	-1.39	-0.53	-0.17

**MC test:**  
**FEI brings x3 yields!**

PRD 98, 112016 (2018)

# B → invisibles



- Adventured by BaBar 2012 and Belle 2012

Mode	Upper limit @ 90% C.L.	Experiment
$B^0 \rightarrow \nu\nu$	$2.4 \times 10^{-5}$	BaBar PRD 86, 051105(R) (2012)
$B^0 \rightarrow \nu\nu\gamma$	$1.7 \times 10^{-5}$	
$B^0 \rightarrow \nu\nu$	$1.3 \times 10^{-4}$	Belle PRD 86, 032002 (2012)

- Opportunity for Belle II

- Much improved tagging algorithm
- Combining hadronic and semileptonic tagging for a higher statistics
- Hadronic  $B_s$  tagging efficiency seen 2 times higher than for  $B^0$
- Possible search for missing every signals as non-standard invisible states  $B \rightarrow X_{dark}$

Observables	Belle $0.71 \text{ ab}^{-1}$ ( $0.12 \text{ ab}^{-1}$ )	Belle II $5 \text{ ab}^{-1}$	Belle II $50 \text{ ab}^{-1}$
$\text{Br}(B^0 \rightarrow \nu\bar{\nu}) \times 10^6$	$< 14$	$< 5.0$	$< 1.5$
$\text{Br}(B_s \rightarrow \nu\bar{\nu}) \times 10^5$	$< 9.7$	$< 1.1$	–

Process	Observable	Theory	Sys. limit (Discovery) [ab <sup>-1</sup> ]	vs LHCb	vs Belle	Anomaly	New Physics
$B \rightarrow \pi l \nu$	$ V_{ub} $	★★★★	10-20	★★★★	★★★★	★★	★
$B \rightarrow X_u l \nu$	$ V_{ub} $	★★	2-10	★★★★	★★	★★★★	★
$B \rightarrow \tau \nu$	$\mathcal{B}$	★★★★	>50 (2)	★★★★	★★★★	★	★★★★
$B \rightarrow \mu \nu$	$\mathcal{B}$	★★★★	>50 (5)	★★★★	★★★★	★	★★★★
$B \rightarrow D^{(*)} l \nu$	$ V_{cb} $	★★★★	1-10	★★★★	★★	★★	★
$B \rightarrow X_c l \nu$	$ V_{cb} $	★★★★	1-5	★★★★	★★	★★	★★
$B \rightarrow D^{(*)} \tau \nu$	$R(D^{(*)})$	★★★★	5-10	★★	★★★★	★★★★	★★★★
$B \rightarrow D^{(*)} \tau \nu$	$P_\tau$	★★★★	15-20	★★★★	★★★★	★★	★★★★
$B \rightarrow D^{**} l \nu$	$\mathcal{B}$	★	-	★★	★★★★	★★	-
$B \rightarrow l \nu \gamma$	$\lambda_B$	★★	-	★★★★	★★★★	★	★★
$B \rightarrow K^{(*)} \nu \nu$	$\mathcal{B}, F_L$	★★★★	>50	★★★★	★★★★	★	★★

# Summary

- Belle II has successfully finished commissioning run and ready for taking physics data
- Improved tagging algorithm increases reconstruction efficiency significantly
- Promising performance of missing energy channels proved by MC studies
- Issues seen in form factor parameterisation need to be understood
- Deviation between inclusive and exclusive measurements still exist
- Upcoming Belle II data will help to resolve these questions...

**Thank you**

## $\bar{B}^0 \rightarrow \pi^+ l^- \nu$ @ Belle

Source	Error (Limit) [%]	
	Tagged [%]	Untagged
Tracking efficiency	0.4	2.0
Pion identification	–	1.3
Lepton identification	1.0	2.4
Kaon veto	0.9	–
Continuum description	1.0	1.8
Tag calibration and $N_{B\bar{B}}$	4.5 (2.0)	2.0 (1.0)
$X_u l \nu$ cross-feed	0.9	0.5 (0.5)
$X_c l \nu$ background	–	0.2 (0.2)
Form factor shapes	1.1	1.0 (1.0)
Form factor background	–	0.4 (0.4)
Total	5.0	4.5
(reducible, irreducible)	(4.6, 2.0)	(4.2, 1.6)

## $B \rightarrow X_u l \nu$ @ Belle

Source	Error on $\mathcal{B}$ (irreducible limit)
$\mathcal{B}(D^{(*)} l \nu)$	1.2 (0.6)
Form factors ( $D^{(*)} l \nu$ )	1.2 (0.6)
Form factors & $\mathcal{B}(D^{(**)} l \nu)$	0.2
$B \rightarrow X_u l \nu$ (SF)	3.6 (1.8)
$B \rightarrow X_u l \nu$ ( $g \rightarrow s\bar{s}$ )	1.5
$\mathcal{B}(B \rightarrow \pi/\rho/\omega l \nu)$	2.3
$\mathcal{B}(B \rightarrow \eta^{(\prime)} l \nu)$	3.2
$\mathcal{B}(B \rightarrow X_u l \nu)$ unmeasured/fragmentation	2.9 (1.5)
Continuum & Combinatorial	1.8
Secondaries, Fakes & Fit	1.0
PID& Reconstruction	3.1
BDT/Normalisation	3.1 (2.0)
Total	8.1
(Total reducible)	7.4
(Total irreducible)	3.2