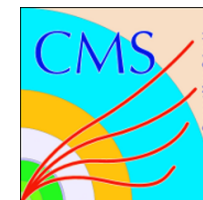




Jul 9, 2024



# Lepton Flavor Universality Violation: the Experimental View.

PASCOS 2024, ICISE, Quy Nhon, Vietnam,  
July 9, 2024

Francesco Forti, INFN and University, Pisa

F.Forti, LFUV



# Outline

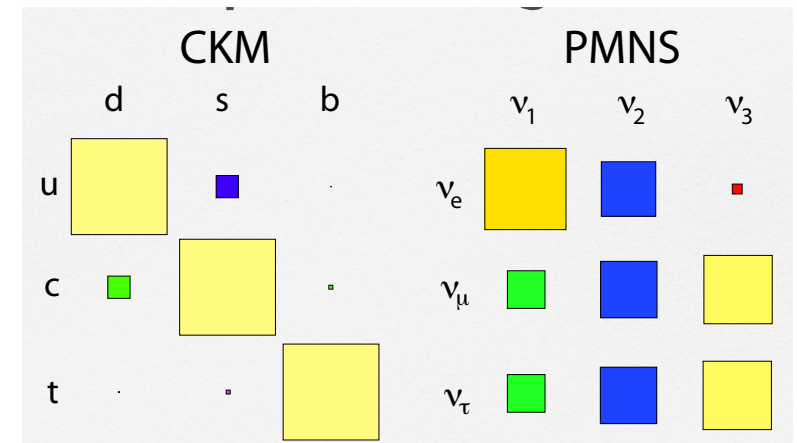
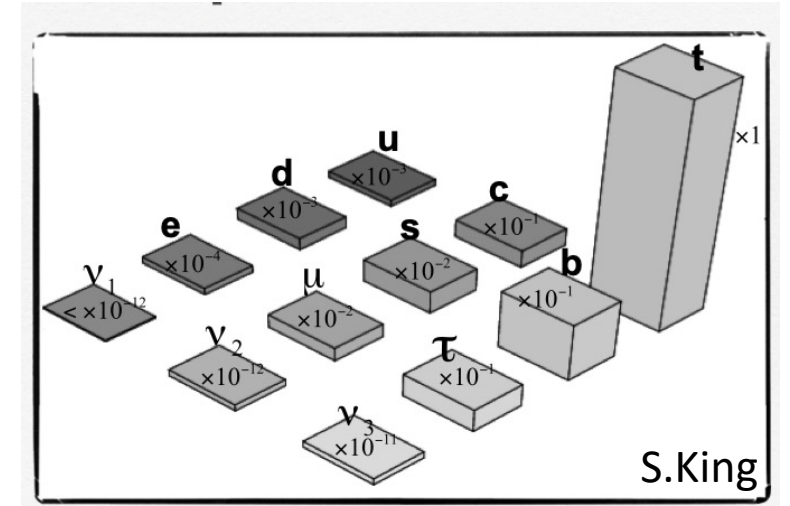
- What is LFUV and why it is relevant
- Experiments and data sets
- Low energy
  - Light mesons decays
  - Tau decays
- High energy:
  - W and Z decays
  - TeV scale
- Heavy flavour transitions
  - $c \rightarrow s \ell \nu$  transitions
  - $b \rightarrow s \ell \ell$  transitions
  - $b \rightarrow c \ell \nu$  transitions
- Conclusions

# What is LFUV and why it matters

- SM: 3 generations of leptons with the same gauge couplings
  - Difference in masses and Higgs coupling
- SM fields do mix:
  - Quarks  $\rightarrow$  CKM matrix
  - Neutrinos  $\rightarrow$  PMNS matrix
- For charged leptons the matrix seems purely diagonal
- Lepton Flavor Violation: out of diagonal term
- Lepton Flavor Universality Violation: diagonal terms not all equal
  - Sensitive to physics beyond the standard model
  - Tensions or anomalies observed in various channels
- Accidental symmetry, not coming from first principles

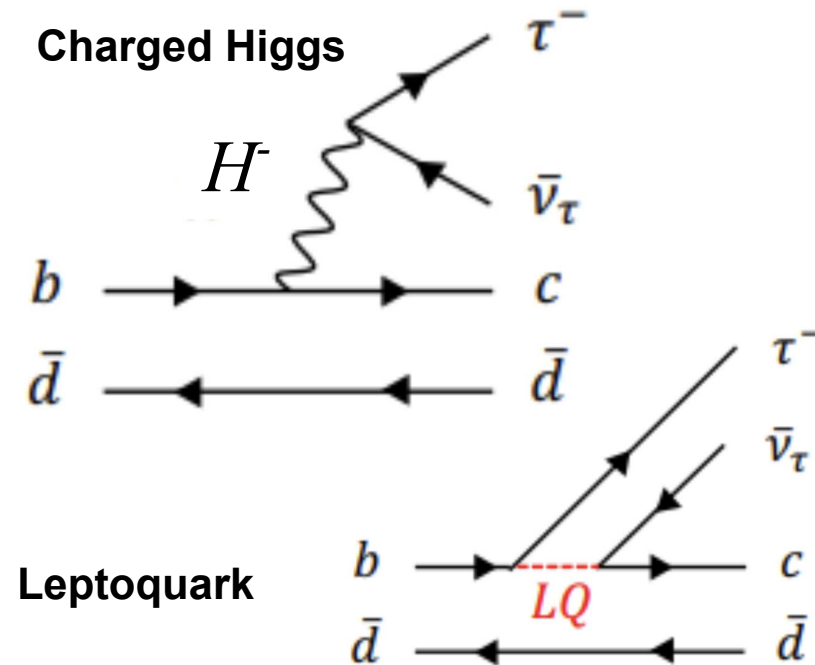
$$m_e \neq m_\mu \neq m_\tau$$

	e	$\mu$	$\tau$
$\nu_{e,e}$	1.	0.	0.
$\nu_{\mu,\mu}$	0.	1.	0.
$\nu_{\tau,\tau}$	0.	0.	1.



# Possible sources of LFUV

- LFUV experimental bounds can be interpreted as constraints on New Physics
- Effective Field Theory
  - Modified  $W\ell\nu$  couplings
  - Four-lepton operators
  - Two-quark-two-lepton operators
- Specific NP models
  - $W'$  boson
  - Vector-like leptons
  - Additional  $SU(2)_L$  scalars
  - $Z'$  boson
  - Leptoquark
  - Charged Higgs



[Annu. Rev. Nucl. Part. Sci. 2022. 72:69–91](#)

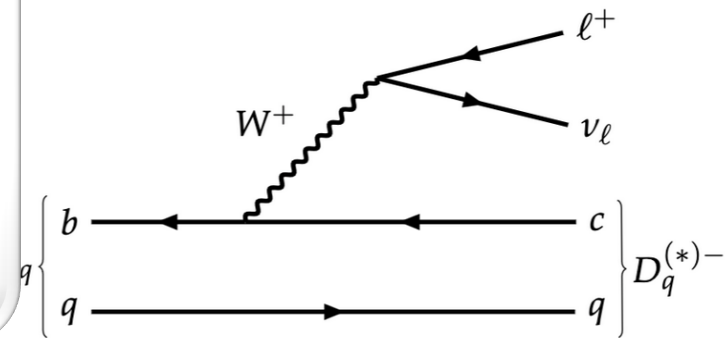
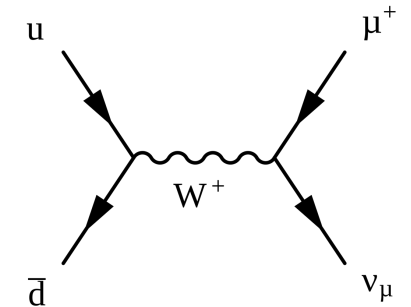
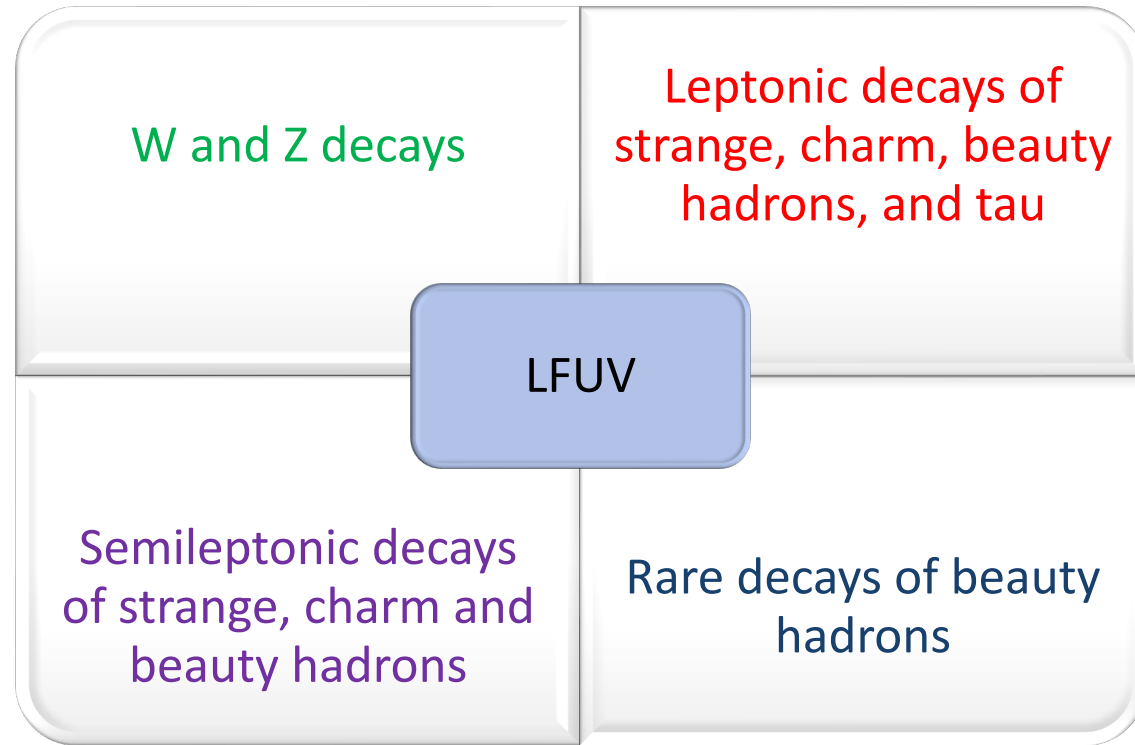
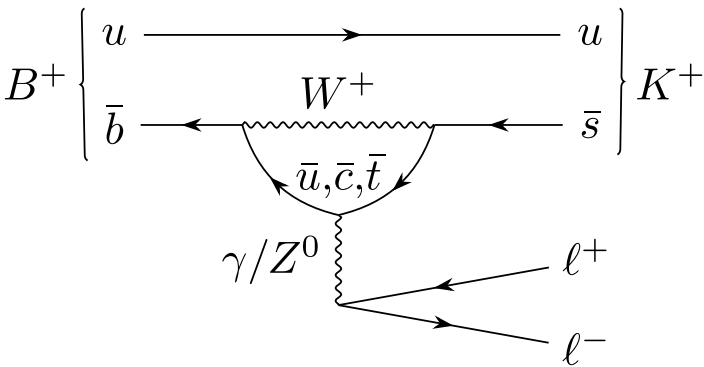


# How can we observe LFUV

- Measure ratios of processes with different leptons to reduce systematics

A.Knue

$$R = \frac{B[\omega \rightarrow \ell_1 \nu_1]}{B[\omega \rightarrow \ell_2 \nu_2]}$$




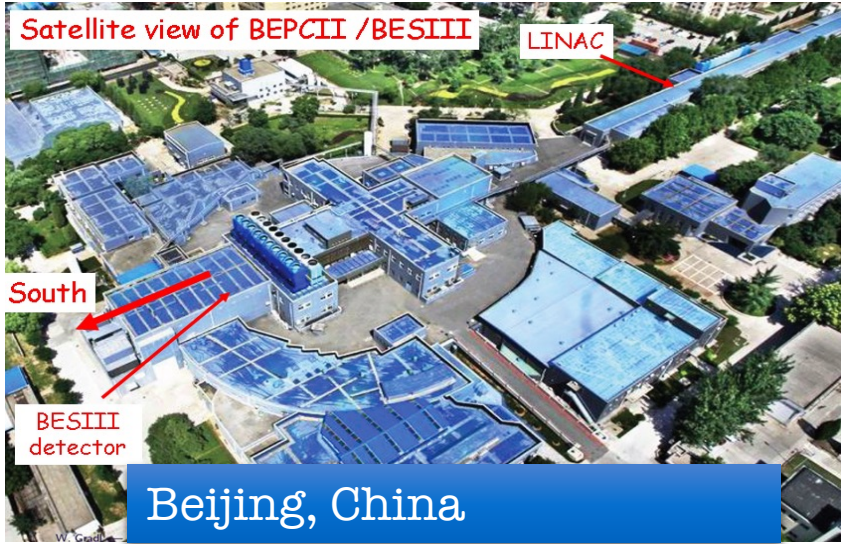
Charge conjugated processes implied

# Experiments and data sets

**Beam energy:** 1.0-2.3 GeV  
**Optimum energy:** 1.89 GeV  
**Designed luminosity:**  $1.00 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$   
**Data taken from:** 2009  
**Achieved luminosity:**  $1.00 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

CM energy	Data set
3.773 GeV	7.9 fb <sup>-1</sup>
4.178 GeV	7.3 fb <sup>-1</sup>
4.6 GeV	4.5 fb <sup>-1</sup>

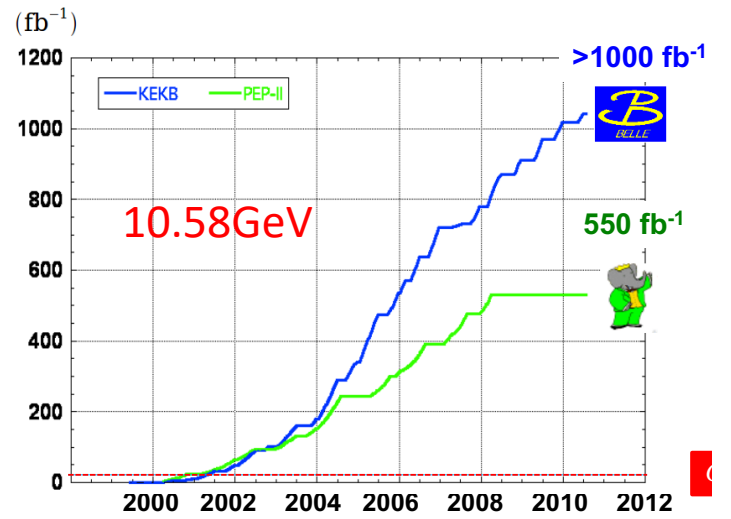
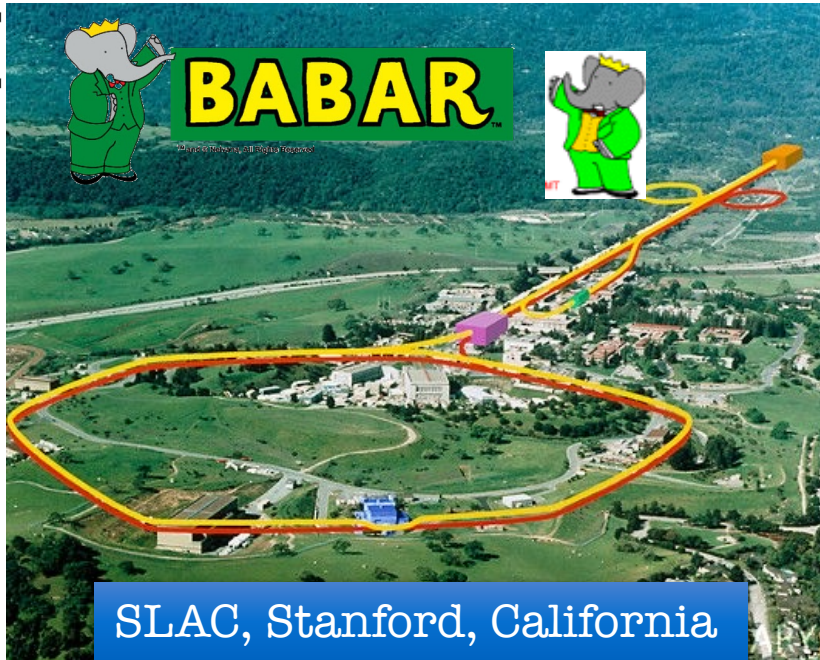
BESS III @ BEPCII: 2009-



Channel	Belle	BaBar
$B\bar{B}$	$7.7 \times 10^8$	$4.8 \times 10^8$
$B_s^{(*)}\bar{B}_s^{(*)}$	$7.0 \times 10^6$	—
$\Upsilon(1S)$	$1.0 \times 10^8$	—
$\Upsilon(2S)$	$1.7 \times 10^8$	$0.9 \times 10^7$
$\Upsilon(3S)$	$1.0 \times 10^7$	$1.0 \times 10^8$
$\Upsilon(5S)$	$3.6 \times 10^7$	—
$\tau\tau$	$1.0 \times 10^9$	$0.6 \times 10^9$

10.58GeV

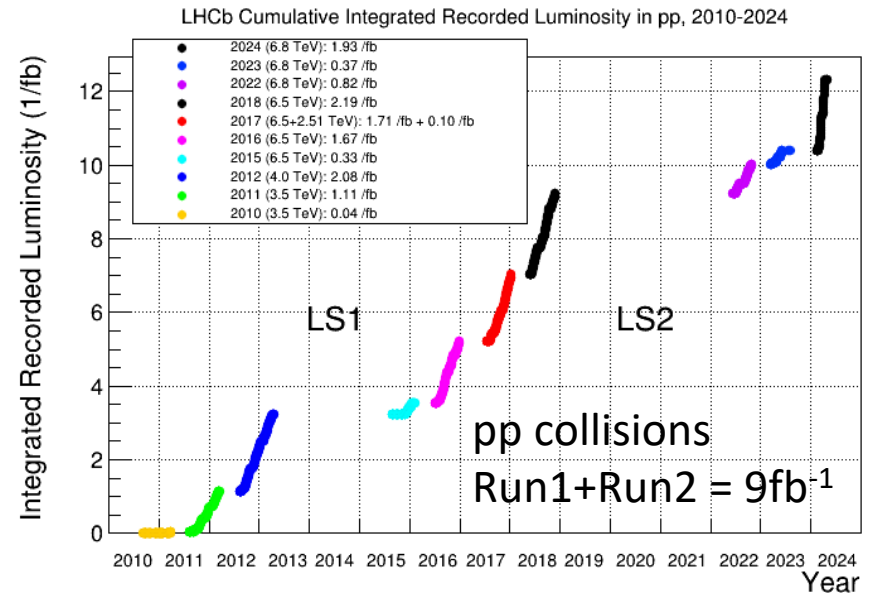
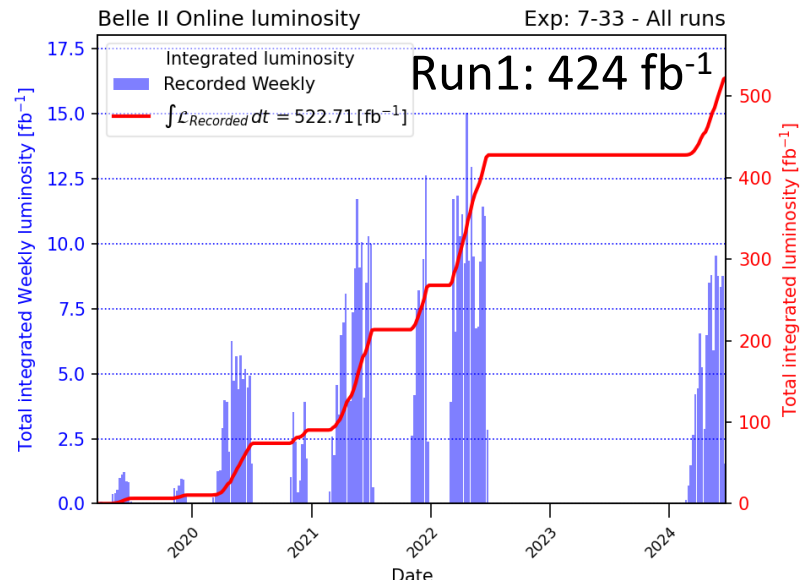
BABAR @ PEP-II: 1999-2008



BELLE @ KEKB: 1999-2010

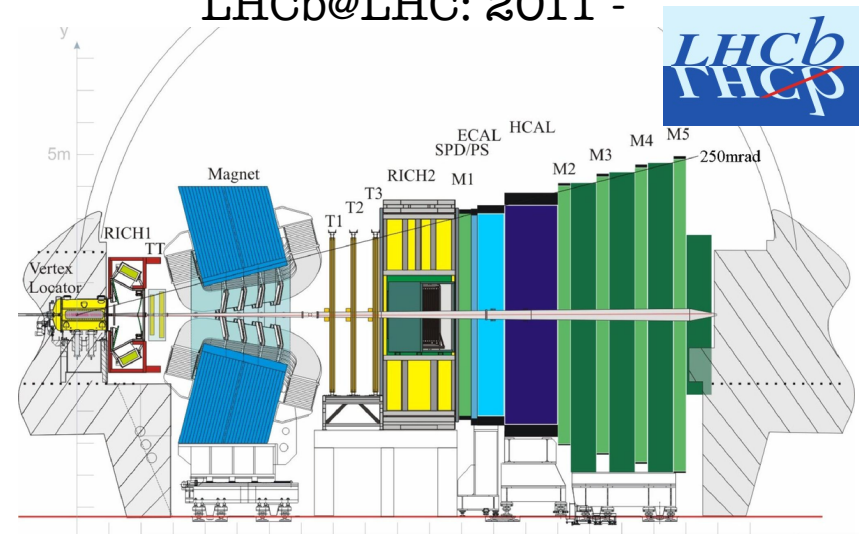
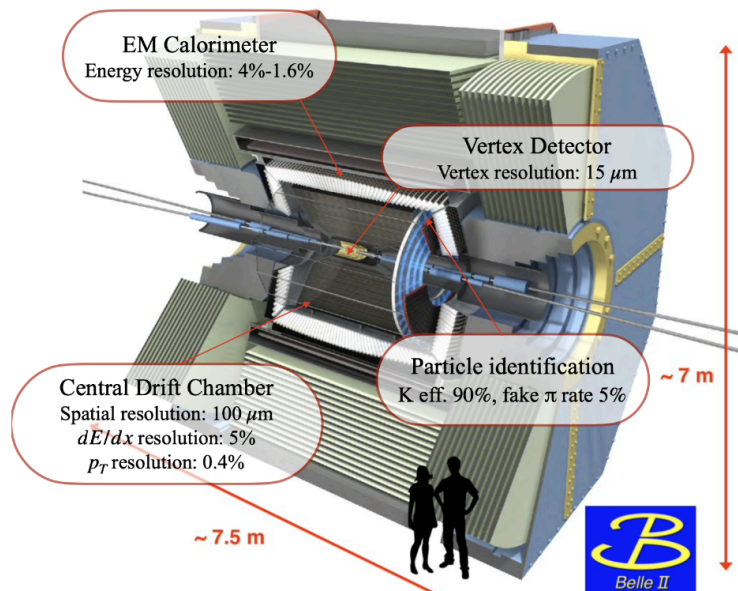






BELLE II @ SuperKEKB: 2019 -

LHCb@LHC: 2011 -



KEK, Tsukuba, Japan

F.Forti, LFUV

CERN, Geneva, Switzerland



# Low Energy



# $\mu/e$ : Light meson decays

- Pseudo scalars leptonic decays

- $P = \pi/K$

$$R_{e/\mu}^P = \frac{\Gamma[P \rightarrow e\bar{\nu}_e(\gamma)]}{\Gamma[P \rightarrow \mu\bar{\nu}_\mu(\gamma)]}, = \bar{R}_{e/\mu}^P \left[ 1 + \Delta_{e^2 Q^0}^P + \dots \right]$$

- Helicity suppressed because of V-A

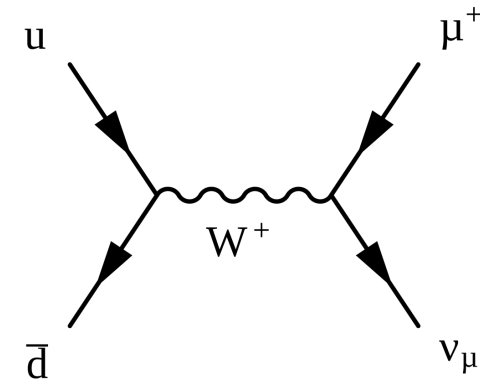
- Can be calculated at  $10^{-4}$  level with radiative corrections

$$\bar{R}_{e/\mu}^P = \frac{m_e^2}{m_\mu^2} \left( \frac{m_P^2 - m_e^2}{m_P^2 - m_\mu^2} \right)^2$$

- Recast in terms of ratios of coupling constants

$$L_{CC} = A_\ell \bar{u} \gamma^\mu P_L d \bar{\nu}_\ell \gamma_\mu P_L \ell,$$

$$\left( \frac{A_\mu}{A_e} \right)_{R_{e/\mu}^\pi} = 1.0010 \pm 0.0009, \quad \left( \frac{A_\mu}{A_e} \right)_{R_{e/\mu}^K} = 0.9978 \pm 0.0018.$$



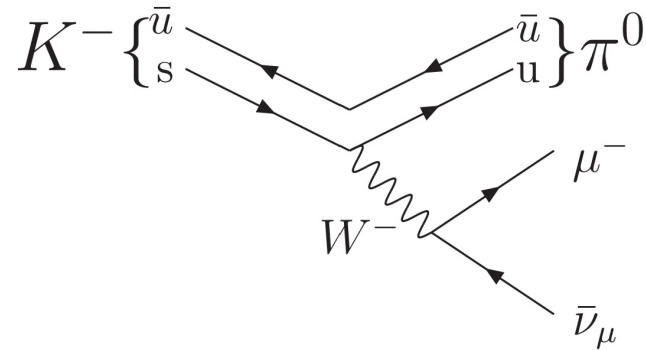
- Compatible with SM

PDG Averages, see

[Annu. Rev. Nucl. Part. Sci. 2022. 72:69–91](#)

# $\mu/e$ : semileptonic decays $s \rightarrow u l \nu$ , $c \rightarrow s l \nu$

- The SM ratio is determined entirely by phase-space factors and long-distance radiative corrections

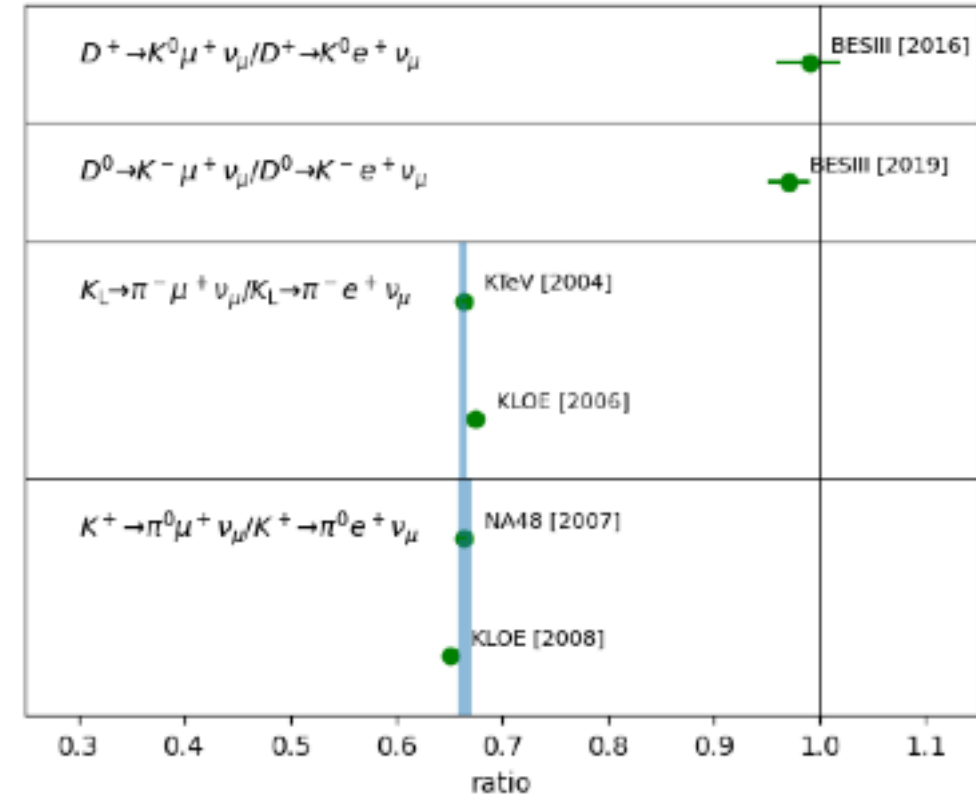


$$\left( \frac{A_\mu}{A_e} \right)_{R_{e/\mu}^{K \rightarrow \pi}} = 1.0009 \pm 0.0018.$$

$K^0/K^{+-}$  average

PDG average see

[Annu. Rev. Nucl. Part. Sci. 2022. 72:69–91](#)



Ratios of Branching Fractions

[http://www.scholarpedia.org/article/Lepton flavour universality](http://www.scholarpedia.org/article/Lepton_flavour_universality)

CM energy	Data set
3.773 GeV	7.9 fb <sup>-1</sup>
4.178 GeV	7.3 fb <sup>-1</sup>
4.6 GeV	4.5 fb <sup>-1</sup>

$\mu/e$  : more  $c \rightarrow sl\nu$

## $D_s$ leptonic decays

BESIII		PRD108(2023)11200, $\mu\nu$	$(5.29 \pm 0.11 \pm 0.09) \times 10^{-3}$
CLEO	PRD79(2009)052002, $\tau_e\nu$	$5.32 \pm 0.47 \pm 0.22$	
CLEO	PRD80(2009)112004, $\tau_\rho\nu$	$5.50 \pm 0.54 \pm 0.24$	
CLEO	PRD79(2009)052001, $\tau_\pi\nu$	$6.47 \pm 0.80 \pm 0.22$	
BaBar	PRD82(2010)091103, $\tau_{e,\mu}\nu$	$4.96 \pm 0.37 \pm 0.57$	
Belle	JHEP09(2013)139, $\tau_{e,\mu,\pi}\nu$	$5.70 \pm 0.21 \pm 0.31$	
<hr/>			
BESIII 6.32 fb <sup>-1</sup>	PRD104(2021)052009, $\tau_\pi\nu$	$5.21 \pm 0.25 \pm 0.17$	
BESIII 6.32 fb <sup>-1</sup>	PRD104(2021)032001, $\tau_\rho\nu$	$5.29 \pm 0.25 \pm 0.23$	
BESIII 6.32 fb <sup>-1</sup>	PRL127(2021)171801, $\tau_e\nu$	$5.27 \pm 0.10 \pm 0.12$	
BESIII 7.33 fb <sup>-1</sup>	PRD108(2023)092014, $\tau_\pi\nu$	$5.44 \pm 0.17 \pm 0.13$	
BESIII 7.33 fb <sup>-1</sup>	JHEP09(2023)124, $\tau_\mu\nu$	$5.37 \pm 0.17 \pm 0.15$	
<b>BESIII</b>	$\tau\nu$	<b><math>5.33 \pm 0.07 \pm 0.08</math></b>	<b>*** Combined</b>

-5

0

5

$B(D_s^+ \rightarrow \tau^+\nu)$  (%)

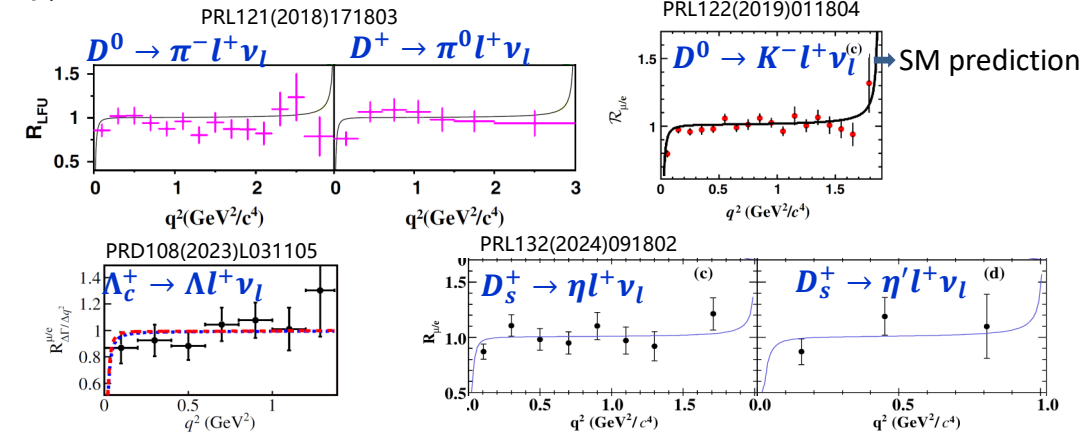
$$R_{\tau/\mu} = \frac{B[D_s^+ \rightarrow \tau^+\nu]}{B[D_s^+ \rightarrow \mu^+\nu]} = 10.05 \pm 0.35, \text{ consistent with the SM prediction } 9.75$$

## $D$ semileptonic decays

★  $\mathcal{R}_{\mu/e}$  obtained by measuring BFs

	Ref	$\mathcal{R}_{\mu/e}$	SM prediction
$D^+ \rightarrow \eta l^+ \nu_l$	PRL124(2020)231801	$0.91 \pm 0.13$	0.97 – 1.00
$D^+ \rightarrow \omega l^+ \nu_l$	PRD101(2020)072005	$1.05 \pm 0.14$	0.93 – 0.99
$D^+ \rightarrow \rho l^+ \nu_l$	PRD104(2021)L091103	$0.90 \pm 0.11$	0.93 – 0.96

★  $\mathcal{R}_{\mu/e}$  in the full kinematic region



Consistent with SM predictions

# LFUV, Beta Decays, and Cabibbo Angle Anomaly

- CKM Unitarity requires

$$\Delta_{\text{CKM}} \equiv |V_{ud}|^2 + |V_{us}|^2 + |\cancel{V_{ub}}|^2 - 1 = 0$$

- Extraction of  $V_{uD}$  ( $= V_{ud}, V_{us}$ )

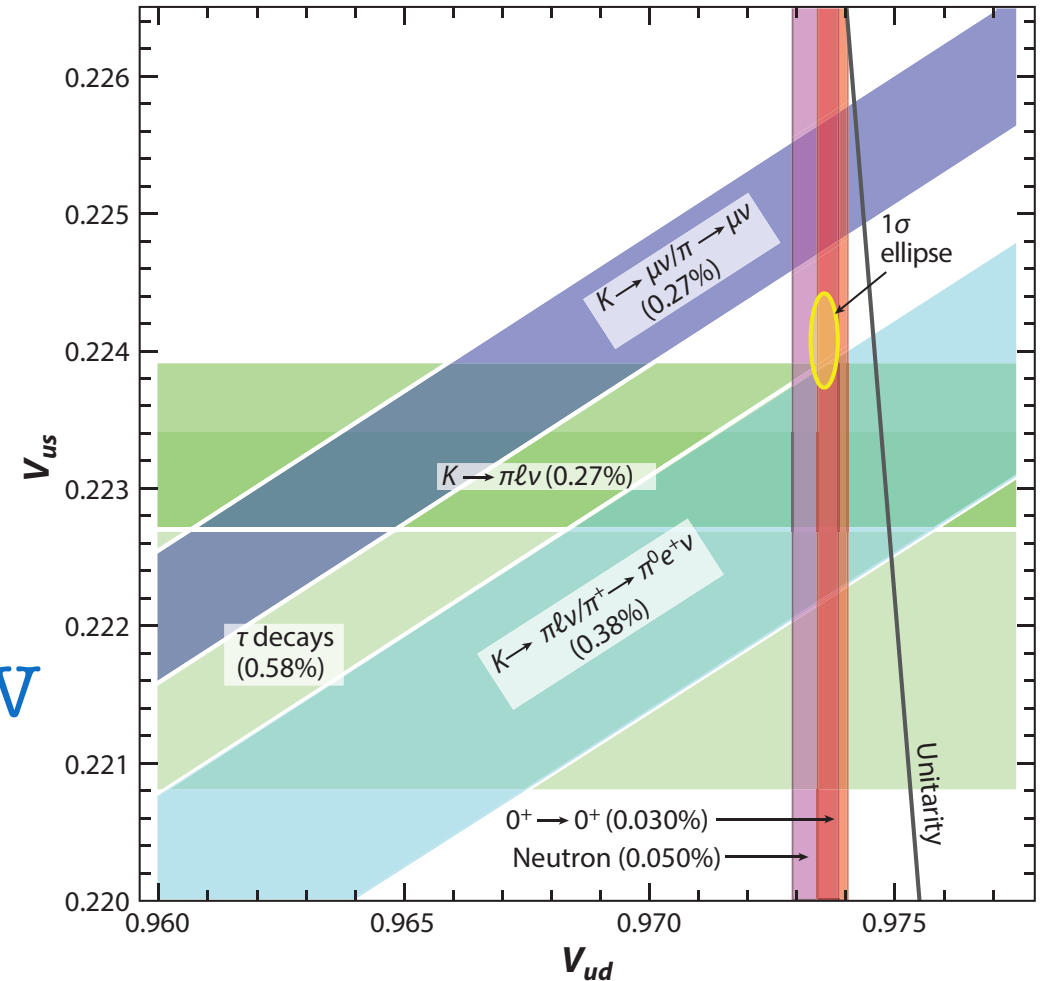
$$\Gamma = G_F^2 \times |V_{uD}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{\text{IsoB}} + \delta_{\text{RC}}) \times F_{\text{kin}}$$

- $G_F$  from  $\mu$  decay
- $V_{ud}$  from  $0^+$  nuclear  $\beta$  decays
- $V_{us}$  from  $\Gamma(K \rightarrow \pi \ell \nu)$

- Interplay between CAA and LFUV

- $3.7\sigma$  tension (CAA)

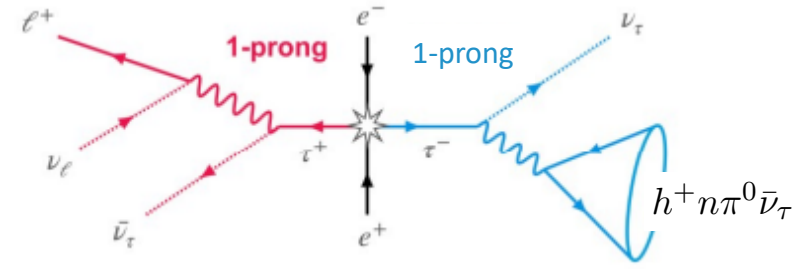
$$\Delta_{\text{CKM}} = (-19.5 \pm 5.3) \times 10^{-4}$$





# $\mu/e; \tau/\mu : \tau$ decays

- In  $e^+e^- \rightarrow \tau^+\tau^-$  one can separate the event in two hemispheres: tag  $\tau$  and signal  $\tau$



[arXiv:2405.14625](https://arxiv.org/abs/2405.14625)  
Submitted to JHEP

## New Belle II analysis

- 362 fb<sup>-1</sup>
- Purity 96% and 92% for electron and muon channel.
- Systematics dominated by electron ID and trigger

$$R_{\mu/e}^{\tau} = \frac{\text{Br}(\tau^- \rightarrow \mu^- \bar{\nu}_{\mu} \nu_{\tau})}{\text{Br}(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau})} \quad \left(\frac{A_{\tau}}{A_{\mu}}\right)_{\tau} = 1.0010 \pm 0.0014,$$

$$R_{\tau/\mu}^{\tau\pi(K)} = \frac{\text{Br}[\tau \rightarrow \pi(K) \nu_{\tau}]}{\text{Br}[\pi(K) \rightarrow \mu \nu_{\mu}]}, \quad \left(\frac{A_{\tau}}{A_e}\right)_{\tau} = 1.0029 \pm 0.0014,$$

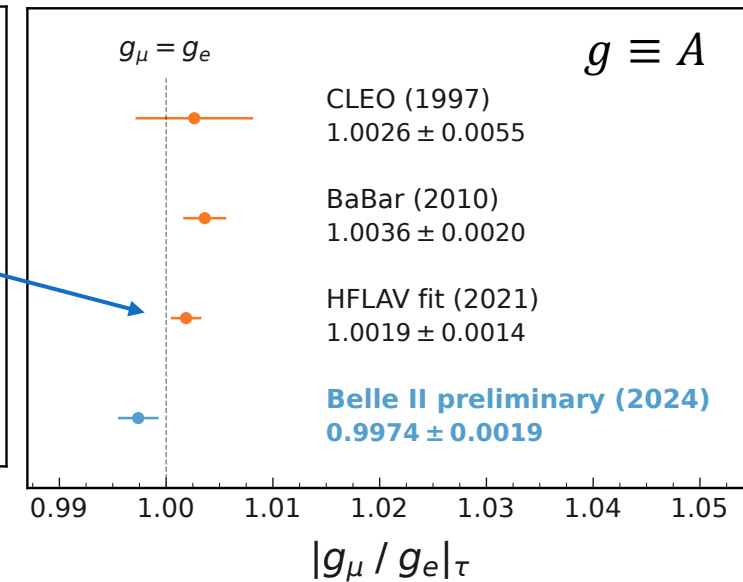
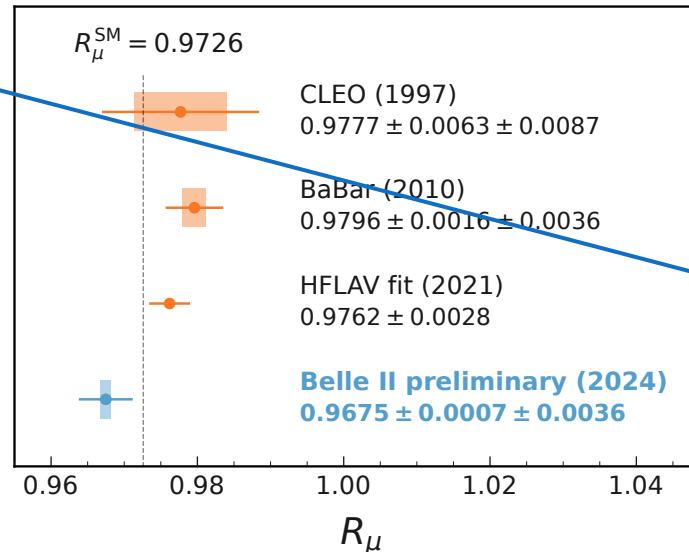
$$R_{\tau/\mu}^{\tau} = \frac{\text{Br}(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau})}{\text{Br}(\mu^- \rightarrow e^- \bar{\nu}_e \nu_{\mu})}, \quad \left(\frac{A_{\mu}}{A_e}\right)_{\tau} = 1.0018 \pm 0.0014.$$

$$R_{\tau/e}^{\tau} = \frac{\text{Br}(\tau^- \rightarrow \mu^- \bar{\nu}_{\mu} \nu_{\tau})}{\text{Br}(\mu^- \rightarrow e^- \bar{\nu}_e \nu_{\mu})} \quad \left(\frac{A_{\tau}}{A_{\mu}}\right)_{\pi} = 0.9964 \pm 0.0038,$$

$$\left(\frac{A_{\tau}}{A_{\mu}}\right)_{K} = 0.9857 \pm 0.0078.$$

From BF to couplings  $\left(\frac{A_{\mu}}{A_e}\right)_{\tau} = \sqrt{R_{\mu/e}^{\tau} \frac{f(m_e^2/m_{\tau}^2)}{f(m_{\mu}^2/m_{\tau}^2)}}$

$$f(x) = -8x + 8x^3 - x^4 - 12x^2 \log x.$$



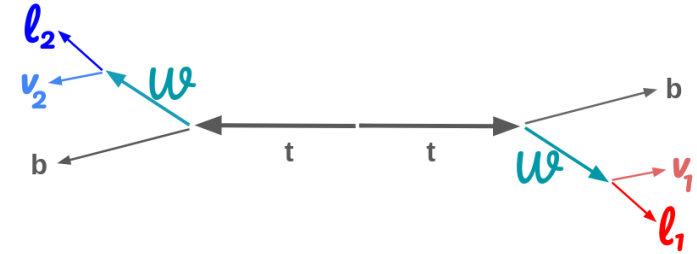
Consistent with the SM at 1.4  $\sigma$



# High Energy

# W/Z decays

- Existing tension from LEP in  $W \rightarrow \tau\nu/W \rightarrow (e, \mu)\nu$
- Very precise Z measurements from LEP/SLD
- CMS and ATLAS can use  $tt$  events



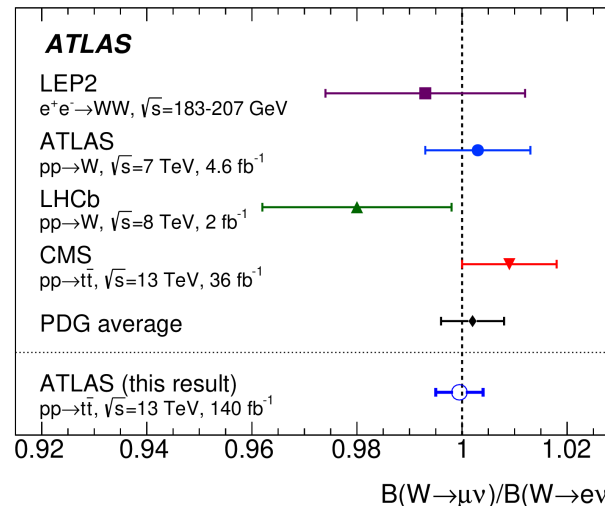
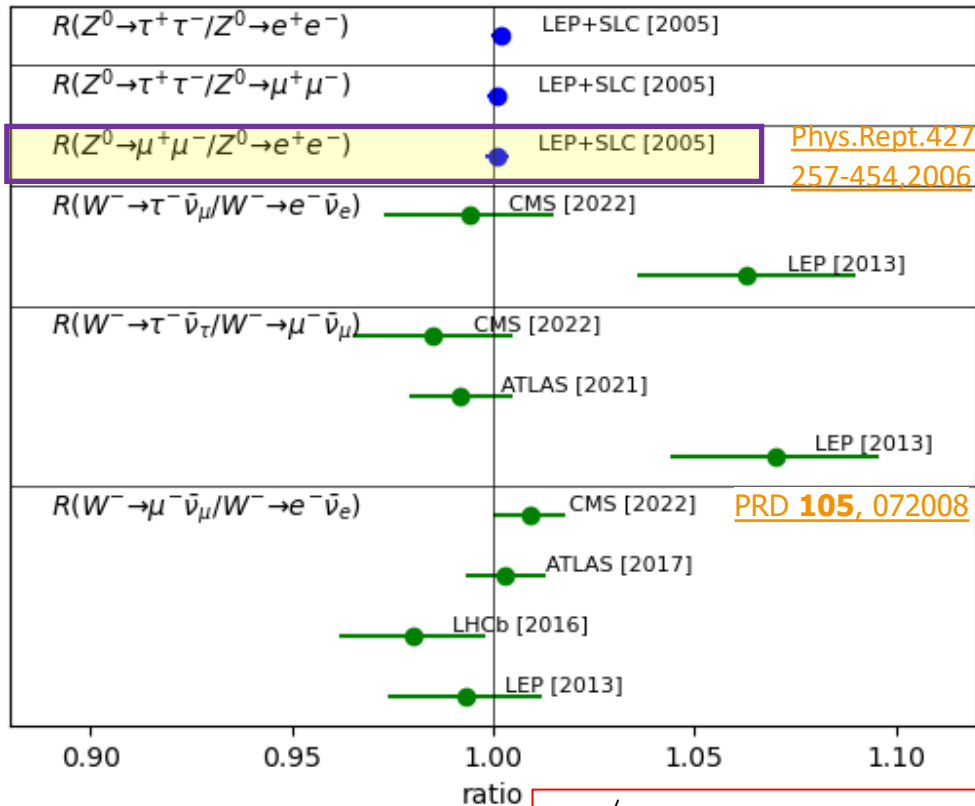
## New ATLAS analysis

- Reduce lepton ID systematics with double ratio
- Get final value using precise LEP/SLD measurement

$$R_{WZ}^{\mu/e} = \frac{R_W^{\mu/e}}{\sqrt{R_Z^{\mu\mu/ee}}}$$

Presented by H.Potti on Monday

$$R_W^{\mu/e}(\text{ATLAS}) = R_{WZ}^{\mu/e}(\text{ATLAS}) \cdot \sqrt{R_Z^{\mu\mu/ee}(\text{LEP+SLD})}$$



- Relative uncertainty of 0.45%
- Most precise single measurement
- Better than PDG average

[arxiv.org/abs/2403.02133](https://arxiv.org/abs/2403.02133)

Accepted in EPJC

$$R_W^{\mu/e}(\text{ATLAS}) = 0.9995 \pm 0.0022 (\text{stat.}) \pm 0.0036 (\text{syst.}) \pm 0.0014 (\text{LEP+SLD})$$



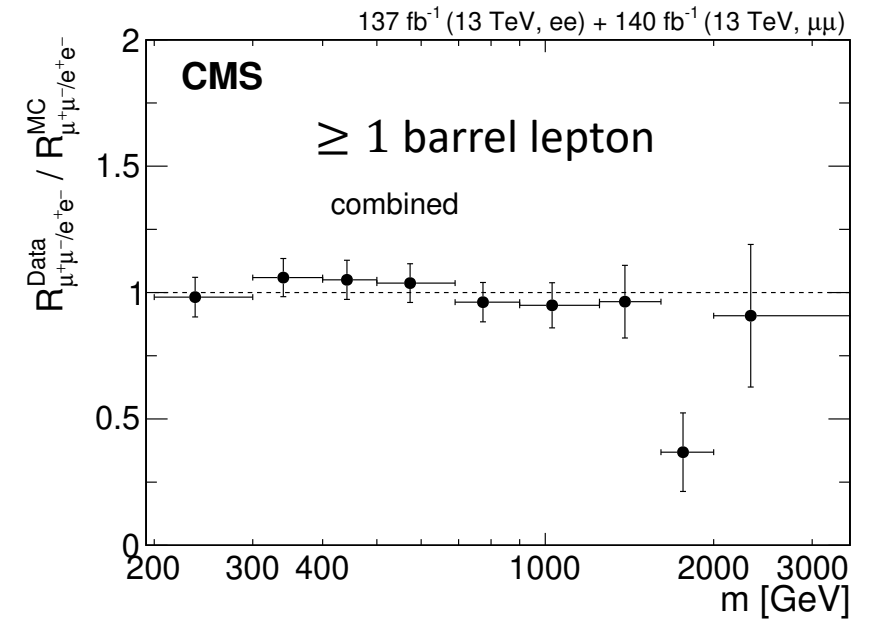
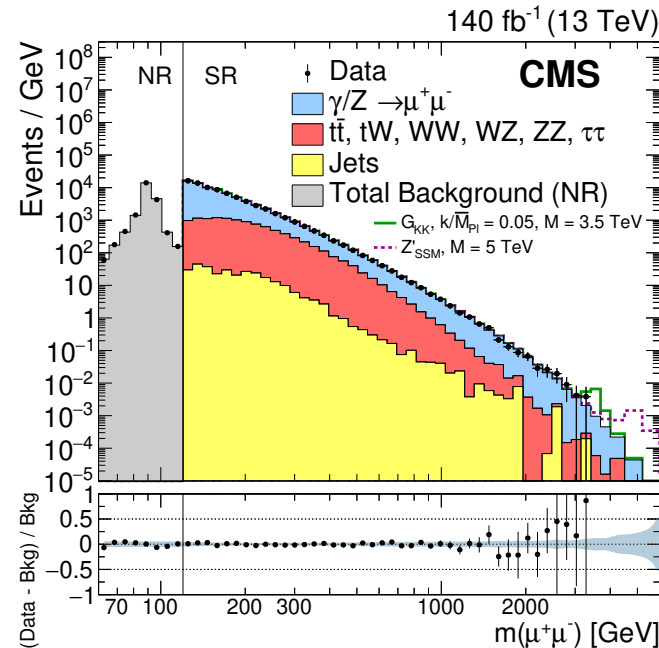
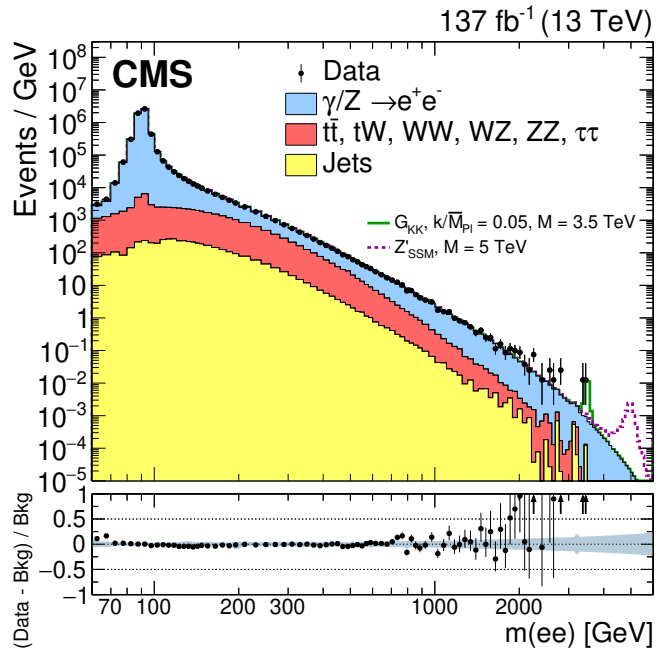
# TeV-scale tests

- Investigation in electron and muon pairs in  $pp$  collisions at 13TeV. Resonant and non resonant
- Experimental challenge: properly model lepton efficiency vs. momentum and angle
- Compare spectrum to MC
- **No significant deviation from LFU observed**

$$R_{\mu^+\mu^-/e^+e^-}^{\text{Data}} / R_{\mu^+\mu^-/e^+e^-}^{\text{MC}}$$

$$R_{\mu^+\mu^-/e^+e^-} = \frac{d\sigma(q\bar{q} \rightarrow \mu^+\mu^-)/dm_{\ell\ell}}{d\sigma(q\bar{q} \rightarrow e^+e^-)/dm_{\ell\ell}}$$

Source	Uncertainty
Electron selection efficiency	6–8%
Muon selection efficiency	1–2% (two-sided), 0–6.5% (one-sided)
Mass scale uncertainty	0–3%
Dimuon mass resolution uncertainty	8.5–15%



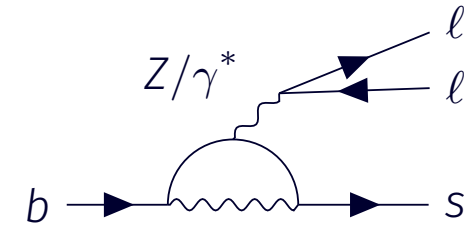


# Heavy Flavor Transitions

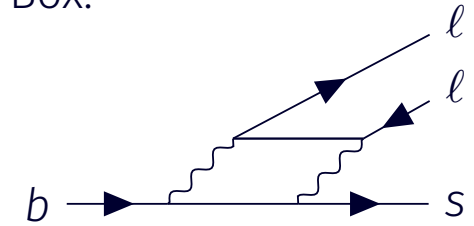
As D. Buttazzo explained, this is where the interesting stuff lies

# $b \rightarrow s \ell \ell$ signals

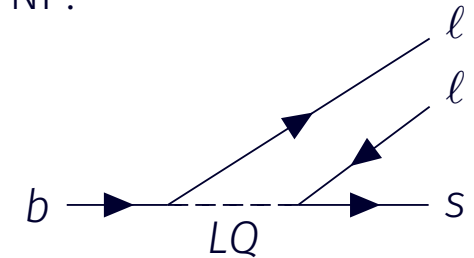
Penguin:



Box:



NP:



- Forbidden at tree level, very sensitive to New Physics signals

$$R_H \equiv \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B} (B \rightarrow H \mu^+ \mu^-)}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B} (B \rightarrow H e^+ e^-)}{dq^2} dq^2} \quad \begin{array}{l} B = B^+, B^0, B_s, \Lambda_b \\ H = K^+, K^{*0}, K_S, pK^- \end{array}$$

- Measure double ratio using  $J/\psi$  resonance to reduce systematics

$$R_K = \frac{\mathcal{B} (B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B} (B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^+)} / \frac{\mathcal{B} (B^+ \rightarrow K^+ e^+ e^-)}{\mathcal{B} (B^+ \rightarrow J/\psi(\rightarrow e^+ e^-) K^+)}$$

- LHCb 2019 showed  $2.4\sigma$  and  $2.5\sigma$  for  $R_{K^{*0}}$  in two bins (Run1:  $3\text{fb}^{-1}$ )

$$R_{K^{*0}} = \begin{cases} 0.66 \pm_{-0.07}^{+0.11} (\text{stat}) \pm 0.03 (\text{syst}) & \text{for } 0.045 < q^2 < 1.1 \text{ GeV}^2/c^4 \\ 0.69 \pm_{-0.07}^{+0.11} (\text{stat}) \pm 0.05 (\text{syst}) & \text{for } 1.1 < q^2 < 6.0 \text{ GeV}^2/c^4 \end{cases} \quad \text{JHEP 08(2017) 55}$$

- LHB 2020 measured  $R_{pK}$  in  $\Lambda_b \rightarrow pK^- \ell \ell$   $R_{pK}|_{0.1 < q^2 < 6 \text{ GeV}^2/c^4} = 0.86 \pm_{-0.11}^{+0.14} \pm 0.05$  [JHEP 05\(2020\) 40](#)

- LHCb 2022 result showed a  $3.1\sigma$  tension for  $R_K$  and  $1.4 - 1.5\sigma$  for  $R_{K_S}, R_{K^{*+}}$

$$R_K(1.1 < q^2 < 6.0 \text{ GeV}^2 c^{-4}) = 0.846 \pm_{-0.039}^{+0.042} \pm_{-0.012}^{+0.013}$$

[Nat. Phys. 18 \(2022\) 277-282](#)

$$R_{K_S^0} = 0.66 \pm_{-0.14}^{+0.20} (\text{stat}) \pm_{-0.04}^{+0.02} (\text{syst}), \quad \text{PRL 128 (2022) 191802}$$

$$R_{K^{*+}} = 0.70 \pm_{-0.13}^{+0.18} (\text{stat}) \pm_{-0.04}^{+0.03} (\text{syst}).$$

# $b \rightarrow s\ell\ell$ update

- LHCb 2023 update simultaneous measurement of  $R_K$  and  $R_{K^*}$  in two  $q^2$  bins for full statistics ( $9\text{fb}^{-1}$ )
- Now compatible with SM
  - $R_{K^*}$ : increase in statistics
  - $R_K$ : more stringent e-ID reducing contribution from processes not properly accounted for; modeling of residual background
- CMS 2024 also measured  $R_K$ , but statistical error still very large
  - Also verified universality of  $J/\psi$  and  $\psi(2s)$  decays

[Rep. Prog. Phys. 87 077802 \(2024\)](#)

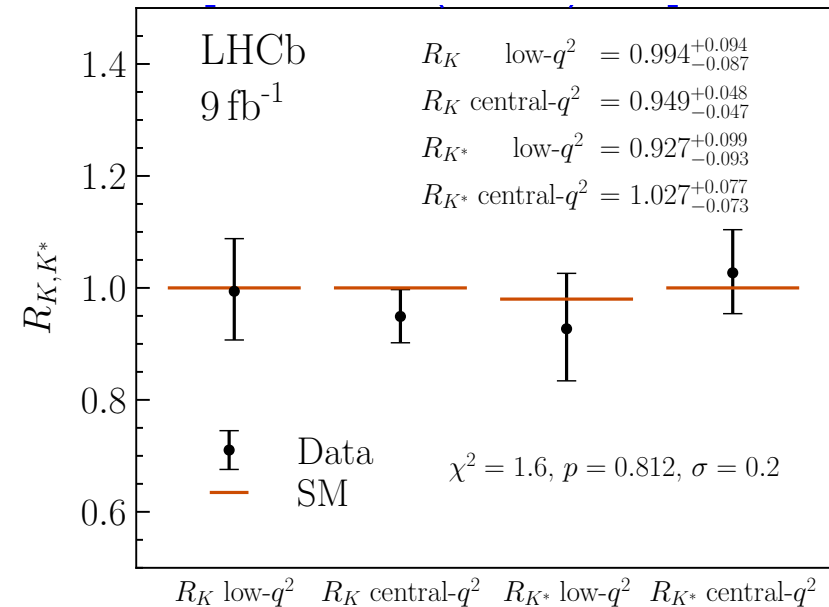
$$R_{J/\psi} = 1.006^{+0.020}_{-0.019}$$

$$R_{\psi(2S)} = 0.966^{+0.071}_{-0.066}$$

$$\text{low-}q^2 \begin{cases} R_K = 0.994^{+0.090}_{-0.082} (\text{stat})^{+0.029}_{-0.027} (\text{syst}), \\ R_{K^*} = 0.927^{+0.093}_{-0.087} (\text{stat})^{+0.036}_{-0.035} (\text{syst}), \end{cases}$$

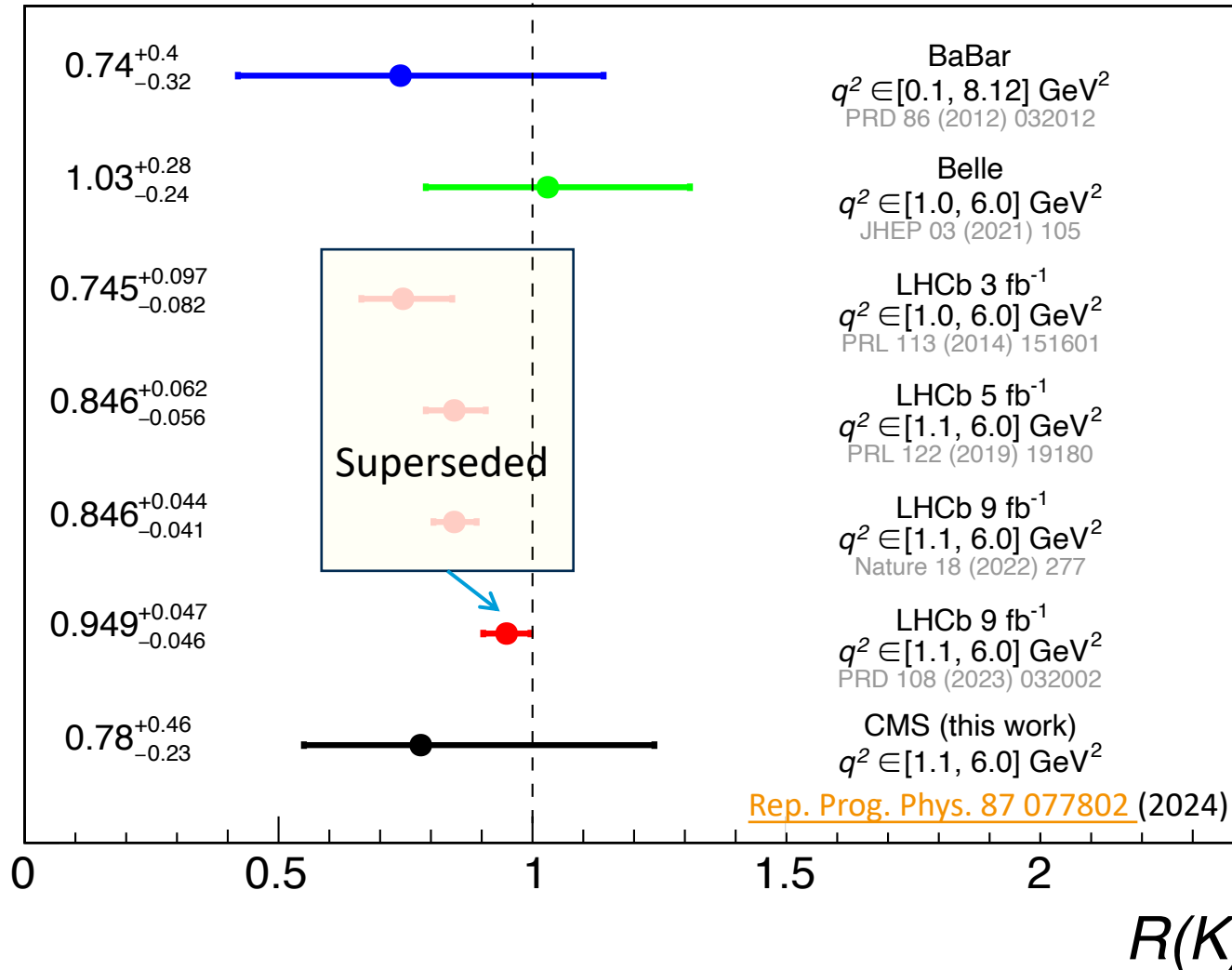
$$\text{central-}q^2 \begin{cases} R_K = 0.949^{+0.042}_{-0.041} (\text{stat})^{+0.022}_{-0.022} (\text{syst}), \\ R_{K^*} = 1.027^{+0.072}_{-0.068} (\text{stat})^{+0.027}_{-0.026} (\text{syst}). \end{cases}$$

[PRL 131 \(2023\) 051803](#) and [PRD 108 \(2023\) 032002](#)





# $b \rightarrow sl\ell$ status and history

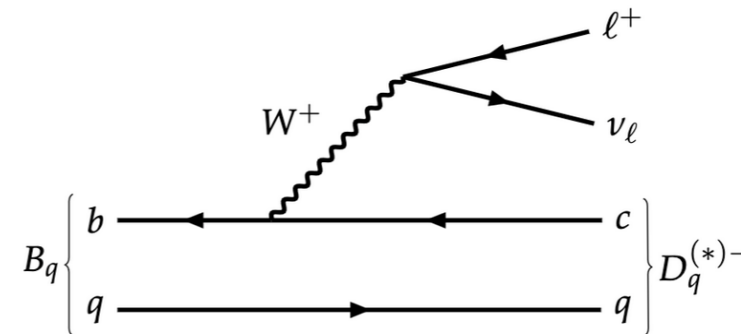


- $b \rightarrow sl\ell$  still very interesting
- Some tension in angular analysis
- precision regime is not yet reached for LFU tests:
  - need to go below 1% uncertainty





# $b \rightarrow c \ell \nu$



- Measure the ratios of rates to different leptons

- Hadronic uncertainties mostly cancel in the ratio
- Reduced experimental systematic uncertainties

$$R(H_c) = \frac{\mathcal{B}(H_b \rightarrow H_c \tau \nu_\tau)}{\mathcal{B}(H_b \rightarrow H_c \mu \nu_\mu)} \quad H_b = B^0, B_{(c)}^+, \Lambda_B^0, B_s^0, \dots$$

$$H_c = D^*, D^0, D^+, D_s, \Lambda_C^{(*)}, J/\psi, \dots$$

History of slight excess of semitauonic decays

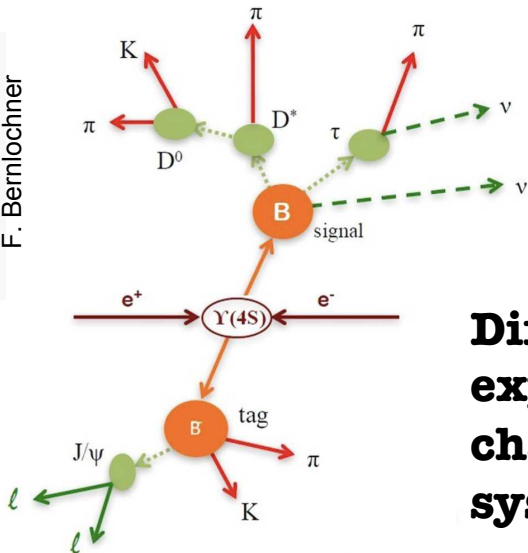
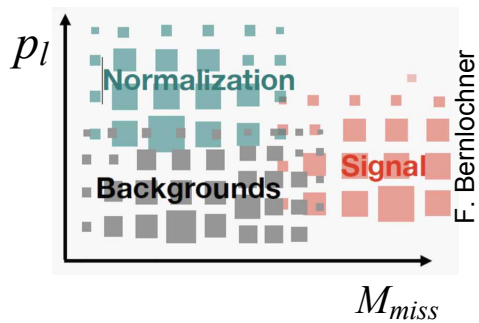
- Angular analysis adds extra power and sensitivity

LHCb		BELLE / BELLE II	
$R(D) - R(D^*)$ with muonic $\tau$	<a href="#">PRL 131, 111802</a> (2023)	$R(D^*)$ with leptonic $\tau$ had tag	<a href="#">arXiv:2401.02840</a> (2024) (Submitted to PRD)
$R(D^*)$ with hadronic $\tau$	<a href="#">PRD 108, 012018</a> (2023)	$R(X_{\mu/e})$ with had tag	<a href="#">PRL 131, 051804</a> (2023)
$R(D^{+(*)})$ with muonic $\tau$	<a href="#">arXiv:2406.03387</a> (2024) (Submitted to PRL)	$R(X_{\tau/\ell})$ with leptonic $\tau$ had tag	<a href="#">PRL 132, 211804</a> (2024)
$R(\Lambda_c)$	<a href="#">PRL 128, 191803</a> (2022)	Angular analysis in $B^0 \rightarrow D^*(e/\mu)\nu$	<a href="#">PRL 131, 181801</a> (2023)
$R(J/\psi)$	<a href="#">PRL 120, 121801</a> (2018)	Angular coefficients	<a href="#">arXiv: 2310.20286</a> (2023) (Accepted by PRL)

# Complementary approaches

## B Factories

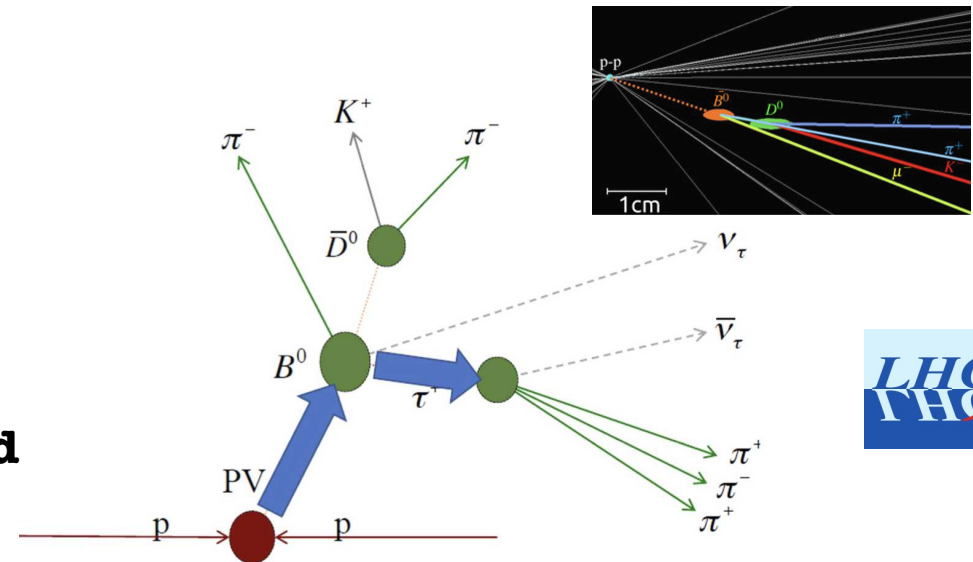
- Full reconstruction of both signal and tagging B meson (low efficiency)
- Closed event kinematics (missing energy)
- $\pi^0$  and neutrals reconstruction
- Simple normalization; high efficiency for both  $\mu$  and  $e$



**Different experimental challenges and systematics**

## LHCb

- Large cross section
- Exploit vertexing for B, D,  $\tau$  reconstruction
- Reliance on all-charged modes and  $\mu$ -ID
- Normalization of signal relative to similar decay processes



C. Bozzi



# R(D) and R(D\*) from LHCb

Leptonic  $\tau$  decays  $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$

$$B^- / \bar{B}^0 \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau$$

$$D^{(*)} = D^0, D^{*+}, D^{*0}$$

where  $D^{*+} \rightarrow D^0 \pi^+$  and  $D^0 \rightarrow K^+ \pi^-$

$$\mathcal{R}(D^{*}) = 0.281 \pm 0.018 \pm 0.024$$

$$\mathcal{R}(D^0) = 0.441 \pm 0.060 \pm 0.066$$

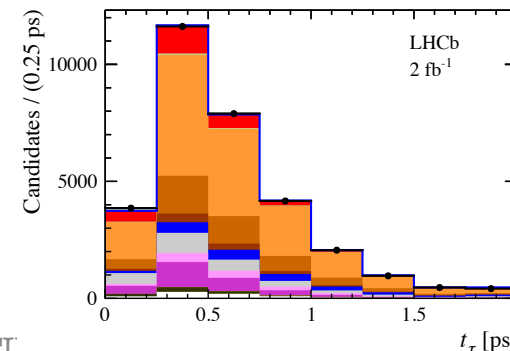
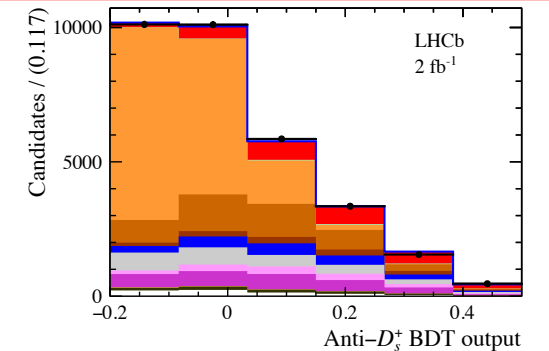
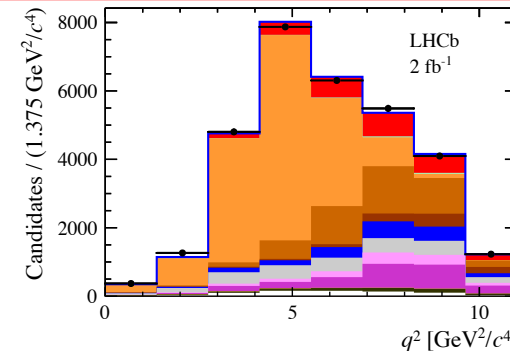
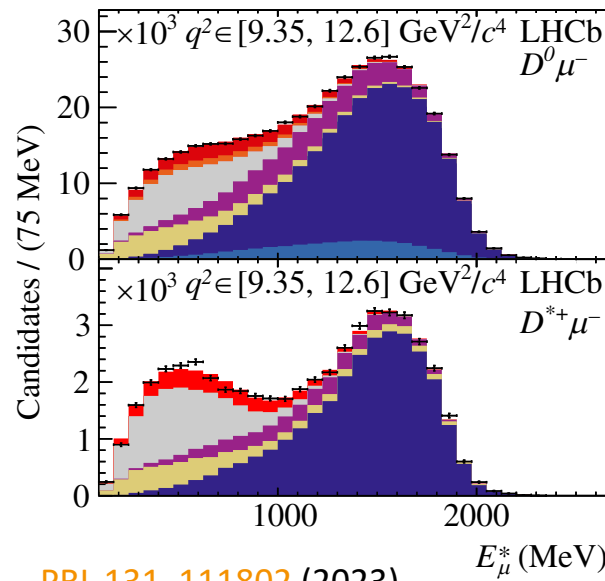
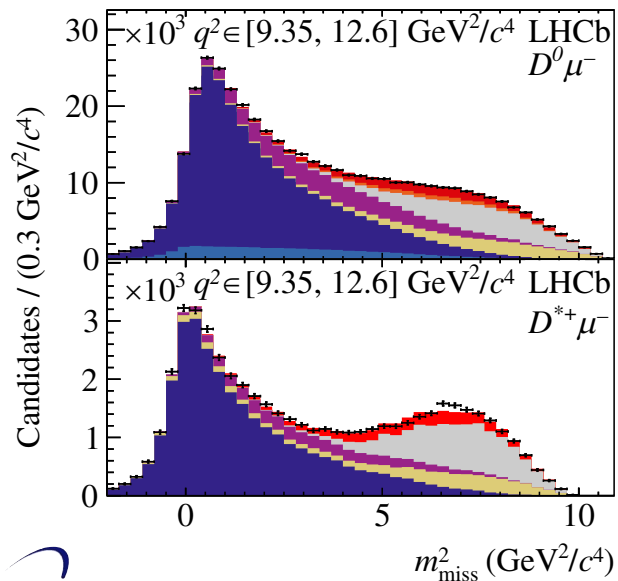
Hadronic  $\tau$  decays  $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ (\pi^0) \bar{\nu}_\tau$

$$B^0 \rightarrow D^{*-} \tau^+ \nu_\tau \quad D^{*-} \rightarrow \pi^- \bar{D}^0 (\rightarrow K^+ \pi^-)$$

Measure relative to  $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ , same visible final state, use known B.F.

$$\mathcal{R}(D^{*-}) = 0.260 \pm 0.015 \text{ (stat)} \pm 0.016 \text{ (syst)} \pm 0.012 \text{ (ext)}$$

- + Data (3 fb<sup>-1</sup>)
- $B \rightarrow D^* \tau \nu$
- $B \rightarrow D \tau \nu$
- $B \rightarrow D^{(*)} D X$
- $B \rightarrow D^{*+} \mu \nu$
- Comb + misID
- $B \rightarrow D^0 \mu \nu$
- $B \rightarrow D^{*0} \mu \nu$
- $B \rightarrow D^{*+} \mu \nu$



- + Data
- $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$
- $B \rightarrow D^{*-} D_s^+(X)$
- $B \rightarrow D^{*+} 3\pi X$
- Comb.  $B^0$
- Comb.  $D^{*-}$
- $B \rightarrow \bar{D}^{*+} \tau^+ \nu_\tau$
- $B \rightarrow D^{*+} D_s^+(X)$
- $B \rightarrow D^{*+} D_s^0(X)$
- Comb.  $\bar{D}^{*+}$
- Total

[PRD 108, 012018 \(2023\)](#)

Revised May 2024

[arXiv:2305.01463v2](#)

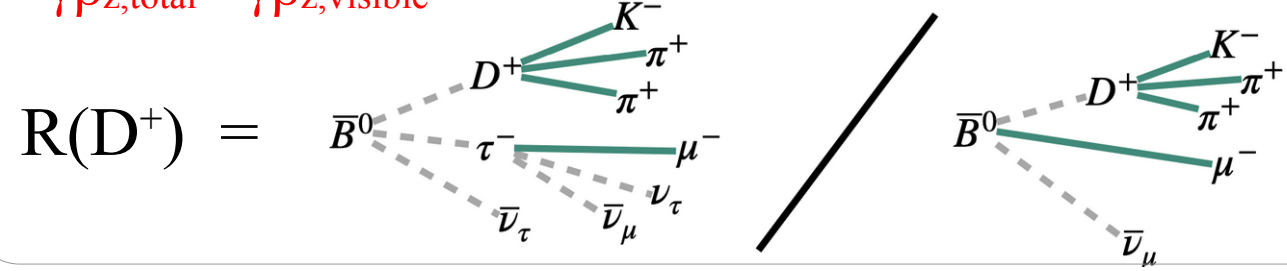
# $R(D^{(*)+})$

$$R(D^{(*)+}) = \frac{\mathcal{B}(B \rightarrow D^{(*)+} \tau^- \nu_{\tau-})}{\mathcal{B}(B \rightarrow D^{(*)+} \mu^- \nu_{\mu-})}$$

## • First LHCb measurement using the $D^+$ ground state

- B momentum at LHC: exploit B flight direction and boost approximation

$$\gamma\beta_{z,\text{total}} = \gamma\beta_{z,\text{visible}}$$



$$R(D^+) =$$

$$R(D^+) = 0.249 \pm 0.043 \pm 0.047$$

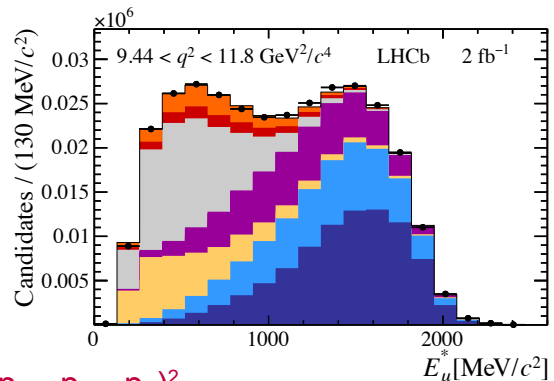
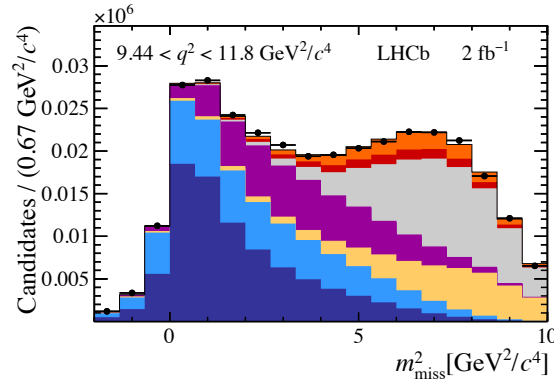
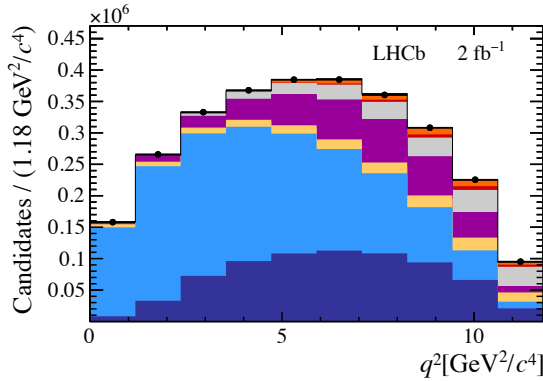
$$R(D^{*+}) = 0.402 \pm 0.081 \pm 0.085$$

$$\rho = -0.39$$

Compatible with SM at  $0.8\sigma$  and with World Average at  $\sim 1\sigma$   
Main systematic uncertainties from form factor parameters and background modeling

Uncertainty on ratio of efficiencies are sub-dominant

See also talk by Alex Fernandez, "Tests of Lepton Flavor Universality in tree-level B Meson Decays at LHCb"  
W1P4, Wed @ 8.30



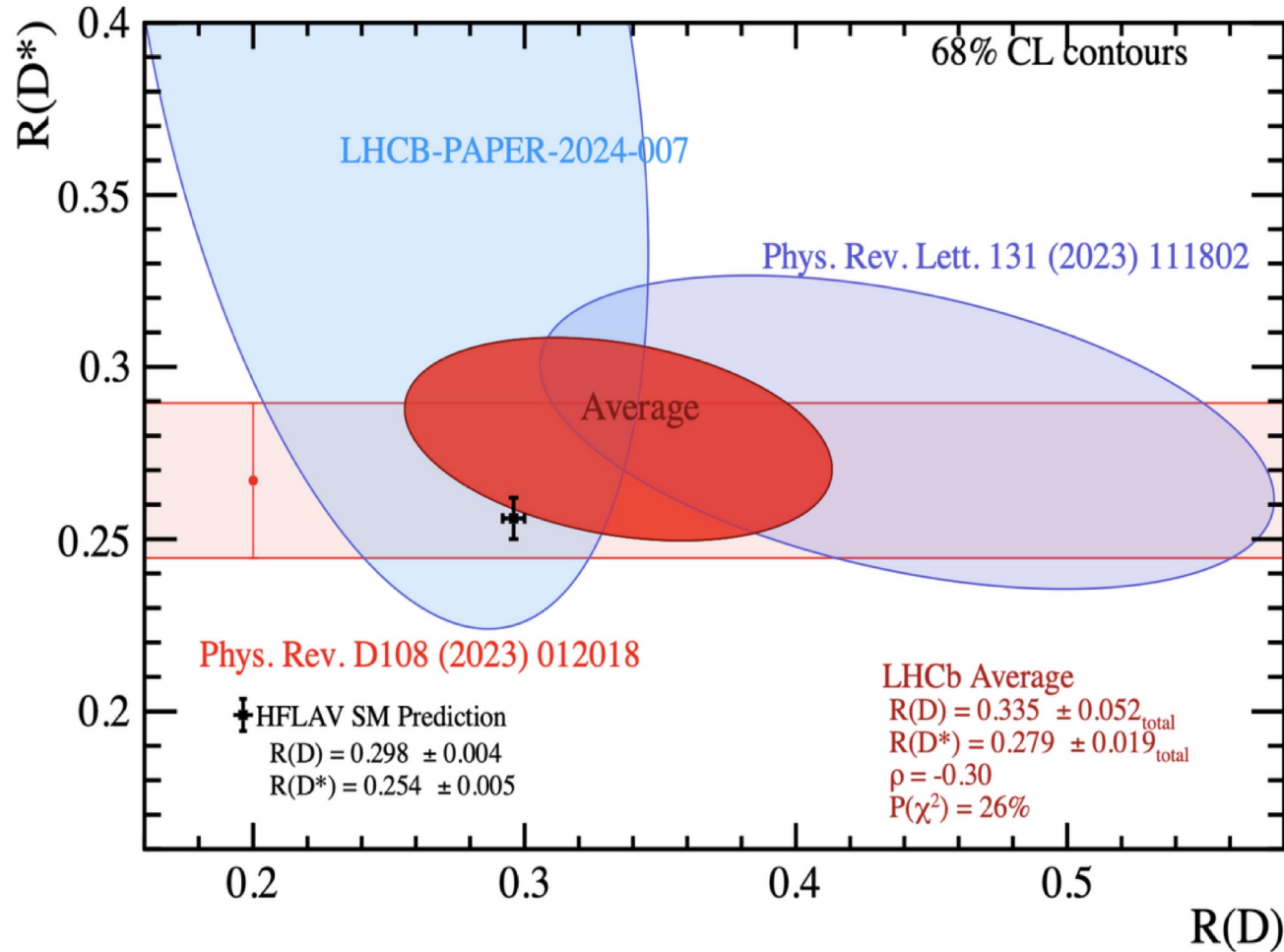
- $\bar{B} \rightarrow D^+ \tau^- \nu$
- $\bar{B} \rightarrow D^{*+} \tau^- \nu$
- $\bar{B} \rightarrow D^+ X_c X$
- $\bar{B} \rightarrow D^{*+} \mu^- \nu$
- Comb + misID
- $\bar{B} \rightarrow D^+ \mu^- \nu$
- $\bar{B} \rightarrow D^{*+} \mu^- \nu$

$$m^2_{\text{miss}} = (p_B - p_D - p_\mu)^2$$

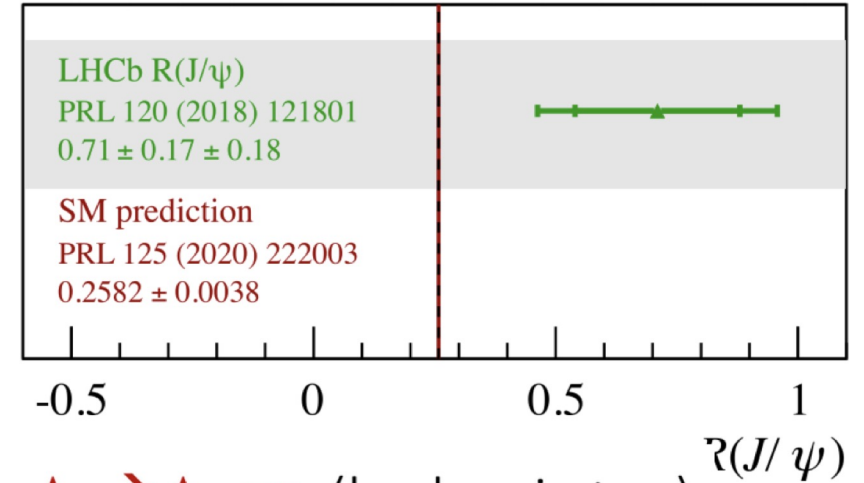
$$E_\mu \text{ muon energy in B rest frame}$$

$$q^2 = (p_B - p_D)^2$$

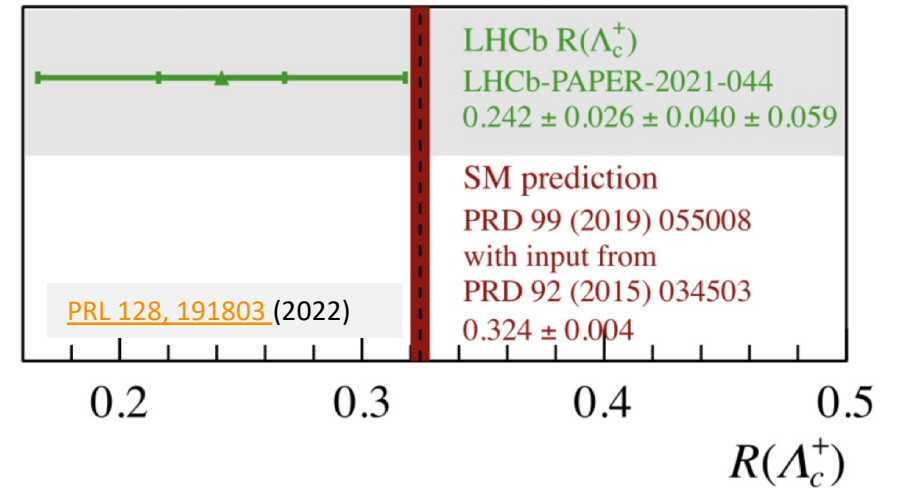
# LHCb Measurements



## $B_c \rightarrow J/\psi \tau \nu$ (muonic tau)



## $\Lambda_b \rightarrow \Lambda_c \tau \nu$ (hadronic tau)







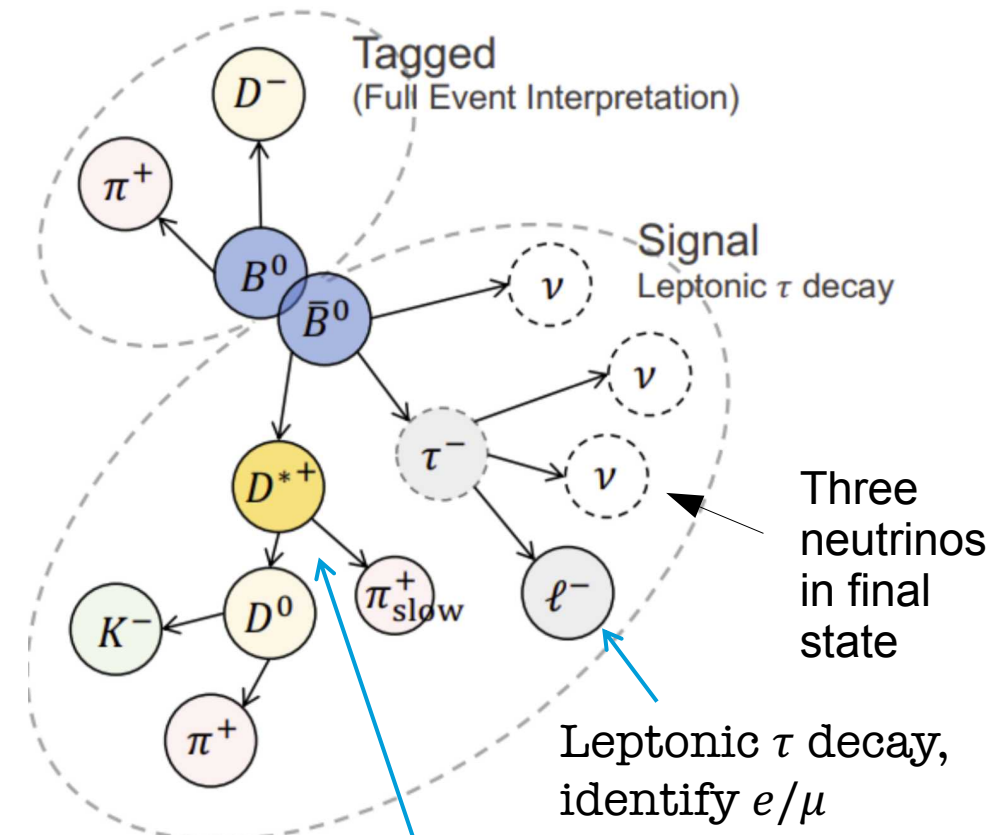
# R(D\*) from Belle II

- Exclusively reconstruct the hadronically-decaying tag B using “Full Event Interpretation” (FEI) method [Comput Softw Big Sci 3, 6 \(2019\)](#)

- Similar methodology to previous BABAR and Belle publications [PRL 109,101802 \(2012\)](#).
- Fully reconstructed D\* [PRD 88, 072012 \(2013\)](#).
- Leptonic tau decay [PRL 118,211801 \(2017\)](#).
- Require that there are no additional charged tracks or  $\pi^0$  candidates left over [PRD 97, 012004 \(2018\)](#).
- To extract the signal, use the residual calorimeter energy  $E_{ECL}$  and the beam-constrained missing mass

$$M_{\text{miss}}^2 = (E_{\text{beam}}^* - E_{D^*}^* - E_{\ell}^*)^2 - (-\vec{p}_{B_{\text{tag}}}^* - \vec{p}_{D^*}^* - \vec{p}_{\ell}^*)^2$$

- Primary experimental challenge is to understand the significant (and poorly known) backgrounds from  $B \rightarrow D^* \ell \nu$



$$D^{*+} \rightarrow D^0 \pi^+ \text{ and } D^+ \pi^0$$

$$D^{*0} \rightarrow D^0 \pi^0$$



# $R(D^*)$ from Belle II

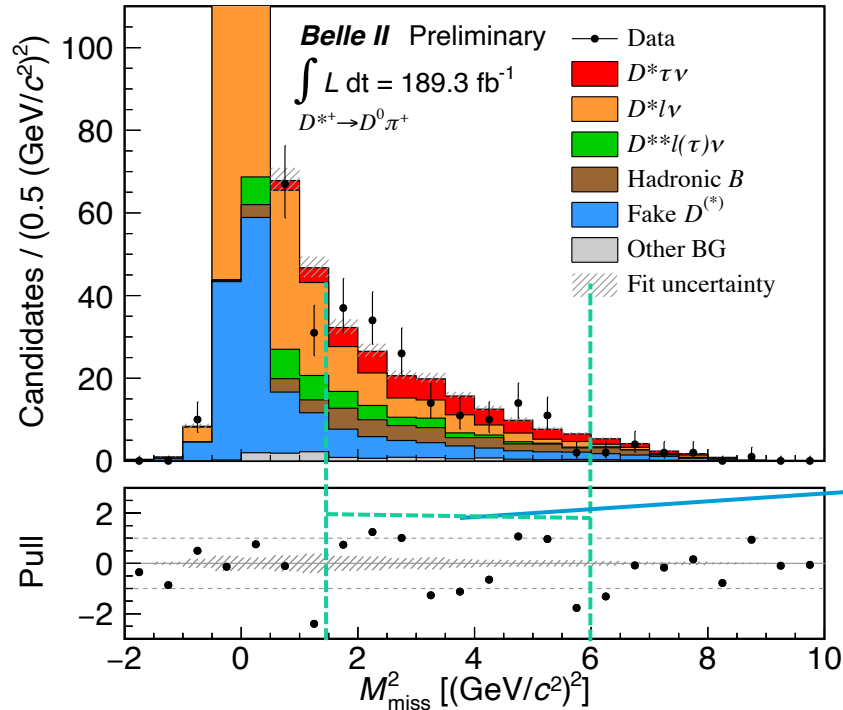
- Signal extraction using 2d binned likelihood fit to  $E_{ECL}$  and  $M_{miss}^2$ .

- First  $R(D^*)$  result from Belle II

$$R(D^*) = 0.262^{+0.041}_{-0.039}(\text{stat})^{+0.035}_{-0.032}(\text{syst})$$

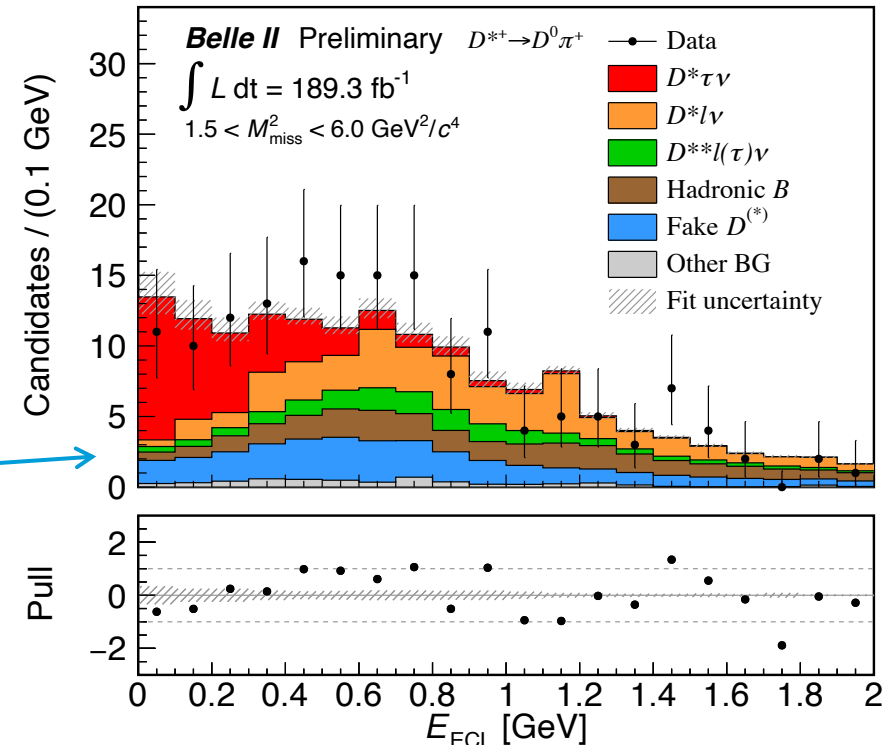
- Consistent with SM and previous results, but still fairly large statistical uncertainty

$$1.5 < M_{miss}^2 < 6.0 \text{ GeV}^2/c^4$$

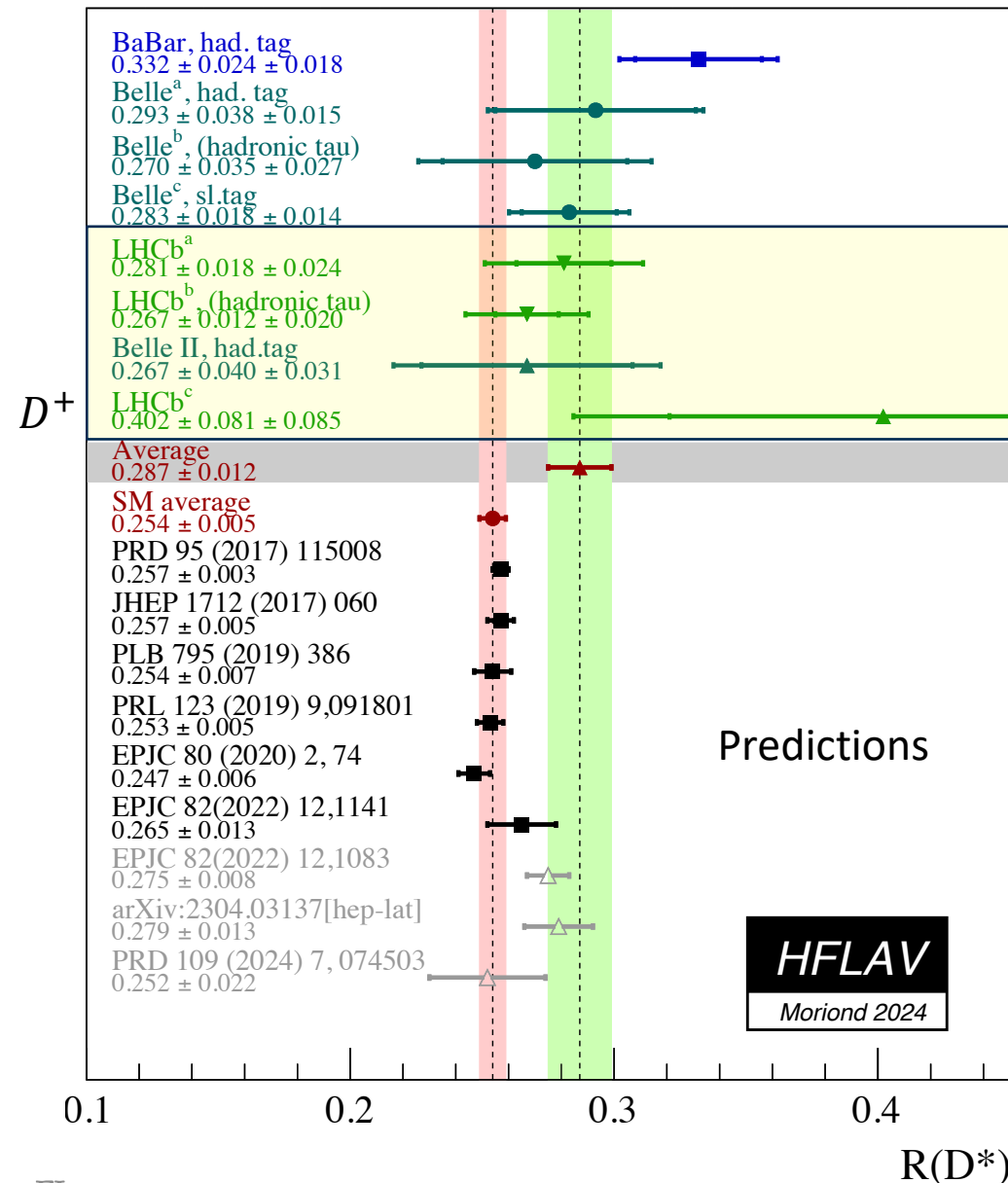
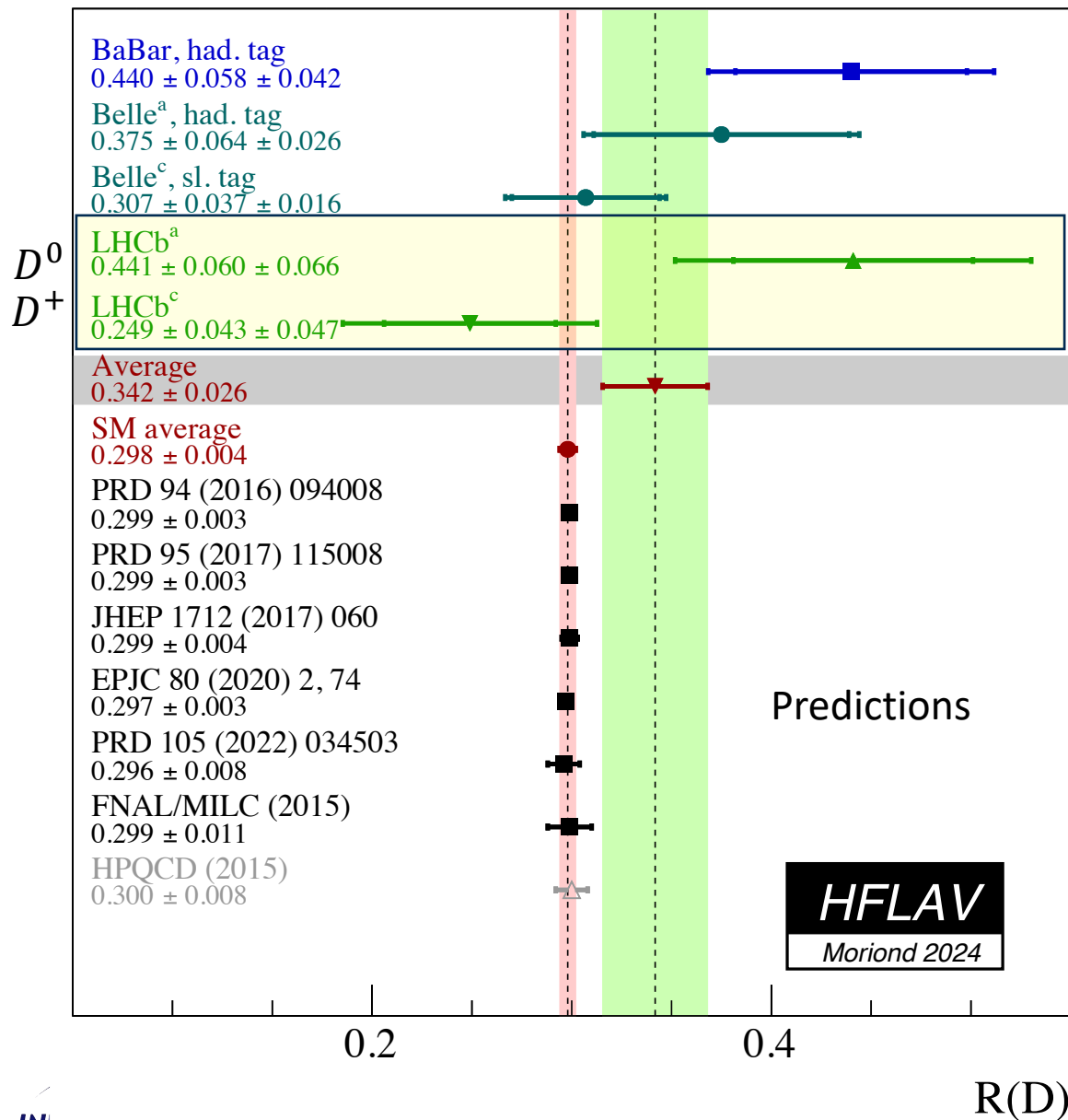


$D^{*+} \rightarrow D^0 \pi^+$

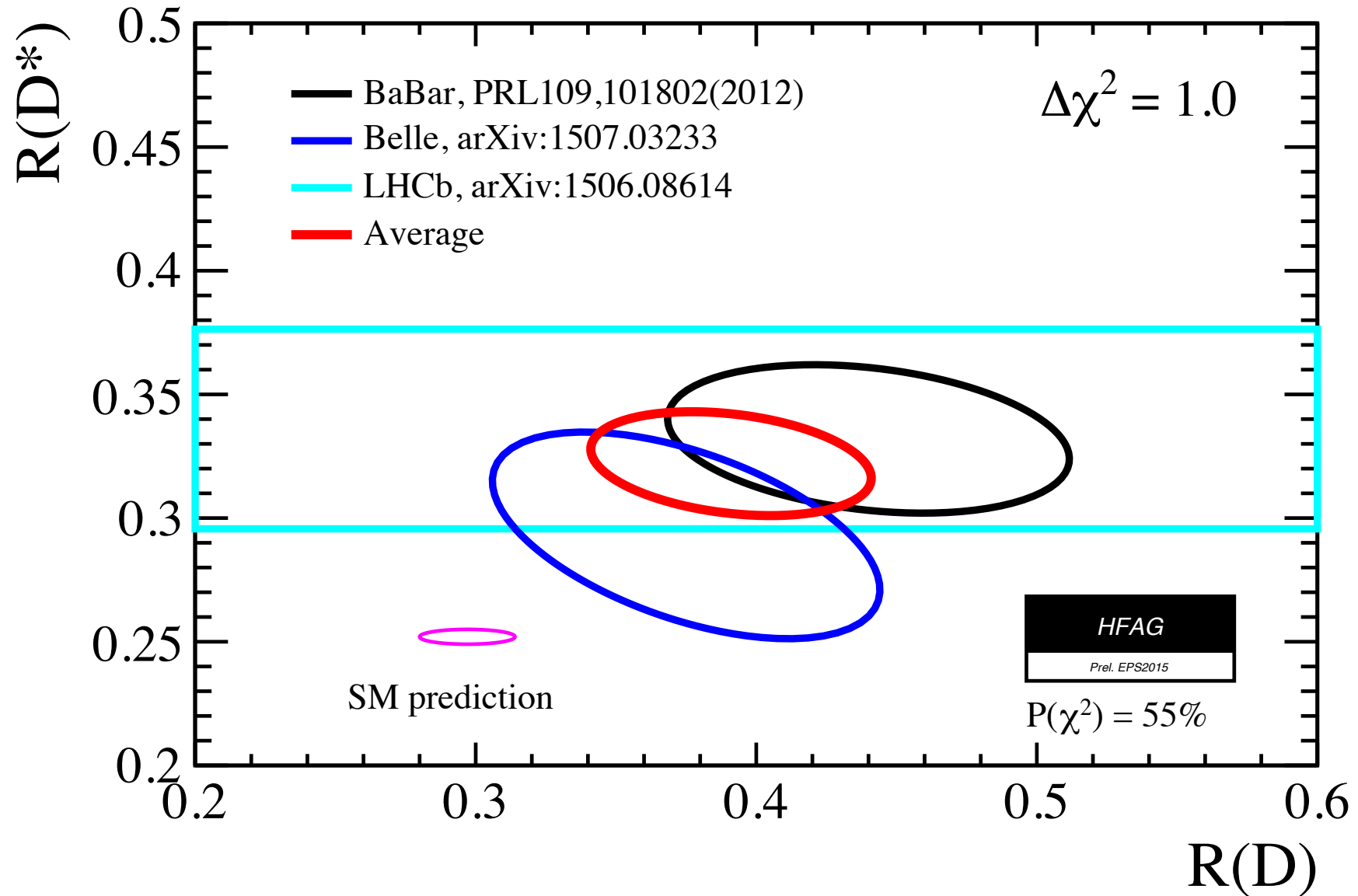
Signal enhanced



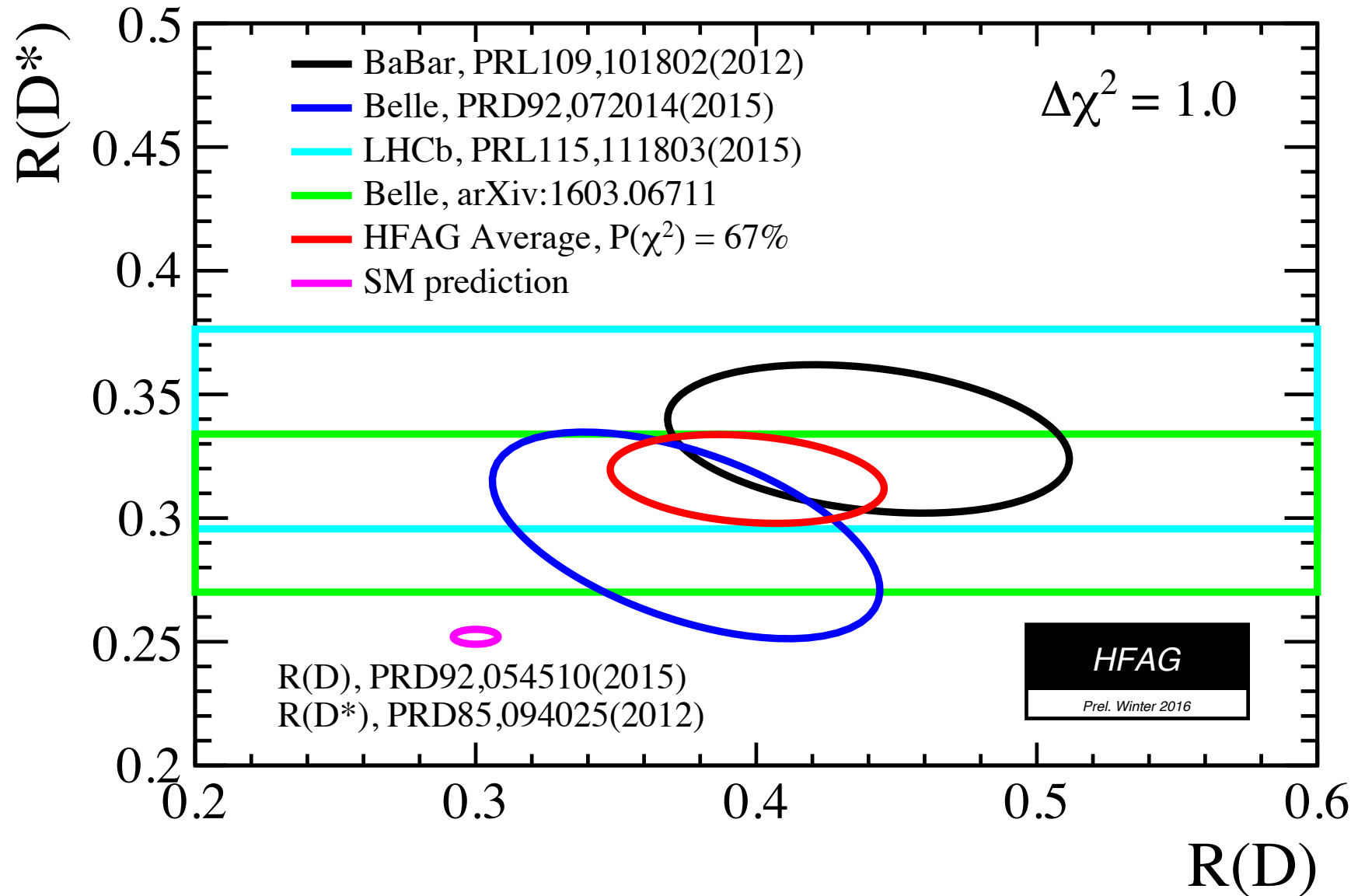
# $R(D)$ & $R(D^*)$ measurements and predictions



# $R(D)$ & $R(D^*)$ EPS 2015

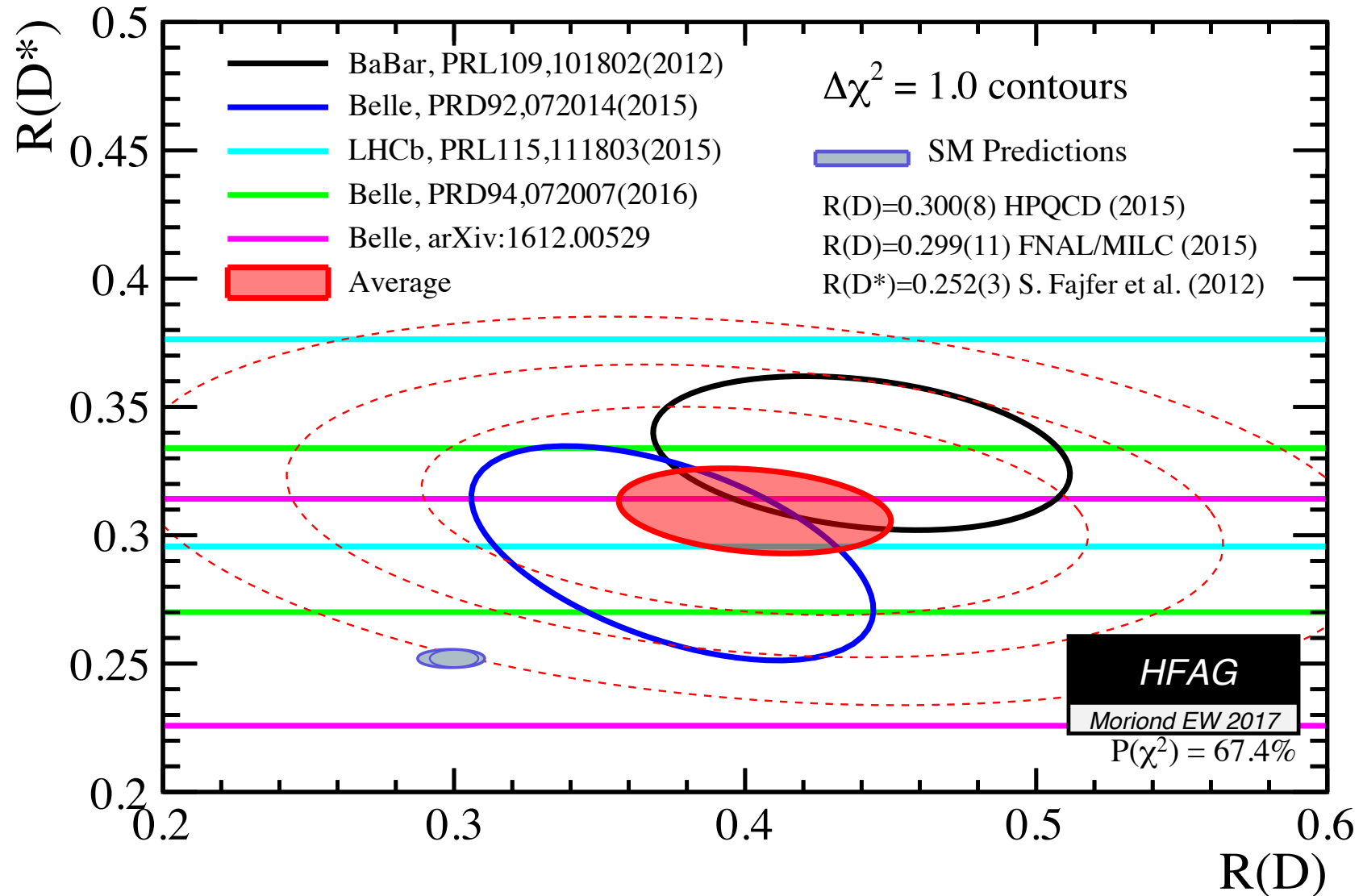


# $R(D)$ & $R(D^*)$ Winter 2016

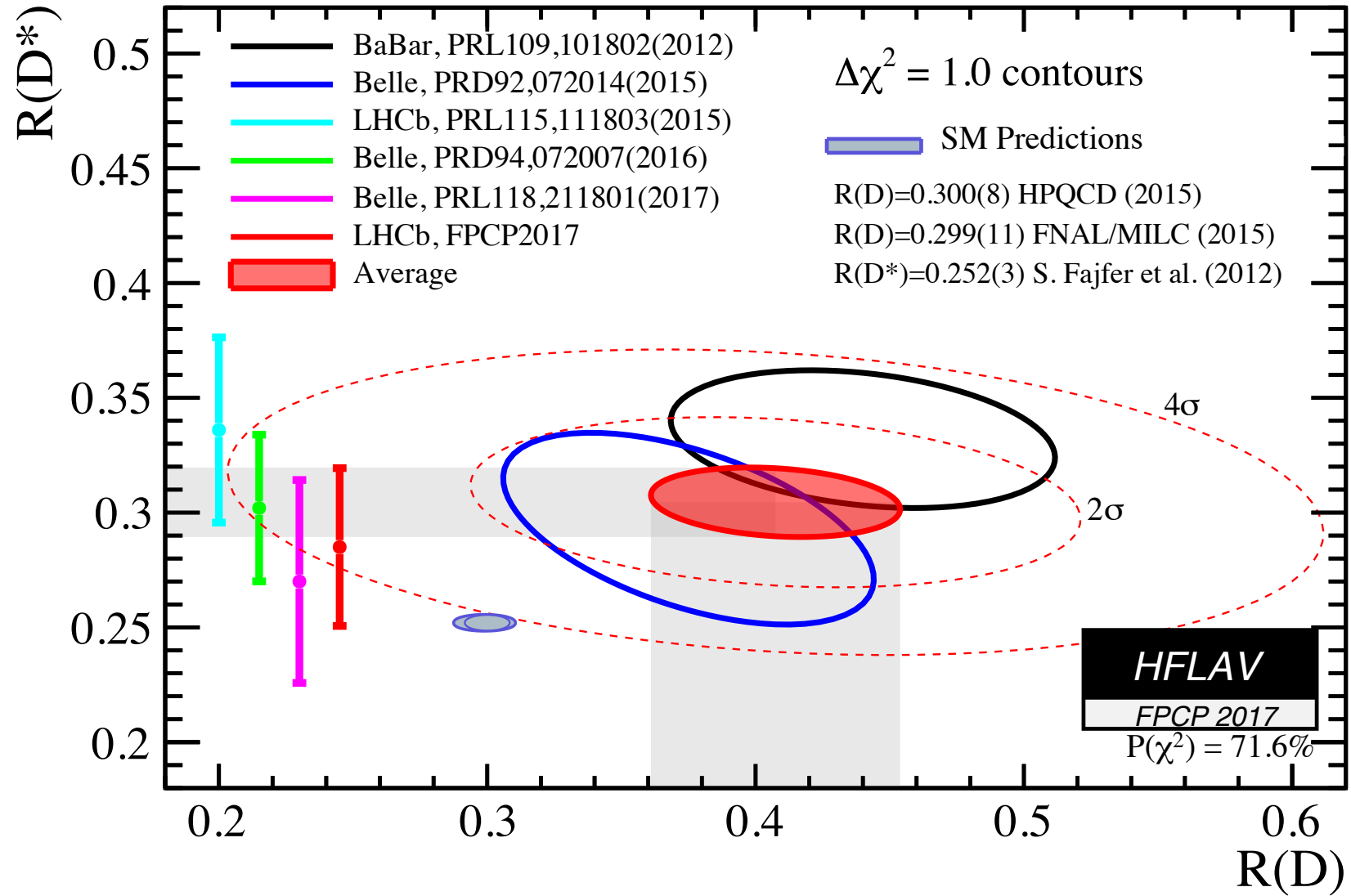




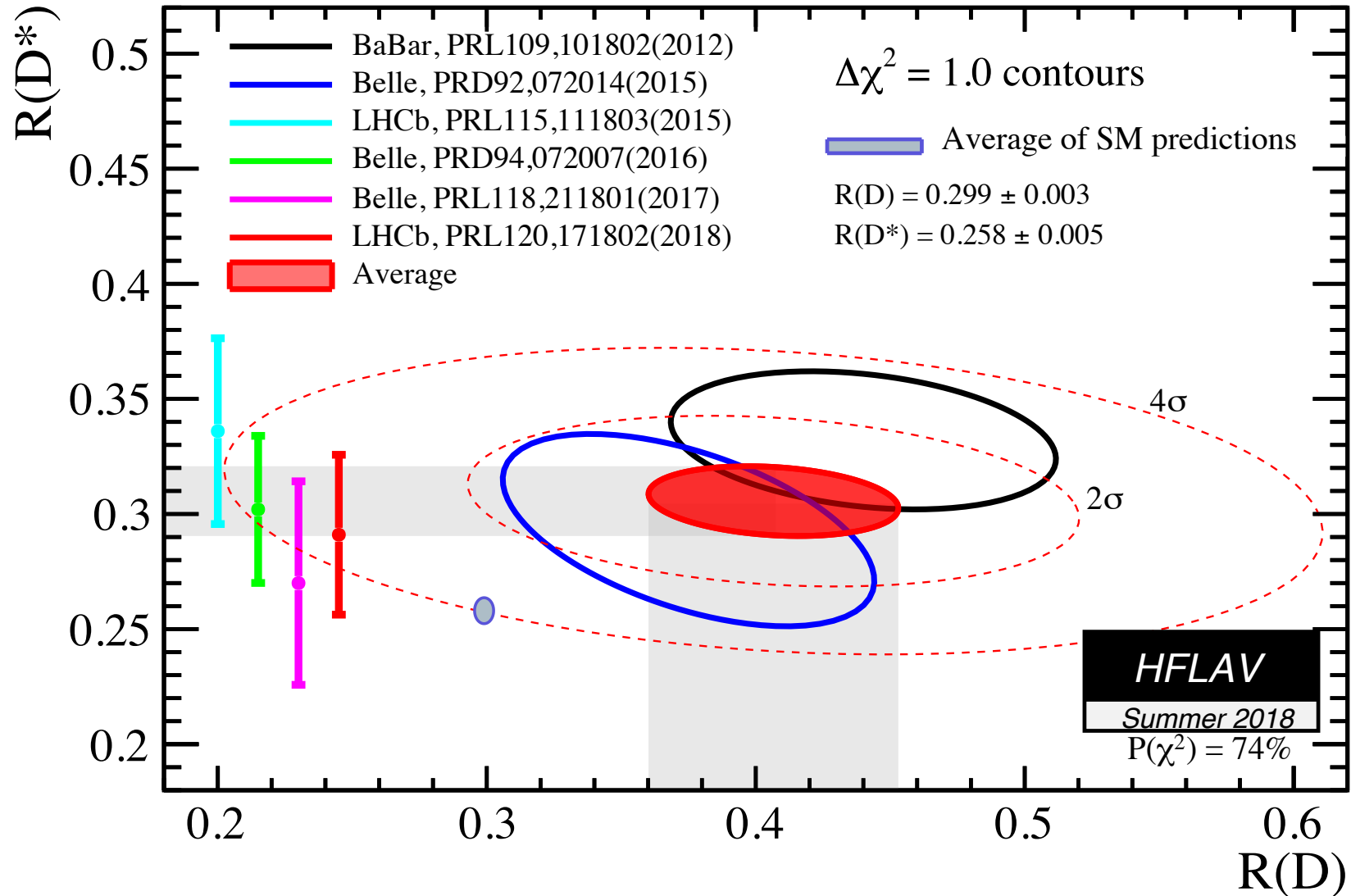
# $R(D)$ & $R(D^*)$ Moriond 2017



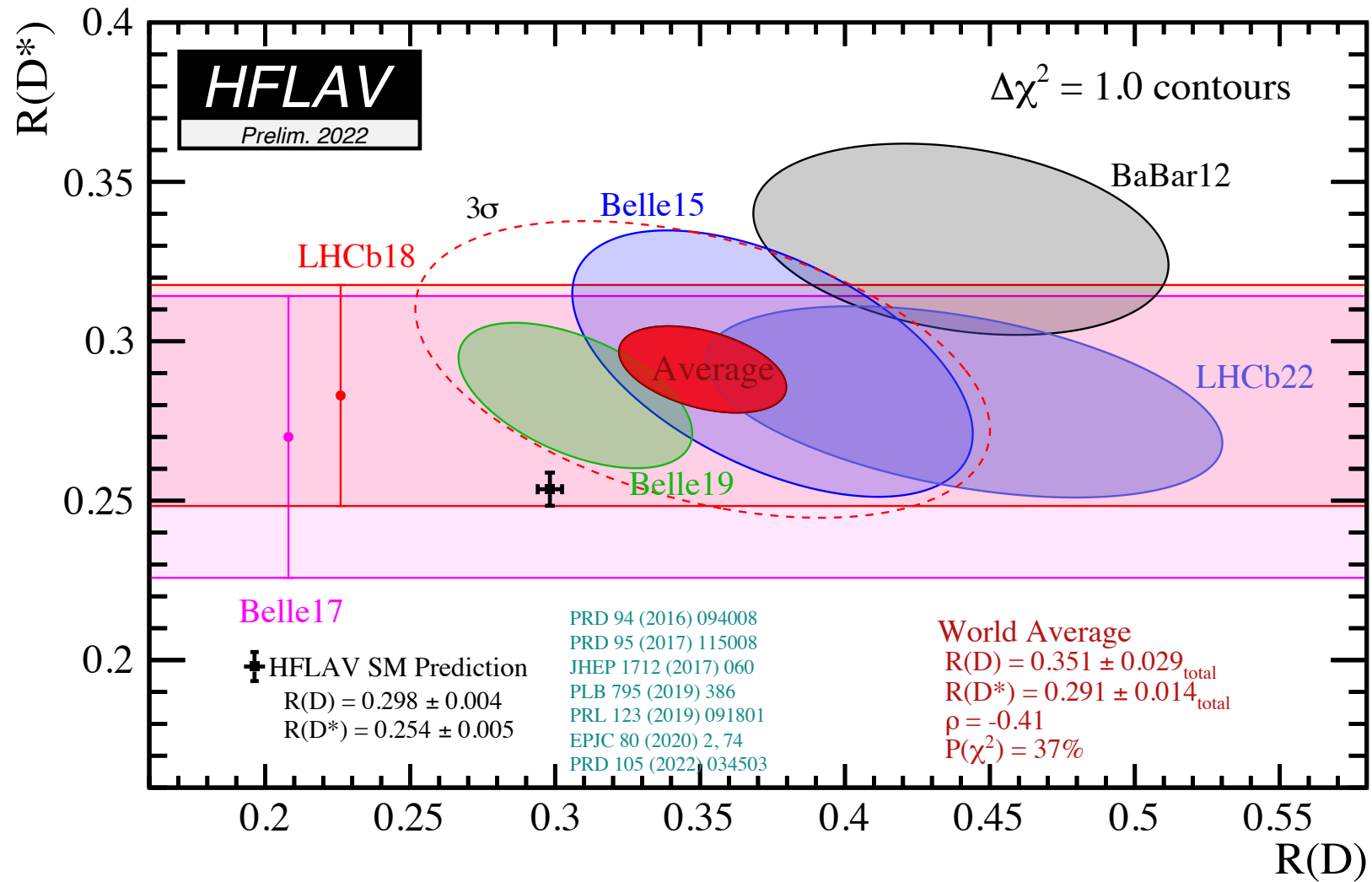
# $R(D)$ & $R(D^*)$ FPCP 2017



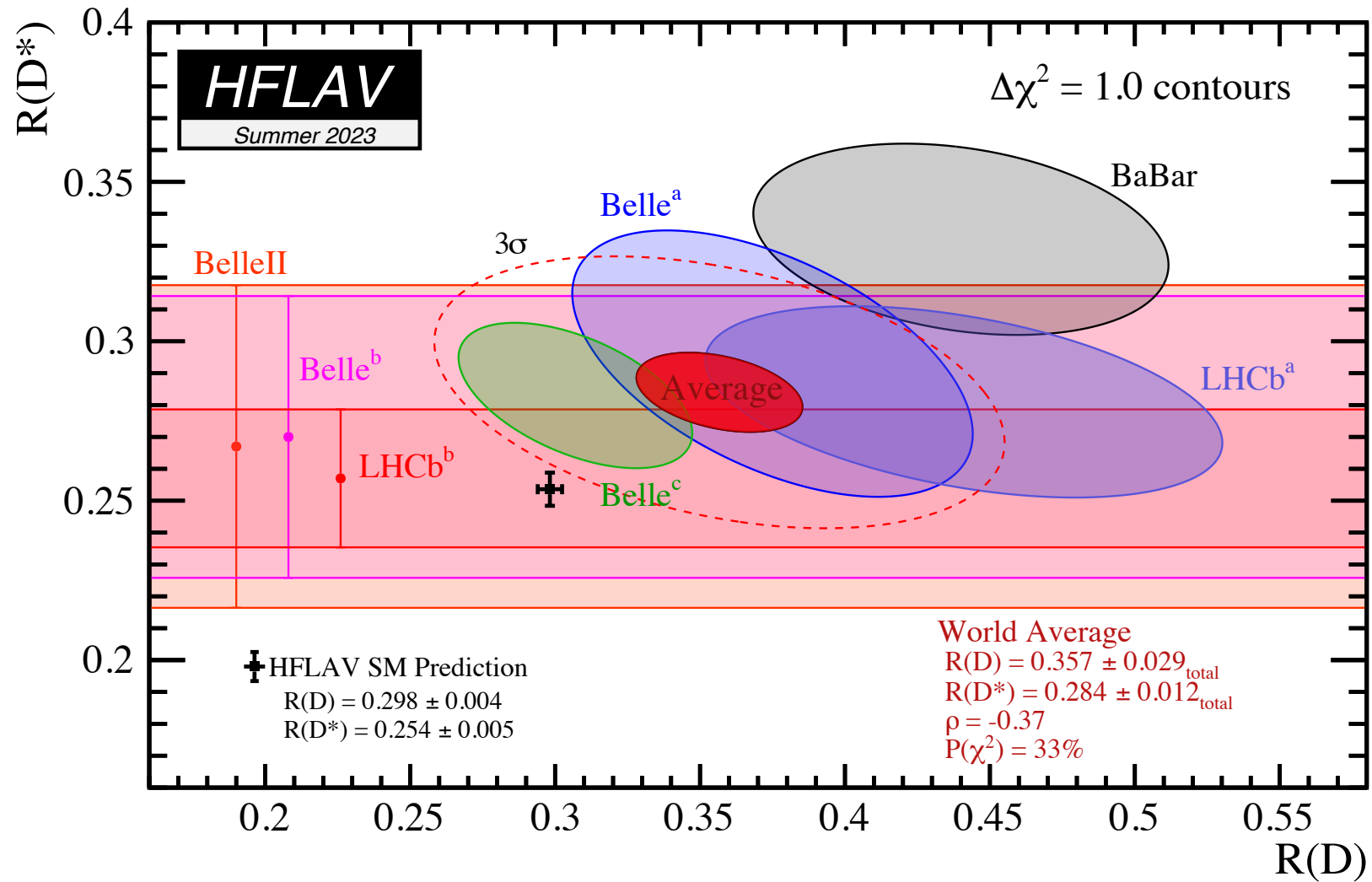
# $R(D)$ & $R(D^*)$ Summer 2018



# $R(D)$ & $R(D^*)$ Fall 2022



# $R(D)$ & $R(D^*)$ Summer 2023





# $R(D)$ & $R(D^*)$

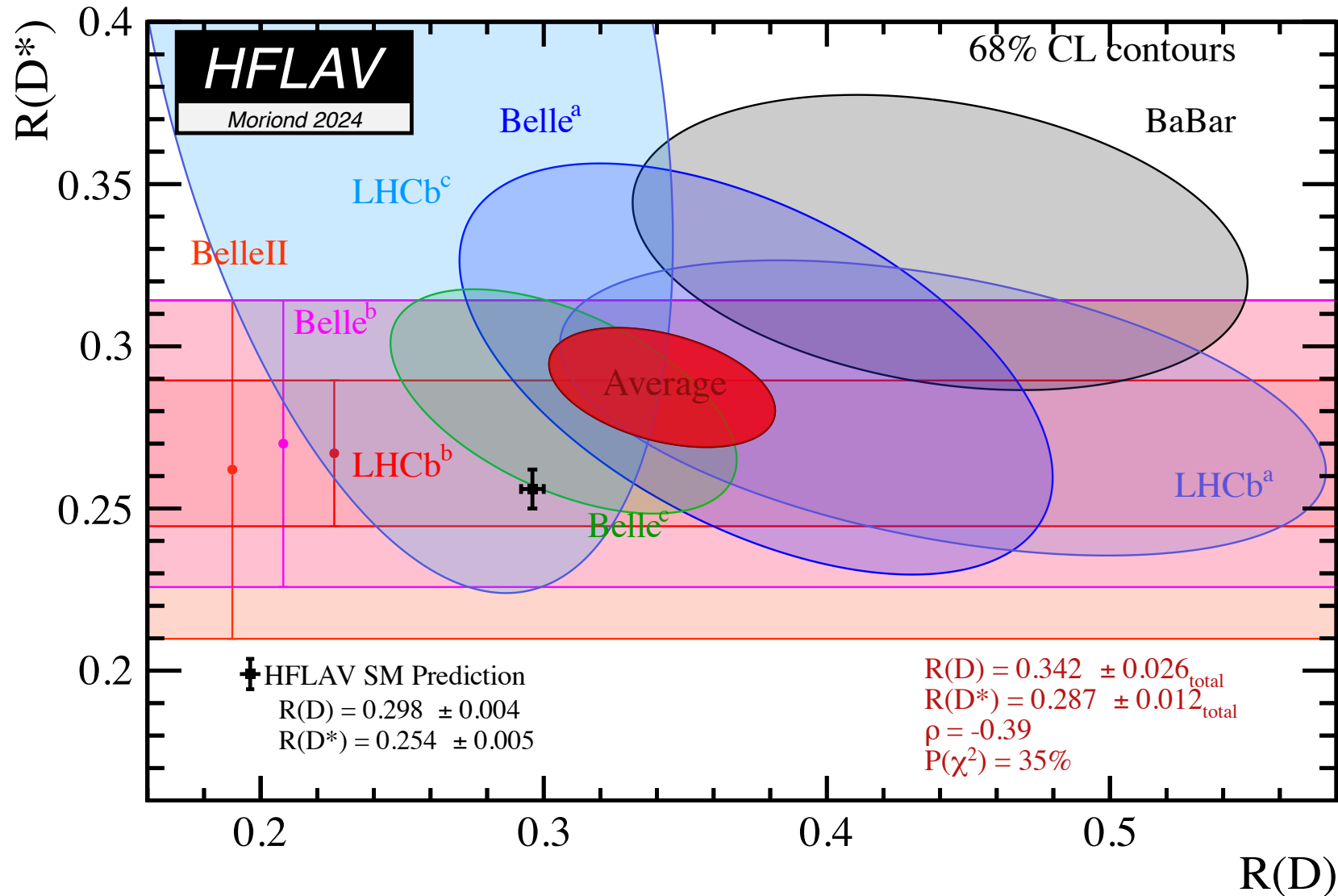
HFLAV

- $R(D)$  and  $R(D^*)$  combined average

- $3.31 \sigma$  tension with the SM prediction considering the correlation

- Is the SM prediction stable?

- $R(D)$ : predictions consistent
- $R(D^*)$ : tensions between some of the calculations





# Inclusive $R(X)$

[PRL 131, 051804 \(2023\)  \$e/\mu\$](#)

[PRL 132, 211804 \(2024\)  \$\tau/\ell\$](#)

189 fb-1

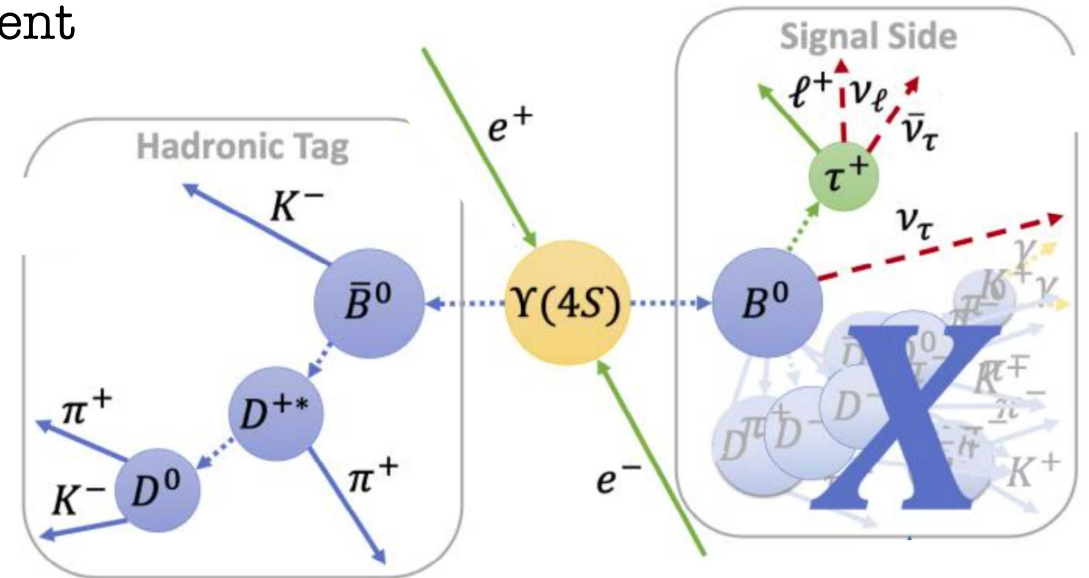
- Possible to compare the inclusive rates
- Tag B reconstructed using FEI method
- Search for the signal B in the rest of the event
  - Leptonic  $\tau \rightarrow e/\mu \bar{\nu} \nu$  decay
  - Remaining reconstructed particles in the event form the hadronic system “X”
  - Additional experimental challenge due to unspecified hadronic “X” system
- Primary experimental challenge is modelling/ characterizing backgrounds:
  - $B \rightarrow X l \nu$  ( $l=e, \mu$ ) decays
  - Generic  $B\bar{B}$  events with mis-reconstruction
  - Continuum  $q\bar{q}$  events

$$R(X) = \frac{\mathcal{B}(B \rightarrow X \tau \nu_\tau)}{\mathcal{B}(B \rightarrow X l \nu_\ell)}$$

$e : p_T/p_{\text{lab}} > 0.3 \text{ GeV}/0.5 \text{ GeV}$

$\mu : p_T/p_{\text{lab}} > 0.4 \text{ GeV}/0.7 \text{ GeV}$

To reject misidentified lepton





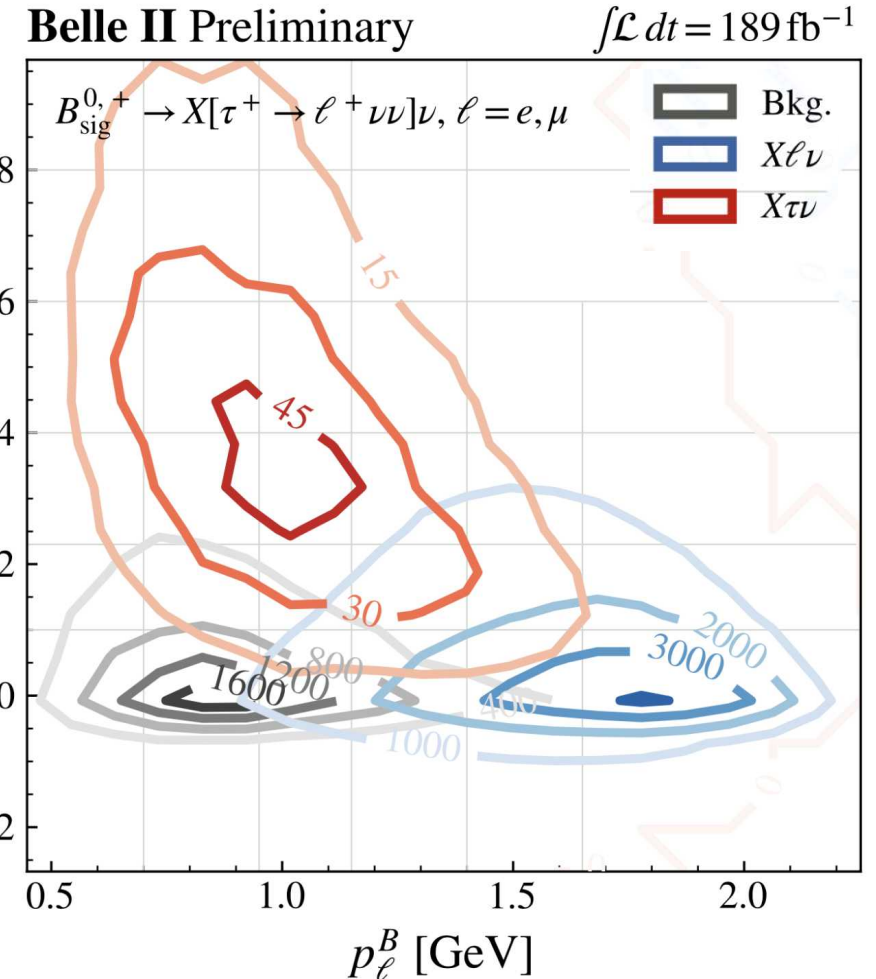
# Inclusive $R(X)$

PRL 131, 051804 (2023)  $e/\mu$   
PRL 132, 211804 (2024)  $\tau/\ell$

189 fb<sup>-1</sup>

- Signal determined from 2D distribution of  $p_\ell^B$  vs  $M_{miss}^2$
- Data-driven  $X\ell\nu$  modelling and reweighting using  $M_X$  distribution in  $p_\ell^B > 1.4$  GeV sideband region
- Systematics dominated by data-driven corrections to background and signal modelling
- Life is hard:

This Letter started as a blind analysis. Unblinding of an earlier version exposed a significant correlation of the results with the lepton momentum threshold, attributed to a biased selection applied in an early data-processing step and to insufficient treatment of low-momentum backgrounds. We reblinded, removed the problematic selection, tightened lepton requirements, and introduced the lepton-secondary and muon-fake reweightings. The results are now independent of the lepton momentum threshold, and are consistent between subsets of the full dataset when split by lepton charge, tag flavor, lepton polar angle, and data collection period. We verify that the reweighting uncertainties cover mismodeling of  $D$ -meson decays by varying the branching ratio of each decay  $D \rightarrow K(\text{anything})$  within its uncertainty as provided in Ref. [35] while fixing the total event normalization.





# Inclusive $R(X)$ results

[PRL 131, 051804](#) (2023)  $e/\mu$

[PRL 132, 211804](#) (2024)  $\tau/\ell$

189 fb<sup>-1</sup>

$$R(X_{e/\mu}) = 1.007 \pm 0.009(\text{stat}) \pm 0.019(\text{syst})$$

$$R(X_{\tau/e}) = 0.232 \pm 0.020(\text{stat}) \pm 0.037(\text{syst}),$$

$$R(X_{\tau/\mu}) = 0.222 \pm 0.027(\text{stat}) \pm 0.050(\text{syst}),$$

Combined

$$R(X_{\tau/\ell}) = 0.228 \pm 0.016(\text{stat}) \pm 0.036(\text{syst})$$

Average of SM expectation:  $0.223 \pm 0.005$

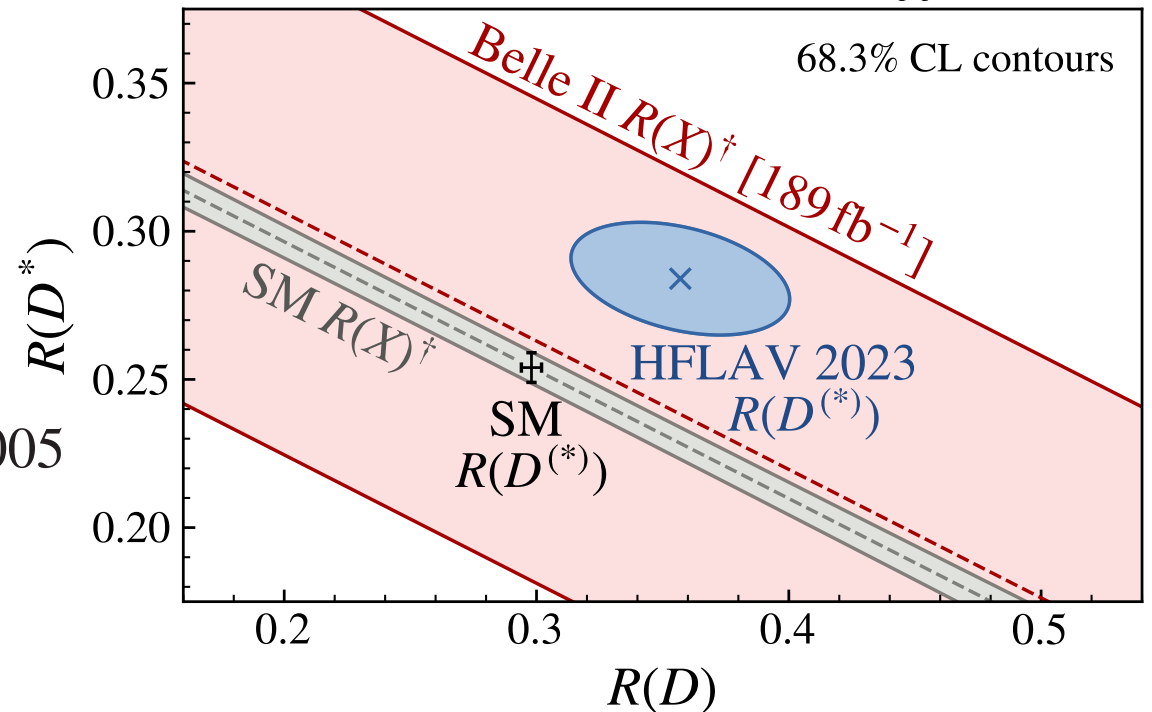
[PRD 105, 073009](#) (2022)

[JHEP 11 007](#) (2022)

Limited by systematics, even with smallish data set

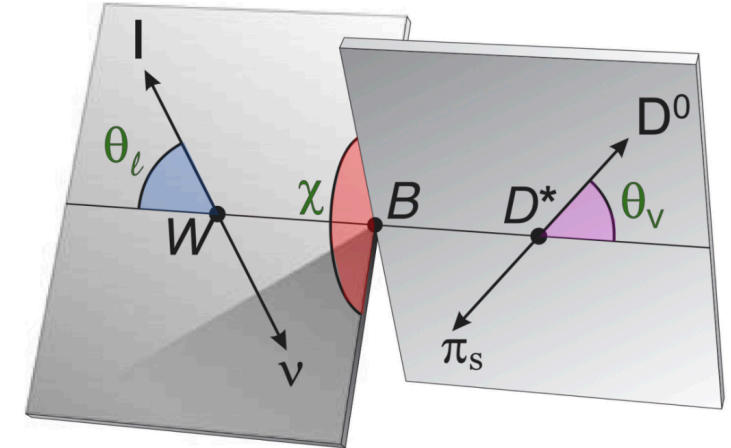
**Main sources of syst. uncertainties:**  $X_c \ell \nu$   $M_X$  shape: 7.1%,  $\mathcal{B}(B \rightarrow X \ell \nu)$ : 7.7%,  $X_c \tau(\ell) \nu$  form factors: 7.8%

† = with expected SM contributions of  $D_{(\text{gap})}^{**}$ ,  $X_u$  removed



# Angular analysis

- Rich phenomenology due to different decay amplitudes encoded in angular distributions (3 angles) as a function of the recoil energy of the  $D^*$
- measure 5 angular asymmetries and **compare them for  $e/\mu$**  in 2 bins of  $w$  ( $1 \leq w_{low} \leq 1.275, 1.275 < w_{high} \leq 1.503$ )



$$A_x(w) \equiv \left(\frac{d\Gamma}{dw}\right)^{-1} \left[ \int_0^1 - \int_{-1}^0 \right] dx \frac{d^2\Gamma}{dw dx} \quad w \equiv \frac{m_{B^0}^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

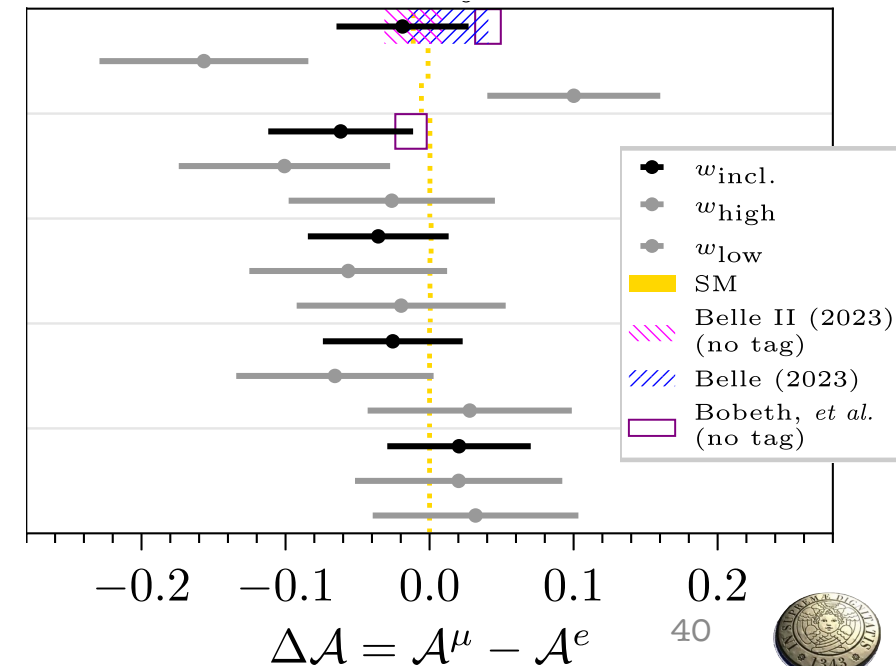
with  $x = \cos \theta_\ell$  for  $A_{FB}$ ,  $\cos 2\chi$  for  $S_3$ ,  $\cos \chi \cos \theta_V$  for  $S_5$ ,  $\sin \chi \cos \theta_V$  for  $S_7$ , and  $\sin 2\chi$  for  $S_9$ , as illustrated in the

$A_{FB}$ : tendency of the lepton to travel along the W direction

$S_3, S_9$ : sensitive to alignment of lepton and  $D^*$  direction

$S_5, S_7$ : measure coupled alignments in the orientation of the D wrt the  $D^*$

- All asymmetry measurements are statistics limited.
- Compatible with SM, no evidence for LFU violation.







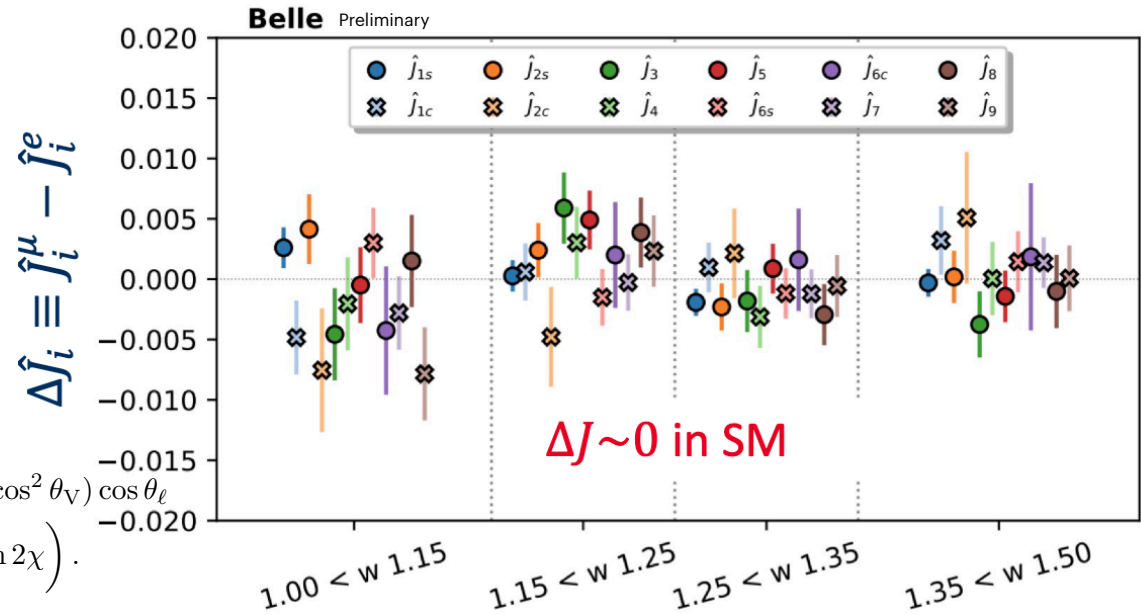
# Angular coefficients

- The differential decay rate can be decomposed in a basis of angular functions with 12 coefficients  $J_i$  all dependent on  $w$ 
  - Measure  $J_i$  in four bins of  $w$
  - Reconstruct D meson in different modes:  $D \rightarrow KK$ ,  $D \rightarrow KK(n)\pi$ ,  $D \rightarrow K(n)\pi$

Difference between electron and muon sensitive to LFU:  $\Delta J_i = J_i^\mu - J_i^e$ .

Difference between electron and muon sensitive to LFU:  $\Delta J_i = J_i^\mu - J_i^e$

No significant deviation from the SM



$$\frac{d\Gamma(\bar{B} \rightarrow D^* \ell \bar{\nu}_\ell)}{dw d\cos\theta_\ell d\cos\theta_V d\chi} = \frac{2G_F^2 \eta_{EW}^2 |V_{cb}|^2 m_B^4 m_{D^*}}{2\pi^4} \times \left( J_{1s} \sin^2 \theta_V + J_{1c} \cos^2 \theta_V \right. \\ + (J_{2s} \sin^2 \theta_V + J_{2c} \cos^2 \theta_V) \cos 2\theta_\ell + J_3 \sin^2 \theta_V \sin^2 \theta_\ell \cos 2\chi \\ + J_4 \sin 2\theta_V \sin 2\theta_\ell \cos \chi + J_5 \sin 2\theta_V \sin \theta_\ell \cos \chi + (J_{6s} \sin^2 \theta_V + J_{6c} \cos^2 \theta_V) \cos \theta_\ell \\ \left. + J_7 \sin 2\theta_V \sin \theta_\ell \sin \chi + J_8 \sin 2\theta_V \sin 2\theta_\ell \sin \chi + J_9 \sin^2 \theta_V \sin^2 \theta_\ell \sin 2\chi \right).$$



# Conclusions

- Lepton Flavour Universality Violation provides powerful tools for exploration of physics beyond standard model
- Experimentally challenging analyses, many channels tried
- Many new results, and more analyses ongoing, just scratching the surface
- Common effort with theory to improve the interpretation of the results and the SM expectations
- Tension with SM has been shrinking with more data and improved analysis

# Conclusions

- Lepton Flavour Unmixing provides powerful tools for exploratory analyses of the standard model
- Experimentally challenging to probe many channels tried
- Many new results are being discovered, just scratching the surface
- Common effort with other groups for the interpretation of the results and
- Tension with SM in some channels, need more data and improved analysis



provides powerful  
standard model  
many channels tried  
going, just  
the interpretation  
with more data and