

Studies of leptonic and semileptonic B decays at Belle and Belle II



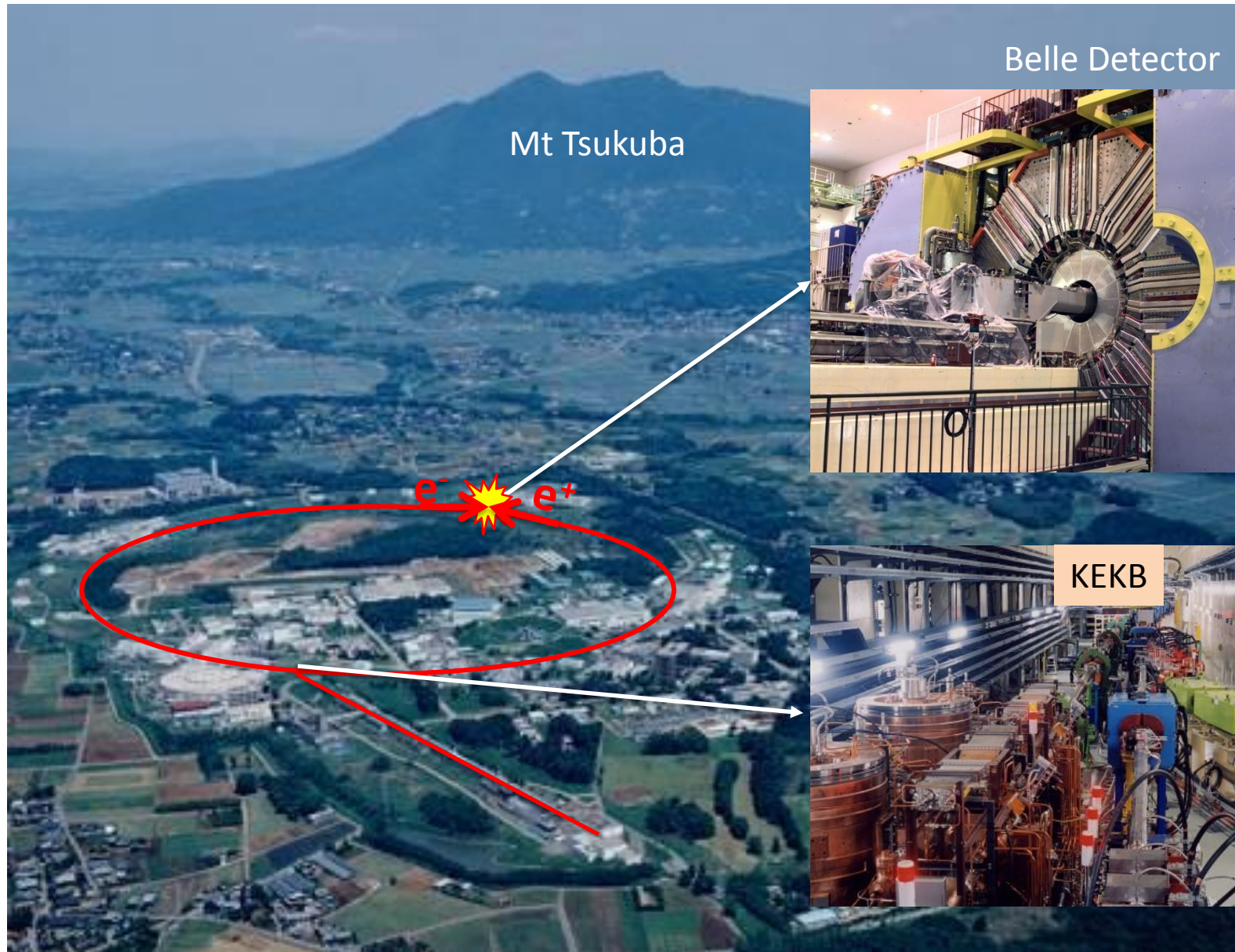
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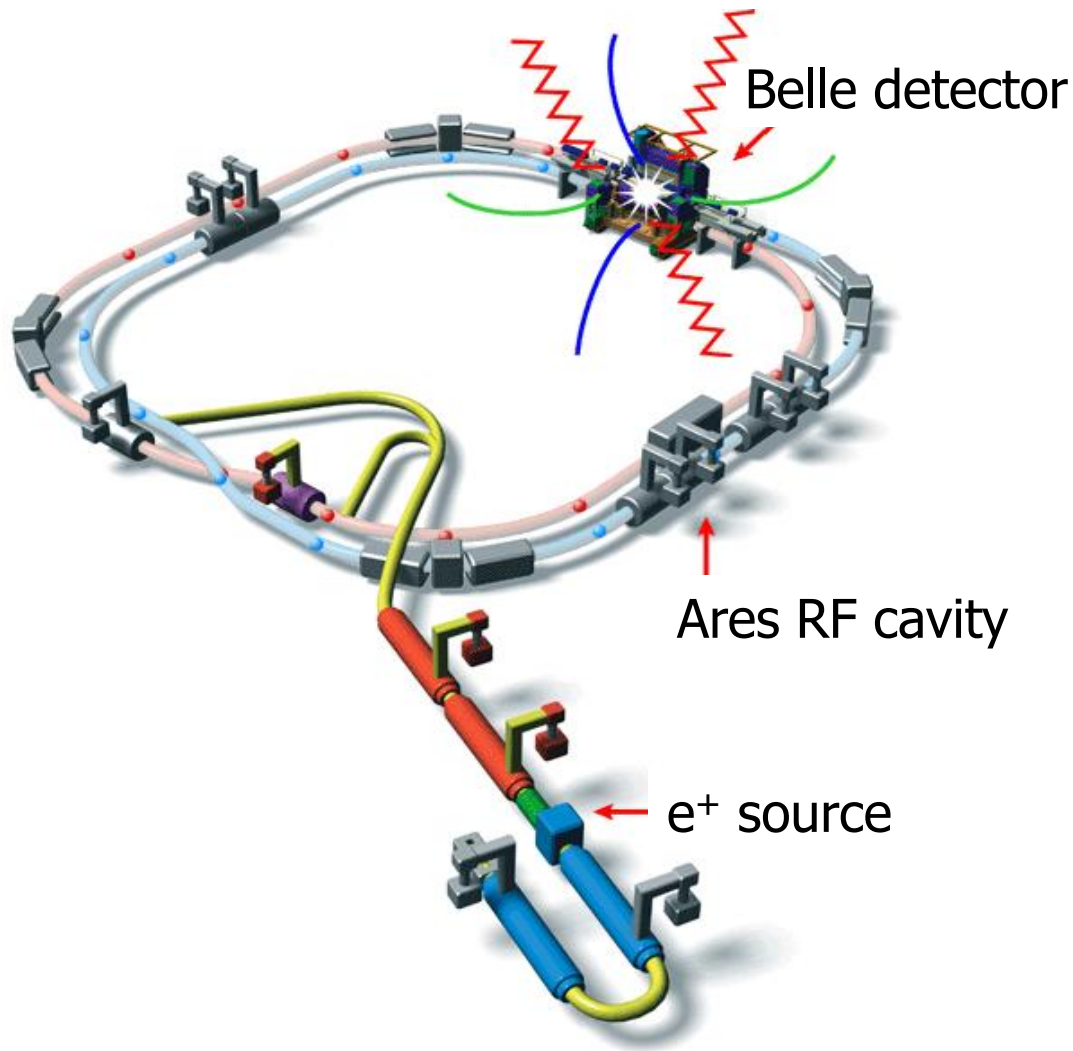
Outline

- KEKB and Belle
- Identification of $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$
- Measurements of $|V_{cb}|, |V_{ub}|$
- $R(D^{(*)})$ and $\mathcal{P}_\tau(D^*)$
- $\mathcal{B}(B^+ \rightarrow \tau^+ \nu)$ measurement

KEK Laboratory, Tsukuba Japan



The KEKB Collider



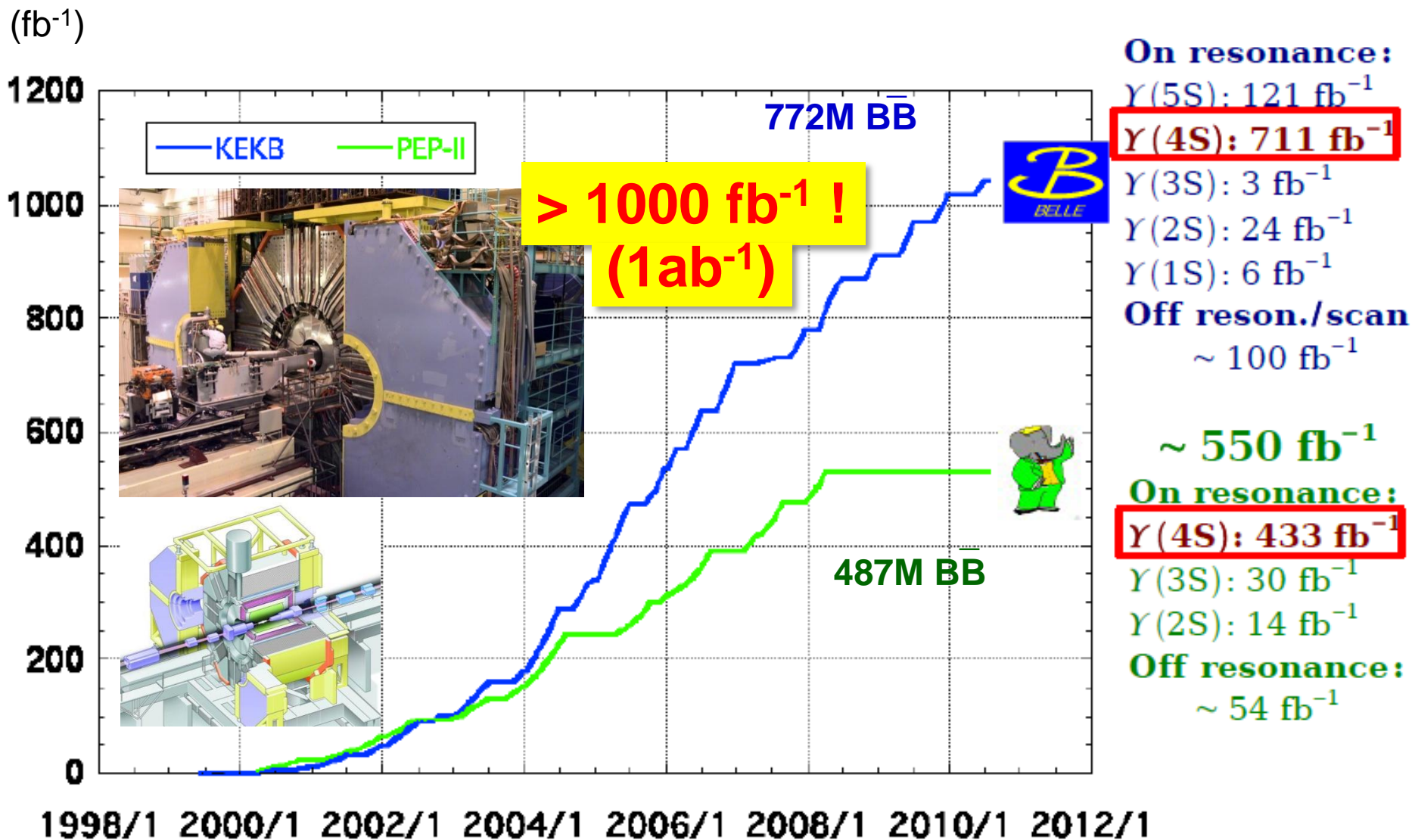
- Asymmetric energy collider
(8 GeV e^- x 3.5 GeV e^+)
 - $\sqrt{s} \approx m_{\Upsilon(4S)}$ ($\Upsilon(nS)$, $n=1,2,3,5$)
 - Lorentz boost: $\beta\gamma=0.425$
- Finite angle beam crossing
(22mrad)

Peak luminosity (WR!) :
 $2.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
=2x design value

First physics run on June 2, **1999**
Last physics run on June 30, **2010**
 $L_{\text{peak}} = 2.1 \times 10^{34} / \text{cm}^2 / \text{s}$

$$\int \mathcal{L} dt = 1.04 \text{ ab}^{-1}$$

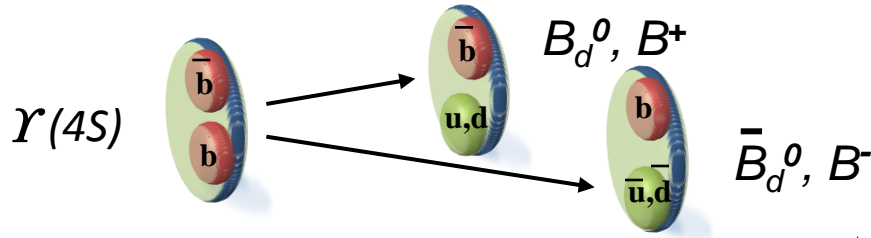
Data at KEKB/Belle



Physics at B factory

Accelerator

“B-Factory”, KEKB @, KEK



“on resonance” production
 $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B_d^0 \bar{B}_d^0, B^+ B^-$

$\sigma(e^+e^- \rightarrow B\bar{B}) \approx 1.1 \text{ nb}$ ($\sim 10^9$ $B\bar{B}$ pairs)

“continuum” production

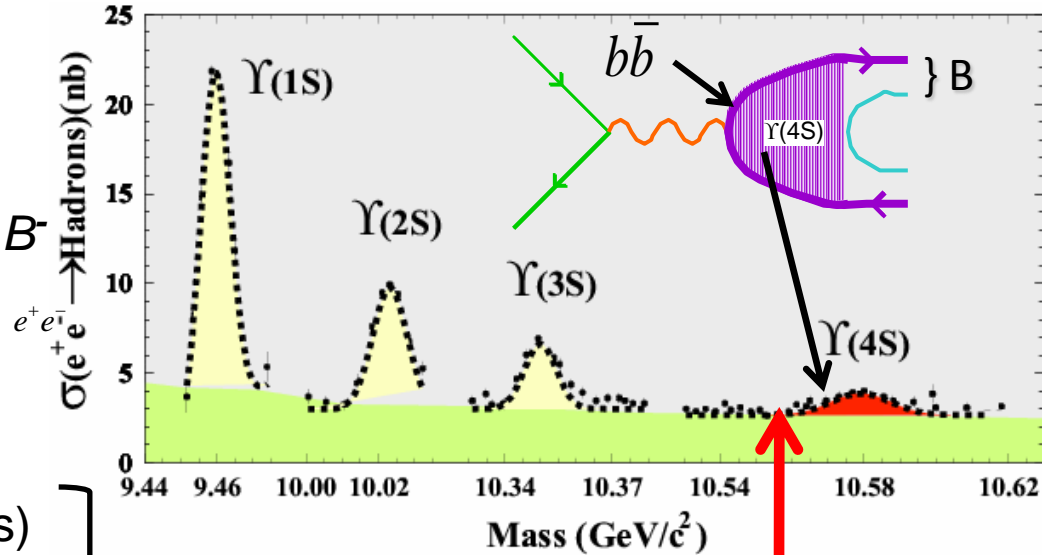
$\sigma(e^+e^- \rightarrow c\bar{c}) \approx 1.3 \text{ nb}$ ($\sim 1.3 \times 10^9$ $X_c \bar{Y}_c$ pairs)

$\tau^+ \tau^-$ production

$\sigma(e^+e^- \rightarrow \tau^+ \tau^-) \approx 0.9 \text{ nb}$ ($\sim 0.9 \times 10^9$ $\tau^+ \tau^-$ pairs)

Running at $\Upsilon(nS)$, e.g. $\Upsilon(5S) \rightarrow (B_s \bar{B}_s)$

Belle $\int \mathcal{L} dt \approx 1020 \text{ fb}^{-1}$



$B\bar{B}$ threshold

Variety of Physics

Primary goal: search for and study of CP violation in weak decays of B meson

DONE !

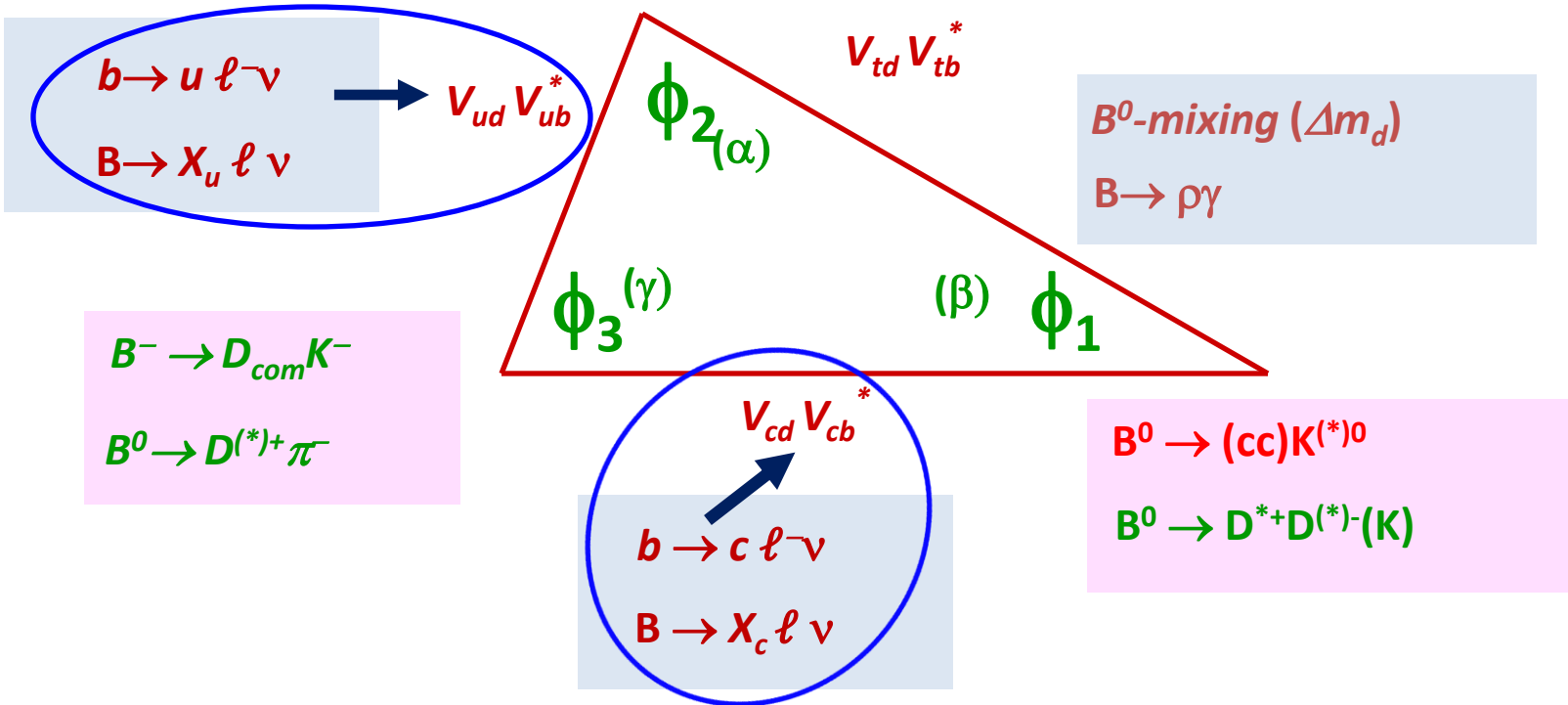
Complete Test of KM & SM

Measurements of CKM

$$B \rightarrow \pi\pi, \rho\pi, \rho\rho$$

Determination of UT

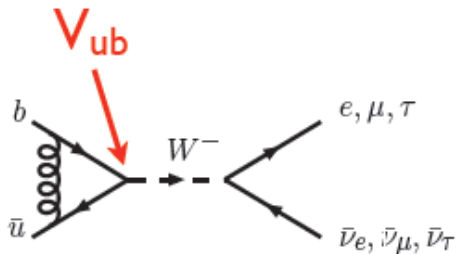
LQCD: important roles



B experiments can provide all measurements !

Measurements of $|V_{ub}|$ and $|V_{cb}|$

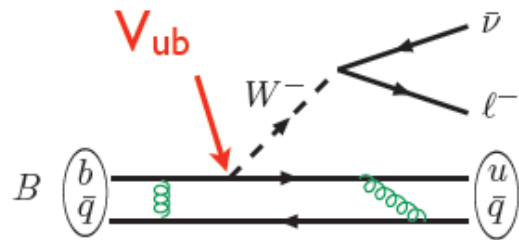
Leptonic



Helicity suppressed

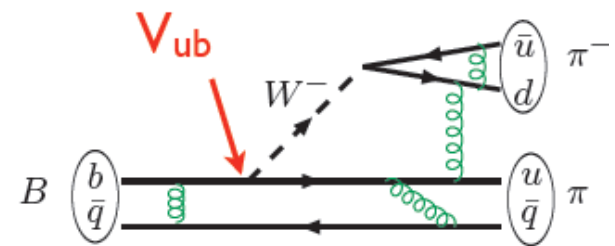
Experimentally difficult

Semileptonic



Leptonic and hadronic currents factorize

Hadronic



Complex QCD interactions

Theoretically challenging

Semileptonic B -decays provide a clean environment

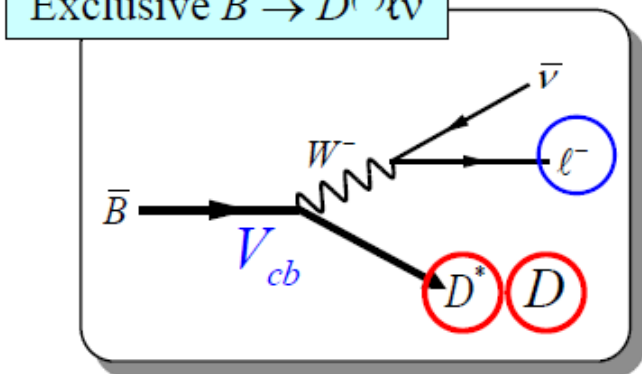
$$B \rightarrow D^{(*)} \ell \nu$$

$$B \rightarrow \pi \ell \nu$$

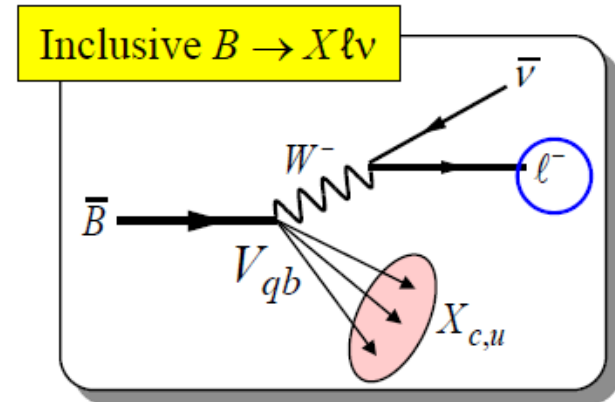
$$B \rightarrow X_c \ell \nu$$

$$B \rightarrow X_u \ell \nu$$

Exclusive $B \rightarrow D^{(*)} \ell \nu$



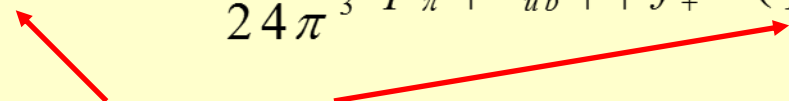
Inclusive $B \rightarrow X \ell \nu$



General strategy for $|V_{ub}|$, $|V_{cb}|$ measurements

- Measure branching fraction of channel(s) involving the associated transition (semileptonic decays used in most cases).
- Extract matrix element using theory input

Example for $|V_{ub}|$:

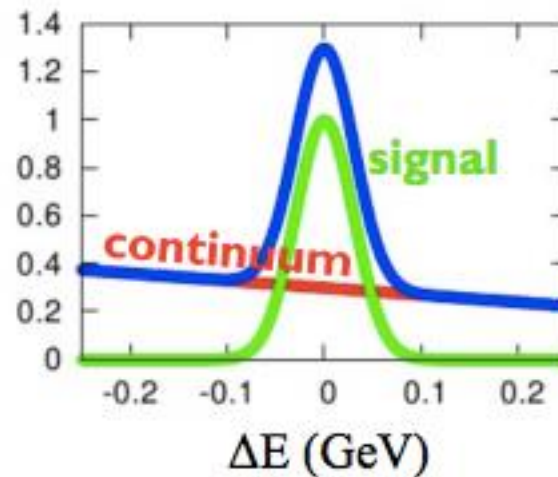
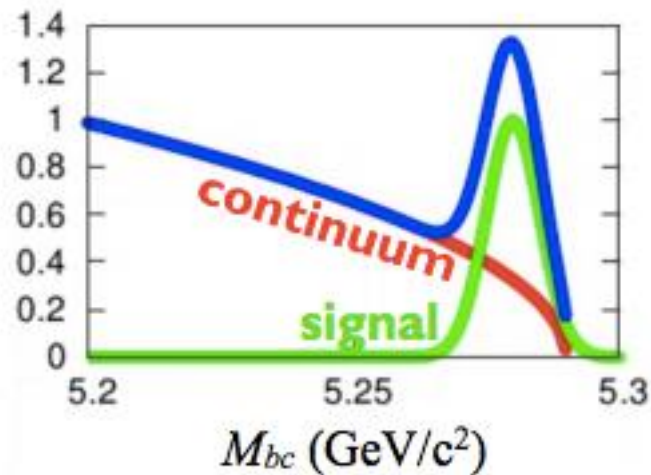
$$\frac{d\mathcal{B}(B \rightarrow \pi l \nu)}{dq^2} = \frac{G_F^2 \tau_B}{24 \pi^3} p_\pi^3 |V_{ub}|^2 |f_+^{B\pi}(q^2)|^2$$


Measure differential \mathcal{B} and form factors to extract $|V_{ub}|$.

Differentiate between exclusive and inclusive measurements, both differ in sample composition and type of theoretical input.

Identification of $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$

Kinematic variables are used to identify B decays:



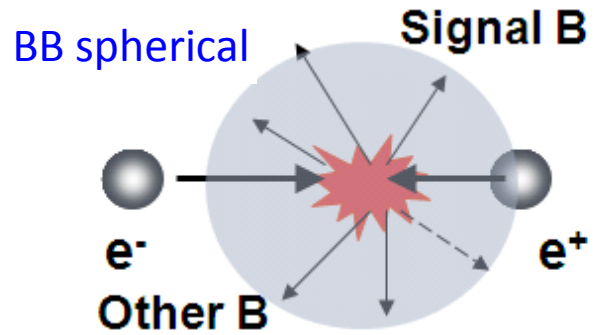
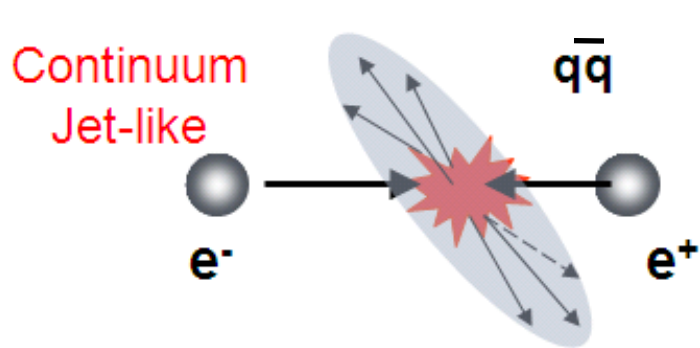
$$M_{bc} = \sqrt{(E_{beam}^*)^2 - (p_B^*)^2}$$

$$\Delta E = E_B^* - E_{beam}^*$$

E_B^* , p_B^* - energy, momentum of a reconstructed B -meson in the CM frame

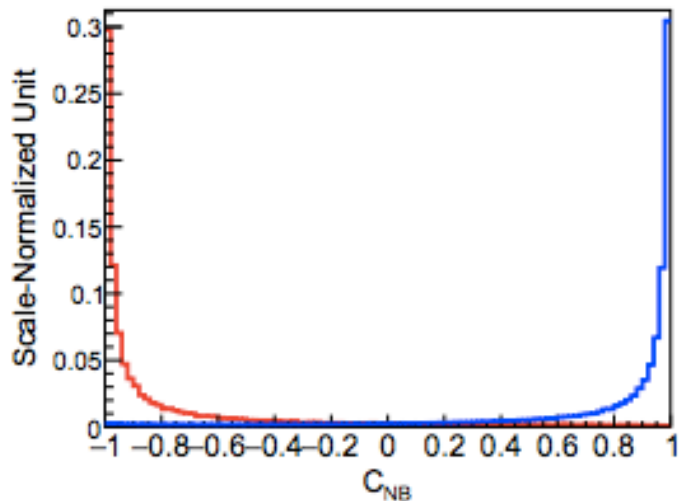
Background suppression

The dominant source of background $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$)

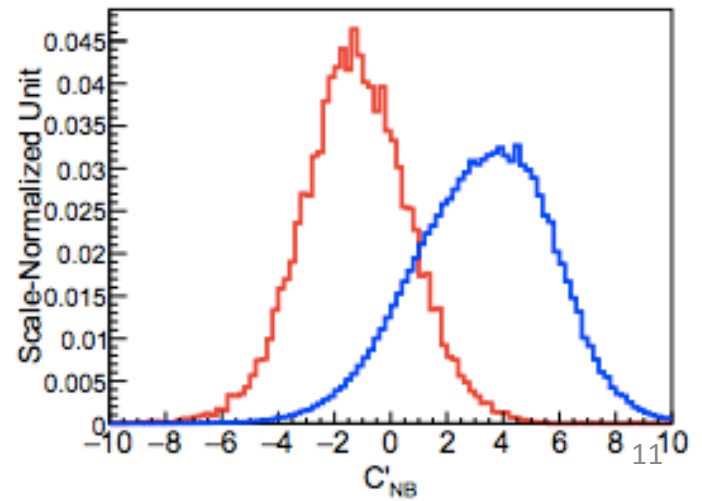


Continuum suppression: a multivariate analyzer based on

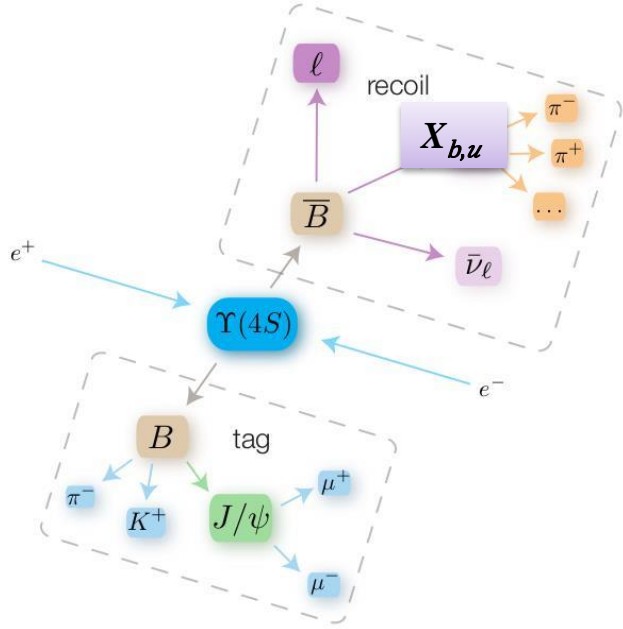
neural network



Fisher discriminant



Tagging techniques for $\Upsilon(4S)$ events



- Tagging provides:
 - Background suppression
 - Information on B_{sig} 4-momentum

$$p(B_{sig}) = p_{e^+e^-} - p(B_{tag})$$

PURITY



EFFICIENCY



Untagged

- No requirement on B_{tag}
- High efficiency, low purity

Semileptonic tag

- $B_{tag} \rightarrow D^{(*)} \ell \nu$
- Efficiency $\sim \mathcal{O}(0.2\%)$

Hadronic tag

- $B_{tag} \rightarrow$ hadrons
- Efficiency $\sim \mathcal{O}(0.1\%)$

$$p_\nu^2 = m_{miss}^2 = 0 \longrightarrow \cos \theta_{B-D^{(*)}\ell} = \frac{2E_{beam}^* E_{D^{(*)}\ell}^* - m_B^2 - M_{D^{(*)}\ell}^2}{2|\vec{p}_B^*| |\vec{p}_{D^{(*)}\ell}^*|}$$

NeuroBayes NN package
Efficiency $\sim \mathcal{O}(0.2-0.3\%)$

$$B \rightarrow D^* \ell \nu$$

$|V_{cb}|$: Exclusive decays

$B^0 \rightarrow D^* \ell^+ \nu$ with hadronic tag

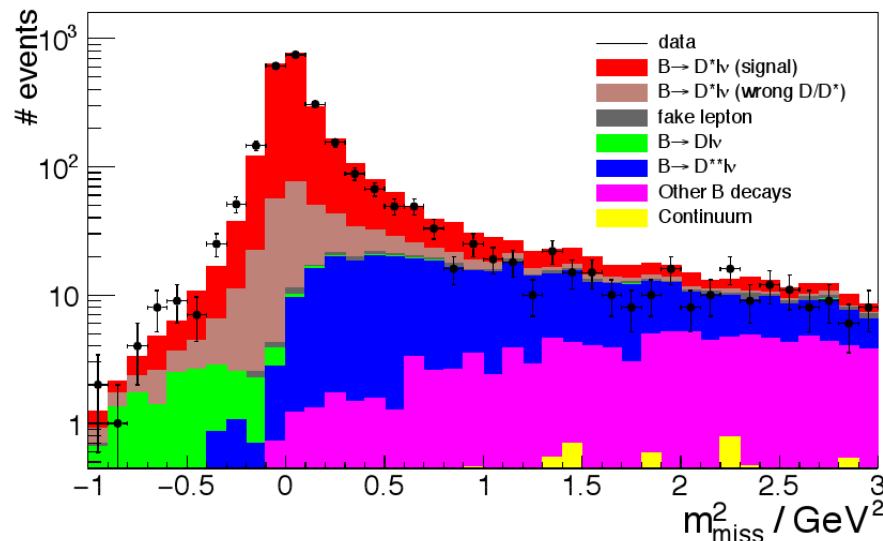
Belle, [arXiv:1702.01521]

Event reconstruction

- **Tag side:** B_{tag} reconstructed in over 1100 hadronic decay chains, 0.2% efficiency for neutral B mesons
- **Signal side:** B_{sig} assembled from an identified charged lepton (electron or muon) and a D^{*+} candidate
 - $D^{*+} \rightarrow D^0 \pi^+, D^+ \pi^0$ (98.4%)
 - $D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^+$ (26.3%), $D^+ \rightarrow K^- \pi^+ \pi^+$ (9.4)%

Signal is extracted from the missing mass distribution by an unbinned maximum likelihood fit

$$p_{\text{miss}} = p_\nu = p_{e^+e^-} - p_{\text{tag}} - p_{D^*} - p_\ell \quad m_{\text{miss}}^2 = p_{\text{miss}}^2 = p_\nu^2$$



ℓ	ν^{sig}
$e + \mu$	2374 ± 53
e	1306 ± 40
μ	1066 ± 34

$$\mathcal{B}(B^0 \rightarrow D^* \ell^+ \nu) = (4.95 \pm 0.11 \pm 0.22) \times 10^{-2}$$

Largest syst: tag calibration ($\sim 0.18 \times 10^{-2}$)¹⁴

$|V_{cb}|$ determination from exclusive $B \rightarrow D^* \ell \nu$

Differential decay ratio with respect to the variable w
in the limit of small lepton masses :

$$\frac{d\Gamma}{dw} = \frac{G_F^2 m_{D^*}^3}{48\pi^3} (m_B - m_{D^*})^2 \sqrt{w^2 - 1} \chi(w) \mathcal{F}^2(w) |V_{cb}|^2$$

w : the Lorentz boost of D^* meson in the B rest frame

$$w = \frac{P_B \cdot P_{D^*}}{m_B m_{D^*}} = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}} \quad (q = p_B - p_{D^*} = p_\ell + p_\nu)$$

- Parameterization of the form factors in the framework of Heavy Quark Effective Theory.

Model **CLN** (Caprini, Lellouch, Neubert, [Nucl.Phys. B530, 153(1998)])

$$\mathcal{F}(w) : \mathcal{F}(1), \rho^2, R_1(1), R_2(1)$$

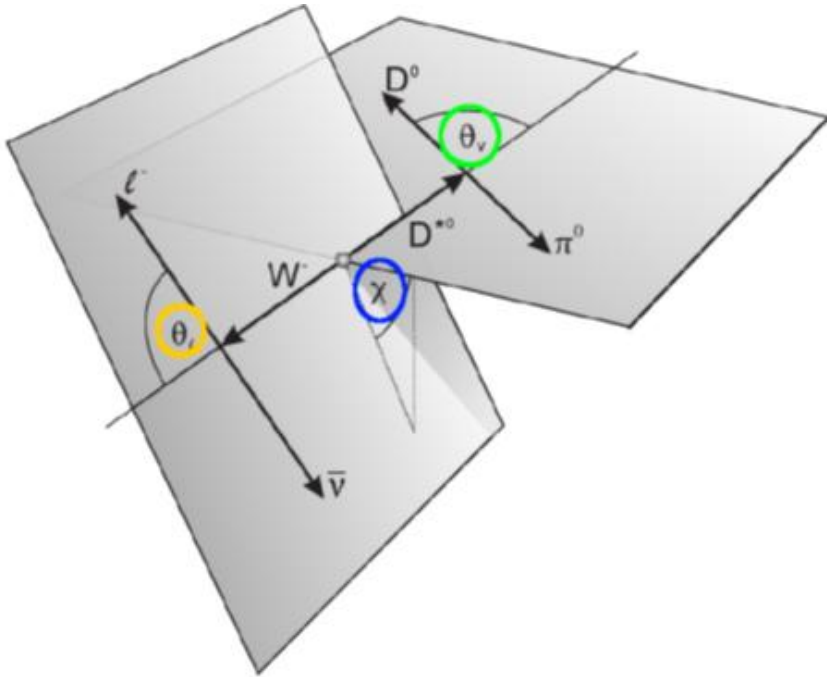
- The form factor normalization at $w = 1$ (zero-recoil) computed by Lattice QCD

$$\mathcal{F}(1) = 0.906 \pm 0.013 \quad [\text{PRD } 89, 114504(2014)]$$

Differential decay ratio is parametrized by 4 parameters: $|V_{cb}|, \rho^2, R_1(1), R_2(1)$

HQFT

Differential fit result

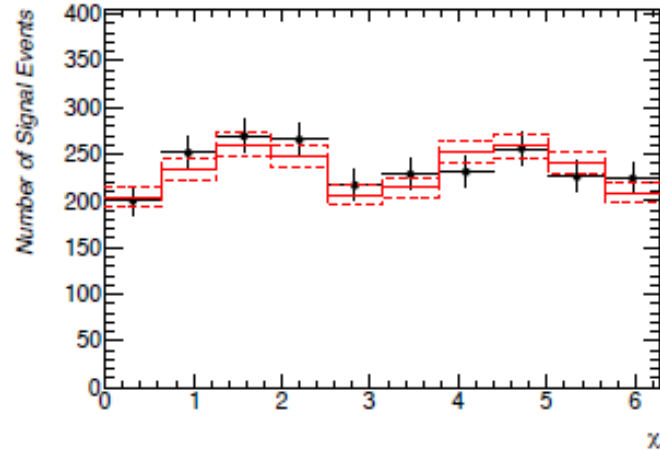
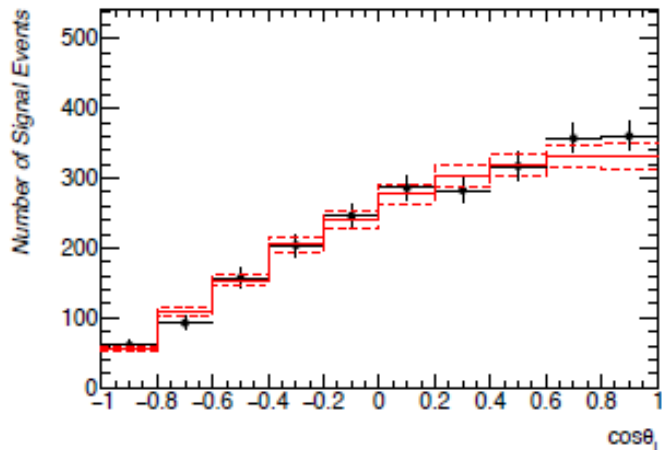
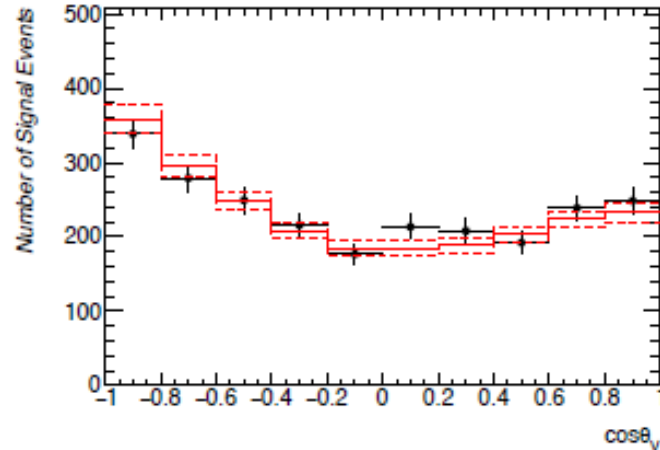
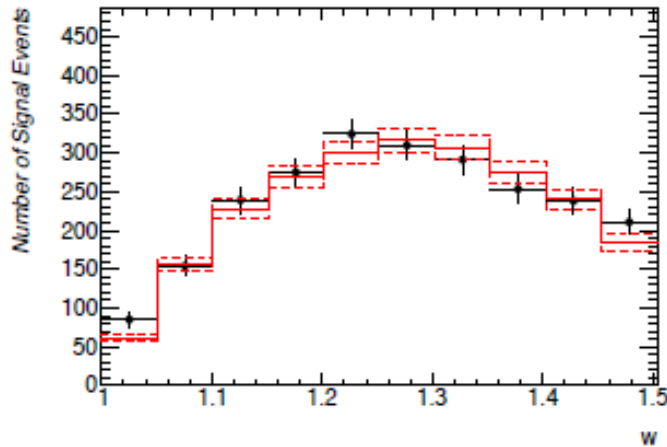


- Kinematics of the decay is characterized by four variables $w, \theta_e, \theta_v, \chi$
- In the experiment yield is extracted in 4x10 bins of $w, \cos \theta_e, \cos \theta_v, \chi$
- Fit to $w, \cos(\theta_e), \cos(\theta_v), \chi$

Variable	Bin	$\Delta\Gamma/\Delta x$ [10^{-15} GeV]
w	1	1.32 ± 0.11
	2	2.08 ± 0.15
	3	2.39 ± 0.15
	4	2.57 ± 0.16
	5	2.63 ± 0.15
	6	2.46 ± 0.14
	7	2.25 ± 0.14
	8	2.08 ± 0.13
	9	1.99 ± 0.12
	10	1.83 ± 0.13
$\cos \theta_v$	1	2.80 ± 0.19
	2	2.30 ± 0.14
	3	1.95 ± 0.13
	4	1.70 ± 0.11
	5	1.58 ± 0.11
	6	1.65 ± 0.11
	7	1.77 ± 0.12
	8	2.00 ± 0.14
	9	2.50 ± 0.16
	10	3.19 ± 0.25
$\cos \theta_e$	1	0.73 ± 0.07
	2	1.18 ± 0.09
	3	1.64 ± 0.11
	4	2.04 ± 0.13
	5	2.34 ± 0.14
	6	2.50 ± 0.15
	7	2.54 ± 0.15
	8	2.68 ± 0.16
	9	2.83 ± 0.20
	10	2.82 ± 0.24
χ	1	1.86 ± 0.16
	2	2.31 ± 0.15
	3	2.59 ± 0.16
	4	2.37 ± 0.15
	5	1.95 ± 0.13
	6	1.87 ± 0.15
	7	2.11 ± 0.15
	8	2.33 ± 0.15
	9	2.15 ± 0.15
	10	1.89 ± 0.16

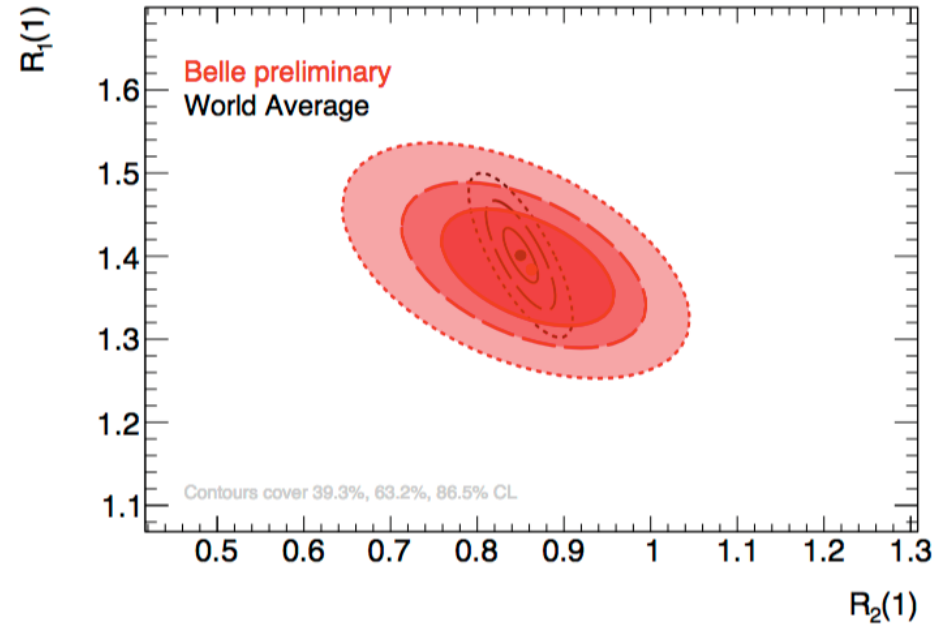
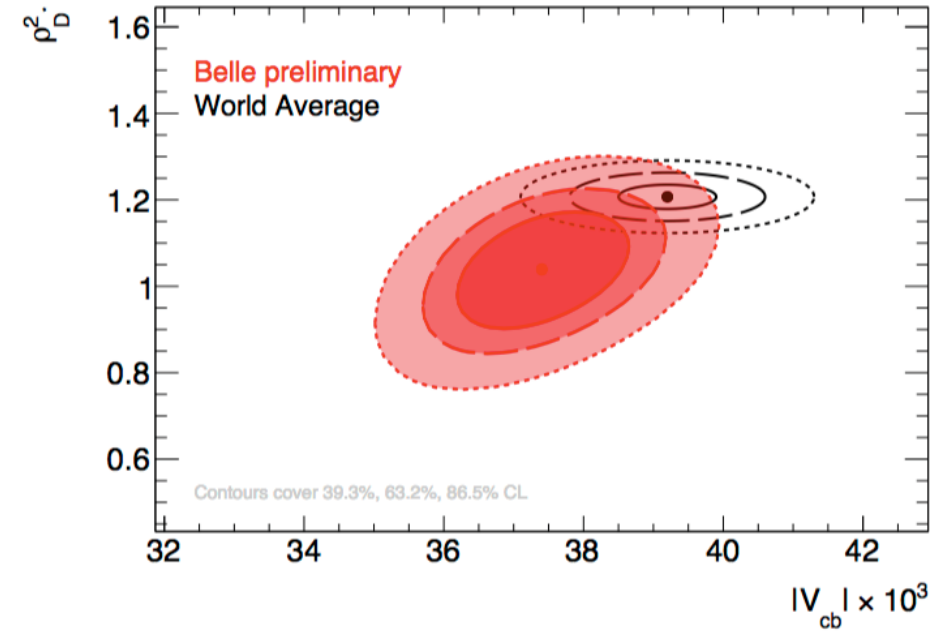
CLN fit to the differential widths

$$\chi^2 = \left(\nu_{\text{sig}} - \nu_{\text{sig}}^{\text{pred}} \right) C^{-1} \left(\nu_{\text{sig}} - \nu_{\text{sig}}^{\text{pred}} \right) + \left(h_{A1}(1) - h_{A1}^{\text{la}}(1) \right)^2 / \left(\sigma_{h_{A1}(1)}^{\text{la}} \right)^2$$



Points with error bars: Belle data,
 red histogram: fit result, dashed histogram: $\Delta\chi^2=1$ contour

CLN fit to the differential widths (2)



Parameter	This result	World Average
$ V_{cb} \times 10^3$	37.4 ± 1.3	39.2 ± 0.7
$\rho_{D^*}^2$	1.03 ± 0.13	1.21 ± 0.03
$R_1(1)$	1.38 ± 0.07	1.40 ± 0.03
$R_2(1)$	0.87 ± 0.10	0.85 ± 0.02

$$C = \begin{pmatrix} 1 & 0.41 & -0.20 & -0.14 \\ 0.41 & 1 & 0.19 & -0.86 \\ -0.20 & 0.19 & 1 & -0.46 \\ -0.14 & -0.86 & -0.46 & 1 \end{pmatrix}$$

Preliminary!

$$B \rightarrow D\ell v$$

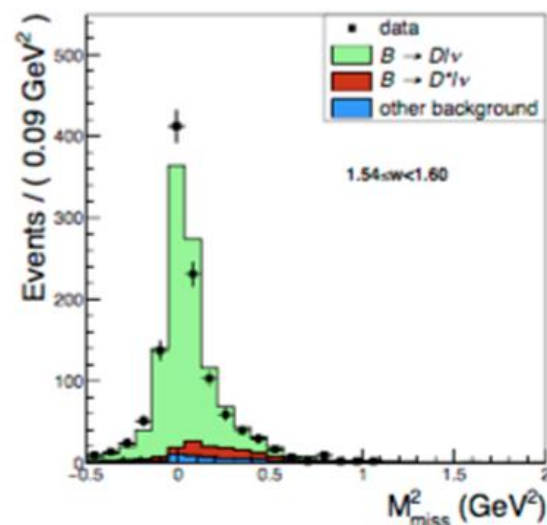
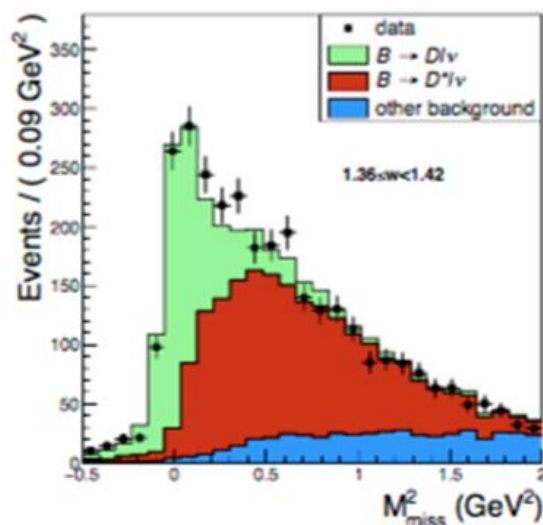
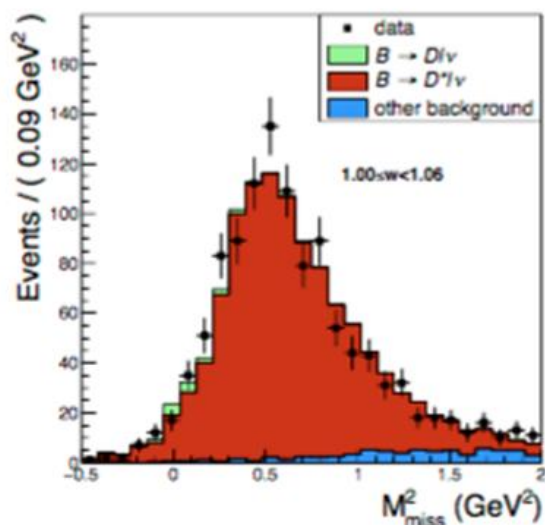
Exclusive $B \rightarrow D \ell \nu$ with hadronic tag

Event reconstruction

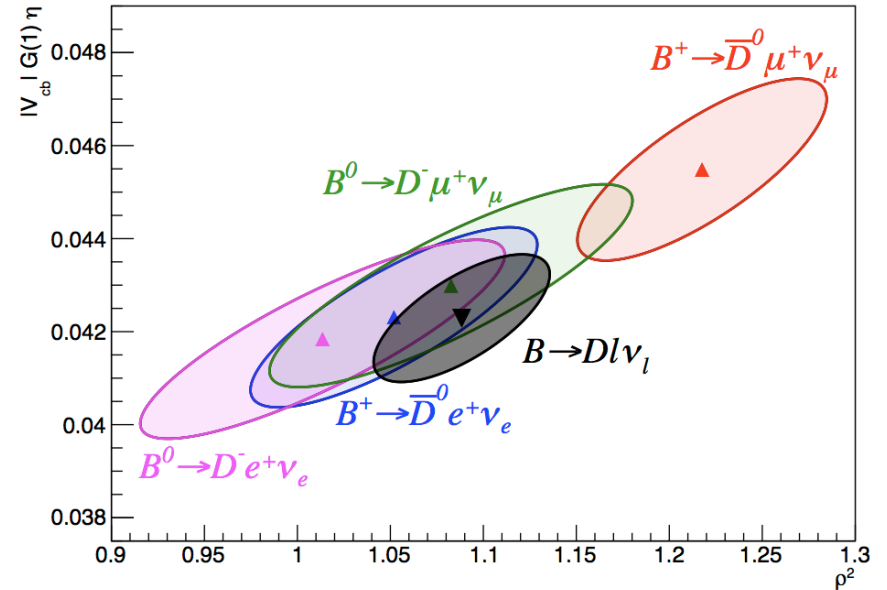
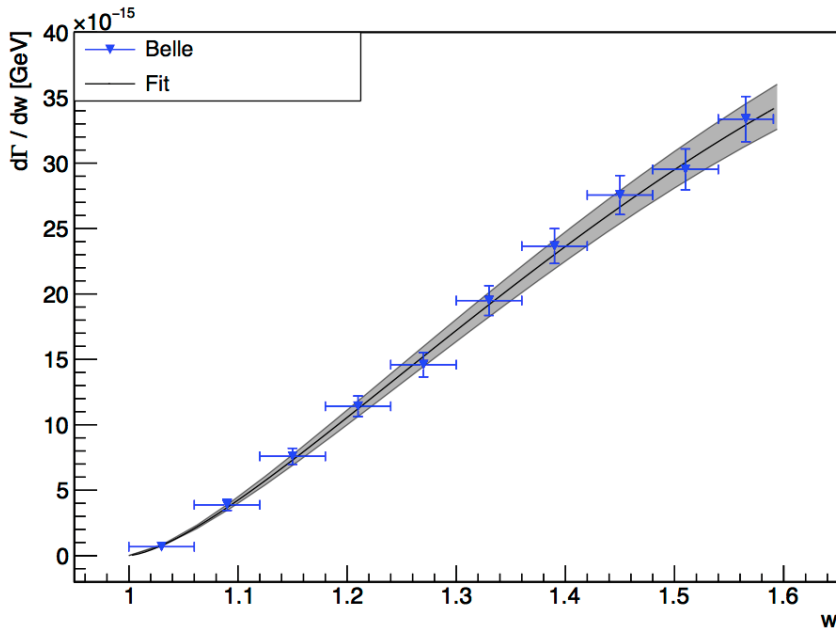
Belle, [Phys.Rev. D93, 032006 (2016)]

- Identical event reconstruction method
- *Signal side*: 15 D^- and 17 D^0 modes are used
- Signal extraction from M^2_{miss} in 10 bins of w
- $16\,992 \pm 192$ signal events
($5\,150 \pm 95$ B^0 events,
 $11\,843 \pm 167$ B^+ events)

Sample	Signal yield	B [%]
$B^0 \rightarrow D^- e^+ \nu_e$	$2848 \pm 72 \pm 17$	$2.44 \pm 0.06 \pm 0.12$
$B^0 \rightarrow D^- \mu^+ \nu_\mu$	$2302 \pm 63 \pm 13$	$2.39 \pm 0.06 \pm 0.11$
$B^+ \rightarrow \bar{D}^0 e^+ \nu_e$	$6456 \pm 126 \pm 66$	$2.57 \pm 0.05 \pm 0.13$
$B^+ \rightarrow \bar{D}^0 \mu^+ \nu_\mu$	$5386 \pm 110 \pm 51$	$2.58 \pm 0.05 \pm 0.13$
$B^0 \rightarrow D^- \ell^+ \nu_\ell$	$5150 \pm 95 \pm 29$	$2.39 \pm 0.04 \pm 0.11$
$B^+ \rightarrow \bar{D}^0 \ell^+ \nu_\ell$	$11843 \pm 167 \pm 120$	$2.54 \pm 0.04 \pm 0.13$
$B \rightarrow D \ell \nu_\ell$	$16992 \pm 192 \pm 142$	$2.31 \pm 0.03 \pm 0.11$



CLN fit to the differential widths



	$B^+ \rightarrow \bar{D}^0 e^+ \nu_e$	$B^+ \rightarrow \bar{D}^0 \mu^+ \nu_\mu$	$B^0 \rightarrow D^- e^+ \nu_e$	$B^0 \rightarrow D^- \mu^+ \nu_\mu$	$B \rightarrow D l \nu_\ell$
$\eta_{EW}G(1) V_{cb} [10^{-3}]$	42.31 ± 1.94	45.48 ± 1.96	41.84 ± 2.14	42.99 ± 2.18	42.29 ± 1.37
ρ^2	1.05 ± 0.08	1.22 ± 0.07	1.01 ± 0.10	1.08 ± 0.10	1.09 ± 0.05
Correlation	0.81	0.77	0.85	0.84	0.69
$\eta_{EW} V_{cb} [10^{-3}]$	40.14 ± 1.86	43.15 ± 1.89	39.69 ± 2.05	40.78 ± 2.09	40.12 ± 1.34
χ^2/n_{df}	2.19/8	2.71/8	9.65/8	4.36/8	4.57/8
Prob.	0.97	0.95	0.29	0.82	0.80

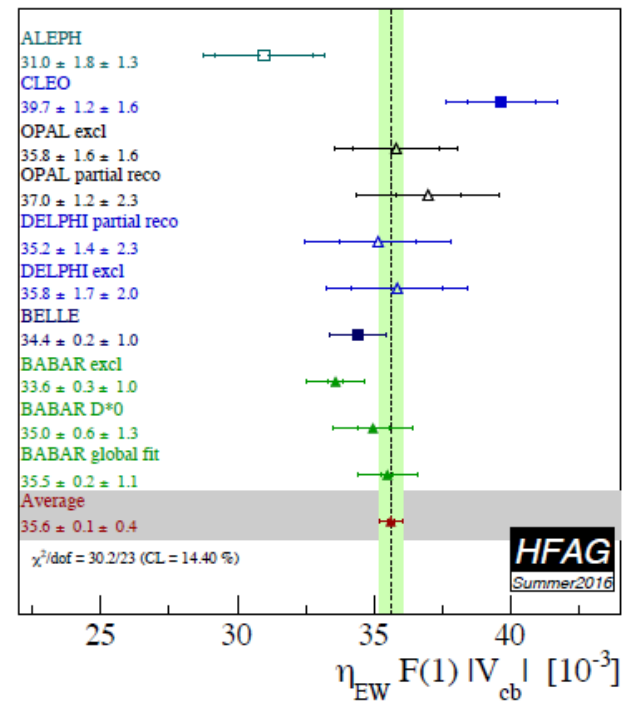
Exclusive Average

$B \rightarrow D^* \ell \nu$

HFAG summer 2016

$$|V_{cb}| = (38.71 \pm 0.47_{\text{exp}} \pm 0.59_{\text{th}}) \times 10^{-3}$$

- HFAG 2016: $\eta_{\text{EW}} \cdot \mathcal{F}(1) \cdot |V_{cb}| = (35.61 \pm 0.11_{\text{stat}} \pm 0.41_{\text{syst}}) \times 10^{-3}$
- LQCD: $\mathcal{F}(1) = 0.920 \pm 0.014$
- Leading EW correction: $\eta_{\text{EW}} = 1.015 \pm 0.005$



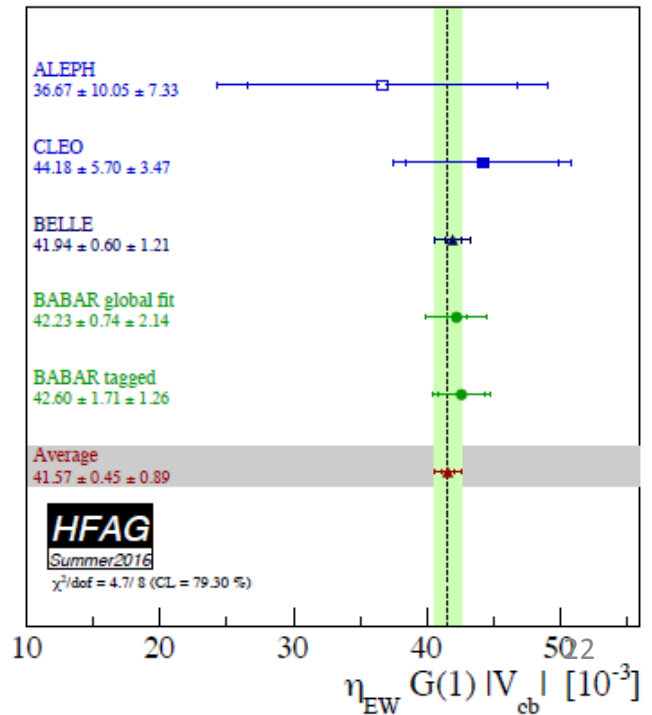
$B \rightarrow D \ell \nu$

$$|V_{cb}| = (39.18 \pm 0.94_{\text{exp}} \pm 0.31_{\text{th}}) \times 10^{-3}$$

- HFAG 2016: $\eta_{\text{EW}} \cdot \mathcal{G}(1) \cdot |V_{cb}| = (41.57 \pm 0.45_{\text{stat}} \pm 0.89_{\text{syst}}) \times 10^{-3}$
- LQCD: $\mathcal{G}(1) = 1.0541 \pm 0.0083$
- Leading EW correction: $\eta_{\text{EW}} = 1.0066 \pm 0.0016$

PDG 2017: average of the results
from $B \rightarrow D \ell \nu$ and $B \rightarrow D^* \ell \nu$

$$|V_{cb}| = (39.2 \pm 0.7) \times 10^{-3} \quad (\text{exclusive})$$



$|V_{cb}|$ inclusive measurements

$|V_{cb}|$ inclusive measurements

$B \rightarrow X_c e \nu$


At parton level, the decay rate for $b \rightarrow c \ell \nu \sim |V_{cb}|^2$ and can be calculated

- To relate measurements of semileptonic B -meson decays to $|V_{cb}|^2$ the parton-level expressions have to be corrected for the effects of non-perturbative effects.
- Operator Product Expansions (OPE)/Heavy-Quark-Expansions (HQE) successful tool to incorporate perturbative and nonperturbative QCD corrections.

The OPE/HQE parameters and $|V_{cb}|^2$ can be extracted from

the moments of the lepton spectrum ($\langle E_\ell^n \rangle$)
$$\langle E_\ell^n \rangle = \frac{1}{\Gamma_{E_\ell > E_{cut}}} \int_{E_\ell > E_{cut}} E_\ell^n \frac{d\Gamma}{dE_\ell} dE_\ell$$

or the moments of the X_c invariant mass squared spectrum ($\langle m_X^{2n} \rangle$)

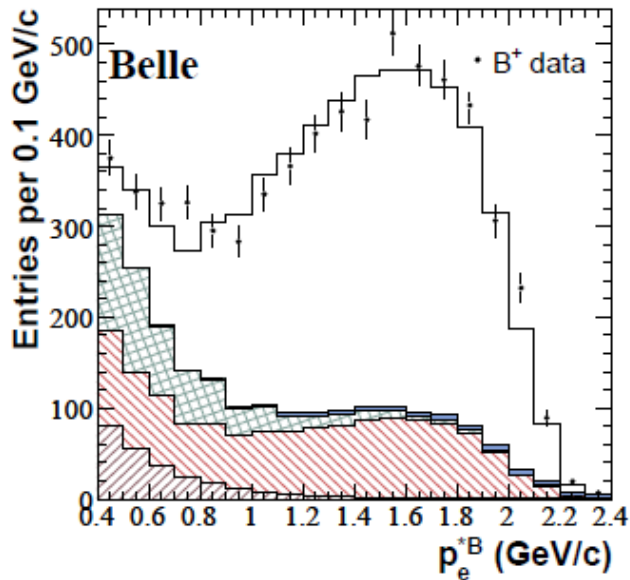
$$\langle m_X^{2n} \rangle = \frac{1}{\Gamma_{E_\ell > E_{cut}}} \int_{E_\ell > E_{cut}} m_X^{2n} \frac{d\Gamma}{dm_X^2} dm_X^2$$


Moments are measured with incremental cuts on the lepton momentum

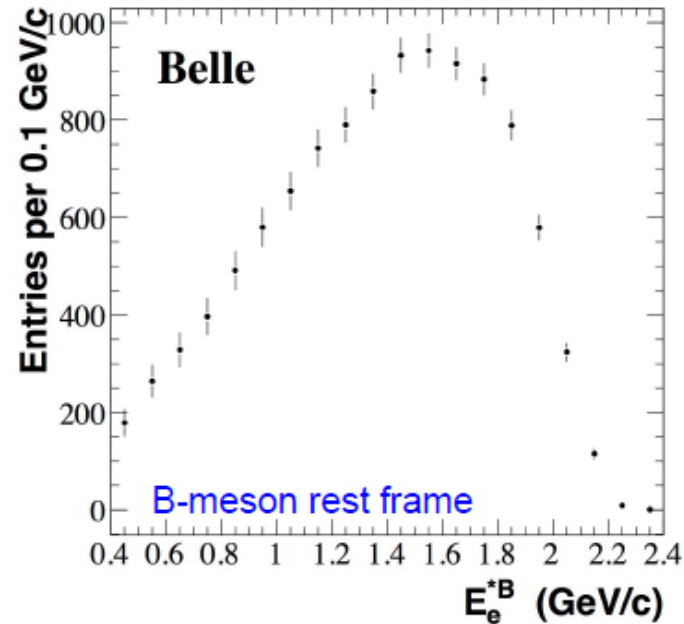
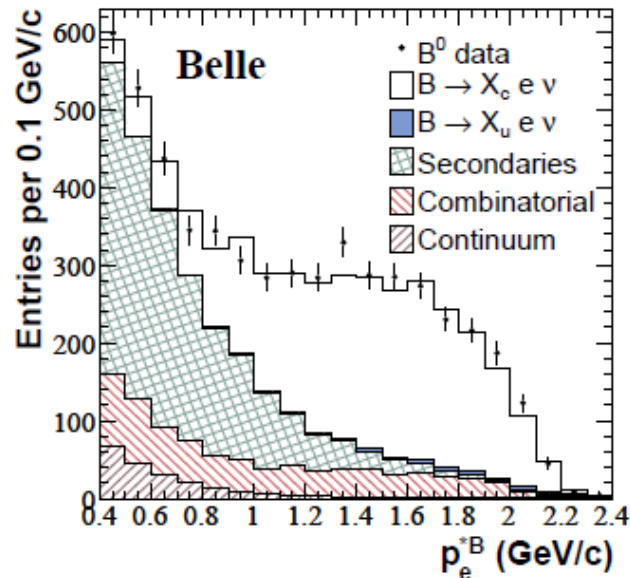
Lepton spectrum measurements

Inclusive semileptonic decays $B \rightarrow X_c e \nu$ (+ hadronic tag)

Belle, [Phys.Rev. D75, 032001 (2007)]

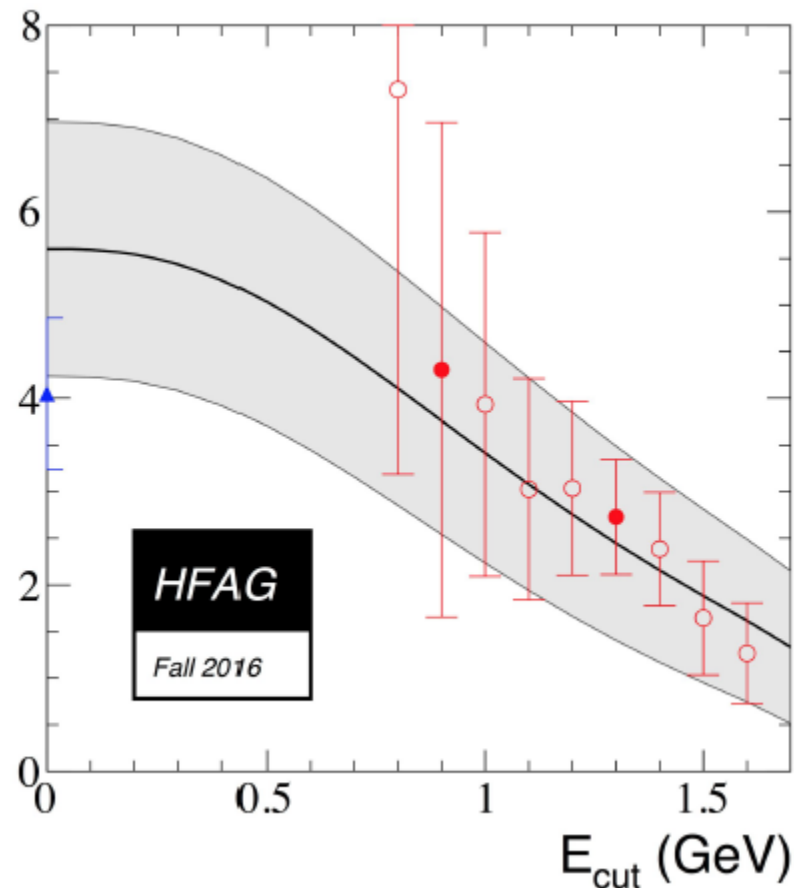
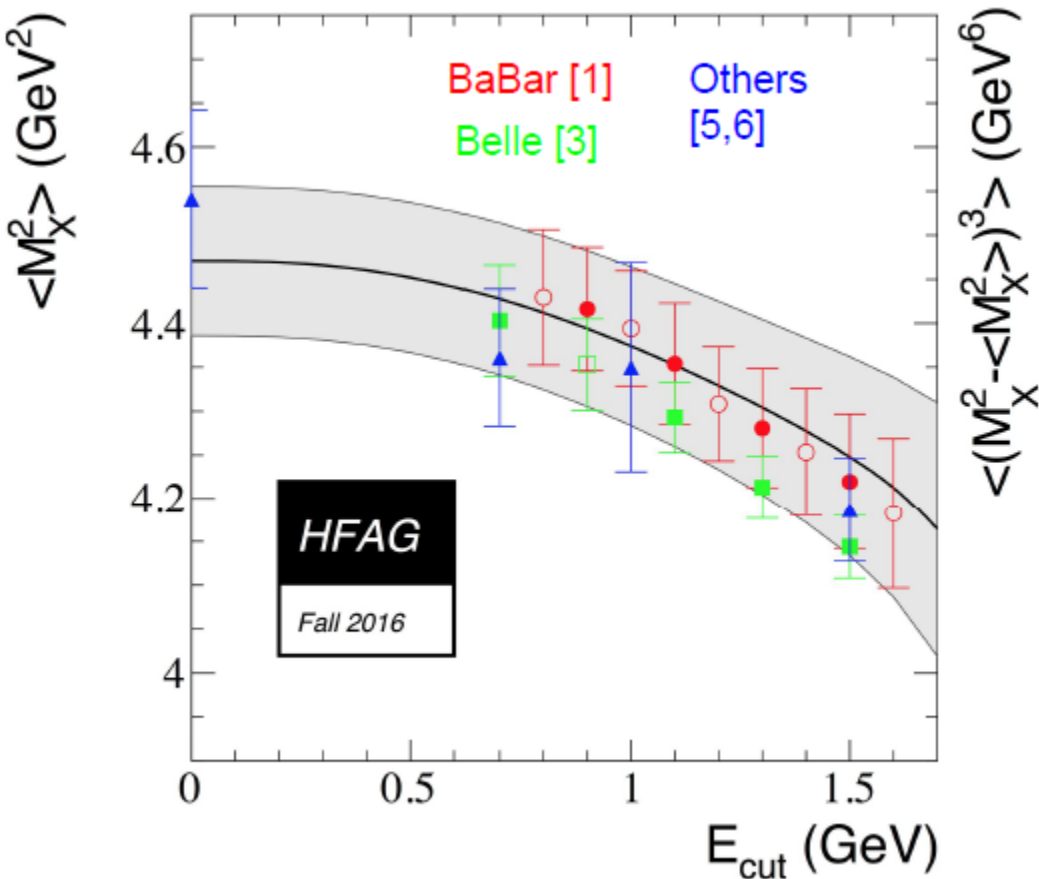


No new experimental results since 2010



Example of the X_c invariant mass moments

grey band: fit error (including theory errors)



$$\mathcal{B}(B \rightarrow X_c \ell \nu) = (10.65 \pm 0.16) \%$$

$$|V_{cb}| = (42.19 \pm 0.78) \times 10^{-3}$$

PDG 2017

$$|V_{cb}| = (42.2 \pm 0.8) \times 10^{-3}$$

(inclusive)

$$|V_{ub}|$$

Measuring $|V_{ub}|$

Exclusive measurement

- Charmless hadronic final states
- $B \rightarrow \pi \ell \nu$ most precise, but only 7% of all $B \rightarrow X_u \ell \nu$
- Others include $X_u = \rho, \omega, \eta$, multi-particle states, ...
- Needs LQCD or Light Cone Sum Rules (LCSR) as theory input

Pseudoscalar

$$\frac{d\mathcal{B}(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2 \tau_B}{24\pi^3} p_\pi^3 |V_{ub}|^2 |f_+^{B\pi}(q^2)|^2$$

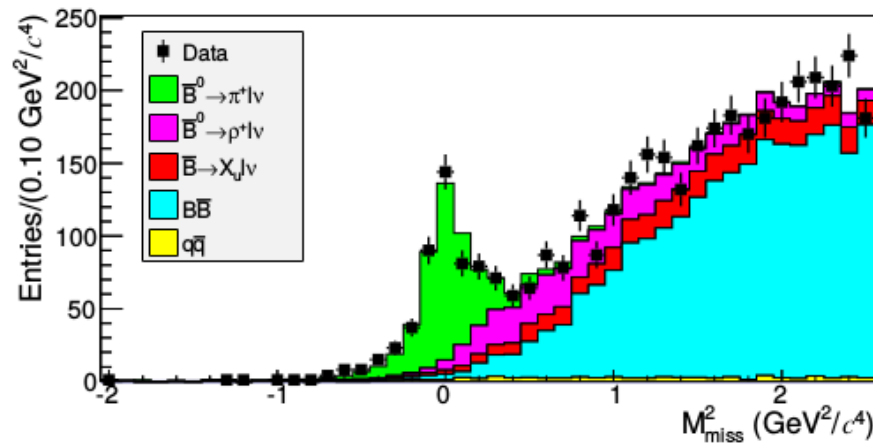
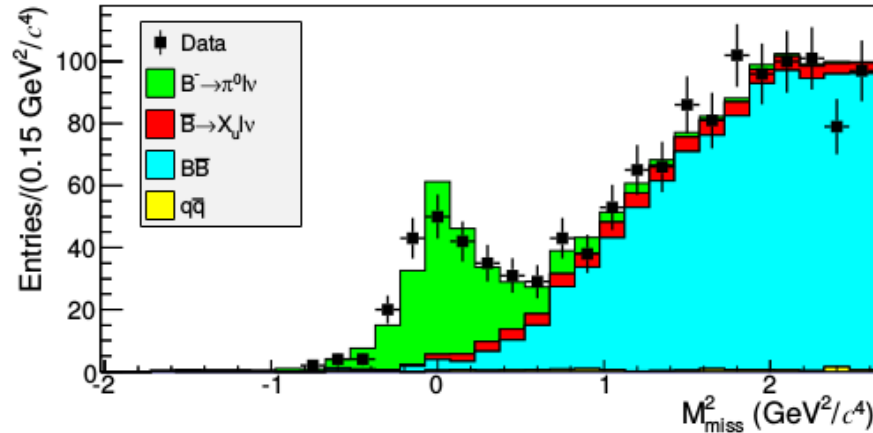
Vector (helicity basis)

$$\frac{d\mathcal{B}(B \rightarrow V \ell \nu)}{dq^2} = \frac{G_F^2 p_V q^2 \tau_B}{96\pi^3 m_B^2} |V_{ub}|^2 \left[|H_0(q^2)|^2 + |H_+(q^2)|^2 + |H_-(q^2)|^2 \right]$$

Experimental measurement of the branching fraction and theoretical input on form factors needed to determine $|V_{ub}|$

$B \rightarrow \pi \ell^+ \nu$ tagged at Belle

Belle, [Phys.Rev. D88, 032005 (2013)]

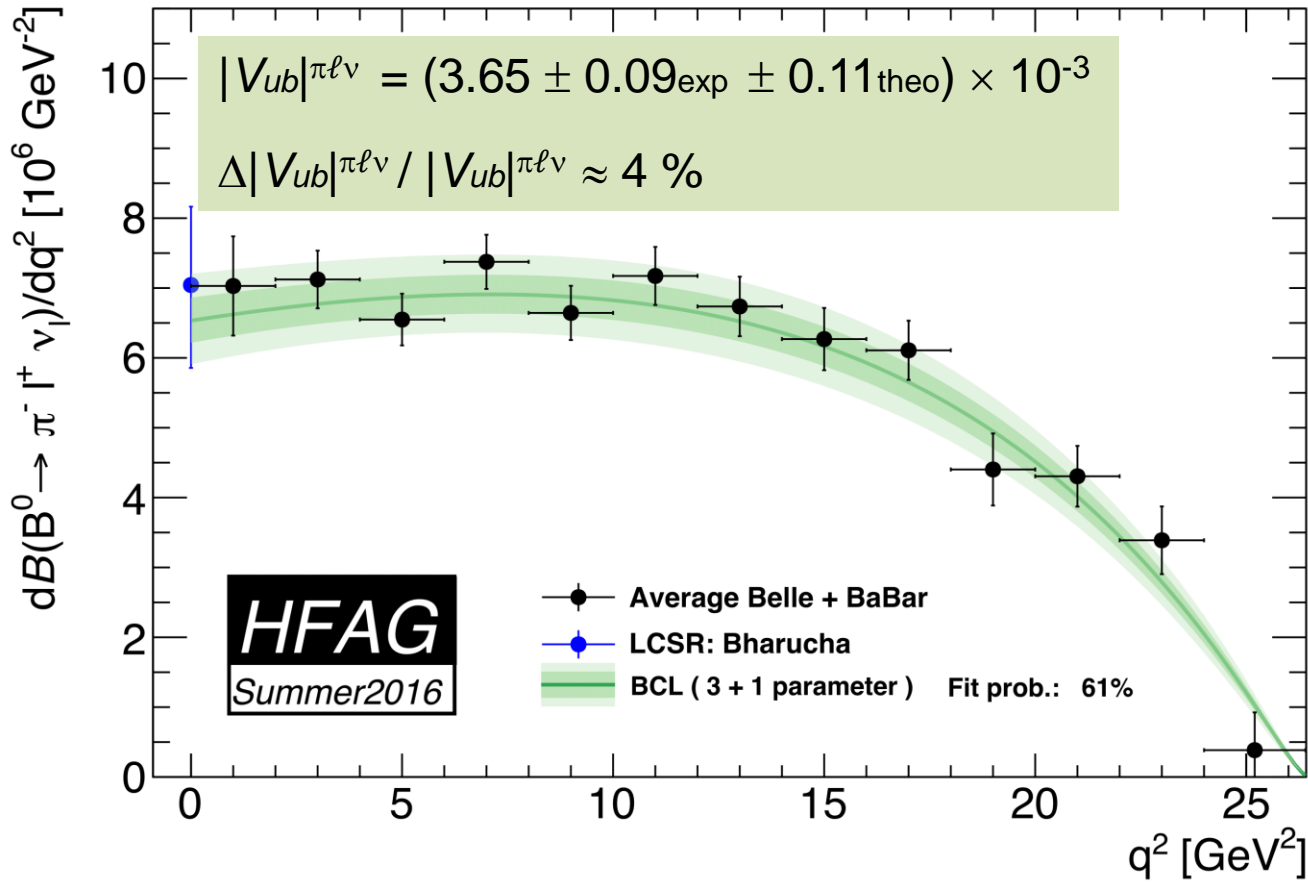


- Data sample: 711 fb^{-1}
- Signal candidates
 $N_{B^0} \approx 500 \pm 30$
 $N_{B^+} \approx 200 \pm 20$
- $d\mathcal{B}/dq^2$ spectrum in
 13 (7) bins for π^- (π^0)

B^+, B^0 combined result:

$$\mathcal{B}(B \rightarrow \pi \ell^+ \nu) = (1.49 \pm 0.08_{\text{stat}} \pm 0.07_{\text{sys}}) \times 10^{-4}$$

$B \rightarrow \pi \ell \nu$



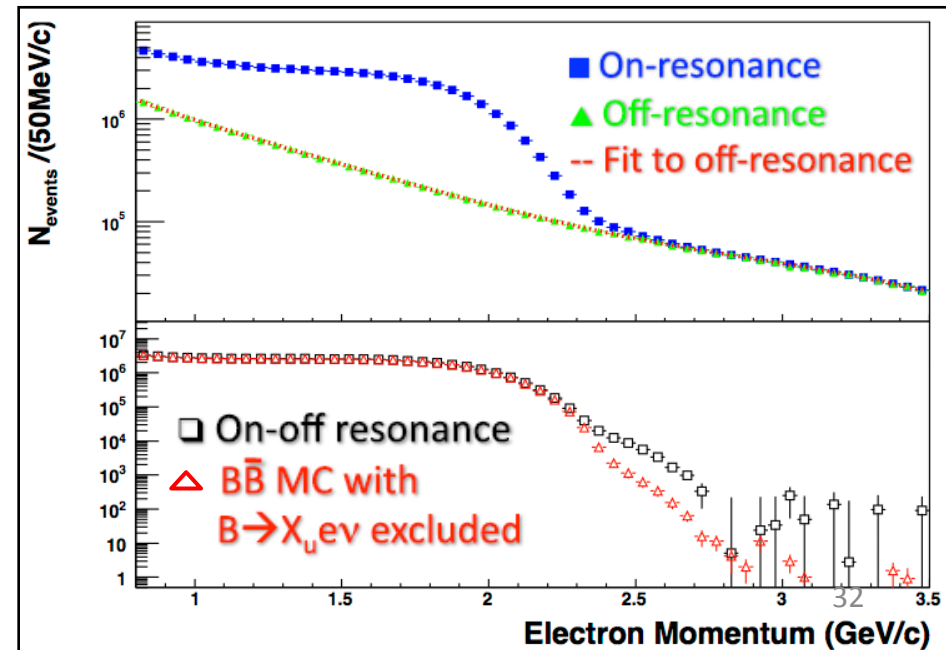
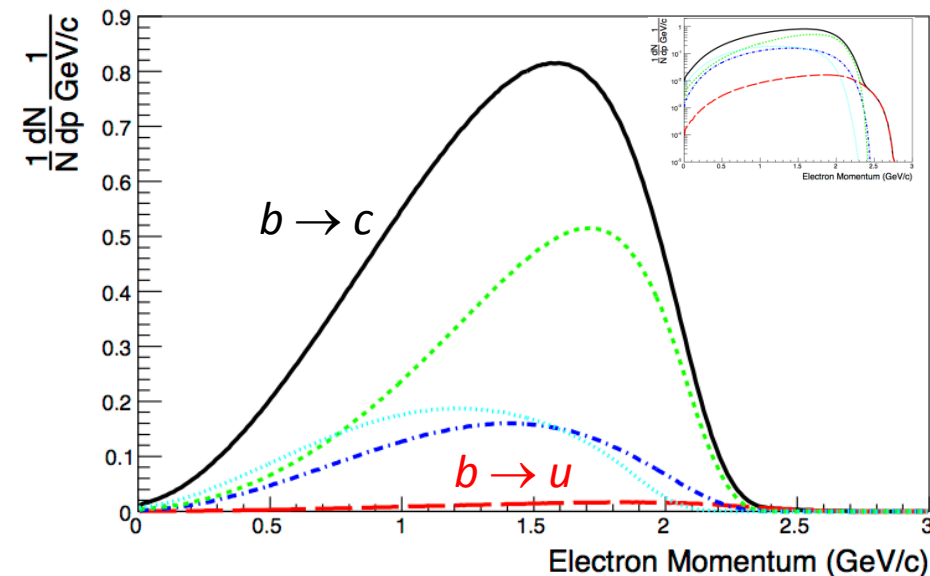
Optimal $|V_{ub}|$ extraction with simultaneous fit to: averaged data (full q^2) + averaged lattice + LCSR with model independent FF parametrization

Fit, data averaging: [F. Bernlochner, S. Duell, J. Dingfelder]
 LQCD averaging: [FLAG-3 review (arXiv:1607.00299)]
 LQCD: [Fermilab/MILC, Phys.Rev. D92 (2015) no.1, 014024]
 LQCD: [RBC/UKQCD, Phys.Rev. D91 (2015) no.7, 074510]
 LCSR: [A. Bharucha, JHEP 1205 (2012) 092]

$|V_{ub}|$ - inclusive measurements

Electron spectrum from B decays at $\Upsilon(4S)$

- $B \rightarrow X_c e \nu$ decays dominate ($\Gamma(B \rightarrow X_c e \nu) \approx 50 \Gamma(B \rightarrow X_u e \nu)$); $B \rightarrow X_u e \nu$ contribute a sizeable fraction only above the $b \rightarrow c$ kinematic endpoint, $E_e > 2.3$ GeV
 - Large contribution from $e^+e^- \rightarrow c\bar{c} \rightarrow eX$ decays; dedicated sample of data collected below BB threshold (off-resonance) needed
 - Additional contributions at lower energy from secondary processes $b \rightarrow c \rightarrow e$ and misidentified hadrons
- Statistical uncertainties on BB spectrum dominated by continuum subtraction
 - Region above 2.3 GeV shows clear contribution from $B \rightarrow X_u e \nu$ decays



Theoretical models and results

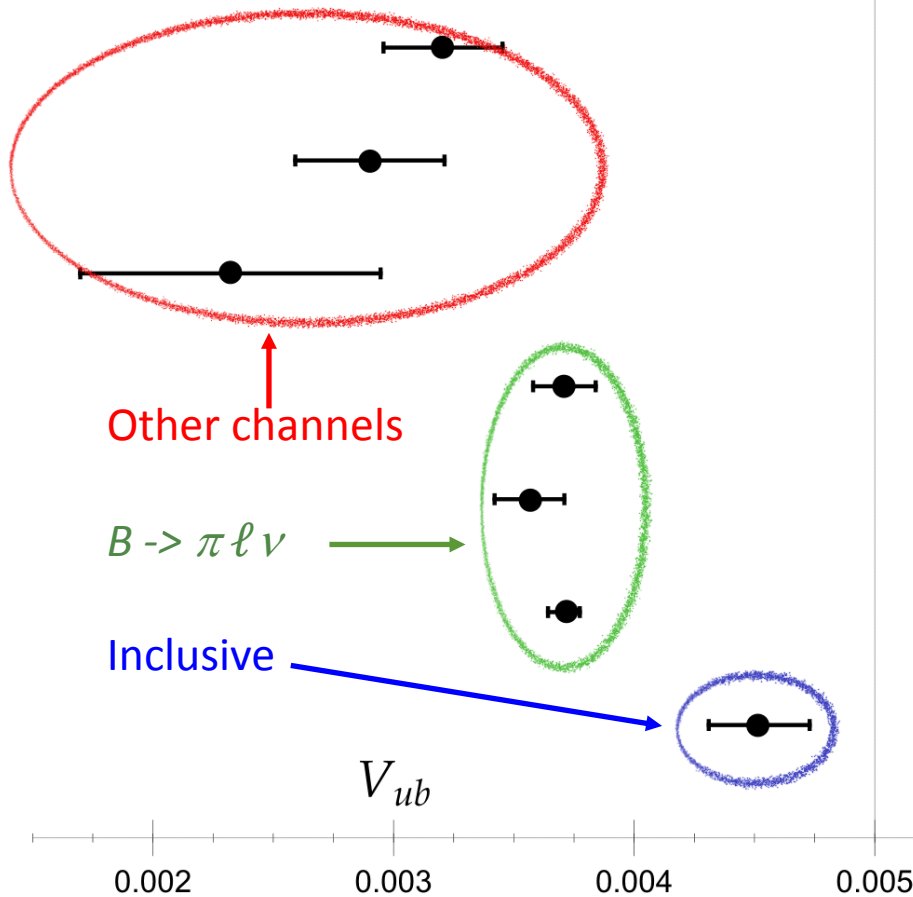
- The OPE calculation is only valid for partial rates that include large portions of the available phase space
 - near the endpoint non-perturbative shape functions (SF) are needed
 - different prescriptions different “models”
- **DN** DeFazio, and Neubert, JHEP 9906, 017 (1999)
- **BLNP** Bosh, Lange, Neubert, Paz, Nucl. Phys. B 699, 335 (2004)
- **GGOU** Gambino, Giordano, Ossola, Uraltsev, JHEP 908 10, 058 (2007)
- **DGE** Andersen, Gardi, JHEP 0601, 097 (2006)

PDG 2017 $|V_{ub}|$ (in units of 10^{-3}) from inclusive $B \rightarrow X_u \ell \nu$ measurements

	BLNP	GGOU	DGE
HFAG average	$4.45 \pm 0.16^{+21}_{-22}$	$4.51 \pm 0.16^{+12}_{-15}$	$4.52 \pm 0.16^{+15}_{-16}$

Overview of various $|V_{ub}|$ values

World Average



$B \rightarrow \rho l \nu$ (data + LCSR)

$B \rightarrow \omega l \nu$ (data + LCSR)

$B \rightarrow \eta l \nu$ (BaBar2012 + LCSR)

$B \rightarrow \pi l \nu$ (data + LCSR + LQCD)

CKMFitter – indirect

CKMFitter – direct

Inclusive (BLNP)

PDG 2017 (average results)

$$|V_{ub}| = (3.72 \pm 0.16) \times 10^{-3}$$

exclusive

$$|V_{ub}| = (4.49 \pm 0.23) \times 10^{-3}$$

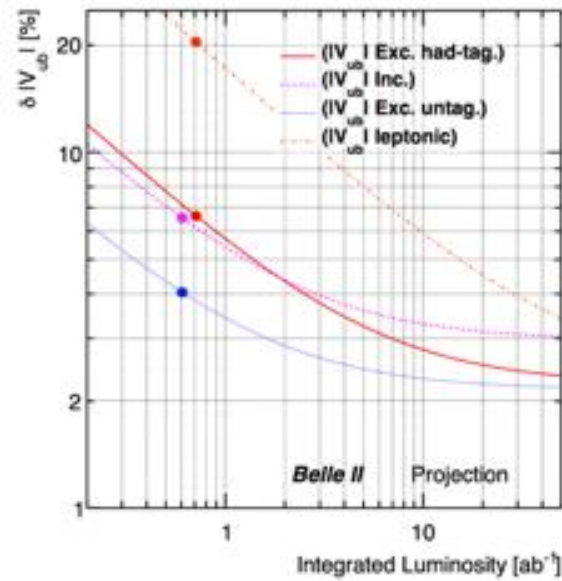
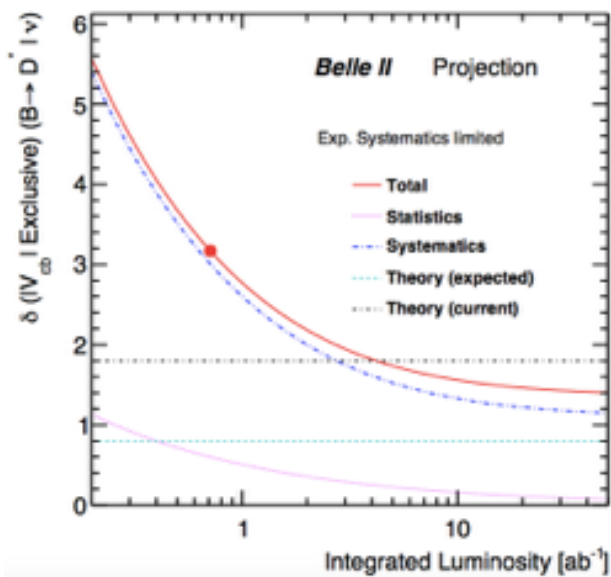
inclusive

$|V_{cb}|$, $|V_{ub}|$ measurements summary

- $|V_{cb}|$ and $|V_{ub}|$ are measured with different methods
- ✓ Inclusive $B \rightarrow X_c \ell \nu$, $B \rightarrow X_u \ell \nu$, Hadronic tag, Semileptonic tag, Untagged
- ✓ Exclusive $B \rightarrow D^{(*)} \ell \nu$, $B \rightarrow \pi \ell \nu$
- Inclusive-Exclusive tension in both $|V_{cb}|$ and $|V_{ub}|$ still exist

	Measurements (10^{-3})	$\delta V/V$	
2.8σ	$ V_{ub} $ Inc.	4.49 ± 0.23	5%
	$ V_{ub} $ Exc.	3.72 ± 0.16	4%
2.9σ	$ V_{cb} $ Inc.	42.2 ± 0.8	2%
	$ V_{cb} $ Exc.	39.2 ± 0.7	2%

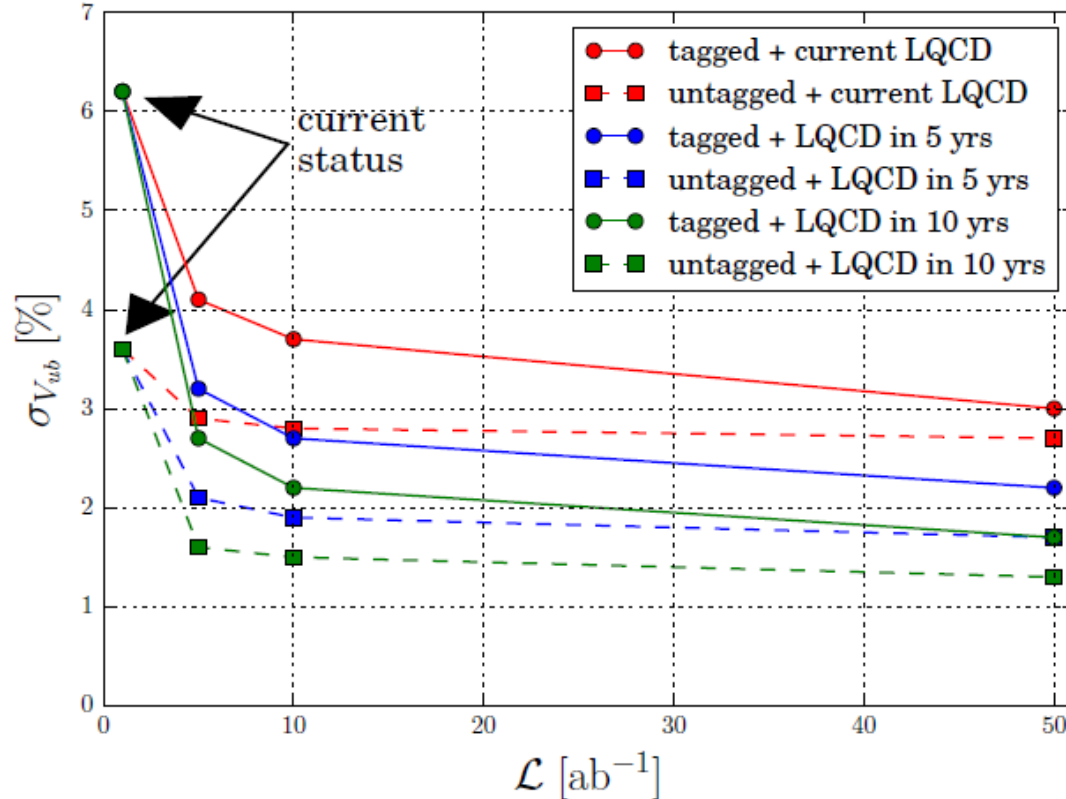
- Belle II will provide more precise measurements ([B2TiP](#))



Belle II: $|V_{ub}|$ from $B \rightarrow \pi \ell \nu$

B2TiP

Toy MC studies based on Belle II MC, LQCD forecasts estimated for 5, 10 and 50 ab^{-1}



$\delta|V_{ub}|$ estimates for 5, 10, 50 ab^{-1}
Tagged: 3.2, 2.7, 1.7 %
Untagged: 2.1, 1.9, 1.3 %

$$B \rightarrow D^{(*)} \tau \nu$$

New physics searches in $B \rightarrow D^{(*)}\tau\nu$ decay

SM extensions - **enhanced coupling to the third generation**

New physics could change \mathcal{B} and τ polarization (\mathcal{P}_τ)

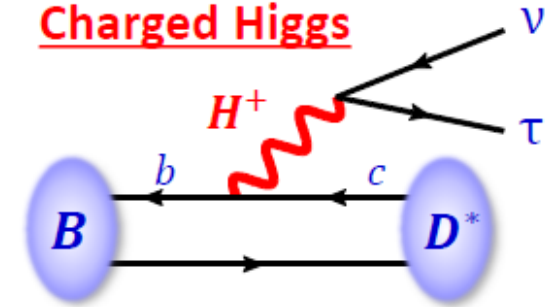
$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)} \quad (\ell = e, \mu)$$

Uncertainties are largely cancelled:
 V_{cb} , form factors, efficiency etc.

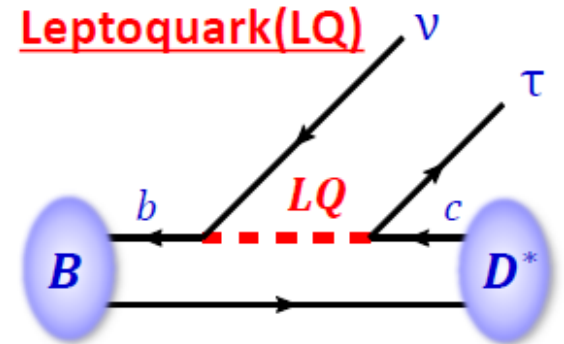
SM:

- $R(D) = 0.300 \pm 0.008$
Fermilab Lattice and MILC Collaborations, Phys. Rev. D 92, 034506 (2015)
- $R(D^*) = 0.252 \pm 0.003$
S. Fajfer, et al., Phys. Rev. D 85, 094025 (2012)
- Belle, BaBar, and LHCb measured
- $\mathcal{P}_\tau(D^*) = -0.497 \pm 0.013$
M. Tanaka, R. Watanabe, PRD 87, 034028 (2013)
- Belle measured

Charged Higgs



Leptoquark(LQ)



Belle: *Phys. Rev. D 92, 072014 (2015)*

hadronic tag, leptonic τ decay : $\tau \rightarrow \ell \nu \nu$

- $R(D) = 0.375 \pm 0.064(\text{stat.}) \pm 0.026(\text{syst.})$
- $R(D^*) = 0.293 \pm 0.038(\text{stat.}) \pm 0.015(\text{syst.})$

$R(D^*)$ with semileptonic tag

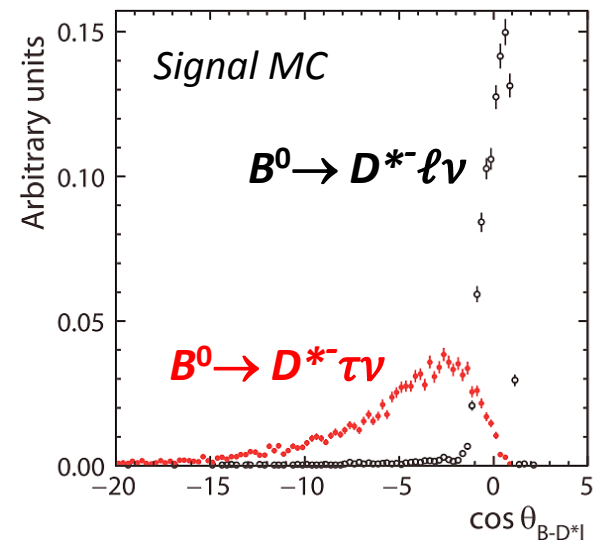
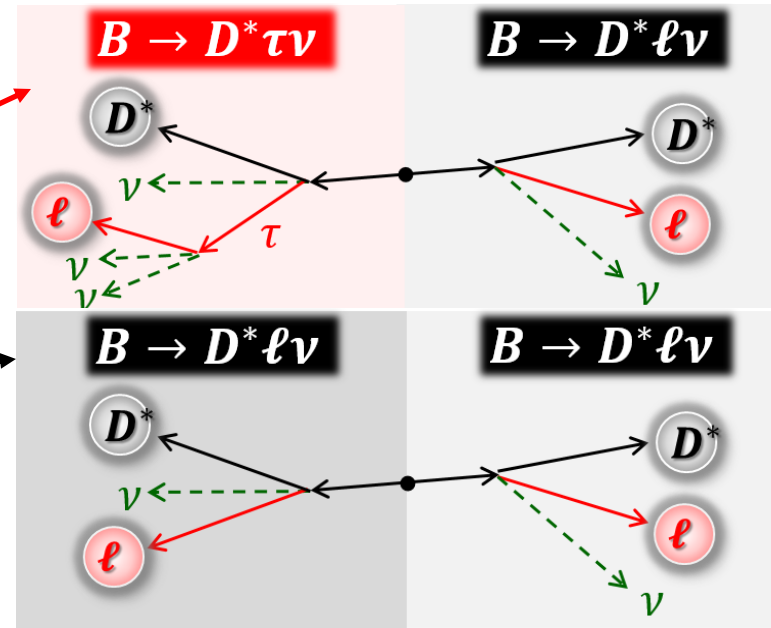
Belle, Phys. Rev. D 94, 072007 (2016)

- “Clean” channels are only used to get high purity

- leptonic τ decay : $\tau \rightarrow \ell \bar{\nu} \nu$
- $B^0 \bar{B}^0 \rightarrow (D^{*-} \ell^+) (D^{*+} \ell^-)$ channel

$$R(D^*) = \frac{\text{signal}}{\text{normalization}}$$

- Signal and normalization are tagged by double semileptonic tag.
- Signal/normalization separation based on smaller $\cos \theta_{B-D^*\ell}$



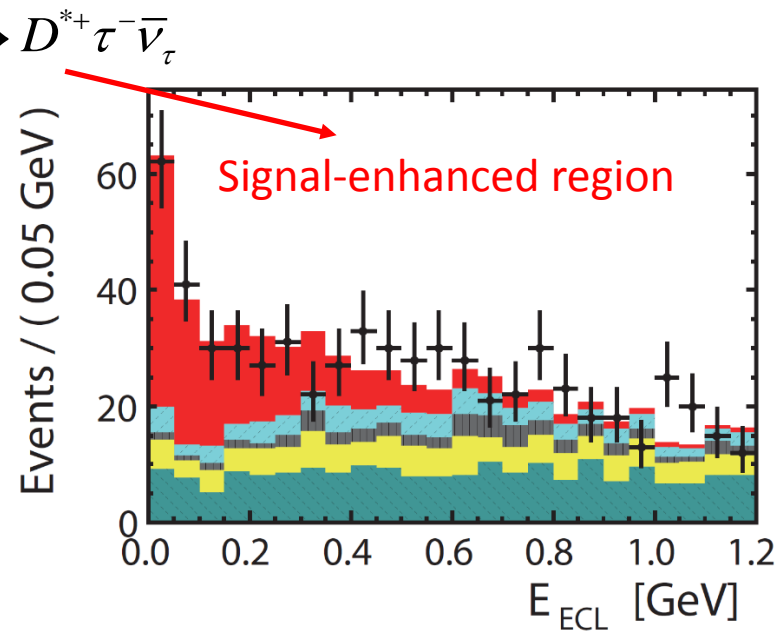
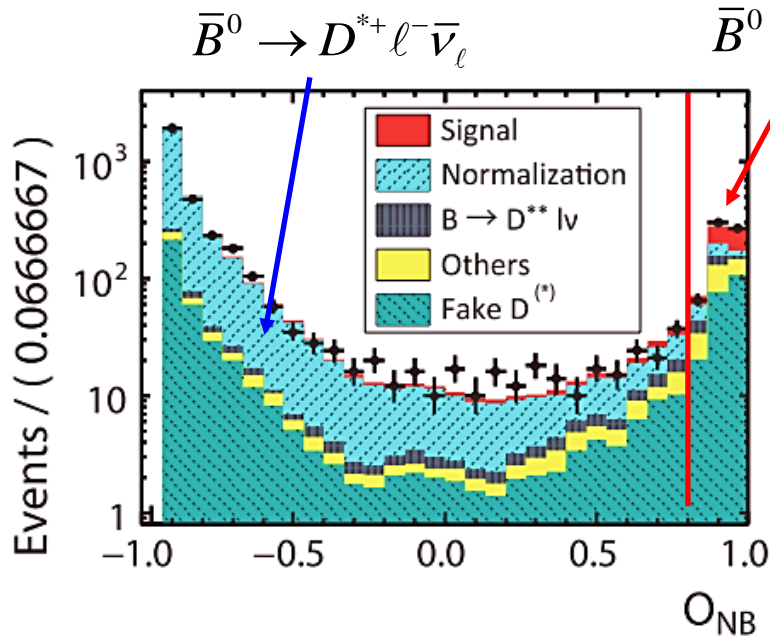
Signal extraction

Belle, Phys. Rev. D 94, 072007 (2016)

Two-dimensional fit to neural network output (O_{NB}) and E_{ECL}

- $\cos \theta_{B-D^*\ell}$
- M_{miss}^2
- Total energy of $B_{tag}+B_{sig}$

Summed energy, not used for the event reconstruction



$$R(D^*) = 0.302 \pm 0.030(\text{stat.}) \pm 0.011(\text{syst.})$$

- ✓ 13.8σ significance including syst. error.
- ✓ Compatibility with the SM is 1.6σ
- ✓ Consistent with other measurements

$R(D^*)$ and $\mathcal{P}_\tau(D^*)$ with hadronic τ decays

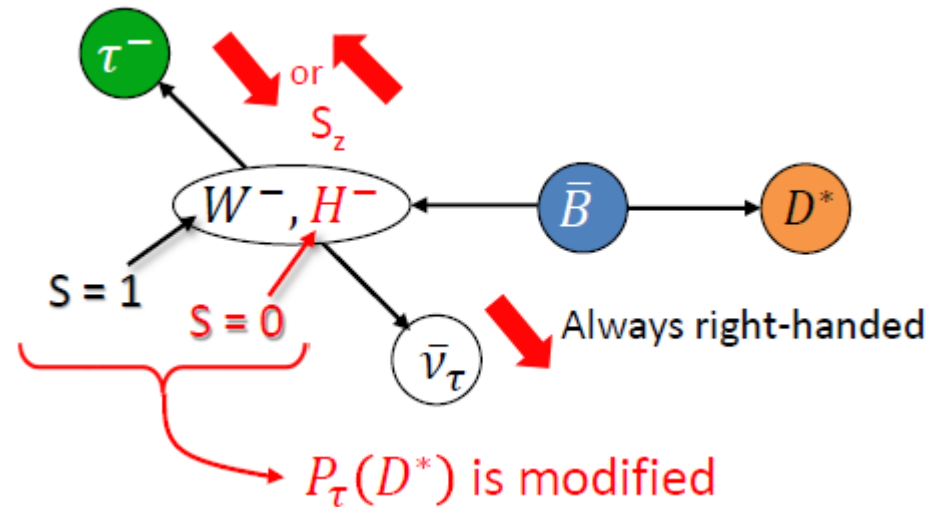
Belle, Phys. Rev. Lett. 118, 211801 (2017)

$$\mathcal{P}_\tau(D^*) = \frac{\Gamma^+ - \Gamma^-}{\Gamma^+ + \Gamma^-}$$

$\Gamma^{+(-)}$ for right-(left-) handed τ

$$\mathcal{P}_\tau(D^*)_{SM} = -0.497 \pm 0.013$$

M. Tanaka and R. Watanabe,
Phys. Rev. D 87, 034028 (2013)



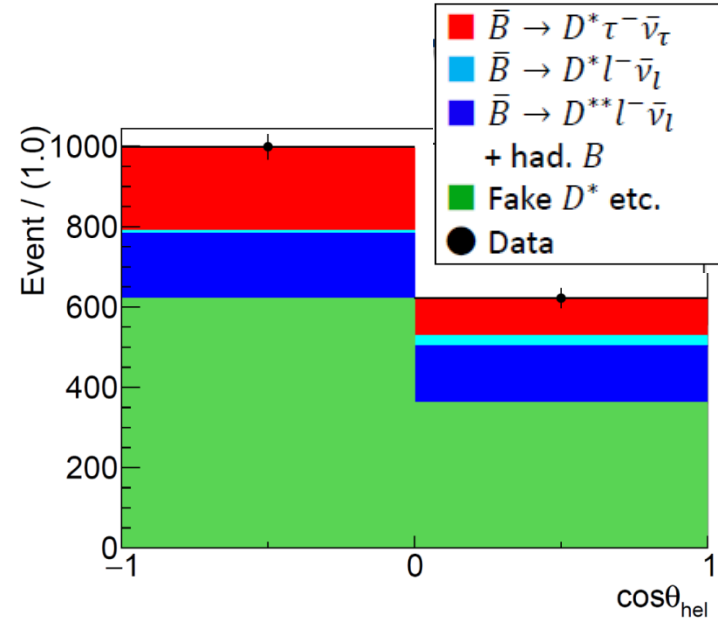
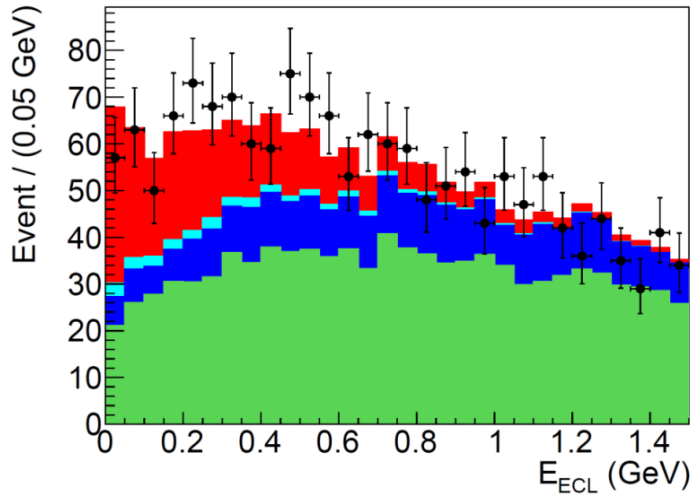
- τ polarization is a variable sensitive to NP
 - It can be measured using two-body decays of τ

Target of this analysis

- First measurement of $\mathcal{P}_\tau(D^*)$ using $\tau^- \rightarrow \pi^- \nu_\tau, \rho^- \nu_\tau$
- New measurement of $R(D^*)$
 - Independent study of previous measurements using $\tau^- \rightarrow \ell^- \bar{\nu} \nu$

Different final state - different background

Results



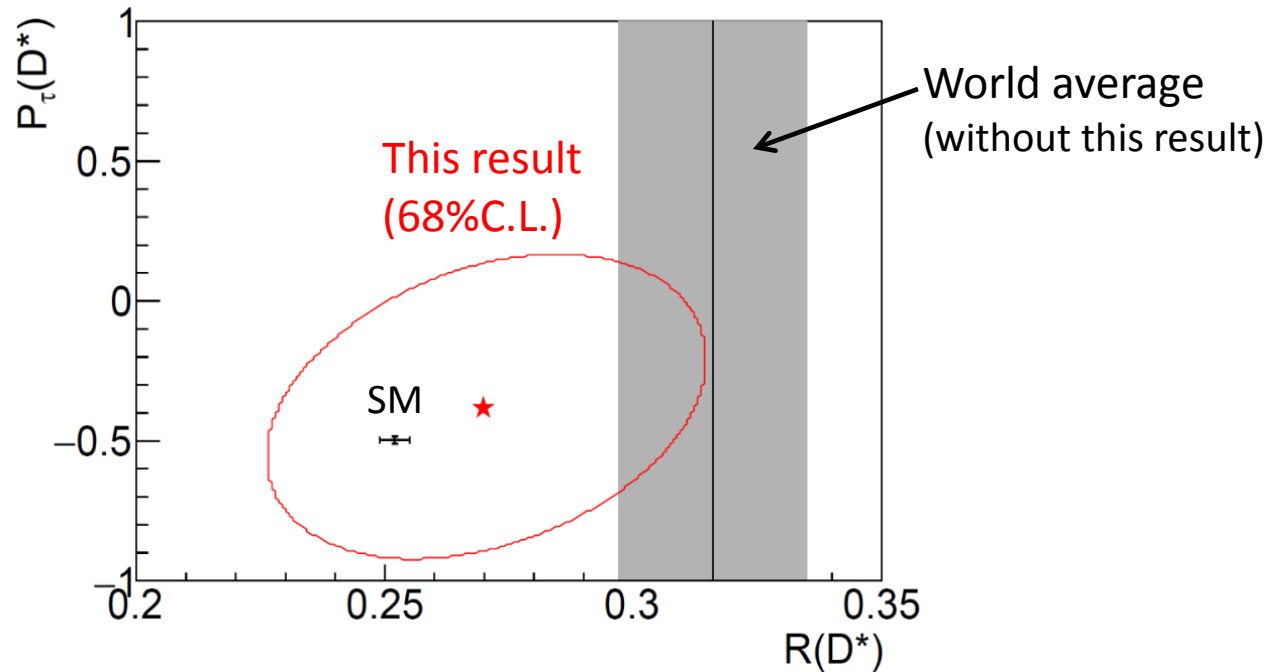
Signal significance of about 7σ

- First observation of the $B \rightarrow D^* \tau \nu$ signal using only hadronic τ decays

$$R(D^*) = 0.270 \pm 0.035(\text{stat.})^{+0.028}_{-0.025}(\text{syst.})$$

$$\mathcal{P}_\tau(D^*) = -0.38 \pm 0.51(\text{stat.})^{+0.21}_{-0.16}(\text{syst.})$$

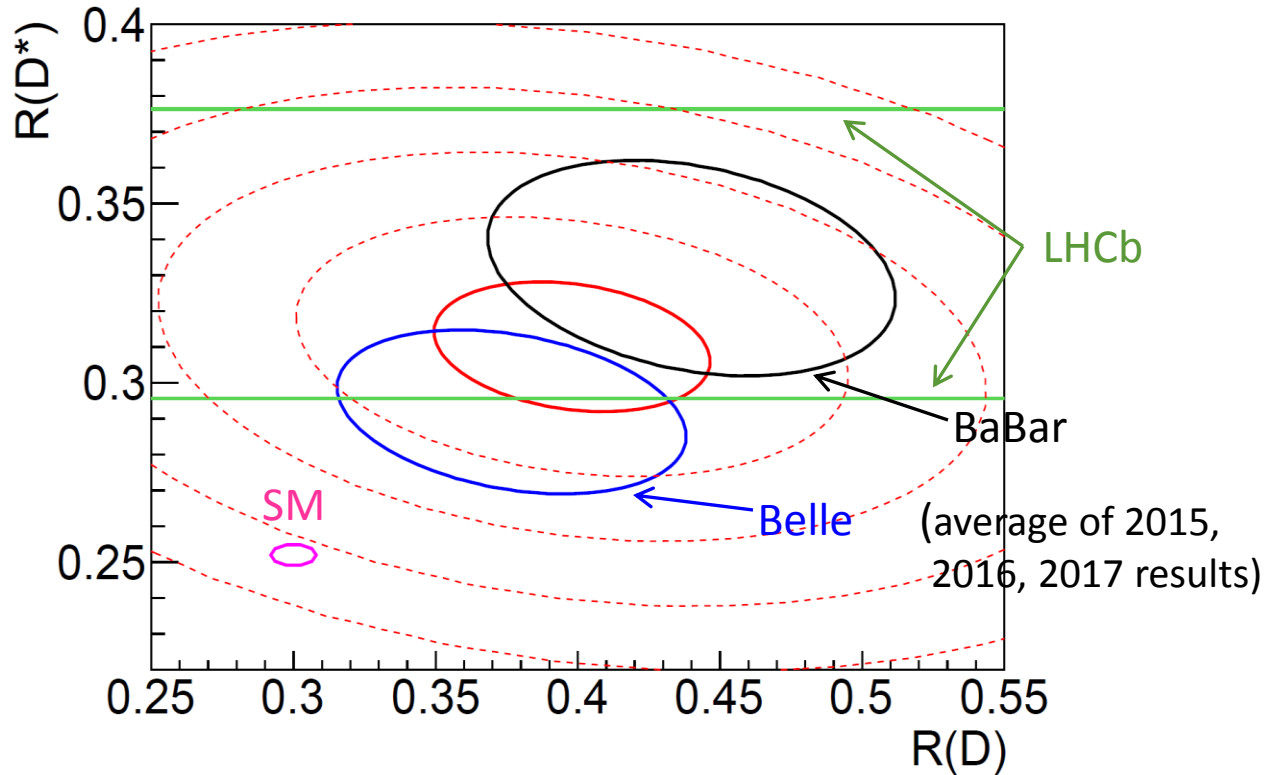
Compatibility with the SM within 0.4σ



- Result is consistent with the SM within 0.4σ
- Excludes $\mathcal{P}_\tau(D^*) > +0.5$ at 90% C.L. \longrightarrow *First measurement of $\mathcal{P}_\tau(D^*)$*
- First $R(D^*)$ measurement only with hadronic τ decays
 - Precision of 16%; comparable to the previous measurements (9-14%)

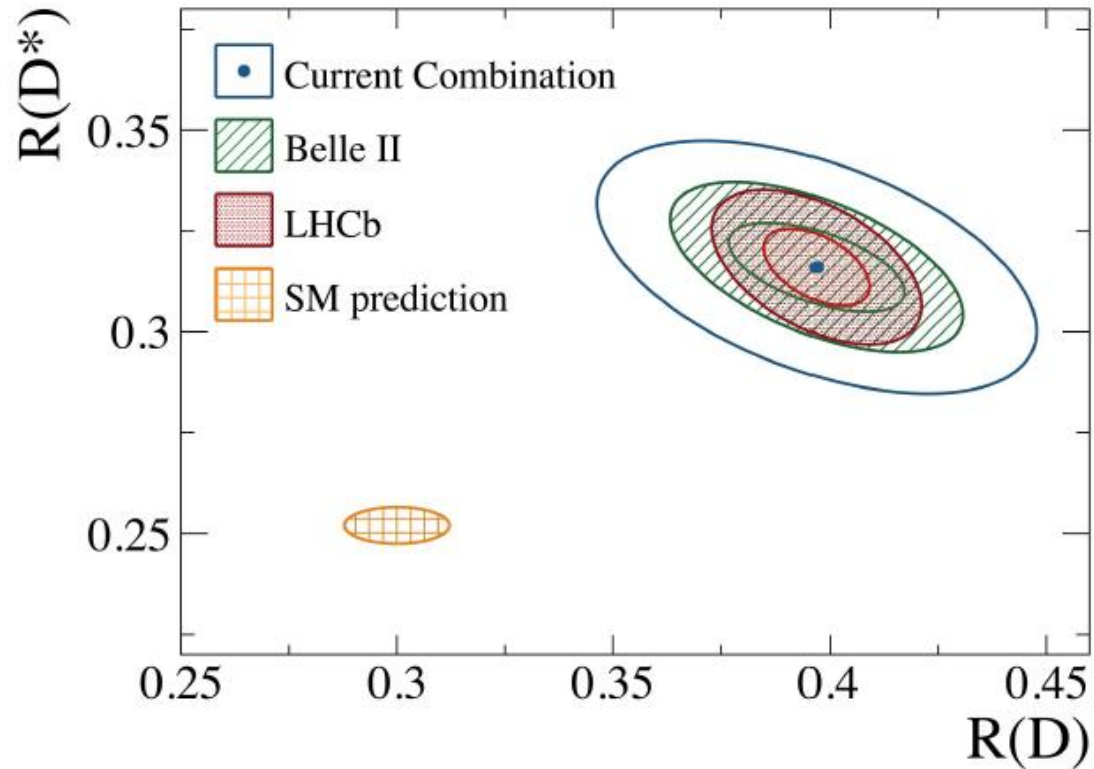
Status of $R(D^{(*)})$

Moriond 2017



- $\sim 4\sigma$ discrepancy from the SM remains
 - All the experiments show the larger $R(D^{(*)})$ than the SM
- More precise measurements at Belle II and LHCb are essential

Future

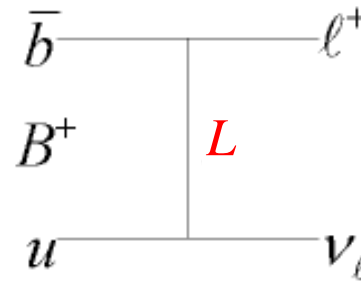
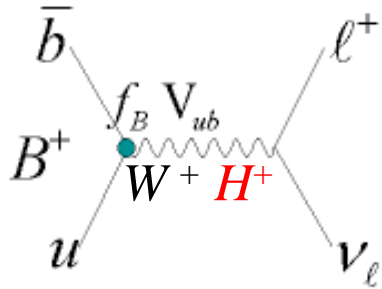


	Belle ~1/ab	Belle II 5/ab	Belle II 50/ab
$R(D)$	~15.8 %	5.6 %	3.2 %
$R(D^*)$	~6.9 %	3.9 %	2.2 %

$$B^+ \rightarrow \tau^+ \nu_\tau$$

$$B^+ \rightarrow \tau^+ \nu_\tau$$

(Decays with Large Missing Energy)



Sensitivity to NP

SM:

$$\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau) = \frac{G_F^2 m_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

NP effects (2-Higgs doublet model (type II))

$$\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = \mathcal{B}_{SM}(B^+ \rightarrow \tau^+ \nu) \times r_H$$

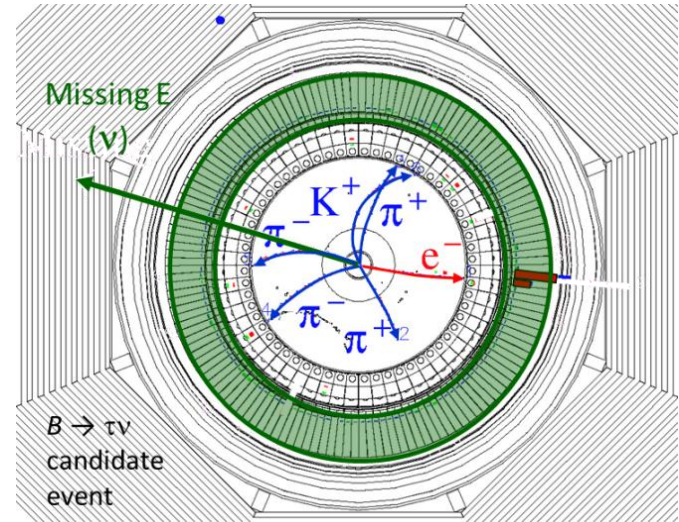
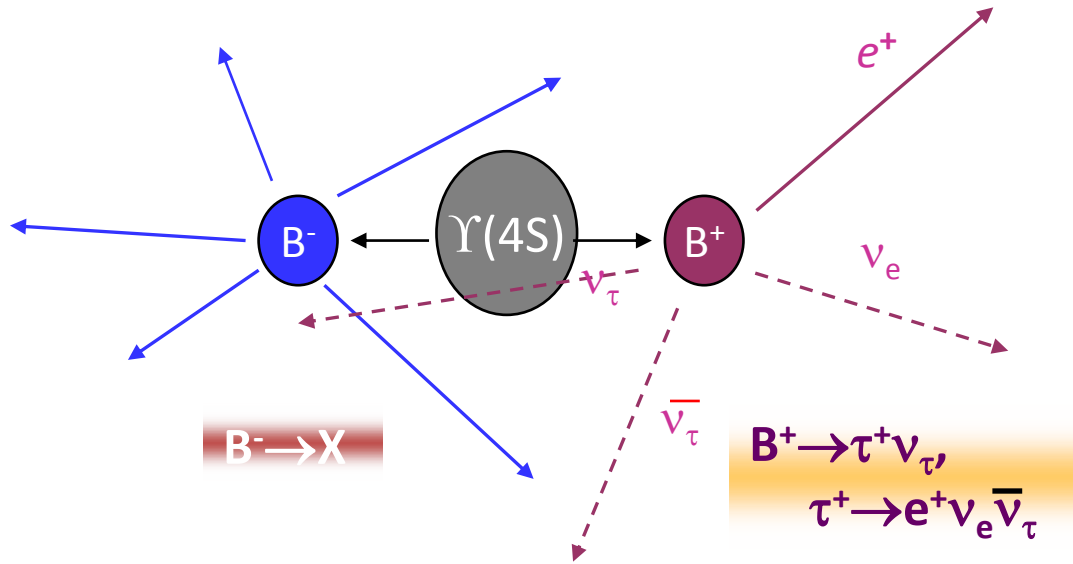
$$r_H = [1 - (m_B^2 / m_H^2) \cdot \tan^2 \beta]^2$$

- very clean place to measure $f_B \cdot |V_{ub}|$ and/or search for new physics (e.g. H^+ , LQ)

- helicity-suppressed: $\mathcal{B} \propto m_\ell^2$
 $\mathcal{B}(B^+ \rightarrow e^+ \nu) \ll \mathcal{B}(B^+ \rightarrow \mu^+ \nu) \ll \mathcal{B}(B^+ \rightarrow \tau^+ \nu)$
 $\sim 10^{-11} \quad \sim 10^{-6} \quad \sim 10^{-4}$

- experimental features $B^+ \rightarrow \tau^+ \nu_\tau$
 large BF, but multiple ν

$B \rightarrow \tau \nu$: Experimental Challenge

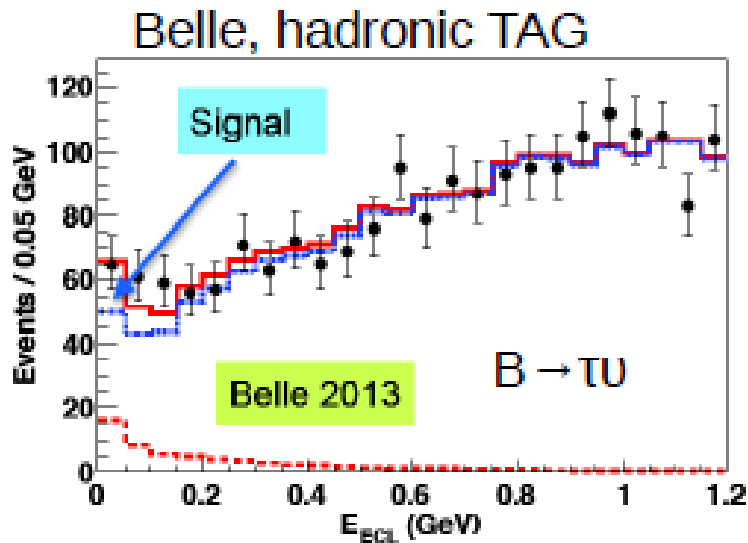


Always ≥ 2 neutrinos appear
 in $B \rightarrow \tau \nu$ decay

Signature : 1 track +invisible

Experimental Challenge !

Belle experimental results

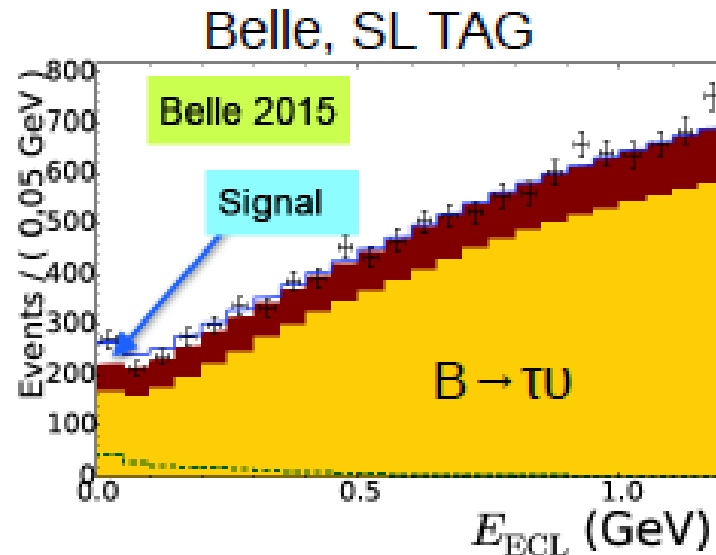


Phys. Rev. Lett. 110, 131801 (2013)

$$N_{sig} = 62^{+23}_{-22} \pm 6 \text{ events}$$

$$\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (0.72^{+0.27}_{-0.25} \pm 0.11) \times 10^{-4}$$

3σ significance



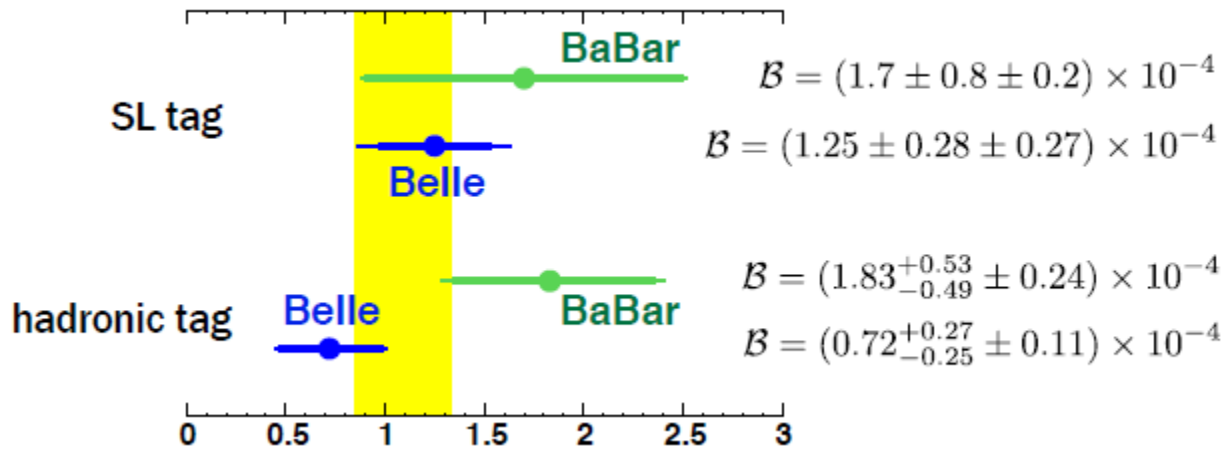
Phys. Rev. D 92, 051102 (R) (2015)

$$N_{sig} = 222 \pm 50 \text{ events}$$

$$\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (1.25 \pm 0.28 \pm 0.27) \times 10^{-4}$$

4.6σ significance

$B^+ \rightarrow \tau^+ \nu$ summary



Belle combined: $\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (0.91 \pm 0.22) \times 10^{-4}$

BaBar combined: $\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (1.79 \pm 0.48) \times 10^{-4}$

World average: $\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (1.09 \pm 0.24) \times 10^{-4}$

► Belle vs. BaBar – consistent within $\sim 1.7\sigma$

► The average is consistent with SM

$$(\mathcal{B}(B^+ \rightarrow \tau^+ \nu))_{\text{SM}} = (0.83 \pm 0.08) \times 10^{-4}$$

Prospect at Belle II

B2TiP

Semileptonic / Leptonic decays with τ final states:

Observable	Belle / LHCb Measurements	SM Prediction	Belle II 5/ab	Belle II 50/ab	LHCb 10/fb	LHCb 22/fb
R(D)	0.397 +/- 0.040 +/- 0.028	0.300 +/- 0.008	5.6%	3.2%	4%	2%
R(D*)	0.316 +/- 0.016 +/- 0.010	0.252 +/- 0.003	3.9%	2.2%	4%	2%
R(π)	1.05 +/- 0.51	0.641 +/- 0.016	19%	8%	-	-
BF(B \rightarrow τ ν)	(1.06 +/- 0.19) x 10 ⁻⁴	(0.83 +/- 0.08) x 10 ⁻⁴	9%	4%	-	-

Summary

- $|V_{cb}|$ and $|V_{ub}|$ are measured at Belle with different methods
 - ✓ Inclusive $B \rightarrow X_c \ell \nu$, $B \rightarrow X_u \ell \nu$, Hadronic tag, Semileptonic tag, Untagged
 - ✓ Exclusive $B \rightarrow D^{(*)} \ell \nu$, $B \rightarrow \pi \ell \nu$
- Inclusive-Exclusive tension in both $|V_{cb}|$ and $|V_{ub}|$ still exist ($\sim 3\sigma$)
- $\sim 4\sigma$ discrepancy from the SM remains for the world average of $R(D^{(*)})$
 - ✓ All the experiments show the larger $R(D^{(*)})$ than the SM
- The world average of $\mathcal{B}(B^+ \rightarrow \tau^+ \nu)$ is consistent with the SM
- The precision of these measurements will be improved by the Belle II experiment (factor $\sim 2-3$) (NP ?...)