



Study of $B^+ \rightarrow J/\psi K^{*+} (\rightarrow K_S^0 \pi^+)$ decays

Natsuki Kuroda and Kenkichi Miyabayashi*

Nara Women's university, Nara, Japan

Abstract

We report a study for reconstruction of the decay chain of $B^0 \rightarrow J/\psi K^{*+}$ followed by $J/\psi \rightarrow \mu^+ \mu^-$, $K^{*+} \rightarrow K_S^0 \pi^+$ and $K_S^0 \rightarrow \pi^+ \pi^-$. The vertex displacement in the same decay where the signal B^+ vertex is reconstructed using all the available tracks or using only the tracks coming from K_S^0 gives an opportunity to investigate possible Data/MC difference in the vertex resolution.

* miyabaya@cc.nara-wu.ac.jp

9 **CONTENTS**

10 1. Introduction 2

11 2. Event selection and relevant quantities' distributions for the signal MC 2

12 3. Analysis on the experimental data 4

13 4. Materials that may be included in backup slides 6

14 Acknowledgment 6

15 A. Event generation 6

16 References 7

17 **1. INTRODUCTION**

18 Checking possible difference between experimental data and Monte Carlo simulation
19 (MC) for the B decay vertex resolution is a key ingredient to perform time-dependent CP
20 violation measurements. Among the $b \rightarrow s$ or $b \rightarrow d$ penguin diagram induced neutral B me-
21 son decays, there are several decay modes for which only $K_S^0 \rightarrow \pi^+\pi^-$ gives charged track
22 information to reconstruct B decay vertex, for example, $B^0 \rightarrow K_S^0 K_S^0 K_S^0$, $K_S^0 \pi^0$, $K_S^0 K_S^0$,
23 $K_S^0 \pi^0 \gamma$ and so on. For these decay modes, the B decay vertex is reconstructed by the kine-
24 matical fit involving proper constraint on the interaction point (IP) and straight track of
25 K_S^0 using its daughter charged pion pair. It is important to confirm there is no significant
26 difference between data and MC for the $K_S^0 \rightarrow \pi^+\pi^-$ based B vertex resolution to figure out
27 the vertex resolution function for time-dependent CP violation. Here, the vertex resolution
28 is different from usual cases such as $B^0 \rightarrow J/\psi K^0$, $\pi^+\pi^-$ and so on where there are charged
29 daughter tracks directly coming from the B decay vertex. The $B^0 \rightarrow J/\psi K^{*+}$ followed by
30 $J/\psi \rightarrow \mu^+\mu^-$, $K^{*+} \rightarrow K_S^0 \pi^+$ and $K_S^0 \rightarrow \pi^+\pi^-$ mode has an advantage compared to the
31 $B \rightarrow D^{(*)}\pi$ mode as a calibration sample because it is free from finite charm meson life-
32 time that gives a sizable smearing in addition to the detector resolution itself. The vertex
33 displacement in the same decay where the signal B^+ vertex is reconstructed using all the
34 available tracks or using only the tracks coming from K_S^0 gives an opportunity to investigate
35 possible Data/MC difference in the vertex resolution.

36 **2. EVENT SELECTION AND RELEVANT QUANTITIES' DISTRIBUTIONS**
37 **FOR THE SIGNAL MC**

38 For charged tracks except for the $K_S^0 \rightarrow \pi^+\pi^-$ daughters, we require $|d_r| < 2$ cm and
39 $|d_z| < 5$ cm. For $J/\psi \rightarrow \mu^+\mu^-$ reconstruction, both tracks are required to be identified
40 as muons to satisfy `muonID` > 0.2. The $J/\psi \rightarrow \mu^+\mu^-$ candidates are selected by requiring
41 $M_{\mu^+\mu^-}$, $3.05 \text{ GeV}/c^2 < M_{\mu^+\mu^-} < 3.15 \text{ GeV}/c^2$ where $M_{\mu^+\mu^-}$ is the di-muon invariant mass.
42 We require $0.491 \text{ GeV}/c^2 < M_{\pi^+\pi^-} < 0.504 \text{ GeV}/c^2$ to select $K_S^0 \rightarrow \pi^+\pi^-$ candidates. In
43 order to select $K^{*+} \rightarrow K_S^0 \pi^+$ (and c.c.), the pion candidate track is required to satisfy
44 `pionID` > 0.05 to reject obvious kaon and proton tracks. The K^{*+} candidates are selected by

45 requiring $0.8 \text{ GeV}/c^2 < M_{K\pi} < 1.0 \text{ GeV}/c^2$ where $M_{K\pi}$ denotes the $K\pi$ invariant mass. The
 46 events having at least one candidate satisfying $-0.3 \text{ GeV} < \Delta E < 0.3 \text{ GeV}$ and $5.2 \text{ GeV}/c^2$
 47 $< M_{bc} < 5.29 \text{ GeV}/c^2$ are retained for further analysis. When multiple candidates are found in one event,
 48 we select the one having the highest χ^2 - p -value. The resultant M_{bc} and ΔE distributions are
 49 shown in Fig. 1. We define B candidate signal box as $5.27 \text{ GeV}/c^2 < M_{bc} < 5.29 \text{ GeV}/c^2$
 50 and $-0.06 \text{ GeV} < \Delta E < 0.04 \text{ GeV}$.

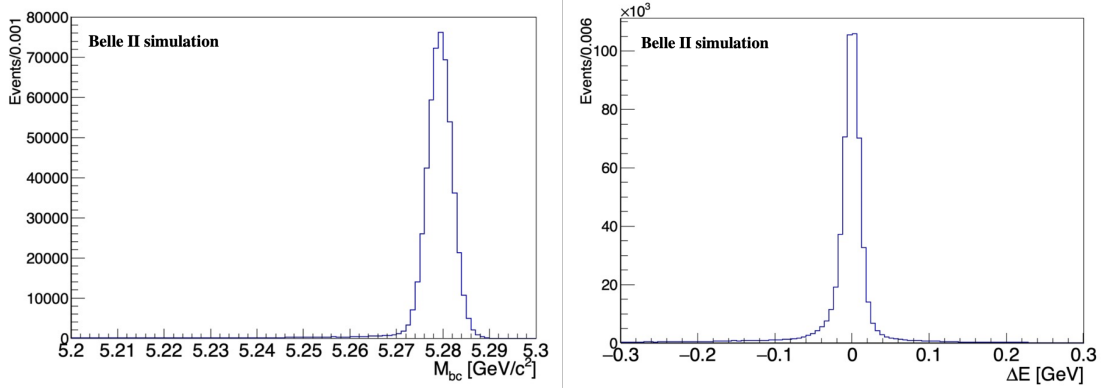


FIG. 1. M_{bc} (left) distribution in $-0.06 \text{ GeV} < \Delta E < 0.04 \text{ GeV}$ region and ΔE (right) distribution
 51 in $5.27 \text{ GeV}/c^2 < M_{bc} < 5.29 \text{ GeV}/c^2$ for the signal MC events.

52
 53 Calling the TreeFit program, we can reconstruct B decay vertex where $J/\psi \rightarrow \mu^+\mu^-$ is
 54 dominant to determine the vertex position. While, to see the $K_S^0 \rightarrow \pi^+\pi^-$ contribution to
 55 obtain the B vertex, the z_0 and d_0 errors are 1000 times inflated for the J/ψ daughter muon
 56 and the pion promptly coming from K^{*+} decay tracks[1]. The z -residual to be defined as
 57 the difference between the reconstructed and generated z coordinates and its distributions
 58 for two different vertex reconstruction methods are shown in Fig.2.

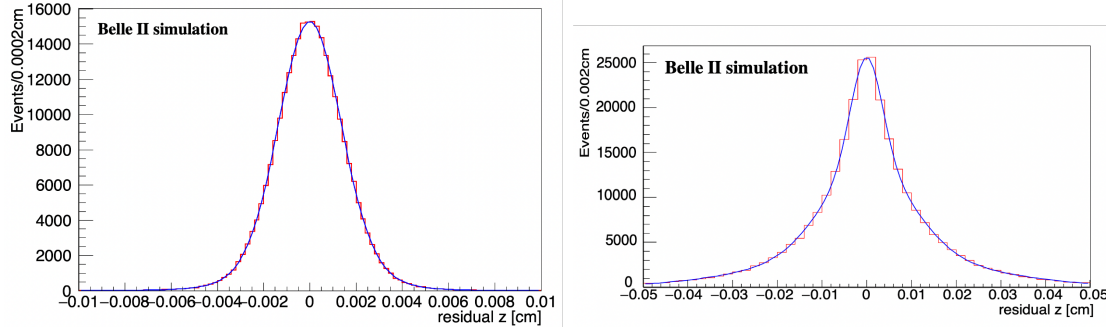


FIG. 2. Distributions of z -residual, difference between the reconstructed and generated z coordi-
 nates of the B decay vertex with usual (left) and $K_S^0 \rightarrow \pi^+\pi^-$ -based (right) cases for the signal
 MC events in the signal region. Fit with triple Gaussian is performed and the standard deviation
 is obtained by the weighted average of three Gaussian's spread: $\sigma = 15.9 \pm 0.5 \mu\text{m}$ and 157.7 ± 1.5
 59 μm for usual and $K_S^0 \rightarrow \pi^+\pi^-$ -based B vertex reconstruction cases, respectively.

60
 61 As the quantity we can directly compare between Data and MC, the $z_{\text{diff}} \equiv z_{\text{usual}} - z_{K_S^0}$
 62 is thought to be functional, where z_{usual} and $z_{K_S^0}$ are the z coordinate for the usual and the
 63 $K_S^0 \rightarrow \pi^+\pi^-$ -based B decay vertex reconstruction cases. The z_{diff} distribution for the signal

64 MC events found in the signal region is shown in Fig.3. As expected, we found the spread
 65 of z distribution is dominated by the B decay vertex resolution by the $K_S^0 \rightarrow \pi^+\pi^-$ -based
 66 reconstruction.

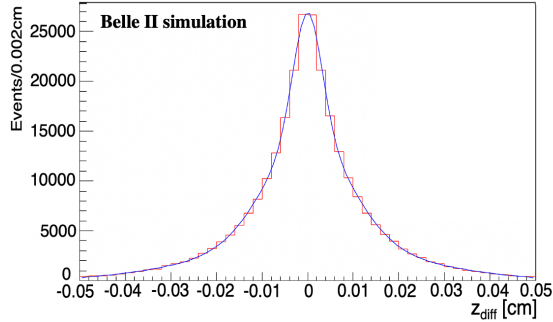


FIG. 3. Distributions of $z_{\text{diff}} \equiv z_{\text{usual}} - z_{K_S^0}$ where z_{usual} and $z_{K_S^0}$ are the z coordinate for the
 usual and the $K_S^0 \rightarrow \pi^+\pi^-$ -based B decay vertex reconstruction cases.. Fit with triple Gaussian
 is performed and the standard deviation is obtained by the weighted average of three Gaussian's
 spread: $\sigma = 150.9 \pm 1.5 \mu\text{m}$.

69 3. ANALYSIS ON THE EXPERIMENTAL DATA

70 We analyzed the Belle II data collected on $\Upsilon(4S)$ resonance corresponding to 362 fb^{-1} .
 71 The resultant M_{bc} and ΔE distributions is shown in Fig.4. From the fit, we found 939 ± 33
 72 signal events and 85 ± 22 background events in the signal region defined as $5.27 \text{ GeV}/c^2 < M_{\text{bc}} < 5.29 \text{ GeV}/c^2$
 73 $< M_{\text{bc}} < 5.29 \text{ GeV}/c^2$ and $-0.06 \text{ GeV} < \Delta E < 0.04 \text{ GeV}$. Since expected background MC
 74 M_{bc} distribution exhibits a small peak at the same position as signal as shown in Fig.7, the
 75 possible difference of the estimated background events is derived by the MC distribution
 76 and it is found to be 110 events.

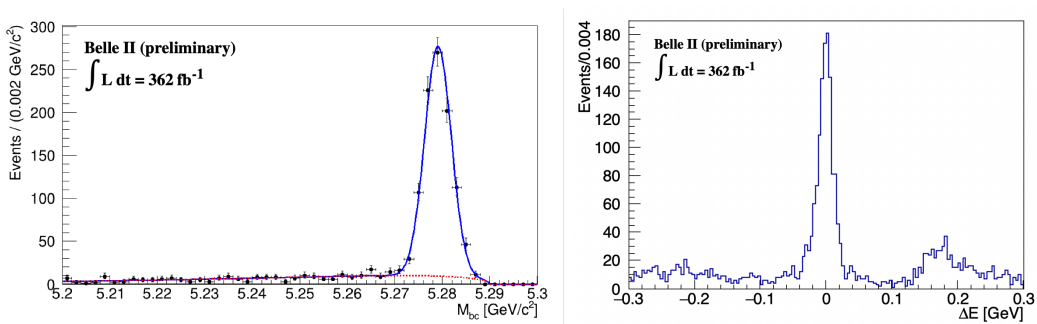
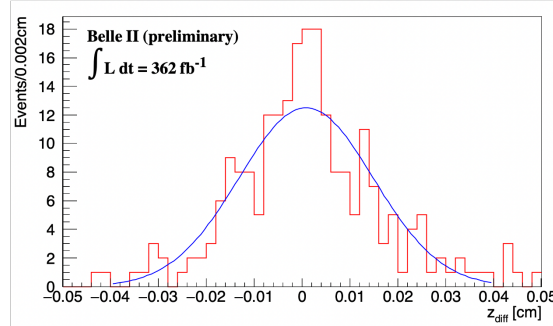


FIG. 4. M_{bc} (left) distribution in $-0.06 \text{ GeV} < \Delta E < 0.04 \text{ GeV}$ region and ΔE (right) distribution
 in $5.27 \text{ GeV}/c^2 < M_{\text{bc}} < 5.29 \text{ GeV}/c^2$ in the Belle II experimental data corresponding to 362 fb^{-1} .
 For M_{bc} distribution, the fit with Gaussian signal + ARGUS background is performed and its
 result is drawn as the lines to express total (blue solid line) and background (red dashed line).

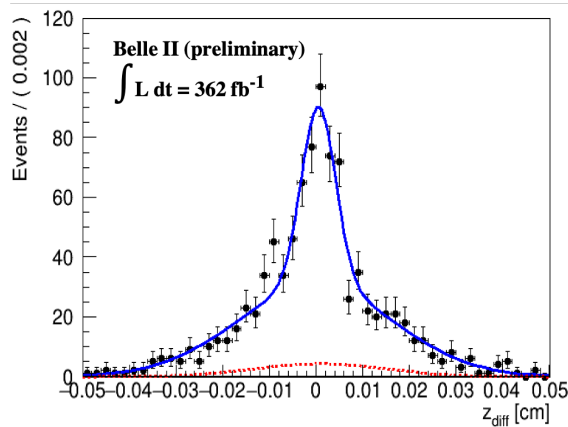
78
 79 As for the z_{diff} distribution, the background probability density function (PDF) is deter-
 80 mined by the M_{bc} sideband ($5.20 \text{ GeV}/c^2 < M_{\text{bc}} < 5.27 \text{ GeV}/c^2$ and $-0.06 \text{ GeV} < \Delta E <$

81 0.04 GeV) events as shown in Fig.5. It is fitted with Gaussian and mean (μ) and standard
 82 deviation (σ) are found to be $\mu = 8.4 \pm 9.0 \mu\text{m}$ and $\sigma = 140 \pm 7 \mu\text{m}$, respectively.



83 FIG. 5. The $z_{\text{diff}} \equiv z_{\text{usual}} - z_{K_S^0}$ distribution in the M_{bc} sideband ($5.20 \text{ GeV}/c^2 < M_{bc} < 5.27$
 84 GeV/c^2 and $-0.06 \text{ GeV} < \Delta E < 0.04 \text{ GeV}$) region. The Gaussian's mean (μ) and standard
 85 deviation (σ) are found to be $\mu = 8.4 \pm 9.0 \mu\text{m}$ and $\sigma = 140 \pm 7 \mu\text{m}$, respectively.

86 The signal z_{diff} distribution is fitted with double Gaussian for signal and the background
 87 PDF determined by the M_{bc} sideband events. The standard deviation of the signal dis-
 88 tribution is found to be $\sigma = 142 \pm 7 \mu\text{m}$ where statistical error only quoted. Systematic



89 FIG. 6. The z_{diff} distribution in the Data signal box. The signal component is described by double
 90 Gaussian and its spread is found to be $\sigma = 142 \pm 7(\text{stat}) \pm 2(\text{syst}) \mu\text{m}$.

91 uncertainty is estimated by varying background PDF's μ , σ and background fraction and
 92 corresponding effects are found to be negligible, $\pm 1 \mu\text{m}$ and $\pm 1 \mu\text{m}$, respectively. Changing
 93 the background from 85 events to 110 events to estimate potential peaking background's
 94 effect, the resultant z_{diff} spread change is found to be $1 \mu\text{m}$. Summing up them in quadrature
 95 results in $\pm 1.7 \mu\text{m}$, so the z_{diff} standard deviation is quoted to be $\sigma = 142 \pm 7(\text{stat}) \pm 2(\text{syst})$
 96 μm . Compared to the one in MC, $\sigma = 150.9 \pm 1.5 \mu\text{m}$, we see a good agreement between
 97 Data and MC. Currently the resolution function for the $K_S^0 \rightarrow \pi^+\pi^-$ -based B decay vertex
 98 reconstruction is mainly based on the knowledge obtained by the MC and validated with a
 99 possible control sample. The result by this work gives a strong support for currently taken
 100 procedure to compose vertex resolution function for $K_S^0 \rightarrow \pi^+\pi^-$ -based B decay vertex
 reconstruction by carrying out an independent study.

101 **4. MATERIALS THAT MAY BE INCLUDED IN BACKUP SLIDES**

102 Generic MC sample is also visited to estimate amount of the background. As shown
 103 in Fig.7, the $B^+ \rightarrow J/\psi K^{*+}$ mode is expected to have high purity $\sim 90\%$. Comparison

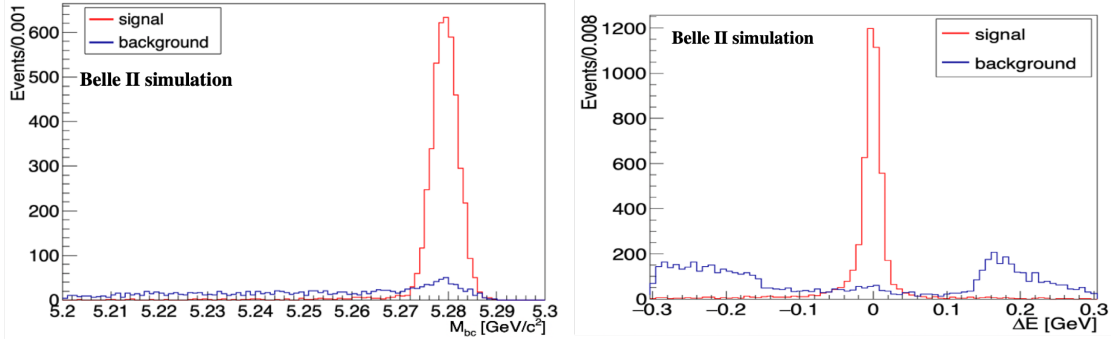
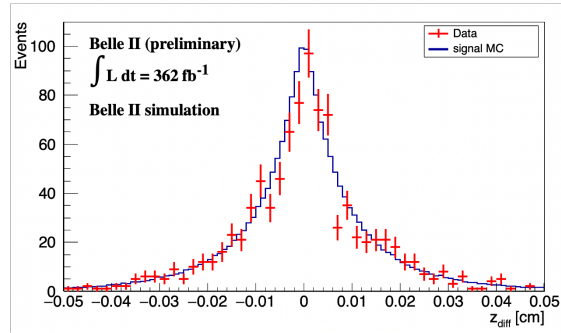


FIG. 7. M_{bc} (left) distribution in $-0.06 \text{ GeV} < \Delta E < 0.04 \text{ GeV}$ region and ΔE (right) distribu-
 104 tion in $5.27 \text{ GeV}/c^2 < M_{bc} < 5.29 \text{ GeV}/c^2$ for the background MC events where the signal MC
 105 expectation is superimposed.

106 between Data and signal MC z_{diff} distributios is shown in FIg.8.



107 FIG. 8. The z_{diff} distribution to compare Data and signal MC.

109 **ACKNOWLEDGMENT**

110 The authors wish to thank Dr. Kazutaka Sumisawa and Prof. Yutaka Ushiroda for their
 111 continuous encouragement and discussion. The authors also thank the time-dependent CP
 112 violation group conveners, Drs. Thibaud and Takeo Higuchi for their support. The authors
 113 also appreciate a lot for the efforts for reviewing and arranging approval process by the
 114 physics coordinator, Dr. Diego Toneli.

115 **Appendix A: Event generation**

116 Since the $B^+ \rightarrow J/\psi K^{*+}$ mode is a Pseudo-Scalar to Vector Vector ($P \rightarrow VV$) decay,
 117 the final state is a linear combination of three amplitudes. Usually the decay amplitude is

118 expressed by the two transverse polarization amplitudes (H_+ and H_-) and one longitudinal
119 polarization amplitude (H_0) basis. Experimentally, common formula is the transversity basis
120 that is expressed as the linear combination of H_+ , H_- and H_0 ;

$$A_{\parallel} = \frac{H_+ + H_-}{\sqrt{2}} \quad (\text{A1})$$

$$A_{\perp} = \frac{H_+ - H_-}{\sqrt{2}} \quad (\text{A2})$$

$$A_0 = H_0. \quad (\text{A3})$$

121 Since the SVVHELAMP model in the EvtGen generator is based on the H_+ , H_- and H_0 for-
122 malism, the $B \rightarrow J/\psi K^*$ decay's polarization measurement presented by the A_{\parallel} , A_{\perp} and
123 A_0 basis in PDG was converted.

124 [1] H. Tanigawa developed the code to inflate specific tracks' d_0 and z_0 errors to see other tracks'
125 contribution to determine the parent B decay vertex.