

Tau physics at Belle and Belle II



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Outline

- **Belle / Belle II Experiments**
- **Tau physics**
 - Program and Motivation
 - Why at Belle / Belle II ?
 - How to reconstruct tau at Belle / Belle II
- **Standard Model measurements**
- **Lepton Flavor Universality (LFU)**
- **Lepton Flavor Violation (LFV)**
- **Summary and Outlook**

Belle and Belle II

- General purpose detector with almost 4π coverage
- Located at (Super)KEKB
→ asymmetric e^+e^- collider in Tsukuba Japan

Belle

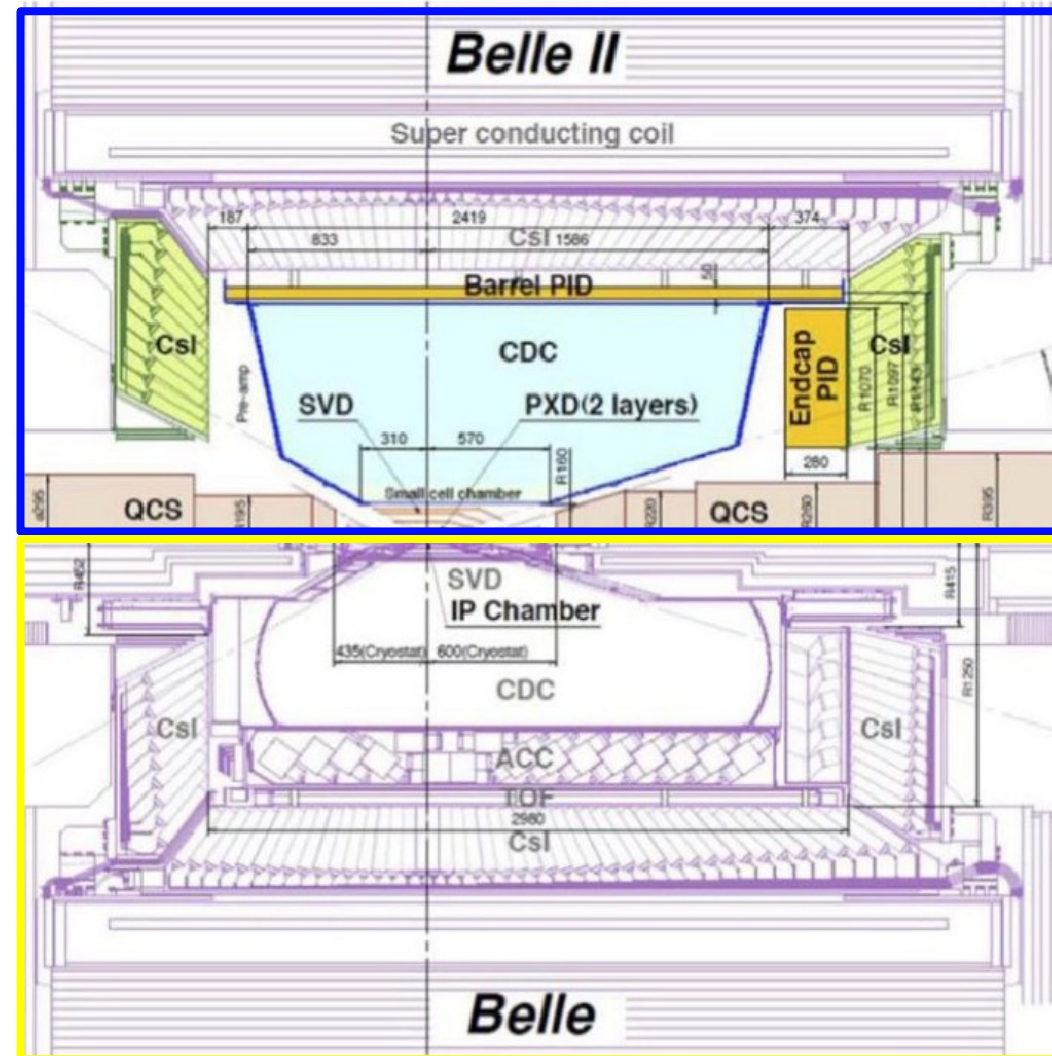
- 1999 – 2010
- 8 GeV electron and 3.5 GeV positron beams
- 980/fb collected

Belle II (successor of Belle)

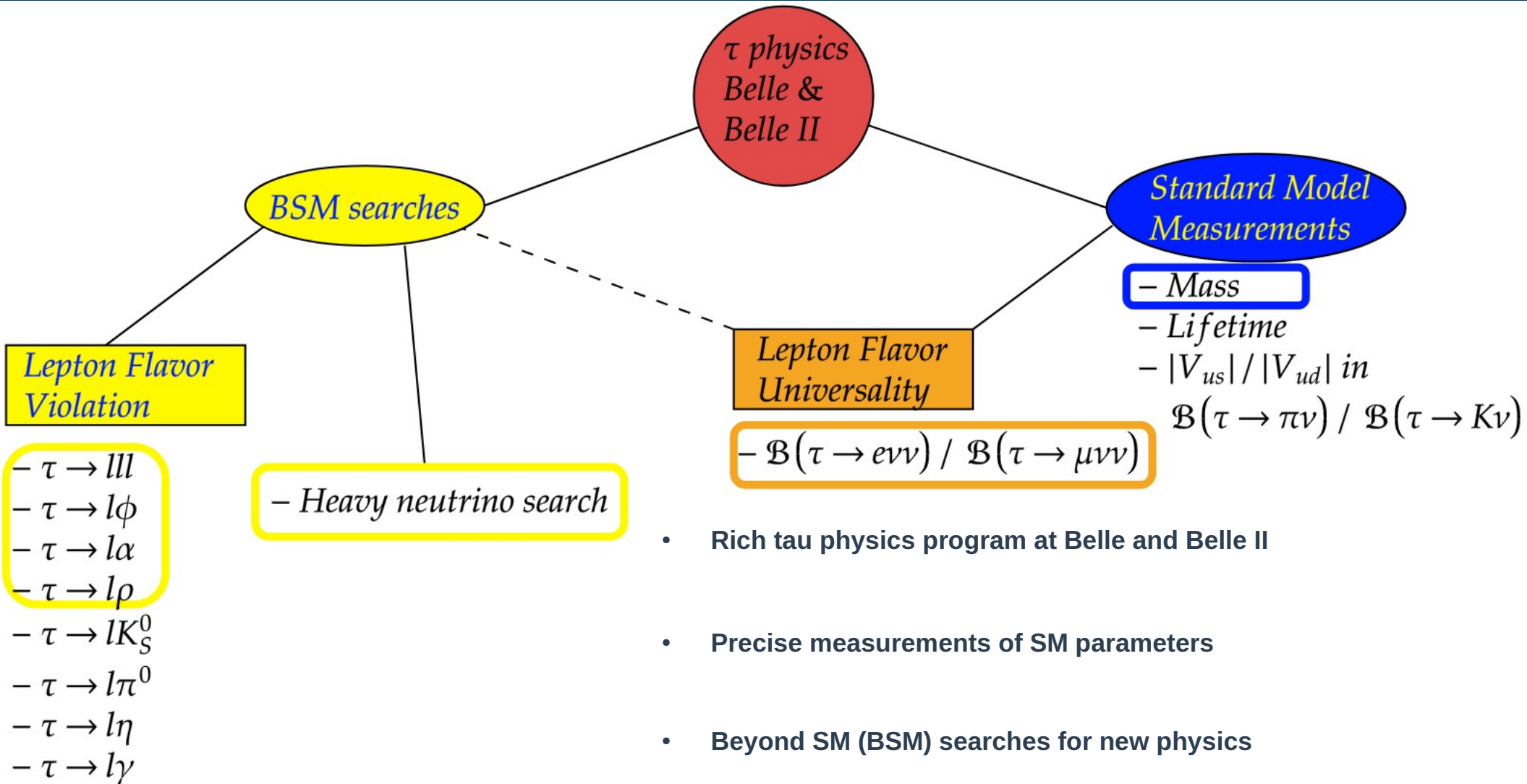
- 2018 - ??
- 7 GeV electron and 4 GeV positron beams
 - Smaller boost → new vertex detector using 2 layers of pixels and 4 layers of strips
- 424/fb up to now → goal : 50/ab

Detection

- Good momentum resolution & particle ID
- Good efficiency for neutral particles
- Missing energy reconstruction
- Specific low-multiplicity event triggers at Belle II

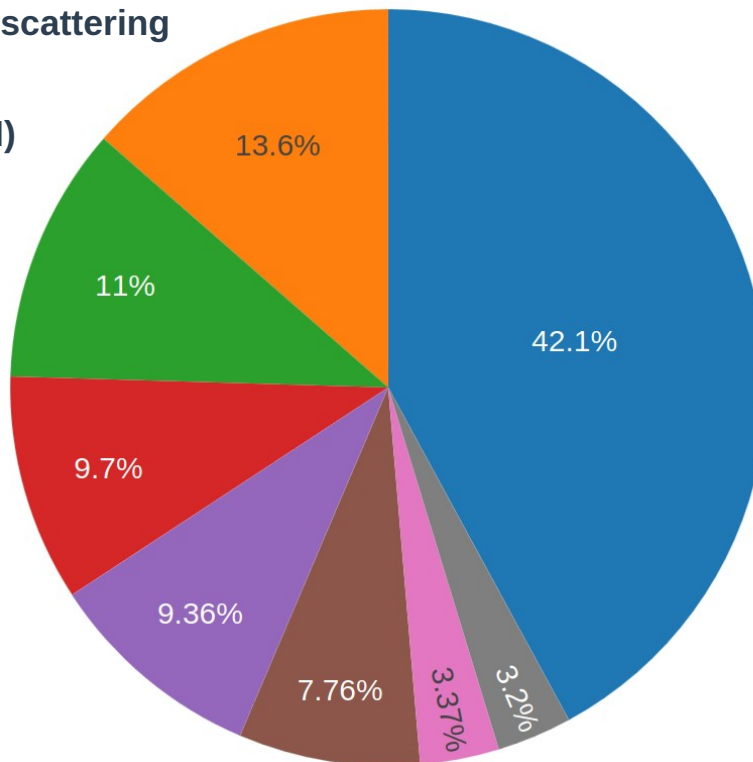


Tau physics : Program and Motivation

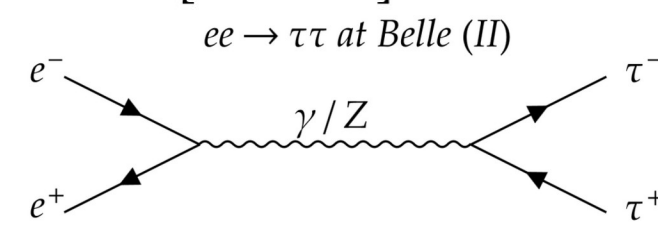
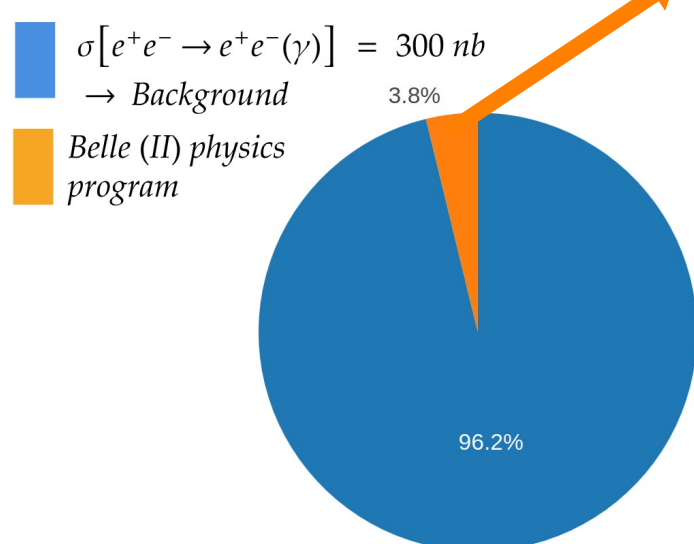


Tau physics : Why at Belle (II) ?

- 96.2 % of ee collisions do Bhabha scattering
→ Background
- Remaining 3.8 % compose Belle (II) physics program
 - 9.7 % $Y(4S) \rightarrow BB$
 - 7.76 % taupair production
→ 45 billion taupairs @ Belle II
 - High precision studies
 - Rare decay searches



- $\sigma[e^+e^- \rightarrow \gamma\gamma(\gamma)] = 4.99 \text{ nb}$
- $\sigma[e^+e^- \rightarrow uu] = 1.61 \text{ nb}$
- $\sigma[e^+e^- \rightarrow cc] = 1.3 \text{ nb}$
- $\sigma[e^+e^- \rightarrow \mu\mu] = 1.15 \text{ nb}$
- $\sigma[e^+e^- \rightarrow Y(4S)] = 1.11 \text{ nb}$
- $\sigma[e^+e^- \rightarrow \tau\tau] = 0.9 \text{ nb}$
- $\sigma[e^+e^- \rightarrow dd] = 0.4 \text{ nb}$
- $\sigma[e^+e^- \rightarrow ss] = 0.38 \text{ nb}$



- Clean physics environment, known initial state
- Missing energy reconstruction
- Dedicated low multiplicity triggers (not present in Belle)

Tau physics : How to reconstruct τ at Belle (II)

- SM τ decays are not fully reconstructable due to missing neutrino
- Identify $\tau^+\tau^-$ events using thrust axis

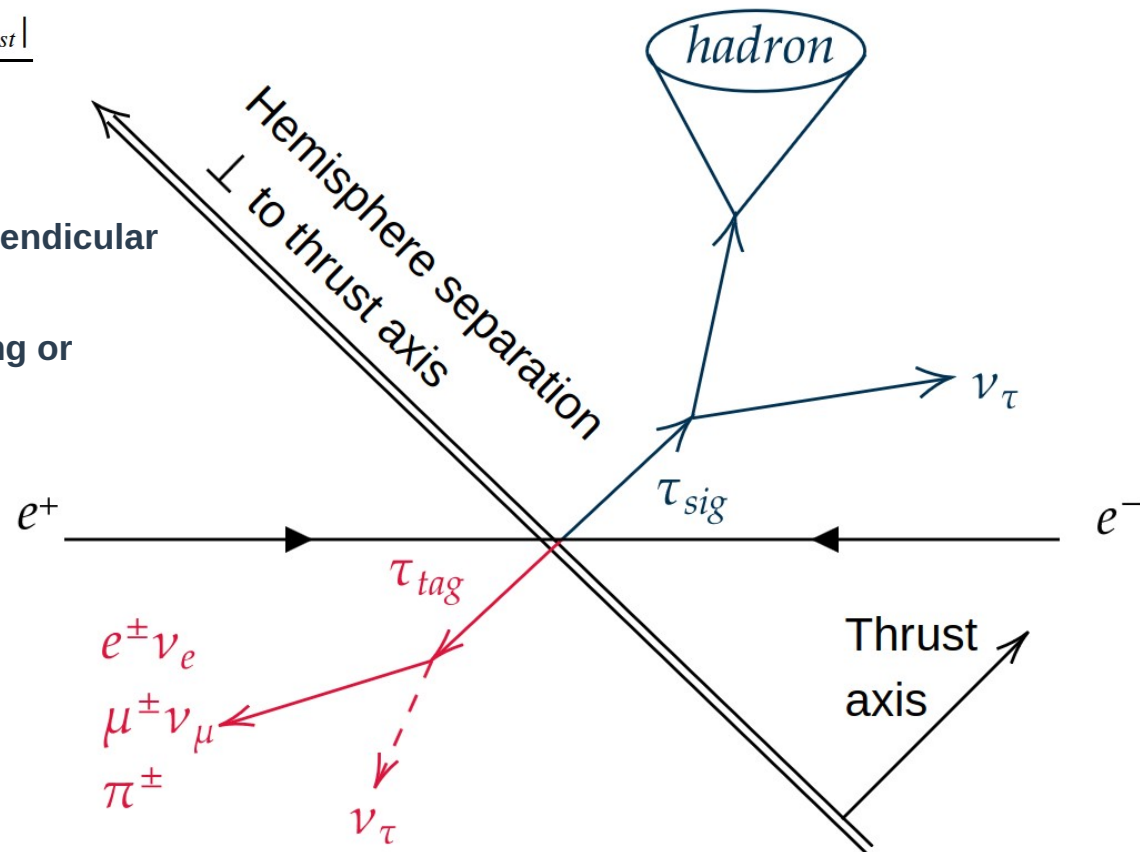
- Maximizes projection of all particle momenta in event

Find \vec{n}_{thrust} which maximizes
$$\frac{\sum_i |\vec{p}_i^{CM} \cdot \vec{n}_{thrust}|}{\sum_i |\vec{p}_i^{CM}|}$$

- Define two hemispheres divided by the plane perpendicular to the thrust axis

- Reconstruct tag-side tau in standard model 1-prong or 3-prong decay

- Exclusive \rightarrow use only 1-prong OR 3-prong events
 - High purity, less efficiency
- Inclusive \rightarrow do not reconstruct tag-side tau in a specific mode
 - Higher signal efficiency
 - Higher background levels



SM Measurements : Motivation

- Precision measurement of tau quantities can have significant impact

- First row unitarity of CKM-Matrix (Cabbibo-angle-anomaly)
- $B(\tau \rightarrow K\nu) / B(\tau \rightarrow \pi\nu) \sim |V_{us}| / |V_{ud}|^2$
- Mass of tau is the one with worst precision among leptons

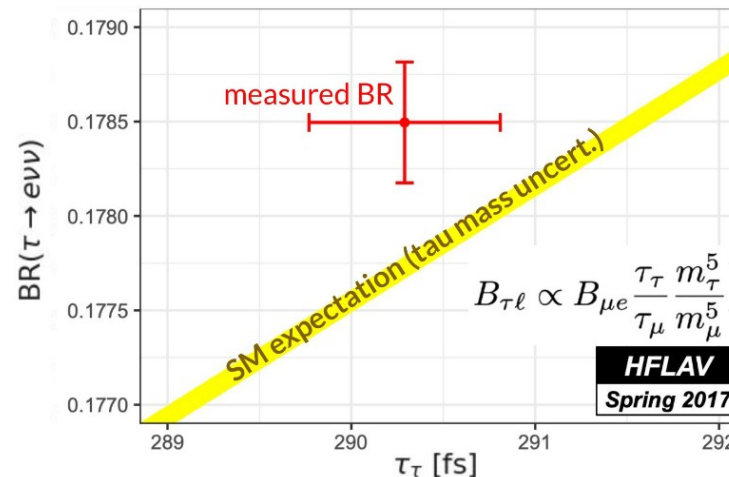
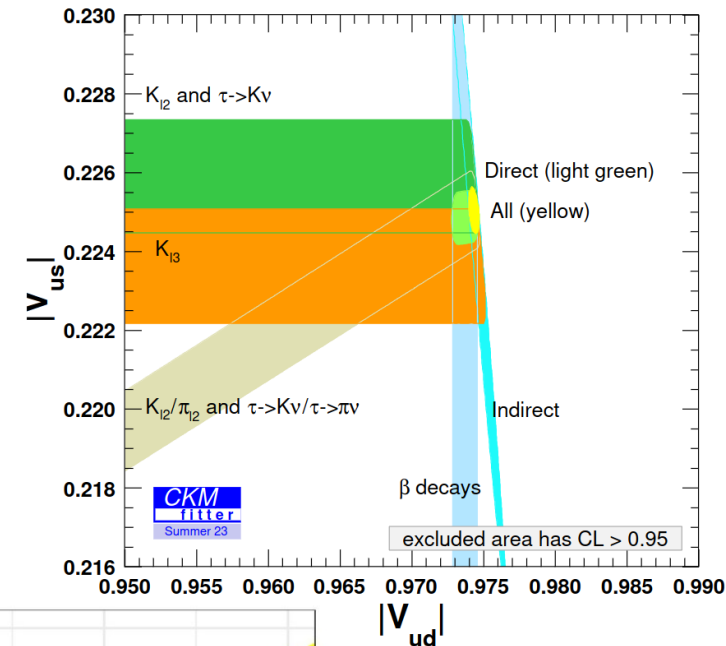
$$m_e = (0.51099895000 \pm 0.00000000015) \text{ MeV}$$

$$m_\mu = (105.6583755 \pm 0.0000023) \text{ MeV}$$

$$m_\tau = (1776.86 \pm 0.12) \text{ MeV}$$

- Lepton Flavor Universality

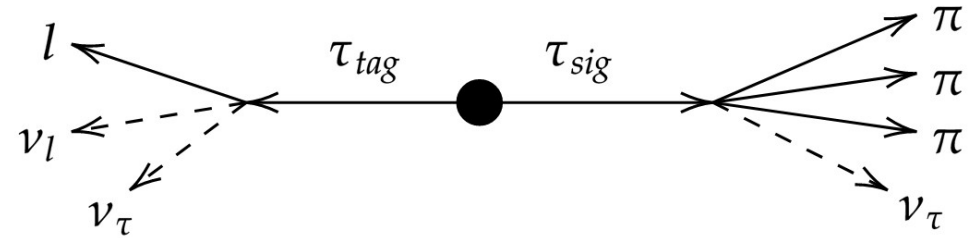
- All leptons are expected to have same coupling strength to W-Boson in SM
 - Different observations would suggest NP contributions
- Mass and lifetime of τ are important inputs to those calculations



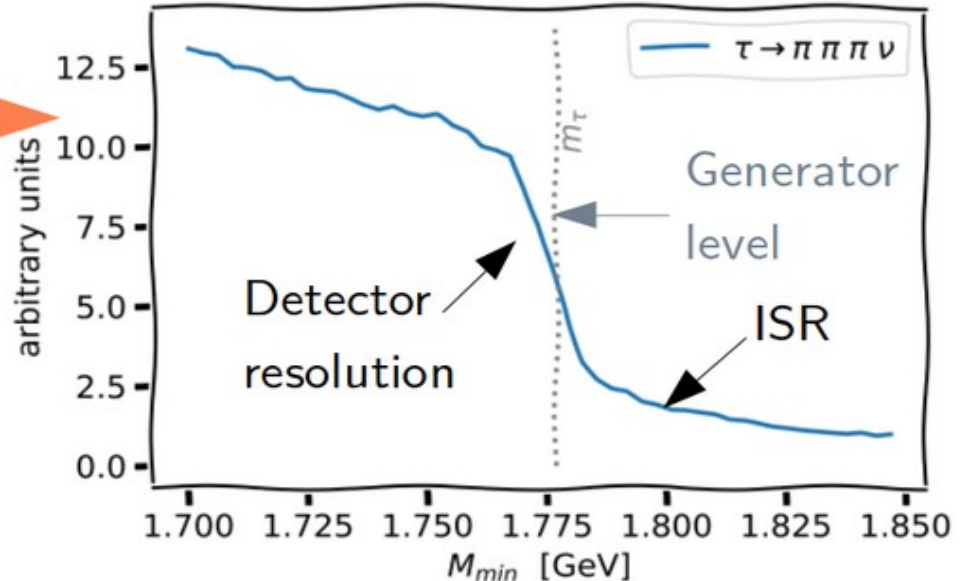
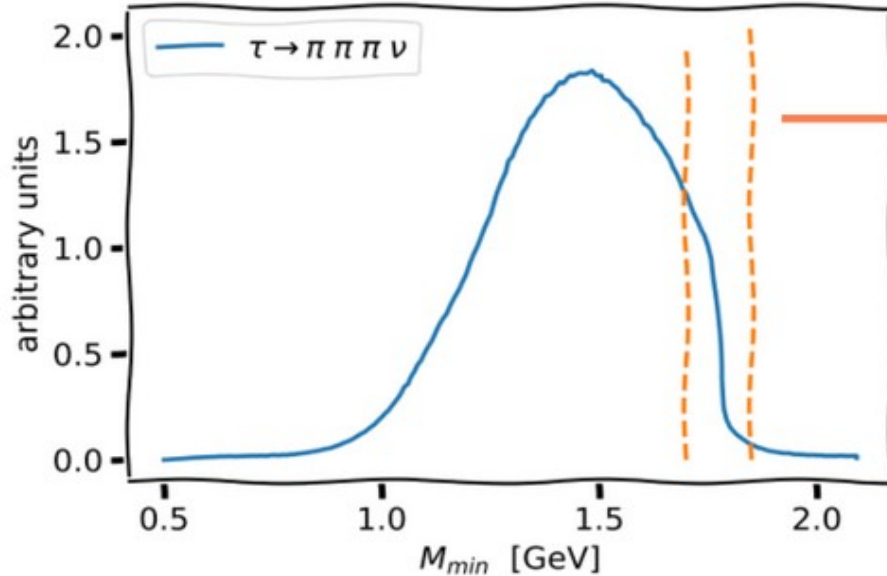
SM Measurements : τ Mass – I

- The τ mass is a fundamental parameter of the SM
- A precise measurement is an important input to LFU tests
- Belle II uses the Pseudomass method
 - Fit kinematic edge of M_{\min} distribution in $\tau \rightarrow 3\pi\nu$ decays with empirical function
 - Smeared edge due to ISR/FSR and detector resolution

PhysRev D. 108.032006 (2013)

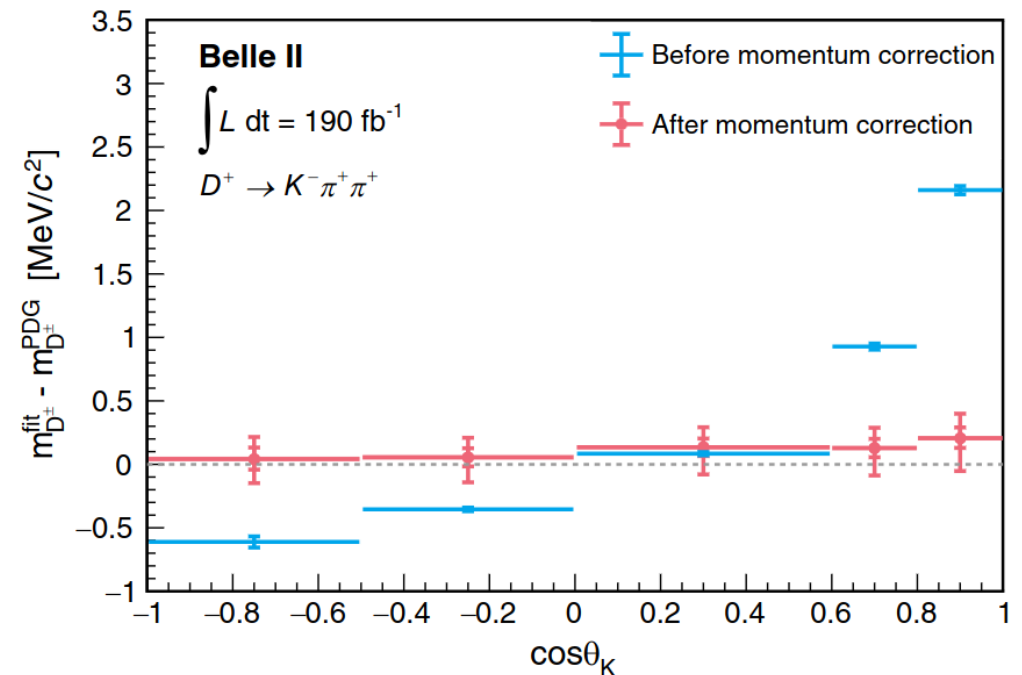
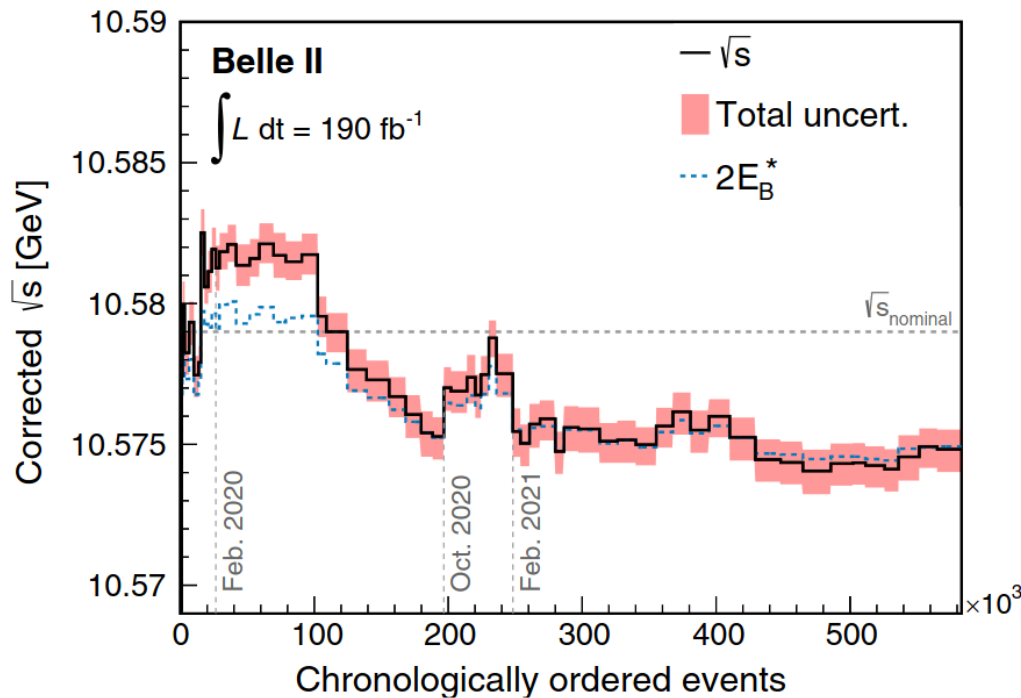


$$M_{\min} = \sqrt{m_{3\pi}^2 + 2(\sqrt{s}/2 - E_{3\pi})(E_{3\pi} - |\vec{p}_{3\pi}|)} \leq m_{\tau}$$



SM Measurements : τ Mass – II

- Beam energy calibration and momentum correction are crucial for this measurement
 - E_{beam} corrected by hadronic B-Meson decays
 - Momentum correction is done with scale factors for π using $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$
 - Originates from imperfect B-field, mismodeling in simulation \rightarrow bias in mass extraction

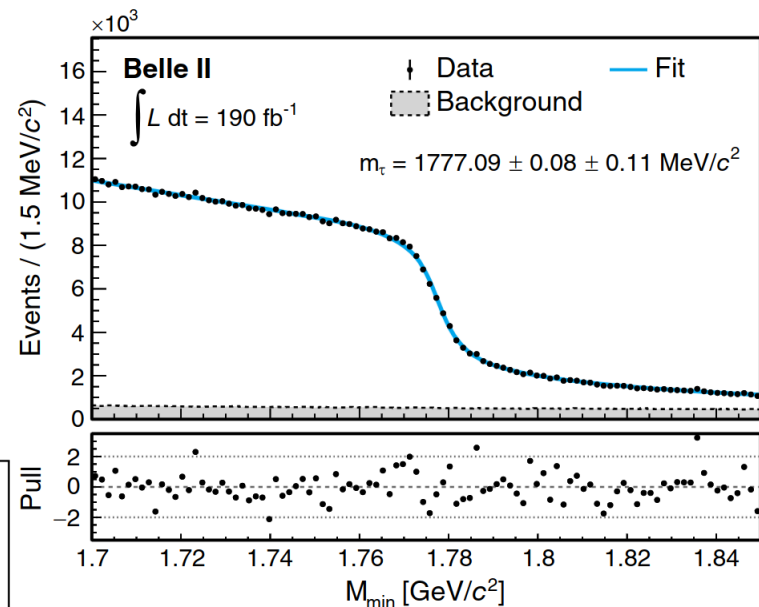


PhysRev D. 108.032006 (2013)

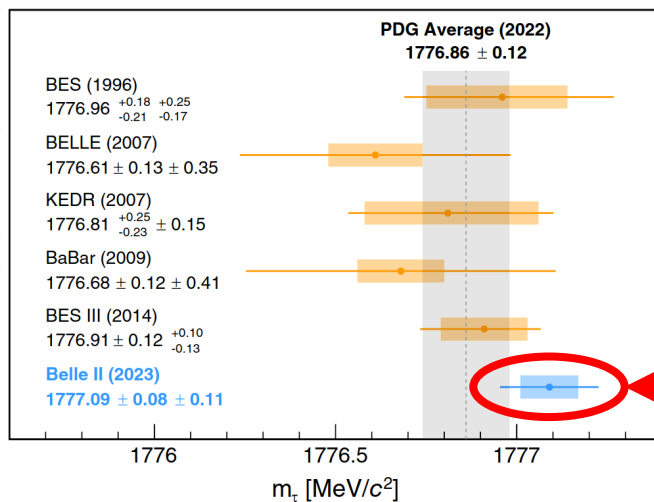
SM Measurements : τ Mass – III

- Perform unbinned maximum likelihood fit to the kinematic edge of the mass distribution

$$M_\tau = 1777.09 \pm 0.08 \pm 0.11 \text{ MeV}/c^2$$



$\int \mathcal{L} dt = 190 \text{ fb}^{-1}$
 $\sim 175 \text{ Million } ee \rightarrow \tau\tau$



Worlds most precise measurement

PhysRev D. 108.032006 (2013)

Source	Uncertainty (MeV/c ²)
Knowledge of the colliding beams:	
Beam-energy correction	0.07
Boost vector	< 0.01
Reconstruction of charged particles:	
Charged-particle momentum correction	0.06
Detector misalignment	0.03
Fit model:	
Estimator bias	0.03
Choice of the fit function	0.02
Mass dependence of the bias	< 0.01
Imperfections of the simulation:	
Detector material density	0.03
Modeling of ISR, FSR and τ decay	0.02
Neutral particle reconstruction efficiency	≤ 0.01
Momentum resolution	< 0.01
Tracking efficiency correction	< 0.01
Trigger efficiency	< 0.01
Background processes	< 0.01
Total	0.11

SM Measurements : LFU – I (NEW)

- SM picture of leptons

- 3 families with different masses and different, separately conserved lepton numbers
- Coupling to W boson is flavor-independent (?) $\rightarrow g_e = g_\mu = g_\tau$
 - lepton universality

- Test LFU (e- μ) in tau decays with g_e, g_μ being proportional to the leptonic branching fractions

$$\left(\frac{g_\mu}{g_e} \right)_\tau^2 \sim \frac{\mathcal{B}(\tau \rightarrow \mu \nu \nu)}{\mathcal{B}(\tau \rightarrow e \nu \nu)}$$

$$\int \mathcal{L} dt = 362 \text{ fb}^{-1}$$

$$\sim 334 \text{ Million } ee \rightarrow \tau\tau$$

- LFU is sensitive to new physics if it violates lepton flavor and/or lepton universality in weak charged-currents

- Belle II analysis uses 1-prong decays with one charged hadron and at least one neutral pion on the tag-side

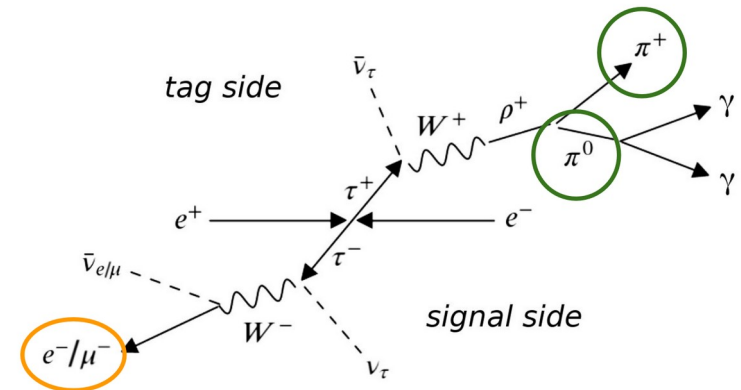
- Large BF $\sim 35\%$ on tag-side, low backgrounds, high trigger efficiency

- Signal side:

- One particle track with lepton ID requirement

- Tag side:

- One track with $E_{\text{cluster}} / p < 0.8$
- At least one neutral pion on tag side

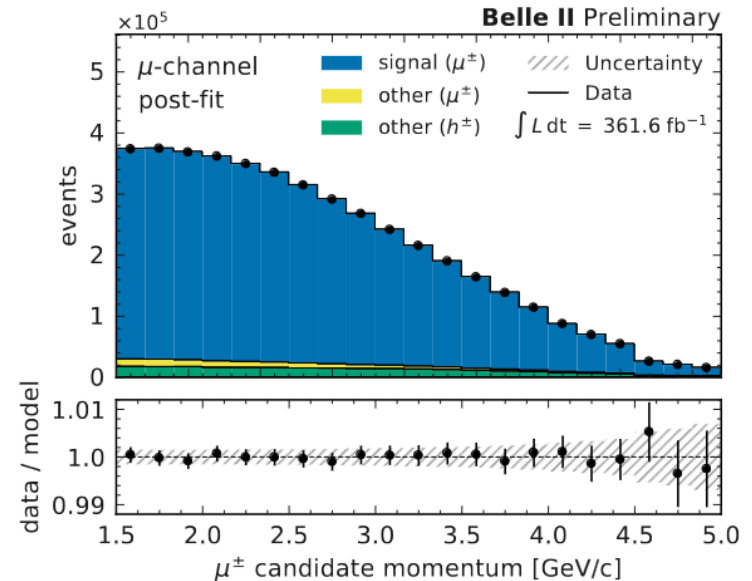
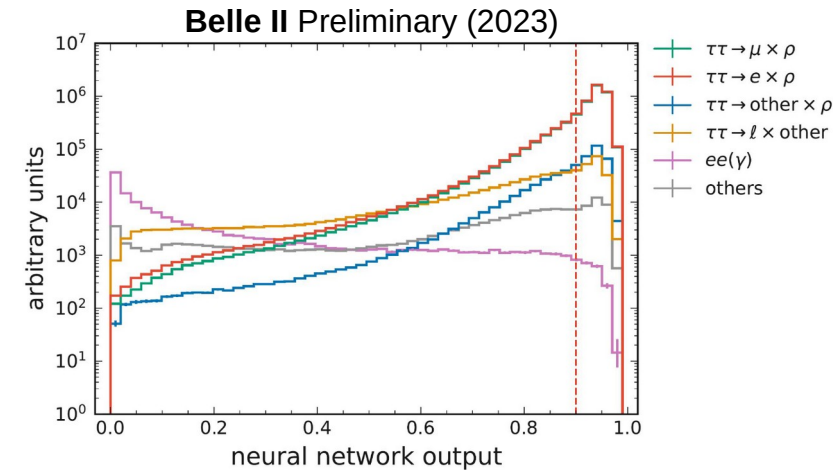


SM Measurements : LFU – II (NEW)

- Event selection is performed with rectangular cuts + neural network
- 94 % purity with 9.6 % signal efficiency for the combined sample
- Main backgrounds:
 - $ee \rightarrow \tau\tau$ (π faking e/μ) ~ 3.3 %
 - $ee \rightarrow \tau\tau$ (wrong tag) ~ 2.3 %
 - $ee \rightarrow ee\tau\tau \sim 0.2$ %

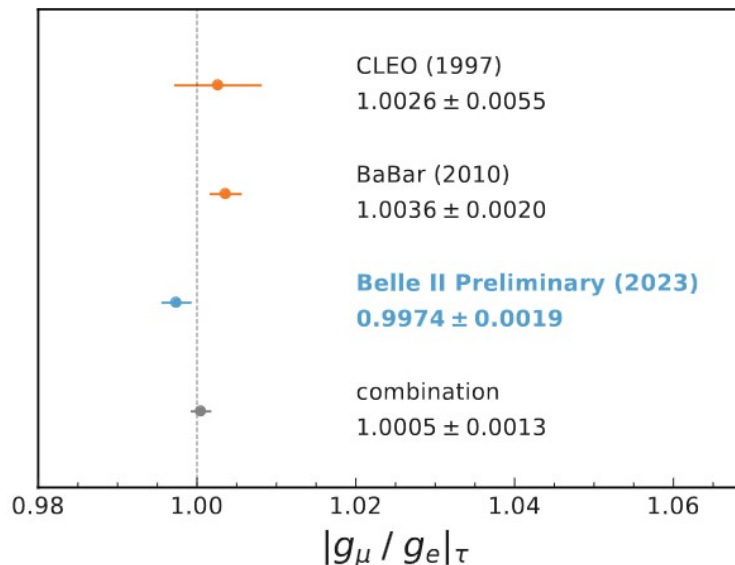
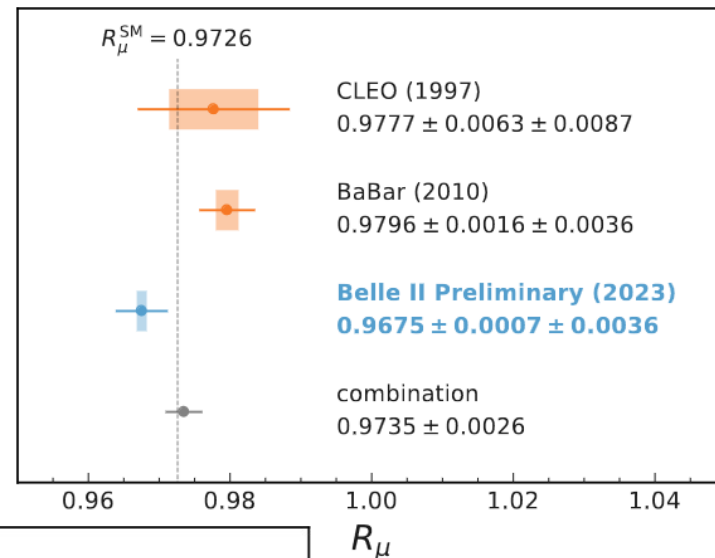
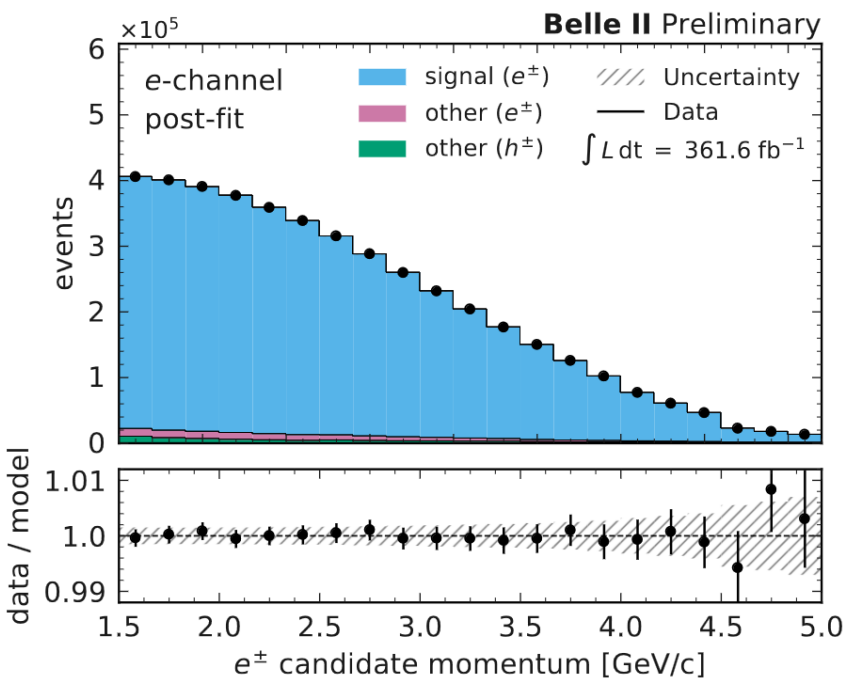
Extraction of R_μ

- Binned maximum likelihood template fit with pyhf in lepton momentum [1.5, 5] GeV
 - Simultaneous for e/μ channel for better constraints
- Systematics included with nuisance parameters modifying the templates
- 3 templates for electron and muon channel
 - Signal decays
 - Background with correct signal side lepton
 - Background with misidentified particle on signal side



SM Measurements : LFU – III (NEW)

- Leading systematics
 - Particle identification 0.32%
 - Trigger 0.10%
- Measured $R = 0.9675 \pm 0.0007 \pm 0.0036$
 - Most precise e-mu universality from tau decays in single measurement



BSM : Heavy neutrino search – I

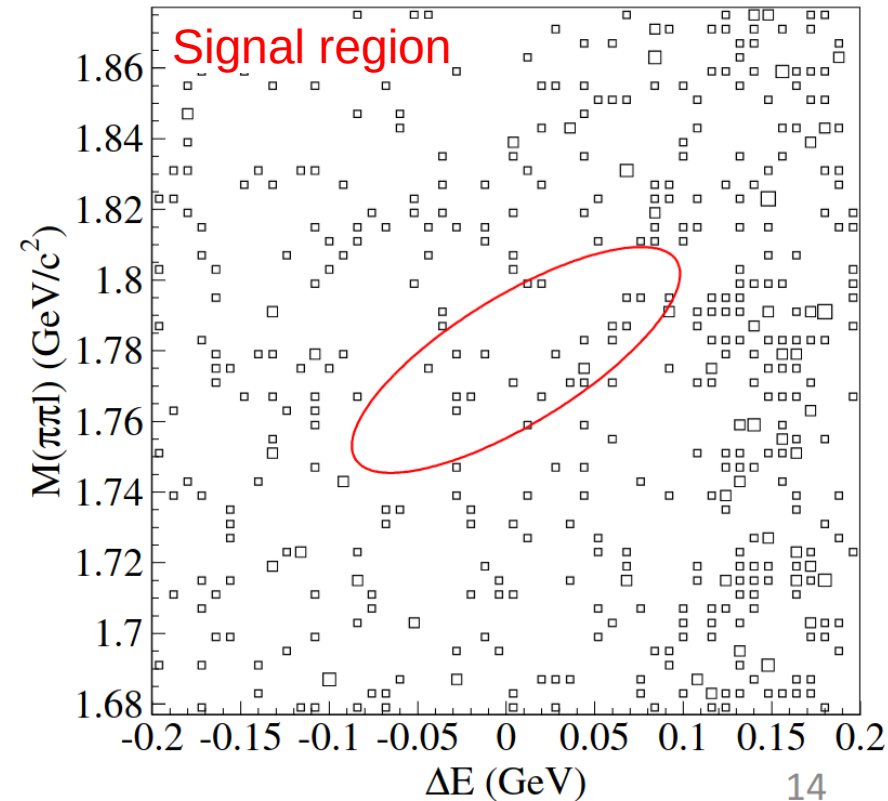
- Neutrino mass is not zero, which needs a mechanism to generate it
 - Including heavy, right-handed neutrinos is an approach to introduce neutrino mass

$$\int \mathcal{L} dt = 980 \text{ fb}^{-1}$$

$$\sim 905 \text{ Million } ee \rightarrow \tau\tau$$

- $\tau^\pm \rightarrow \pi^\pm \nu_h$ **with** $\nu_h \rightarrow \pi^\pm l^\mp$
 - ν_h long-lived Majorana neutrino, $l = e/\mu$

Data in M- ΔE plane

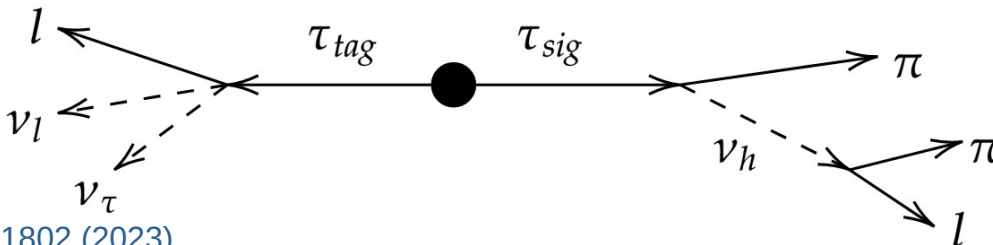


- Signal-side : require two pions and a lepton with common vertex
- Tag-side : 1 or 3-prong tau decay
- Backgrounds originate from $ee \rightarrow qq, \tau\tau, ll, eell$

- Suppress them with M and ΔE cuts

$$\Delta E = (E_{\pi\pi l}^{CM} - \sqrt{s}/2)$$

- Search for signal-like narrow peak



BSM : Heavy neutrino search – II

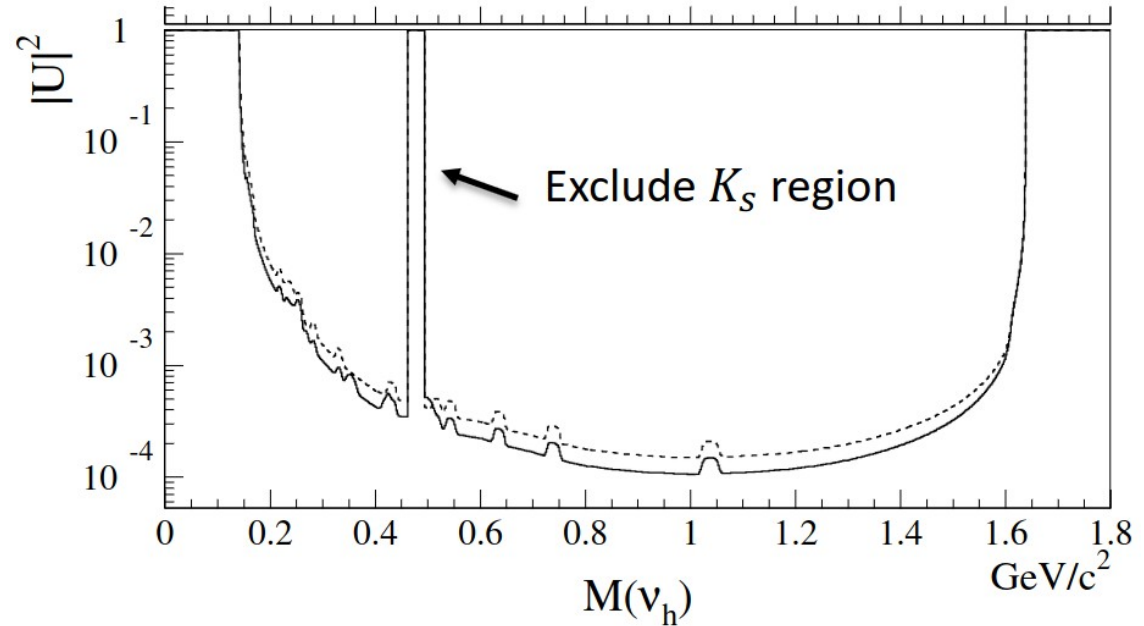
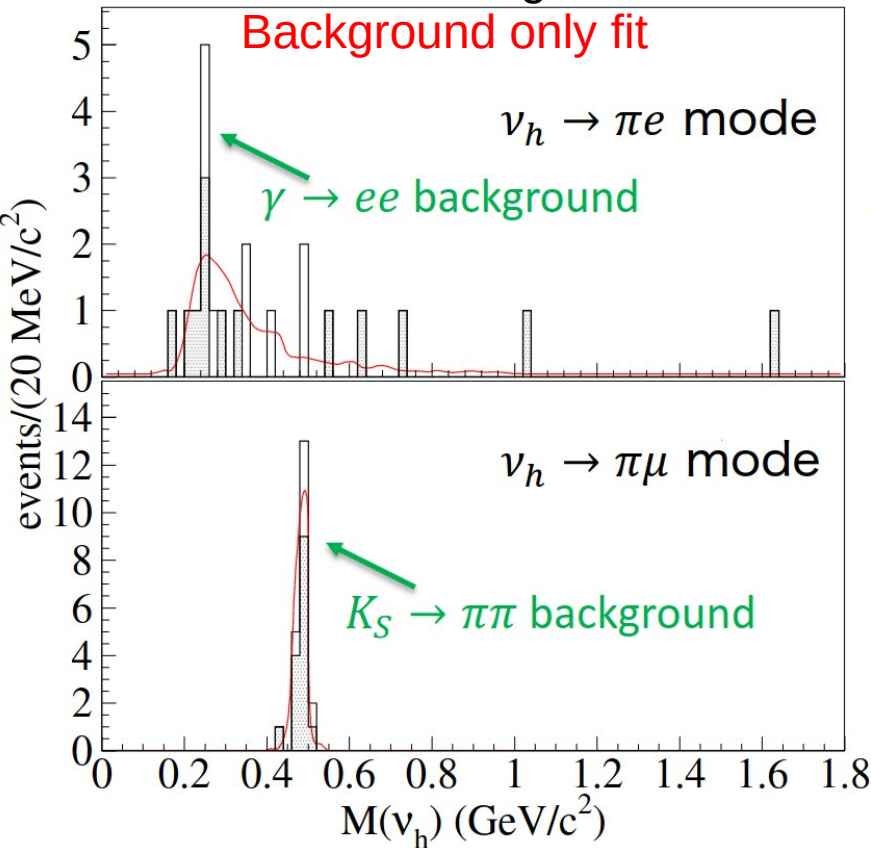
- No narrow signal peak found in $M(\nu_h \rightarrow \pi l)$ distribution
 - Set upper limit at 95% confidence level

$$\int \mathcal{L} dt = 980 \text{ fb}^{-1}$$

$$\sim 905 \text{ Million } ee \rightarrow \tau\tau$$

Data as histogram

Background only fit



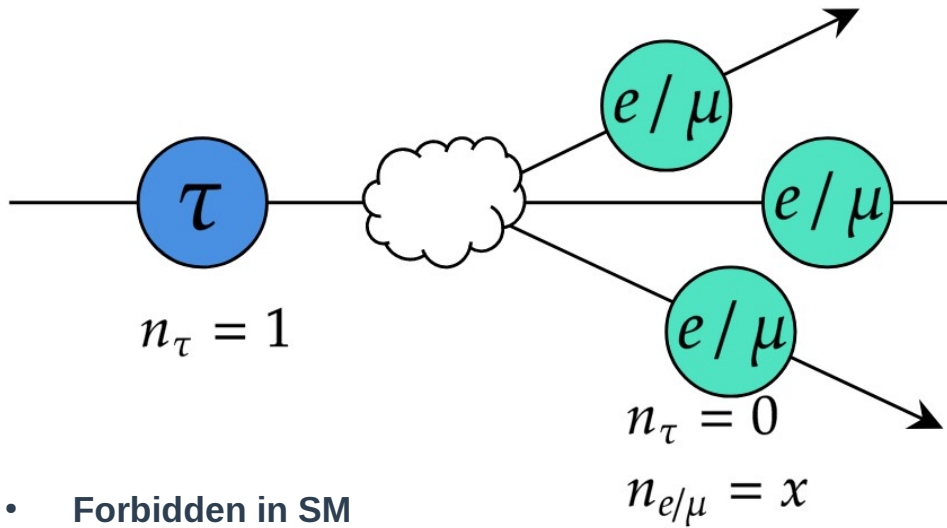
UL on the heavy neutrino mixing set in the mass range $0.2 < M(\nu_h) < 1.6 \text{ GeV}/c^2$

1.4×10^{-4} (1.5×10^{-4}) in Dirac-like limit for normal (inverted) hierarchy

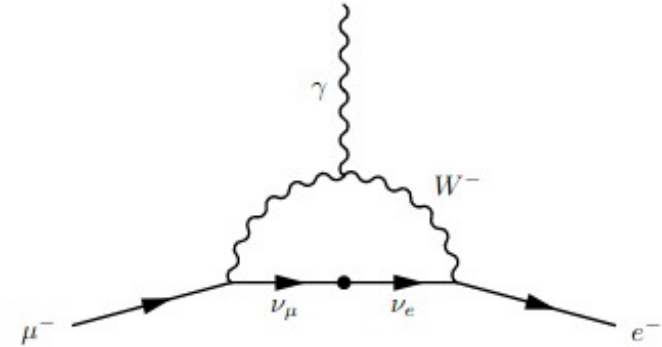
1.0×10^{-4} (1.1×10^{-4}) in Majorana-like limit for normal (inverted) hierarchy

LFV – Motivation

- Lepton Flavor Violation (LFV)

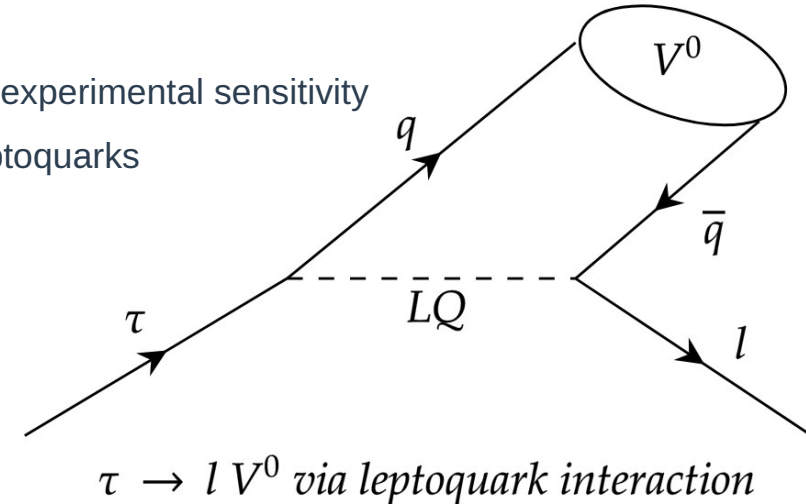


Example: LFV decay $\mu^- \rightarrow e^- \gamma$ via neutrino oscillations:

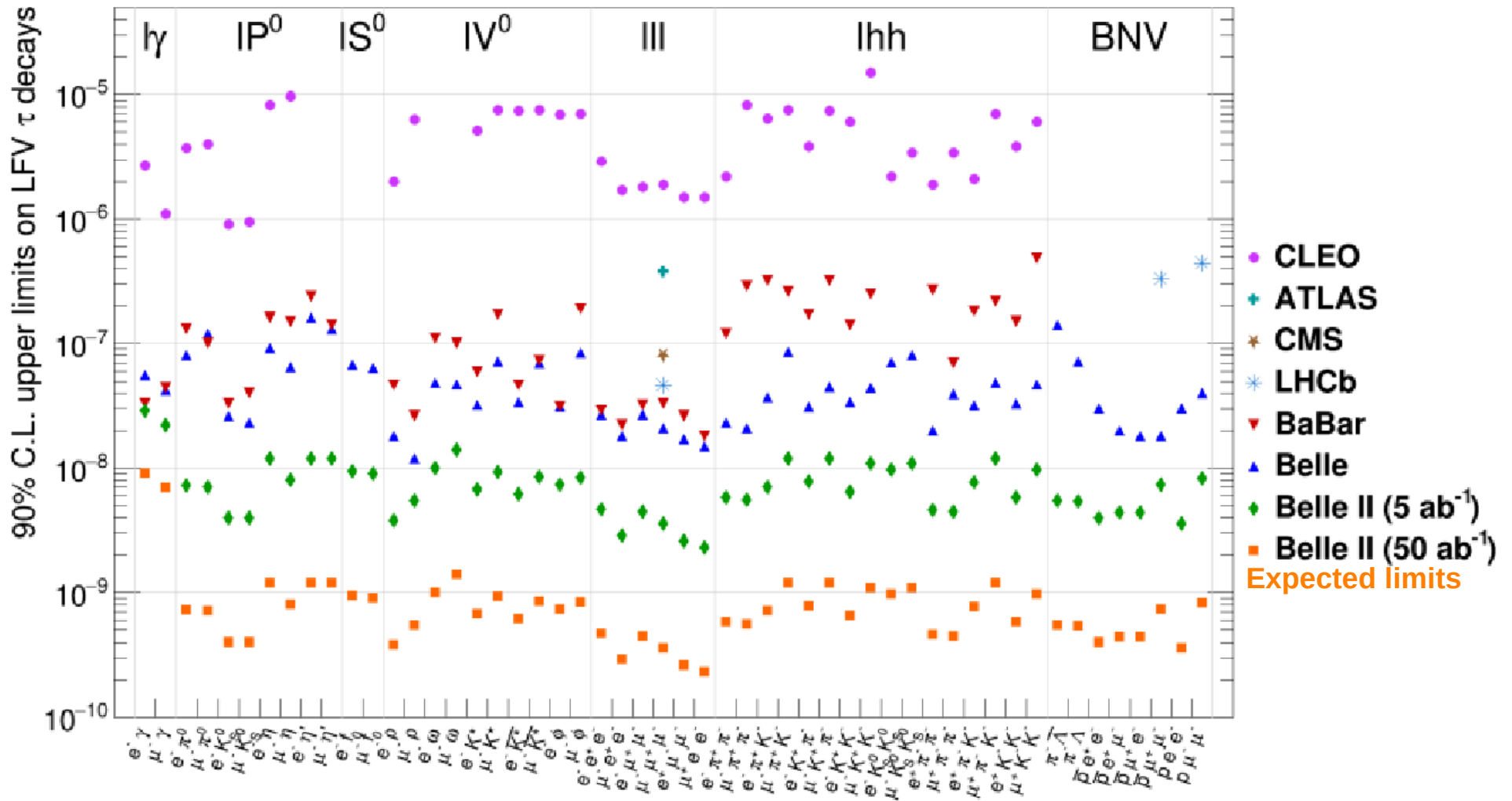


- Forbidden in SM

- Only possible due to neutrino oscillation BR $\sim O(10^{-50}) \rightarrow$ beyond any experimental sensitivity
- Extensions to the SM (New Physics) predict such decays e.g. via Leptoquarks
 - Can couple to quarks and leptons and so feature LFV decays
- Observation would be new physics



LFV – Past searches and projections



→ Belle II is expected to set new upper limits on a wide range of channels

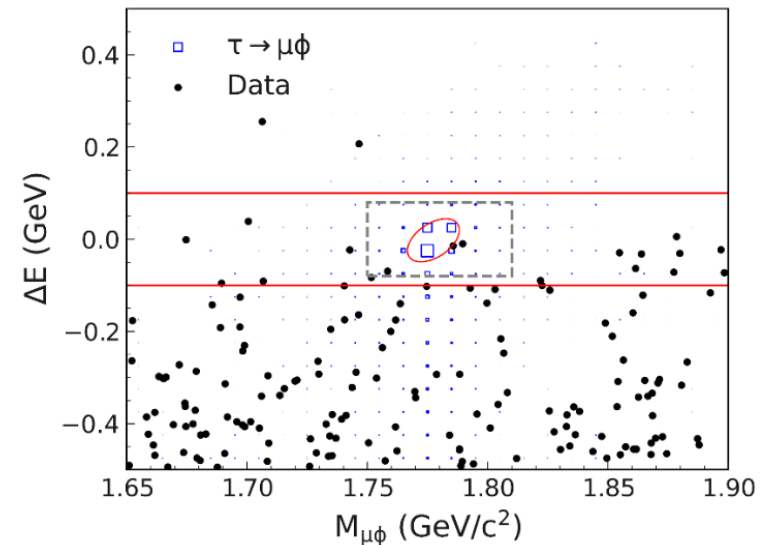
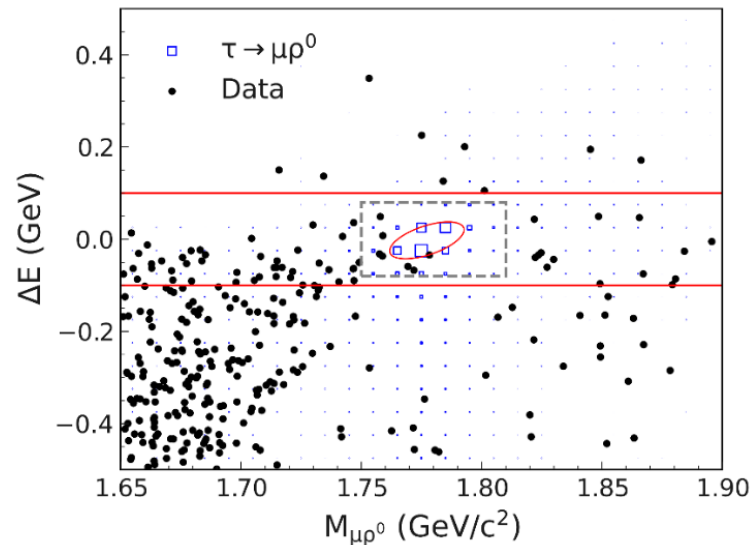
LFV : $\tau \rightarrow |V^0 - |$

- **Signal side:**
 - Reconstruct lepton and $V^0 \in [\rho, \phi, \omega, K^*]$
- **Tag side:**
 - Reconstruct 1 or 3-prong tau
- **Backgrounds:**
 - $\tau \rightarrow 3\pi\nu$ and $ee \rightarrow qq$
 - Suppression with BDT

Source	σ_{syst} (%)
Integrated luminosity	1.4
$ee \rightarrow \tau\tau(\gamma)$ cross section [48]	0.3
$\mathcal{B}(\phi \rightarrow K^+K^-)$ and $\mathcal{B}(\omega \rightarrow \pi^+\pi^-\pi^0)$	1.2 and 0.7
Trigger efficiency	0.2–0.9
Tracking efficiency	$0.35 \times N_{\text{track}}$
Electron identification efficiency	$1.7 \times N_{\text{electron}}$
Muon identification efficiency	$1.8 \times N_{\text{muon}}$
K^\pm and π^\pm identification efficiency	1.6 (ρ^0), 1.8 (ϕ) and 1.1 (K^{*0} and \bar{K}^{*0})
π^0 efficiency	$2.2 \times N_{\pi^0}$
Electron veto for hadrons	0.4–1.2
MC statistics	0.3–0.5
Track energy resolution	0.3–1.3
Photon energy resolution	0.0–0.4

$$\int \mathcal{L} dt = 980 \text{ fb}^{-1}$$

$$\sim 905 \text{ Million } ee \rightarrow \tau\tau$$



LFV : $\tau \rightarrow l V^0 - II$

World leading results

- No significant excess observed \rightarrow set ULs at 90% CL

Mode	ε (%)	N_{BG}	σ_{syst} (%)	N_{obs}	\mathcal{B}_{obs} ($\times 10^{-8}$)
$\tau^\pm \rightarrow \mu^\pm \rho^0$	7.78	$0.95 \pm 0.20(\text{stat.}) \pm 0.15(\text{syst.})$	4.6	0	< 1.7
$\tau^\pm \rightarrow e^\pm \rho^0$	8.49	$0.80 \pm 0.27(\text{stat.}) \pm 0.04(\text{syst.})$	4.4	1	< 2.2
$\tau^\pm \rightarrow \mu^\pm \phi$	5.59	$0.47 \pm 0.15(\text{stat.}) \pm 0.05(\text{syst.})$	4.8	0	< 2.3 *
$\tau^\pm \rightarrow e^\pm \phi$	6.45	$0.38 \pm 0.21(\text{stat.}) \pm 0.00(\text{syst.})$	4.5	0	< 2.0 *
$\tau^\pm \rightarrow \mu^\pm \omega$	3.27	$0.32 \pm 0.23(\text{stat.}) \pm 0.19(\text{syst.})$	4.8	0	< 3.9 *
$\tau^\pm \rightarrow e^\pm \omega$	5.41	$0.74 \pm 0.43(\text{stat.}) \pm 0.06(\text{syst.})$	4.5	0	< 2.4 *
$\tau^\pm \rightarrow \mu^\pm K^{*0}$	4.52	$0.84 \pm 0.25(\text{stat.}) \pm 0.31(\text{syst.})$	4.3	0	< 2.9 *
$\tau^\pm \rightarrow e^\pm K^{*0}$	6.94	$0.54 \pm 0.21(\text{stat.}) \pm 0.16(\text{syst.})$	4.1	0	< 1.9 *
$\tau^\pm \rightarrow \mu^\pm \bar{K}^{*0}$	4.58	$0.58 \pm 0.17(\text{stat.}) \pm 0.12(\text{syst.})$	4.3	1	< 4.3 *
$\tau^\pm \rightarrow e^\pm \bar{K}^{*0}$	7.45	$0.25 \pm 0.11(\text{stat.}) \pm 0.02(\text{syst.})$	4.1	0	< 1.7 *

$$B(\tau \rightarrow e V^0) < (1.7 - 2.4) \times 10^{-8}$$

$$B(\tau \rightarrow \mu V^0) < (1.7 - 4.3) \times 10^{-8}$$

Improvement $\sim 30\%$ compared to previous results!

LFV : $\tau \rightarrow l \phi$



- **Untagged inclusive reconstruction: do not reconstruct the tag side into a specific decay**
 - Higher Signal efficiency (~32% improvement), more background, use of rest of event variables

$$\int \mathcal{L} dt = 190 \text{ fb}^{-1}$$

$$\sim 75 \text{ Million } ee \rightarrow \tau\tau$$

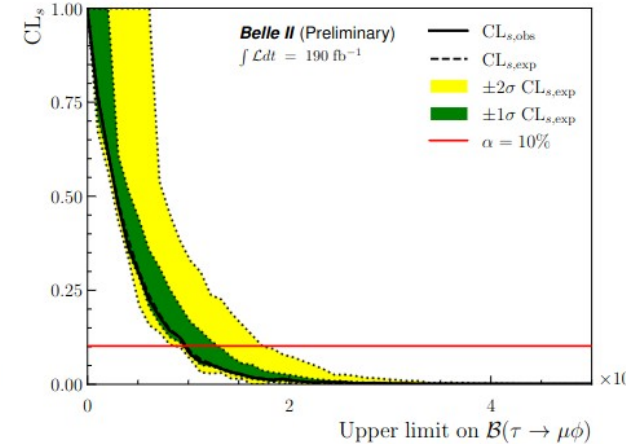
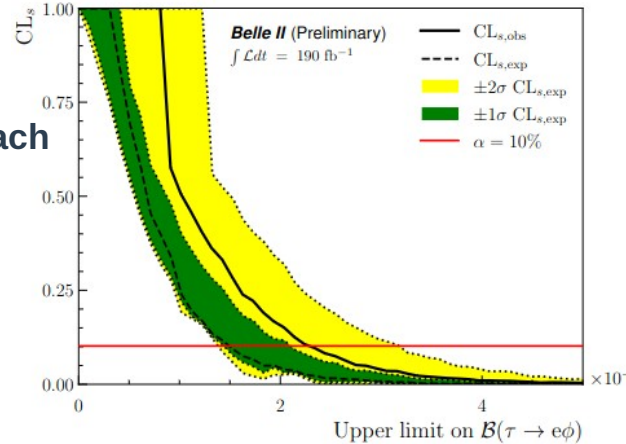
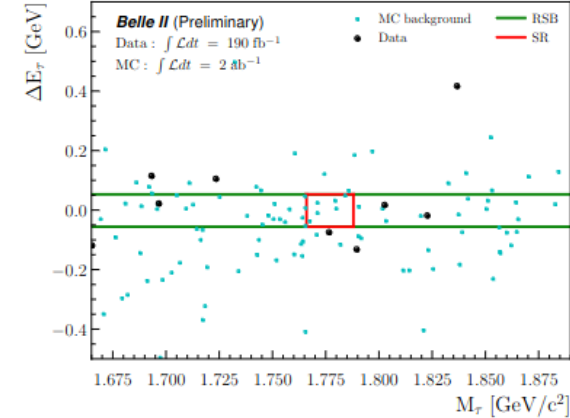
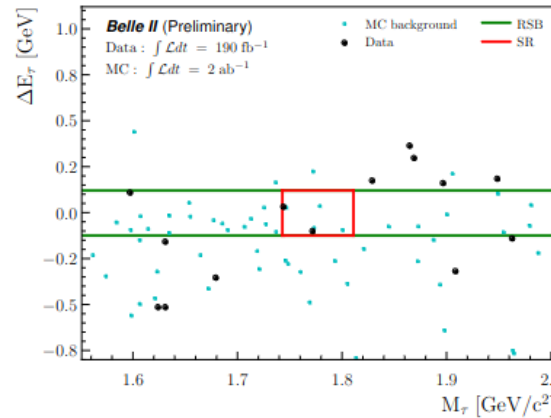
- **Backgrounds reduced with pre selections and a BDT trained against qqbar events**

- **Observed UL @ 90% CL**

- Electron channel : 1.0×10^{-7}
- Muon channel : 6.6×10^{-8}

- **No improvement to Belle/BaBar**
→ Small data set

- **First, successful untagged strategy approach for tau physics**



Experiment	$\mathcal{B}_{UL}^{90}(e\phi) (\times 10^{-8})$	$\mathcal{B}_{UL}^{90}(\mu\phi) (\times 10^{-8})$
	exp. / obs.	exp / obs.
BaBar	5.0 / 3.1	8.2 / 19
Belle	4.3 / 3.1	4.9 / 8.4

Babar : 451/fb
Belle : 854/fb

<https://arxiv.org/abs/2305.04759>

LFV : $\tau \rightarrow l\alpha - l$

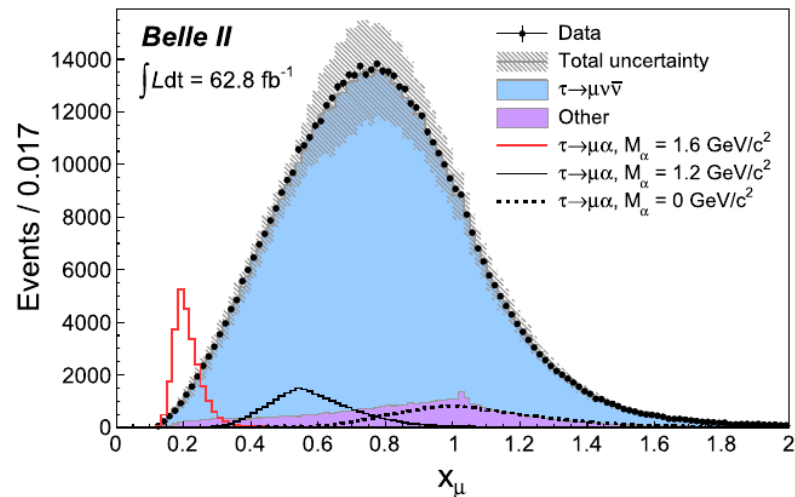
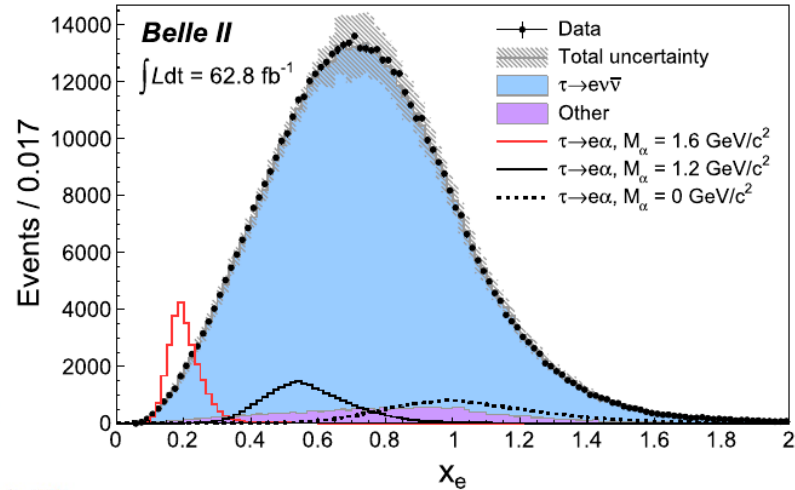
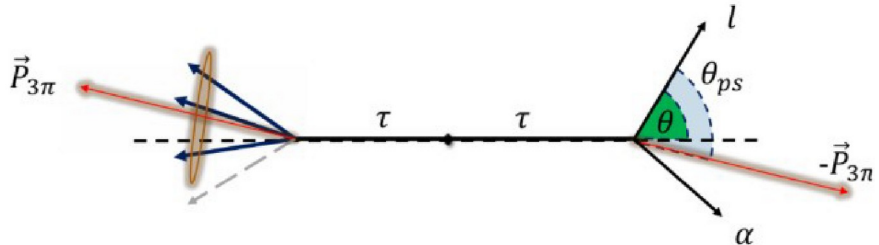
- α is an invisible spin-0 boson
 - Predicted by many models trying to incorporate neutrino-oscillation, muon magnetic moment anomaly or indirect evidence of dark matter in SM

• This direct search probes BSM theories with high sensitivity

- Previous limits from ARGUS: 10^{-2} to 10^{-3} 0.5/fb of data $\int \mathcal{L} dt = 62.8 \text{ fb}^{-1}$
 - Result from 1995 $\sim 57.7 \text{ Million } ee \rightarrow \tau\tau$

- Tau momentum cannot be determined from the decay particles directly
 - Approximate the energy in CMS as half of the beam energy and its direction opposite to the 3 hadrons on the tag-side pseudo rest frame
 - Search for an excess above the $\tau \rightarrow l\nu\nu$ normalized lepton energy spectrum with E_l^* the energy of the charged lepton in pseudo rest frame

$$x_\ell \equiv \frac{E_\ell^*}{m_\tau c^2 / 2}$$



PRL 130 181803 (2023)

LFV : $\tau \rightarrow l\alpha - II$

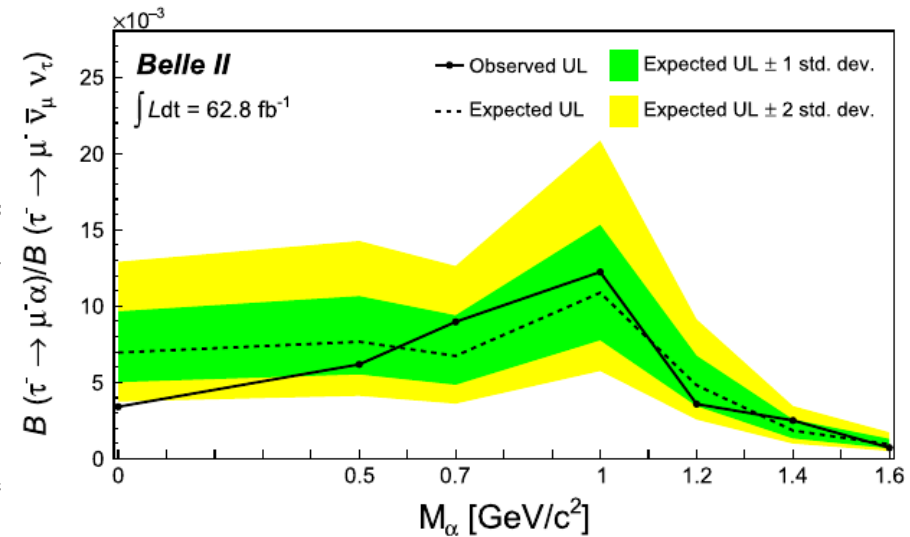
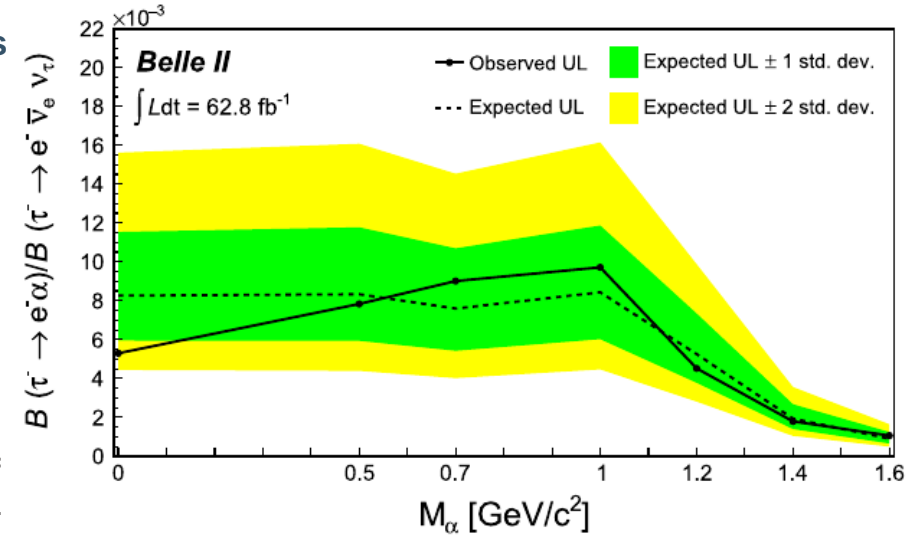
- Simulation derived templates fit for different α mass hypotheses
- Measure $\mathcal{B}_{\ell\alpha}/\mathcal{B}_{\ell\nu\nu} \equiv \mathcal{B}(\tau^- \rightarrow \ell^- \alpha) / \mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$ with $\tau \rightarrow l\nu\nu$ as normalization channel
 - Some systematics cancel \rightarrow higher precision
- 2 to 14 times more stringent than ARGUS
 - Still only early data set in use

$$\int \mathcal{L} dt = 62.8 \text{ fb}^{-1}$$

$$\sim 57.7 \text{ Million } ee \rightarrow \tau\tau$$

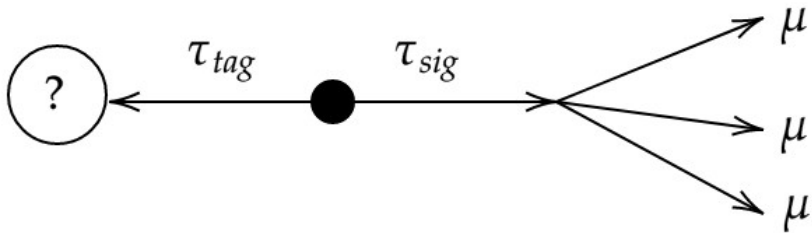
M_α [GeV/c ²]	$\mathcal{B}_{e\alpha}/\mathcal{B}_{e\nu\nu}$ ($\times 10^{-3}$)	UL at 95% C.L. ($\times 10^{-3}$)	UL at 90% C.L. ($\times 10^{-3}$)
0.0	-8.1 ± 3.9	5.3(0.94)	4.3(0.76)
0.5	-0.9 ± 4.3	7.8(1.40)	6.5(1.15)
0.7	1.7 ± 4.0	9.0(1.61)	7.6(1.36)
1.0	1.7 ± 4.2	9.7(1.73)	8.2(1.47)
1.2	-1.1 ± 2.6	4.5(0.80)	3.7(0.66)
1.4	-0.3 ± 1.0	1.8(0.32)	1.5(0.26)
1.6	0.2 ± 0.5	1.1(0.19)	0.9(0.16)

M_α [GeV/c ²]	$\mathcal{B}_{\mu\alpha}/\mathcal{B}_{\mu\nu\nu}$ ($\times 10^{-3}$)	UL at 95% C.L. ($\times 10^{-3}$)	UL at 90% C.L. ($\times 10^{-3}$)
0.0	-9.4 ± 3.7	3.4(0.59)	2.7(0.47)
0.5	-3.2 ± 3.9	6.2(1.07)	5.1(0.88)
0.7	2.7 ± 3.4	9.0(1.56)	7.8(1.35)
1.0	1.7 ± 5.4	12.2(2.13)	10.3(1.80)
1.2	-0.2 ± 2.4	3.6(0.62)	2.9(0.51)
1.4	0.9 ± 0.9	2.5(0.44)	2.2(0.38)
1.6	-0.3 ± 0.5	0.7(0.13)	0.6(0.10)



LFV : $\tau \rightarrow \mu \mu \mu - I$ (NEW)

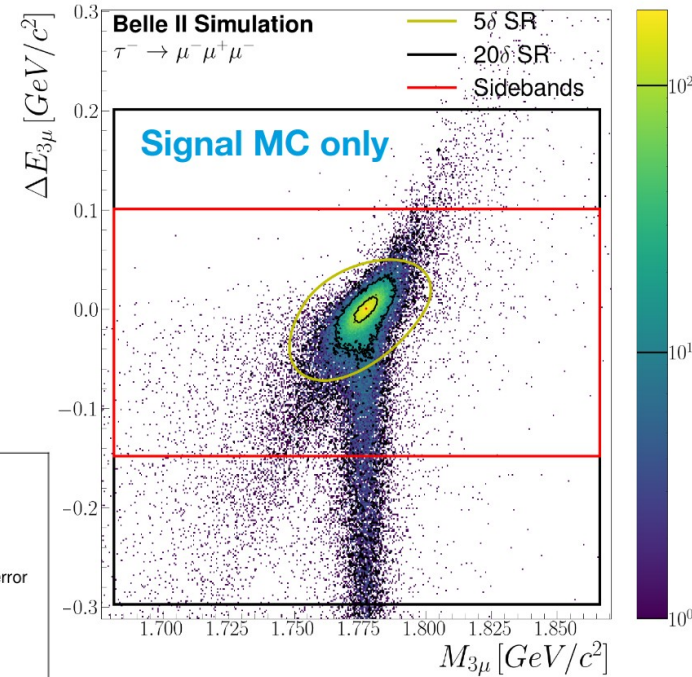
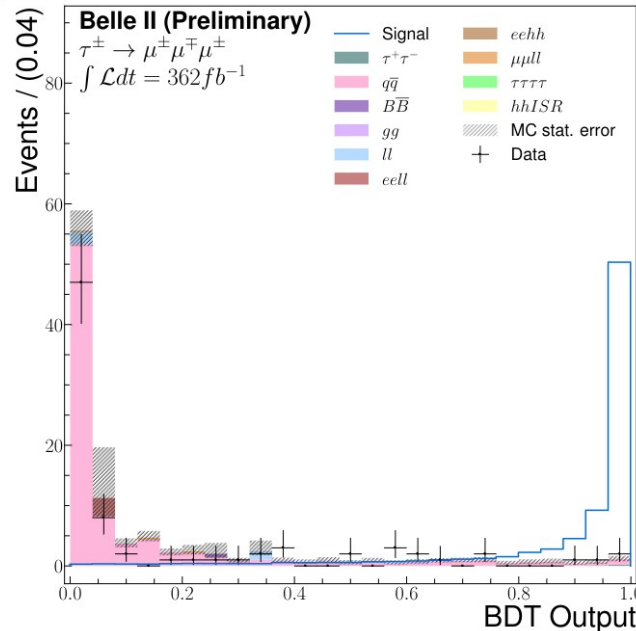
- Best previous upper limit from Belle 2.1×10^{-8} @90% CL with 782/fb
- Inclusive \rightarrow ~30% gain in signal efficiency, larger backgrounds
 - Selection and background rejection based on BDT



- Fully reconstructed tau signal
- No peaking background from SM processes

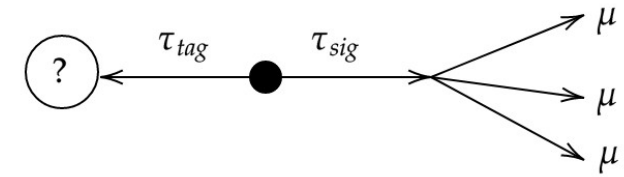
$$\int \mathcal{L} dt = 424 \text{ fb}^{-1}$$

$$\sim 391 \text{ Million } ee \rightarrow \tau\tau$$

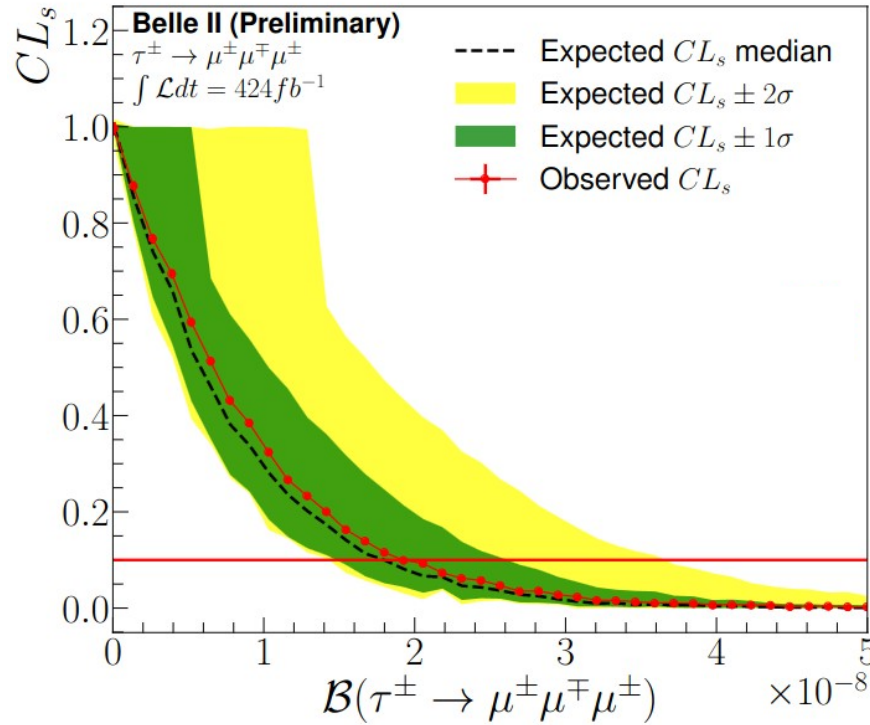
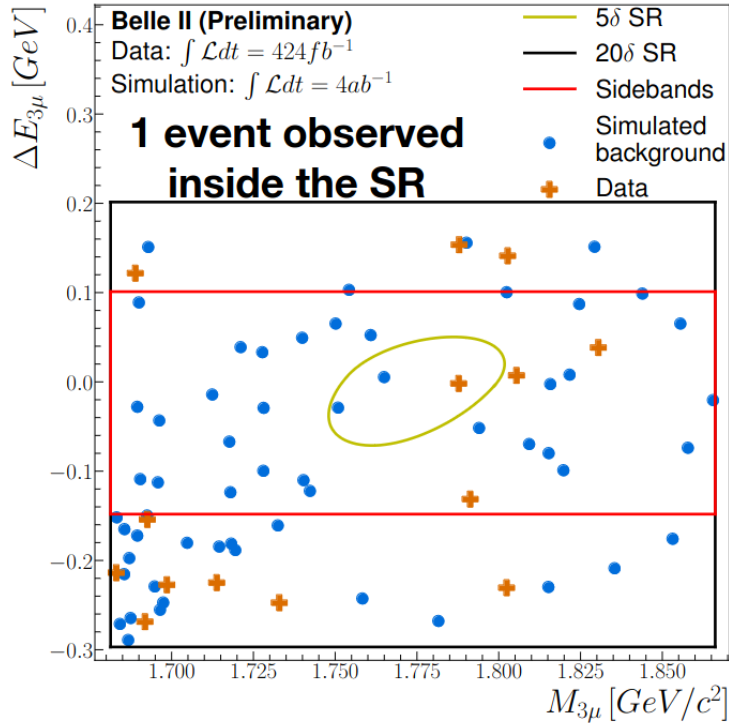


LFV : $\tau \rightarrow \mu \mu \mu$ - II (NEW)

- XGBoost BDT with 32 variables
 - Inputs from signal tau, event tag-side and event shape/kinematic variables
 - $\epsilon = 20.42\%$ ~ 3 times larger than Belle
 - Expected background events : $0.5^{+1.4}_{-0.5}$
- No significant excess \rightarrow calculate UL @90% CL with 424/fb using CLs method



Recent CMS result
UL @ 90%CL : 2.9×10^{-8}



UL @ 90% CL:
 1.9×10^{-8}
 \rightarrow most stringent!

Summary

- **B factories are a good environment for tau physics!**
- **Belle and Belle II will contribute to the understanding of tau lepton properties**
 - Searches for BSM physics
 - LFU
 - Precision measurements of SM parameters
- **Analysis with combined Belle & Belle II data sets are ongoing**
- **A lot more to come with more data**
 - Now 424/fb, next run starting in the coming weeks
- **Topics not covered:**
 - Michel Parameters : [PRL 131.021801 \(2023\)](#)
 - Tau lifetime → ongoing study
 - LFV → ongoing studies