



Measurement of the branching fraction for $B^0 \rightarrow \pi^0 \pi^0$ decays reconstructed in 2019–2020 Belle II data

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Abstract

We report the first reconstruction of the $B^0 \rightarrow \pi^0 \pi^0$ decay mode at Belle II using samples of 2019 and 2020 data that correspond to 62.8 fb^{-1} of integrated luminosity. We find $14.0_{-5.6}^{+6.8}$ signal decays, corresponding to a significance of 3.4 standard deviations and determine a branching ratio of $\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = [0.98_{-0.39}^{+0.48} \pm 0.27] \times 10^{-6}$. The results agree with previous determinations and contribute important information to an early assessment of detector performance and Belle II's potential for future determinations of α/ϕ_2 using $B \rightarrow \pi\pi$ modes.

1. INTRODUCTION

Effective constraints on physics beyond the Standard Model are provided by high-precision measurements. The study of charmless decays at Belle II can provide improved measurements of the Cabibbo–Kobayashi–Maskawa (CKM) angle $\alpha/\phi_2 \equiv \arg(-\frac{V_{td}V_{cb}^*}{V_{ud}V_{ub}^*})$, where V_{ij} are elements of the quark-mixing matrix. If $B^0 \rightarrow \pi^+\pi^-$ decays proceeded through only the tree level ($b \rightarrow u$) process, the mixing-induced CP violation parameter, \mathcal{S}_{CP} , would be proportional to $\sin(2\phi_2)$. However the value of ϕ_2 is shifted by an amount $\Delta\phi_2$ due to the presence of penguin contributions ($b \rightarrow d$). The tree and penguin contributions can be disentangled using $B \rightarrow \pi\pi$ isospin relations [1].

$$A^{+0} = \frac{1}{\sqrt{2}}A^{+-} + A^{00}, \quad \bar{A}^{-0} = \frac{1}{\sqrt{2}}\bar{A}^{+-} + \bar{A}^{00} \quad (1)$$

where A^{ij} is the amplitude of the decay $\bar{B} \rightarrow \pi^i\pi^j$ and is represented geometrically in the complex plane in Figure 1.

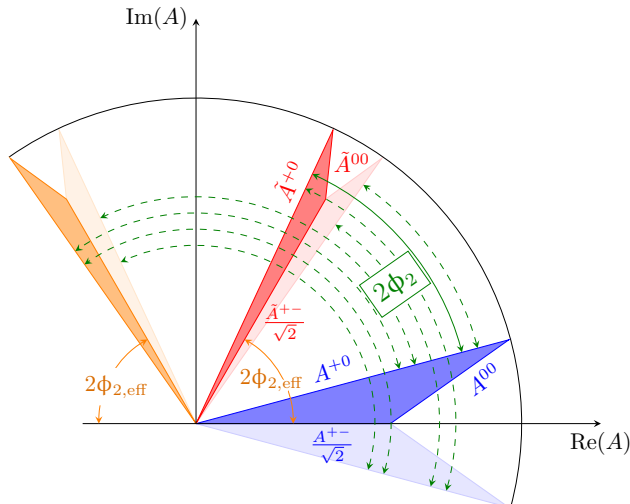


FIG. 1. Geometrical representation of the isospin triangular relations in the complex plane of $B^{i+j} \rightarrow h^i h^j$ amplitudes. The blue and the red shaded areas correspond to the isospin triangles. The angle between the CP conjugate charged amplitudes A^{+-} and \bar{A}^{+-} corresponds to twice the weak phase $\alpha_{\text{eff}}/\phi_{2,\text{eff}}$ (orange solid arcs). The angle between the CP conjugate charged amplitudes A^{+0} and \bar{A}^{+0} corresponds to twice the CKM angle α/ϕ_2 (green solid arc). The other triangles with lighter shading represent the mirror solutions allowed by the discrete ambiguities in the isospin relationships, with the corresponding values for α/ϕ_2 represented by the green dashed curves.

Taking advantage of these relations requires precise measurements of the branching fraction \mathcal{B} and CP violation parameters of each $B \rightarrow \pi\pi$ decay. The relatively large uncertainties on the current value of $\mathcal{B}(B^0 \rightarrow \pi^0\pi^0)$ and $\mathcal{A}_{CP}(B^0 \rightarrow \pi^0\pi^0)$, measured by BaBar [2] and Belle [3], poses the greatest limitation to fully exploiting the isospin relation. The $B^0 \rightarrow \pi^0\pi^0$ mode has a low branching ratio, $(1.59 \pm 0.26) \times 10^{-6}$ [4], since it is both color-suppressed and, at tree level, is proportional to the CKM matrix element V_{ub} , whose magnitude is small. In addition, the π^0 decays via $\pi^0 \rightarrow \gamma\gamma$ with a branching ratio of $\approx 99\%$ and hence the final state particles consist entirely of photons. Belle II with its clean e^+e^- environment and large

acceptance for photons ranging from 20 MeV to 4 GeV is the only running experiment that can competitively study this decay mode.

The Belle II experiment features significantly upgraded detectors and new analysis software providing better particle identification, background suppression and B -meson flavour determination compared to its predecessor Belle. The Belle II experiment, complete with its silicon vertex detector, commenced taking data in March 2019. The sample used in this analysis corresponds to an integrated luminosity of 62.8 fb^{-1} at the $\Upsilon(4S)$ resonance. We report the first Belle II measurement of the branching fraction of the $B^0 \rightarrow \pi^0 \pi^0$ decay. Charge-conjugate decays are implied in what follows.

2. BELLE II DETECTOR

A full description of the Belle II detector is given in Ref. [5]. The detector consists of several subdetectors arranged in a cylindrical structure around the beam pipe. Compared to its predecessor Belle [6], a pixel detector (PXD) has been added at a minimum radius of 1.4 cm. This improves the resolution of the impact parameter to about $12 \mu\text{m}$ in the transverse direction for high momentum tracks [7], which helps to reject background events for this analysis. The PXD is surrounded by a four-layer double-sided silicon strip detector, referred to as the silicon vertex detector, and a central drift chamber (CDC). A time-of-propagation counter and an aerogel ring-imaging Cherenkov counter cover the barrel and forward endcap regions of the detector, respectively, and are essential for charged-particle identification (PID). The electromagnetic calorimeter (ECL) makes up the remaining volume inside a superconducting solenoid, which operates at 1.5 T. A dedicated detector to identify K_L^0 mesons and muons is installed in the outermost part of the detector. The z-axis of the laboratory frame is defined as the symmetry axis of the solenoid, and the positive direction is approximately given by the incoming electron beam. The polar angle θ , as well as the longitudinal and the transverse direction are defined with respect to the z-axis. The ECL is most relevant for this work as it is the only subdetector that can detect photons.

2.1. Data and simulation

We use all 2019-2020 data corresponding to an integrated luminosity of 62.8 fb^{-1} collected with the Belle II detector at the asymmetric-energy e^+e^- collider SuperKEKB [8], which is located at the KEK laboratory in Tsukuba, Japan. Data were collected at the center-of-mass (c.m.) energy of the $\Upsilon(4S)$ resonance ($\sqrt{s} = 10.58 \text{ GeV}$). The energies of the electron and positron beams are 7 GeV and 4 GeV, respectively, resulting in a boost of $\beta\gamma = 0.28$ of the c.m. frame relative to the laboratory frame. We also use all off-resonance data collected at an energy about 60 MeV lower and corresponds to an integrated luminosity of 9.2 fb^{-1} . All events are required to satisfy loose hadronic event selection criteria, based on total energy and neutral-particle multiplicity in the events, targeted at reducing sample sizes to a manageable level with minimal impact on signal efficiency. All data are processed using the Belle II analysis software [9].

We use GEANT4 [10] based Monte Carlo (MC) simulation data to optimize the event selection, compare the distribution observed in experimental data with expectations, and model the distribution in fits. We use 2×10^6 signal simulated data. Generic background MC samples consists of charged and neutral B meson pairs ($B^0 \bar{B}^0$ and $B^+ B^-$), and continuum

processes ($e^+e^- \rightarrow q\bar{q}$ with $q = u, d, s, c$ quarks) in realistic proportions, which correspond to a 4 ab^{-1} sample. To validate our experimental procedure, the $B^0 \rightarrow \bar{D}^0 (\rightarrow K^- \pi^+ \pi^0) \pi^0$ decay is used as a control mode as it contains two π^0 particles in the final state. The total yield is expected to be 10 – 20 times larger than the expected signal yield from the $B^0 \rightarrow \pi^0 \pi^0$ decay. We use 1×10^6 simulated control-mode events.

3. EVENT SELECTION AND CANDIDATE RECONSTRUCTION

We form photon candidates by requiring the energy in the ECL barrel and endcaps to be greater than 20 MeV and 22.5 MeV respectively. Further photon selections using a binary boosted decision-tree classifier, described in subsection 3.1, is applied to suppress hadronic interactions and photons from non-signal sources. The photon candidates are paired to form π^0 candidates and we require the invariant mass and helicity angle to be $0.105 < M_{\gamma\gamma} < 0.150 \text{ GeV}/c^2$ and $|\cos\theta_{\text{helicity}}| < 0.98$, respectively, to suppress combinatorial background from collinear soft photons. The mass of the π^0 candidates is constrained to its known value in a kinematic fit to improve the momentum resolution. The B meson candidates are reconstructed by pairing the π^0 candidates. To select signal B , two kinematic variables are defined,

$$M_{\text{bc}} = \sqrt{E_{\text{beam}}^2 - |\vec{p}_B|^2}, \quad \Delta E = E_B - \sqrt{s}/2 \quad (2)$$

where M_{bc} is the mass-energy relation where the energy of the B meson has been replaced by half of the c.m. energy, which is extremely well-defined by the accelerator, and \vec{p}_B is the B meson momentum, both measured in the $\Upsilon(4S)$ frame. $\Delta E = E_B - \sqrt{s}/2$ is the difference between the total energy of the B candidate and half the collision energy, both measured in the $\Upsilon(4S)$ frame. B meson candidates are required to have $5.26 < M_{\text{bc}} < 5.29 \text{ GeV}/c^2$ and $-0.3 < \Delta E < 0.2 \text{ GeV}$. For correctly reconstructed B meson candidates, ΔE should peak at zero except for resolution. However, observed ΔE distributions peak below zero since energy is lost via either electromagnetic interactions in the material before the calorimeter or via energy leakage from the ECL cluster. In addition, the photon energy and momentum can only be determined from the ECL cluster energy and hence there is a small correlation between ΔE and M_{bc} in our reconstructed $B^0 \rightarrow \pi^0 \pi^0$ events.

3.1. Optimized photon selection

Due to the long decay time of signal in CsI(Tl), Bhabha events ($e^+e^- \rightarrow e^+e^-$) can deposit large amounts of energy in the CsI(Tl) crystals of the ECL that are still present when another hadronic event occurs. A random photon from the hadronic event can be combined with the residual energy (misreconstructed photon) in the CsI(Tl) crystals to form a π^0 . This misreconstructed π^0 and a genuine π^0 can then be misreconstructed into a B^0 candidate. In the Belle analysis of $B^0 \rightarrow \pi^0 \pi^0$ [11], these were suppressed by requiring ECL signals to be in time with the rest of the e^+e^- event. Rather than using one-dimensional requirements on the photon's time of interaction, we train a fast boosted decision-tree (FBDT) [12] to distinguish between genuine and misreconstructed photons using ECL variables that have high discriminating power. To create samples of genuine and misreconstructed photons, we reconstruct $B^0 \rightarrow \pi^0 \pi^0$ candidates in simulated signal-only data with no requirements on the

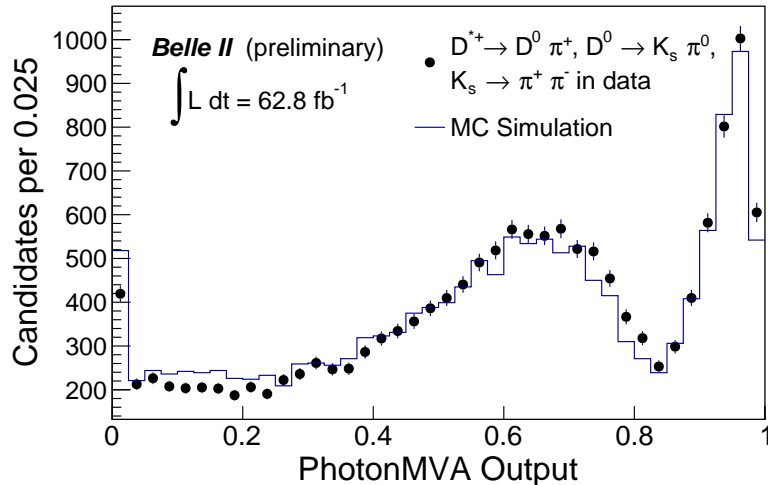


FIG. 2. The output of the FBDT classifier for photons in $D^{*+} \rightarrow \bar{D}^0 \pi^+$, $\bar{D}^0 \rightarrow K_s^0 \pi^0$, $K_s^0 \rightarrow \pi^+ \pi^-$ decays.

photons. Photons that do not originate from the signal are regarded as misreconstructed. We train and validate data using two independent data sets consisting of 50 000 genuine and 50 000 misreconstructed photons. We find that this classifier, which we call the **photonMVA**, can efficiently suppress most misreconstructed photons. Based on MC studies requiring the **photonMVA** output to exceed 0.2 retains 97.05% of genuine photons while rejecting 73.3% of misreconstructed photons.

To validate the **photonMVA** we use the $D^{*+} \rightarrow \bar{D}^0 (\rightarrow K_s^0 (\rightarrow \pi^+ \pi^-) \pi^0) \pi^+$ decay mode. The reconstruction uses similar final state selections as the signal decay. We first reconstruct π^\pm candidates from charged-particle candidates reconstructed in the full polar-angle acceptance ($17^\circ < \theta < 150^\circ$), and originating close to the interaction point in the longitudinal ($|dz| < 3.0$ cm) and radial ($|dr| < 0.5$ cm) directions to reduce beam-background-induced tracks. For K_s^0 reconstruction, we pair oppositely charged π^\pm candidates and require that they originate from a common space-point and have dipion mass in the range 0.47 – 0.53 GeV/c^2 . For D^0 reconstruction, we combine the K_s^0 with a π^0 and require that candidates have masses in the range 1.80 – 2.50 GeV/c^2 with momenta in the c.m. frame greater than 2.5 GeV/c . Finally, we reconstruct D^{*+} candidates by combining the D^0 and π^+ in a kinematic vertex fit. We choose one candidate per event by selecting the π^0 candidate with the lowest χ^2 value of the mass-constraint diphoton fit. The difference between the mass of the D^{*+} and \bar{D}^0 , $\Delta M = M_{D^{*+}} - M_{\bar{D}^0}$, is a powerful discriminator between signal and background. We require $0.144 < \Delta M < 0.147 \text{ GeV}/c^2$ to ensure the D^{*+} is reconstructed with high purity.

The final-state reconstruction is performed with and without the **photonMVA** requirement. The signal yields and backgrounds are determined using fits to the ΔM distribution. The signal and background retention are consistent between MC and experimental data. Requiring the **photonMVA** to exceed 0.2 reduces the D^{*+} background by 47% (absolute) and reduces signal reconstruction efficiency by 3.7% (absolute) compared to the standard photon selection [13]. In addition we compare the **photonMVA** distribution in the MC and 62.8 fb^{-1} data as shown in Figure 2 and find that they are in agreement.

4. MULTIVARIATE BACKGROUND SUPPRESSION

The $B^0 \rightarrow \pi^0\pi^0$ decay has large continuum background even relative to other charmless B decay modes because of its small branching ratio. To discriminate against such background, we use the FBDT classifier to combine 28 variables associated with event topology, which are known to provide statistical discrimination between B -meson signal and continuum background. We additionally require that these variables have correlations with ΔE and M_{bc} below 5%. We train the classifier to identify statistically significant signal and background features using unbiased simulated samples. We validate the input and output distributions of the classifier by comparing data with simulation using the control mode $B^0 \rightarrow \bar{D}^0 (\rightarrow K^- \pi^+ \pi^0) \pi^0$. No inconsistency is observed.

The optimal FBDT threshold is determined by maximizing the figure of merit $S/\sqrt{S+B}$, where S and B are the simulated signal and background yield, respectively, both determined in the signal-enhanced region $5.27 < M_{bc} < 5.29 \text{ GeV}/c^2$ and $-0.1 < \Delta E < 0.15 \text{ GeV}$. The resulting threshold criterion rejects 97.8% of the background while retaining 57.9% of the signal. The signal efficiency after $B^0 \rightarrow \pi^0\pi^0$ candidate reconstruction and continuum suppression is 21%. About 1.6% of selected events have more than one candidate. We choose the candidate with the minimum absolute deviation, $|dM(\pi_1^0)| + |dM(\pi_2^0)|$, of the reconstructed invariant masses from the known value. This is 98% efficient in selecting the correct B^0 . In addition, we reconstruct the vertex of the accompanying tag-side B meson and identify the flavor using a category-based flavor tagger [14].

To validate the FBDT, 9.2 fb^{-1} of off-resonance data is used as it contains only continuum events. We apply the same $B^0 \rightarrow \pi^0\pi^0$ selection as discussed previously except for the requirements $M_{bc} > 5.2 \text{ GeV}/c^2$ and $|\Delta E| < 0.5 \text{ GeV}$ imposed to retain as many continuum events as possible. We impose the FBDT requirement and determine the continuum rejection to be 97.4%, which agrees with MC expectation.

Backgrounds due to non-signal B decays are denoted as $B\bar{B}$. All the $B\bar{B}$ background effectively consists of $B^+ \rightarrow \rho^+\pi^0$ decays where the charged pion from the subsequent $\rho^+ \rightarrow \pi^+\pi^0$ is unreconstructed, and $B^0 \rightarrow K_S^0 (\rightarrow \pi^0\pi^0) \pi^0$ decays where one of the π^0 is unreconstructed. This background peaks at similar values of M_{bc} and T_c but has ΔE shifted to negative values due to missing energy from the unreconstructed particle. Since the topology of $B\bar{B}$ events is similar to the signal mode, the FBDT removes approximately the same fraction of $B\bar{B}$ and signal events.

5. DETERMINATION OF SIGNAL YIELDS

Signal yields are determined with a three-dimensional $(M_{bc}, \Delta E, T_c)$ simultaneous unbinned maximum likelihood fit for each b flavor, q , in 8 bins of the dilution factor, r . T_c is the log transform of the continuum suppression FBDT variable and is used to transform the FBDT output into a Gaussian-like shape. By convention $q = +1$ tags a B^0 while $q = -1$ tags a \bar{B}^0 . The dilution factor is determined by a category-based flavor tagger [14] with $r = 0$ meaning no flavor discrimination between B^0 and \bar{B}^0 and $r = 1$ meaning unambiguous flavor assignment. Bins are spaced so that each bin has an approximately equal number of candidates. Fit models are determined empirically from simulation, with shifts of peak positions in ΔE determined in the $B^0 \rightarrow \bar{D}^0 (\rightarrow K^- \pi^+ \pi^0) \pi^0$ control mode. A negative shift in ΔE relative to simulated data is observed. The value of the shift favored by control data

is determined using a likelihood-ratio test to be -10 MeV. This is included in the ΔE fit model for the signal and $B\bar{B}$ component.

To validate the MC $q \cdot r$ distributions, we compare the $q \cdot r$ fractions in experimental and simulated data restricted to a continuum-enriched sideband defined as $5.20 < M_{bc} < 5.26$ GeV/ c^2 where continuum events are dominant. The continuum suppression requirement is removed to have a sufficient sample size. The results show excellent agreement.

For all components, T_c is modelled using the sum of a Gaussian and a bifurcated Gaussian with a common mean to avoid peak splitting. For the signal and $B\bar{B}$ components, the correlation between M_{bc} and ΔE is taken into account with a two-dimensional kernel density estimation. We employ a data-driven method to determine the parameters of the continuum background probability density function (PDF) by fitting to the sideband region defined as $5.24 < M_{bc} < 5.27$ GeV/ c^2 and $0.1 < \Delta E < 0.3$ GeV. The range is limited since selections too far from the signal region may accept candidates too far kinematically from the signal region. The $B\bar{B}$ background has a negligible contribution as within both ranges, only 0.07% survive and we expect $B\bar{B}$ to be only a tenth of the total background. All signal and $B\bar{B}$ PDF parameters are fixed from simulated data while all continuum PDF parameters are fixed from experimental sideband data. The PDF parameters are identical for all $q \cdot r$ bins. The signal, continuum and $B\bar{B}$ bin fractions are fixed while the yields are allowed to float. The full PDF for the signal component is given by

$$P_i^s(M_{bc}, \Delta E, T_c, q) = [1 - q \times \Delta w_i + q(1 - 2w_i) \times (1 - 2\chi_d)\mathcal{A}_{CP}]P^s(M_{bc}, \Delta E, T_c), \quad (3)$$

where q is determined for the i^{th} bin of the data set, $P^s(M_{bc}, \Delta E, T_c)$ is the signal PDF in M_{bc} , ΔE , and T_c , \mathcal{A}_{CP} is the direct CP violation parameter, $\chi_d = 0.1875 \pm 0.0017$ is the time-integrated $B^0\bar{B}^0$ -mixing asymmetry, w_i is the wrong-tag fraction, and Δw_i is the difference in wrong tag fraction between positive and negative b-flavor tags for bin i . The values of w_i , and Δw_i are all fixed from MC. The \mathcal{A}_{CP} parameter is allowed to float but is not reported due to limited statistics.

6. SYSTEMATIC UNCERTAINTIES

With the current 62.8 fb $^{-1}$ data set the dominant uncertainty is statistical. As more experimental data are collected, the systematic uncertainties will become more important. At this stage, we only examine the largest sources of systematic uncertainty. We assume the sources to be independent and add in quadrature the corresponding uncertainties. Table I summarizes the systematic uncertainty.

6.1. π^0 reconstruction efficiency

The systematic uncertainty associated with possible data-simulation discrepancies is studied using the decays $B^0 \rightarrow D^{*-}(\rightarrow \bar{D}^0(\rightarrow K^+\pi^-\pi^0)\pi^-)\pi^+$ and $B^0 \rightarrow D^{*-}(\rightarrow \bar{D}^0(\rightarrow K^+\pi^-\pi^0)\pi^-)\pi^+$ where the selection of charged particles is identical and the π^0 selection is the same as the signal mode. The signal yields of the two control channels are used to determine the π^0 reconstruction efficiency

$$\epsilon^{\pi^0} = \frac{N(K^-\pi^+\pi^0)}{N(K^-\pi^+)} \cdot \frac{\mathcal{B}(\bar{D}^0 \rightarrow K^+\pi^-)}{\mathcal{B}(\bar{D}^0 \rightarrow K^+\pi^-\pi^0) \cdot \mathcal{B}(\pi^0 \rightarrow \gamma\gamma)} \quad (4)$$

We compare the yields obtained from fits to the ΔE distribution of reconstructed B candidates and obtain an efficiency $\epsilon_{\text{data}}^{\pi^0}$ in data that agrees with the value observed in simulation within a 10% uncertainty, which is used as a systematic uncertainty. The uncertainties on the efficiencies for two π^0 s are completely correlated and hence our total systematic uncertainty is 20%.

6.2. Number of $B\bar{B}$

The calculation of the branching fraction uses the number of $B^0\bar{B}^0$ pairs, which is computed using the integrated luminosity, the $e^+e^- \rightarrow \Upsilon(4S)$ cross-section [15], and the known value of the branching fraction of $\Upsilon(4S) \rightarrow B^0\bar{B}^0$. We assign a systematic uncertainty of 1.34%, which includes the uncertainties on the above quantities and uncertainties associated with the beam-energy spread and potential offset of the c.m. energy.

6.3. Continuum PDF modeling

The continuum is modelled with an ARGUS function for M_{bc} , a first order Chebyshev function for ΔE , and the sum of a Gaussian and bifurcated Gaussian for T_c . The continuum background uses a total of 8 parameters, which are fixed from a fit to the sideband. The sideband for M_{bc} is defined as $0.1 < \Delta E < 0.2$ GeV while the sideband for ΔE and T_c is defined as $5.26 < M_{\text{bc}} < 5.27$ GeV/ c^2 . We vary the eight parameters of the sideband-based modeling of continuum accounting for correlation and obtain a 10% systematic uncertainty.

Source	Systematic Uncertainty (%)
π^0 efficiency	20.0
$N(B\bar{B})$	1.34
Continuum PDF	10.0
Total	22.4

TABLE I. Major systematic uncertainties where the total is calculated by adding all the systematic uncertainties in quadrature.

7. DETERMINATION OF BRANCHING RATIO

We determine the branching fraction as

$$\mathcal{B} = \frac{N}{\epsilon \times 2 \times N_{B\bar{B}}} \quad (5)$$

where N is the signal yield obtained from the fits, ϵ is the reconstruction and selection efficiency, and $N_{B\bar{B}}$ is the number of $B\bar{B}^0$ pairs. The number of $B^0\bar{B}^0$ pairs is obtained from the product of the measured integrated luminosity, the $e^+e^- \rightarrow \Upsilon(4S)$ cross section (1.110 ± 0.008 nb) [15], and the $\Upsilon(4S) \rightarrow BB^0$ branching fraction ($f^{00} = 0.487 \pm 0.010 \pm 0.008$) [16].

Decay	ϵ [%]	Yield	$\mathcal{B}[10^{-6}]$
$B^0 \rightarrow \pi^0 \pi^0$	21.0	$14.0_{-5.6}^{+6.8}$	$0.98_{-0.39}^{+0.48}$

TABLE II. Summary of signal efficiency ϵ , signal yield in 2019-2020 Belle II data and resulting branching fraction. Only the statistical contributions to the uncertainties are given here.

Based on simulations, we expect a signal yield of 21.0 ± 3.4 events and 373 background events in our selection region. In data, we obtain a signal yield of $14.0_{-5.6}^{+6.8}$ as shown in Figure 4 with a statistical significance of 3.4 and 403 background events in our selection region. The statistical significance is assessed by comparing the likelihood ratio observed in data with the distribution on a sample of background-only simulated experiments. The branching fraction is calculated to be $\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = (0.98_{-0.39}^{+0.48} \pm 0.24) \times 10^{-6}$. The first uncertainties are statistical while the second is systematic. This agrees with the previously measured value, $(1.59 \pm 0.26) \times 10^{-6}$. The result is summarized in Table II. The yield for the control mode is 295 ± 31 , as shown in Figure 3, consistent with 288 expected from simulation.

8. SUMMARY

We report the first reconstruction of the $B^0 \rightarrow \pi^0 \pi^0$ decay in Belle II using 62.8 fb^{-1} of data. An improved method of selecting photons for signal reconstruction, `photonMVA`, that utilizes a boosted decision tree rather than rectangular cuts is validated on experimental data. We find a signal yield of $14.0_{-5.6}^{+6.8}$ events, corresponding to a significance of 3.4 standard deviations and determine $\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = (0.98_{-0.39}^{+0.48} \pm 0.27) \times 10^{-6}$, where the first uncertainty is statistical and the second, systematic. With much larger data samples that are expected in the near future, Belle II will be able to measure the direct CP violation parameter, $\mathcal{A}_{CP}(B^0 \rightarrow \pi^0 \pi^0)$ and provide improved constraints on α/ϕ_2 .

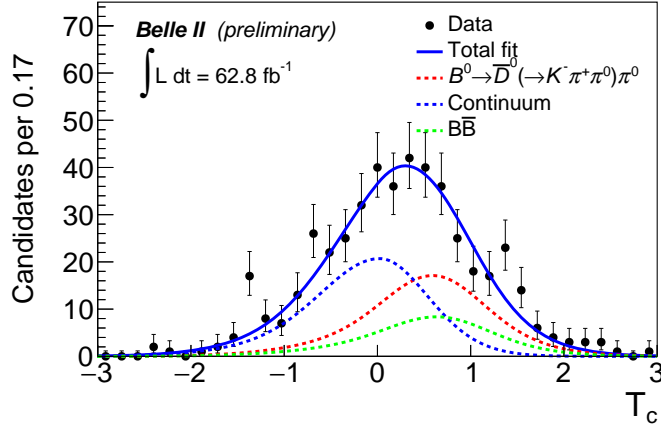
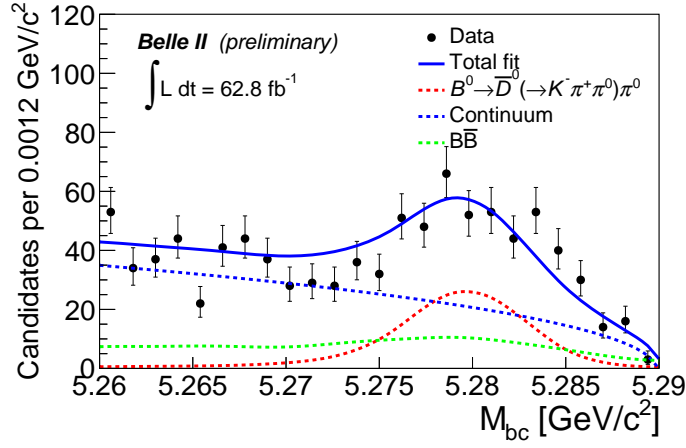
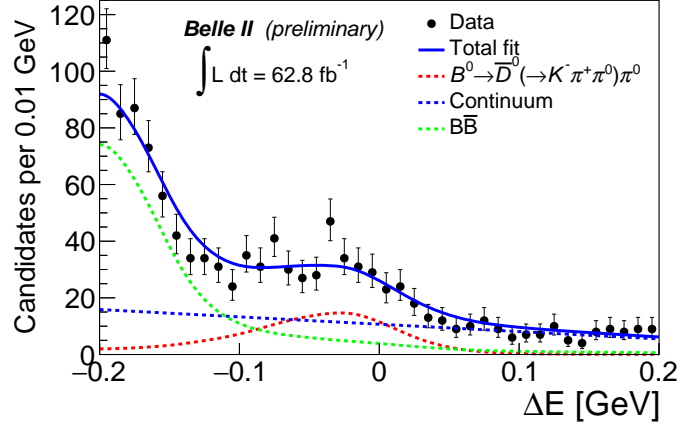


FIG. 3. Distributions of ΔE (top), M_{bc} (middle), and T_c (bottom) for $B^0 \rightarrow \bar{D}^0(\rightarrow K^- \pi^+ \pi^0) \pi^0$ reconstructed in 2019–2020 Belle II data. The distributions are shown in signal-enriched regions of $5.275 < M_{bc} < 5.285 \text{ GeV}/c^2$ and $-1 < T_c < 2$ for ΔE , $-0.1 < \Delta E < 0.05 \text{ GeV}$ and $-1 < T_c < 2$ for M_{bc} and $5.275 < M_{bc} < 5.285 \text{ GeV}/c^2$ and $-0.1 < \Delta E < 0.05 \text{ GeV}$ for T_c . Fit projections are overlaid.

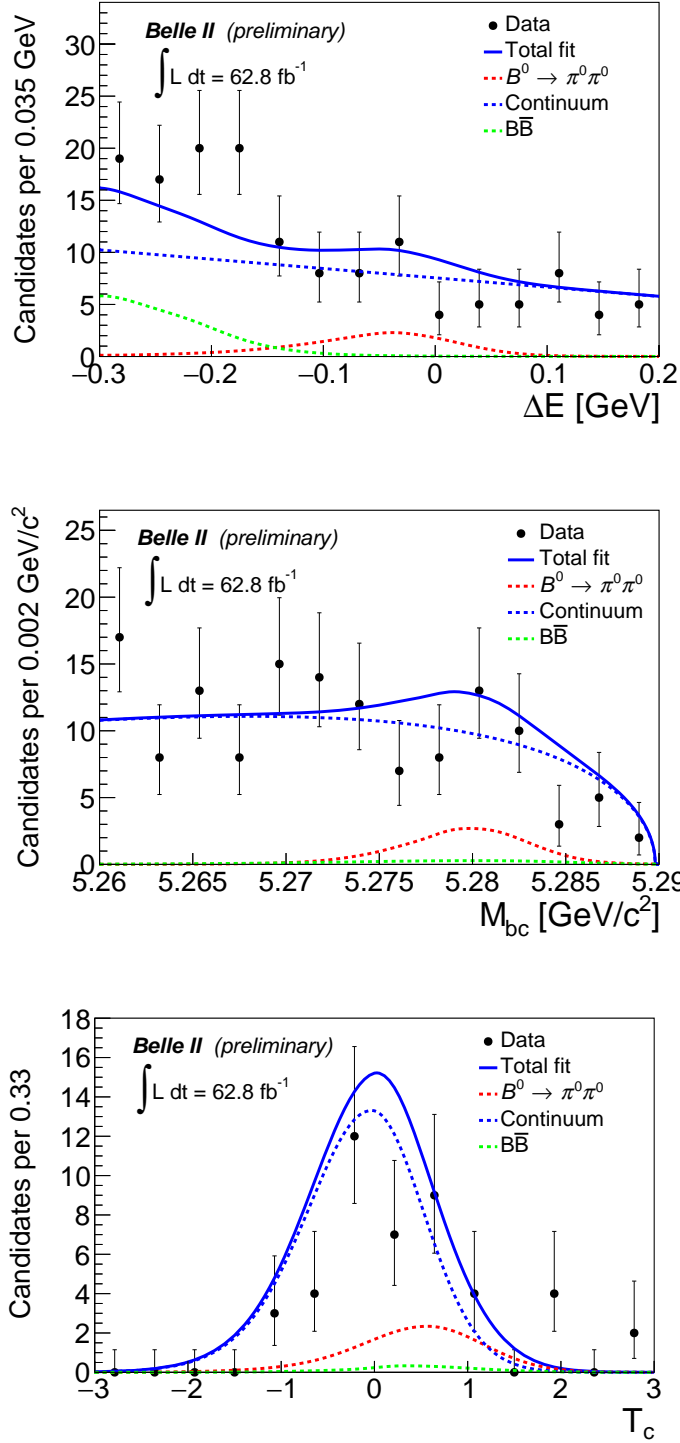


FIG. 4. Distributions of ΔE (top), M_{bc} (middle), and T_c (bottom) for $B^0 \rightarrow \pi^0 \pi^0$ reconstructed in 2019–2020 Belle II data. The distributions are shown in signal-enriched regions of $5.275 < M_{bc} < 5.285 \text{ GeV}/c^2$ and $-1 < T_c < 2$ for ΔE , $-0.1 < \Delta E < 0.05 \text{ GeV}$ and $-1 < T_c < 2$ for M_{bc} and $5.275 < M_{bc} < 5.285 \text{ GeV}/c^2$ and $-0.1 < \Delta E < 0.05 \text{ GeV}$ for T_c . Fit projections are overlaid.

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