



Istituto Nazionale di Fisica Nucleare  
SEZIONE DI TORINO



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# *Bottomonium at Belle (II)*

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*Excited QCD 2024*

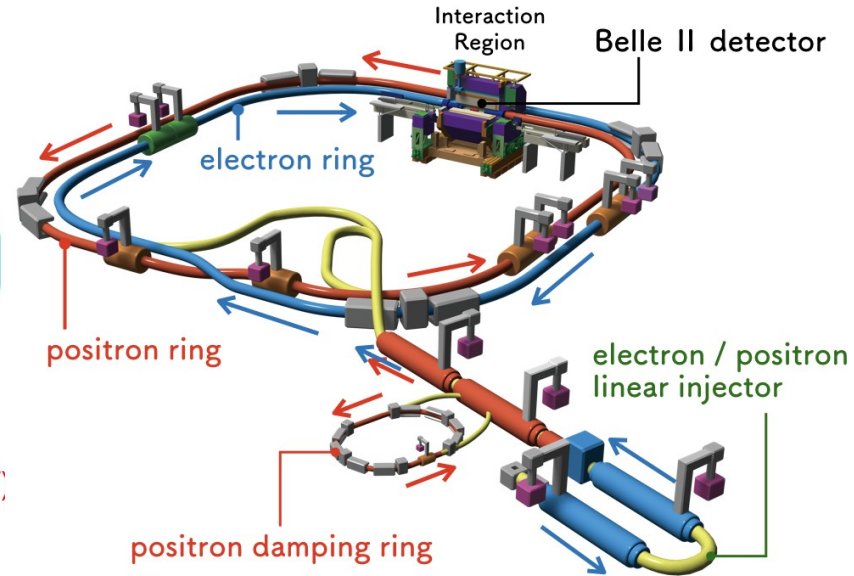
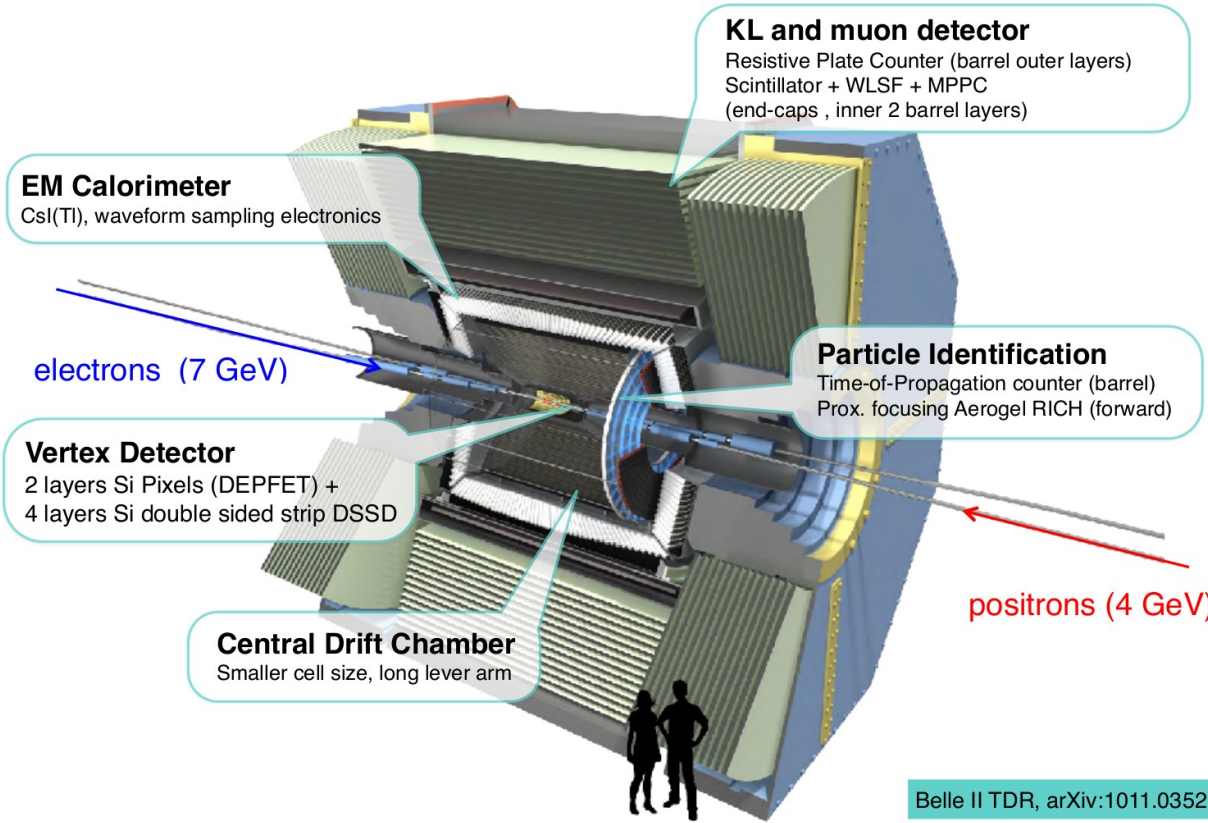
*Benasque, January 19<sup>th</sup> 2024*

Umberto Tamponi

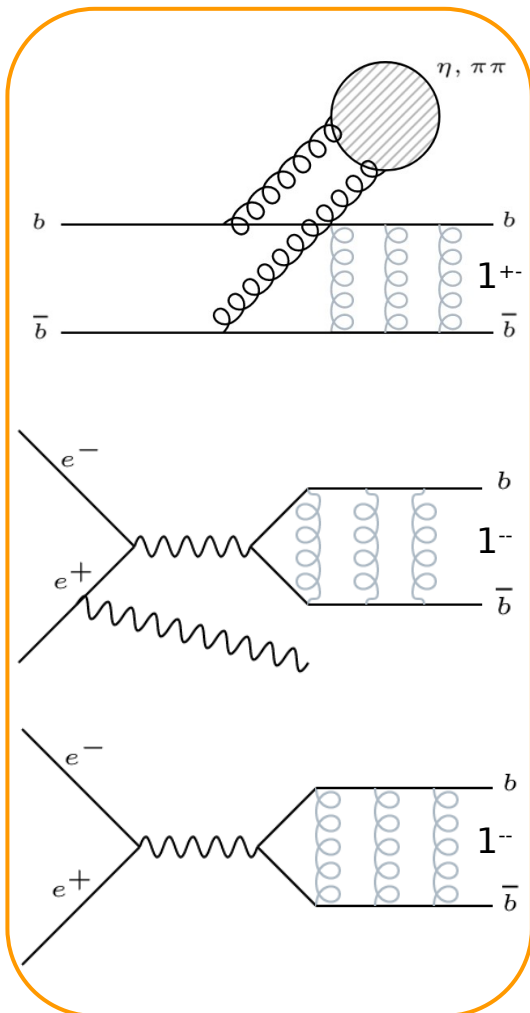
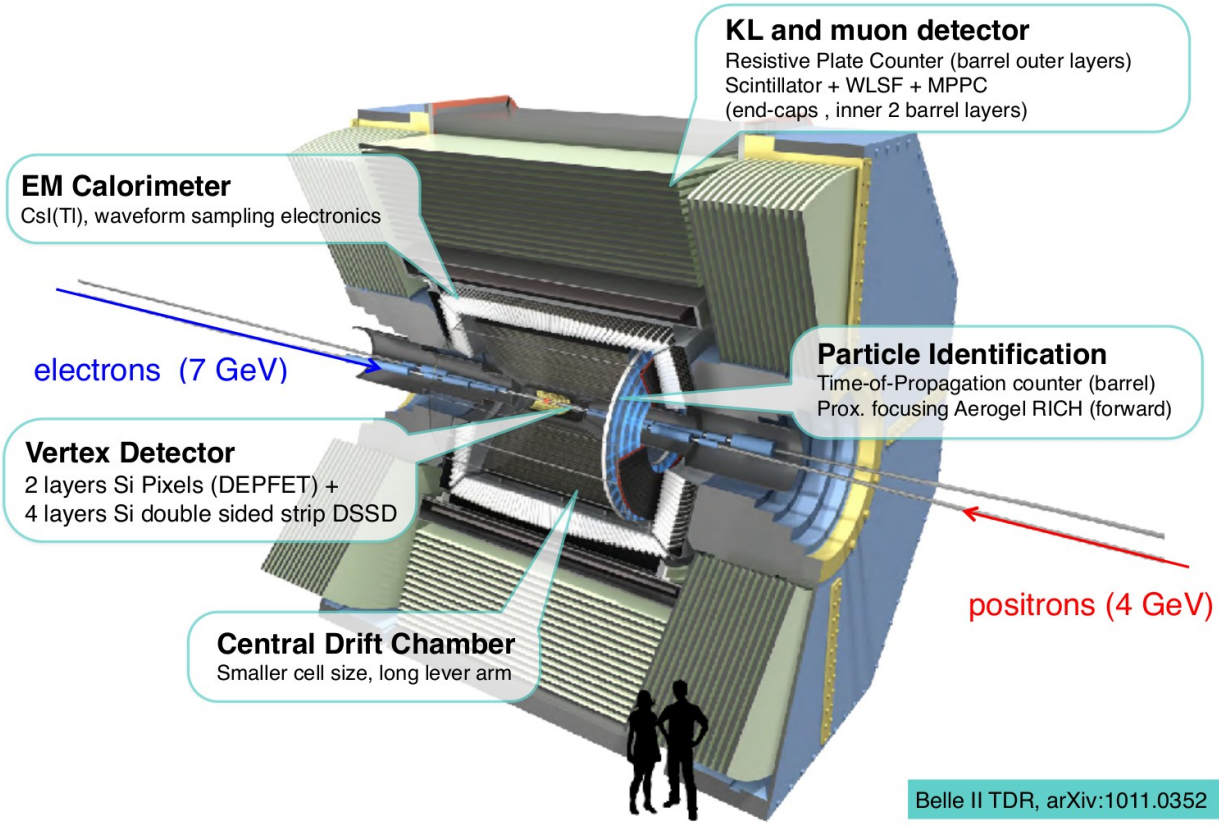
*tamponi@to.infn.it*

*INFN – Sezione di Torino*

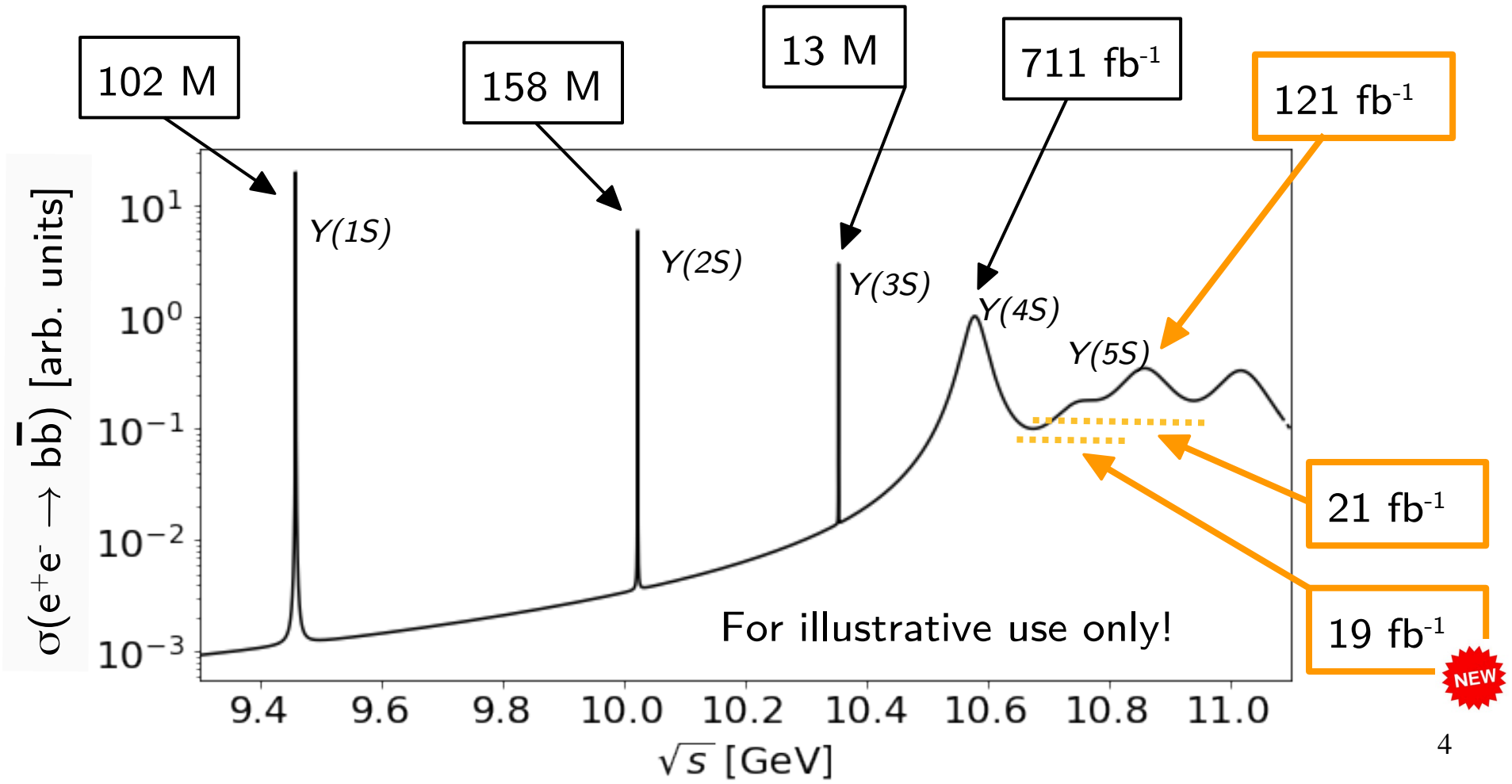
# The Belle II detector



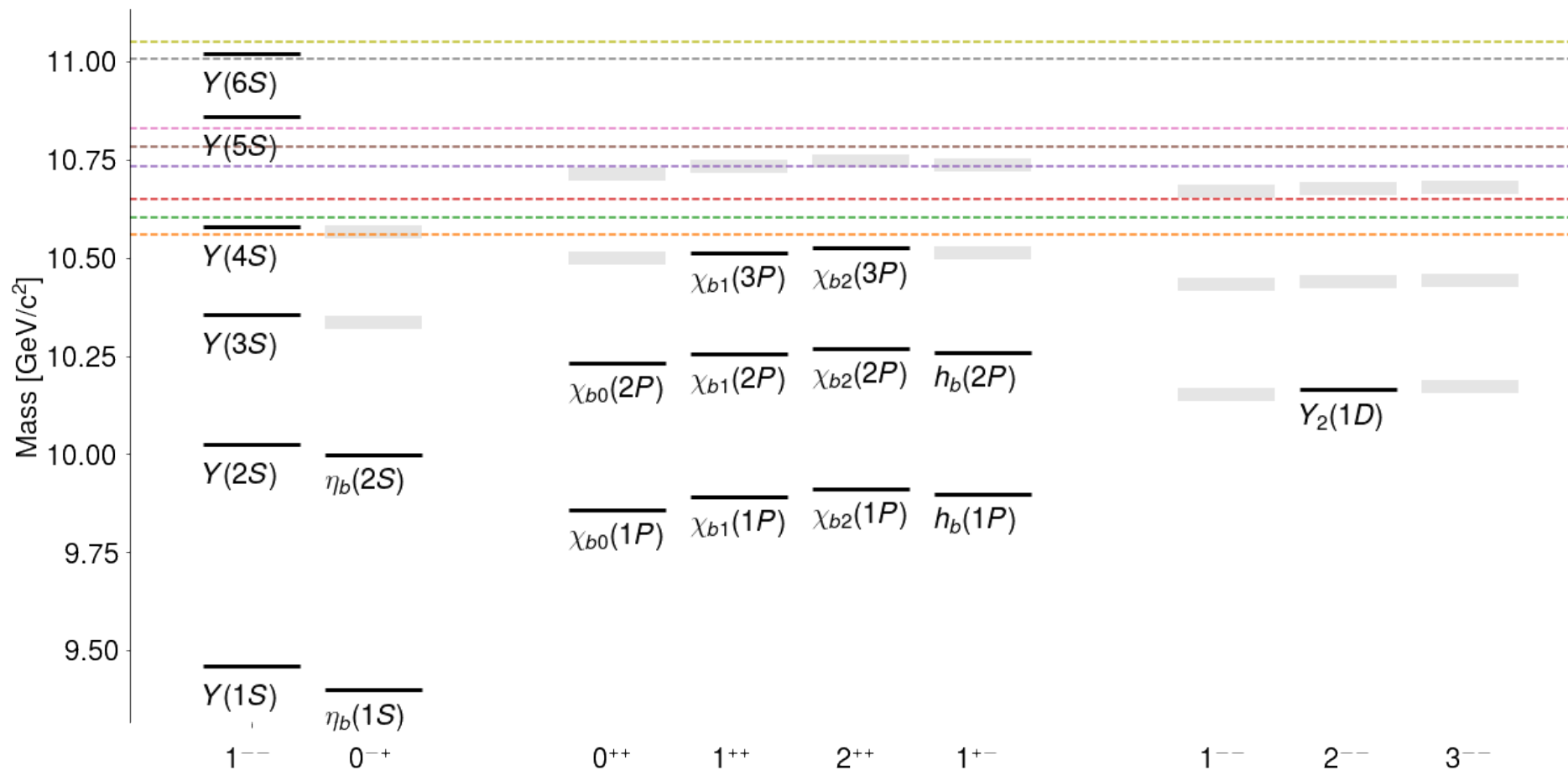
# Belle II and Bottomonia



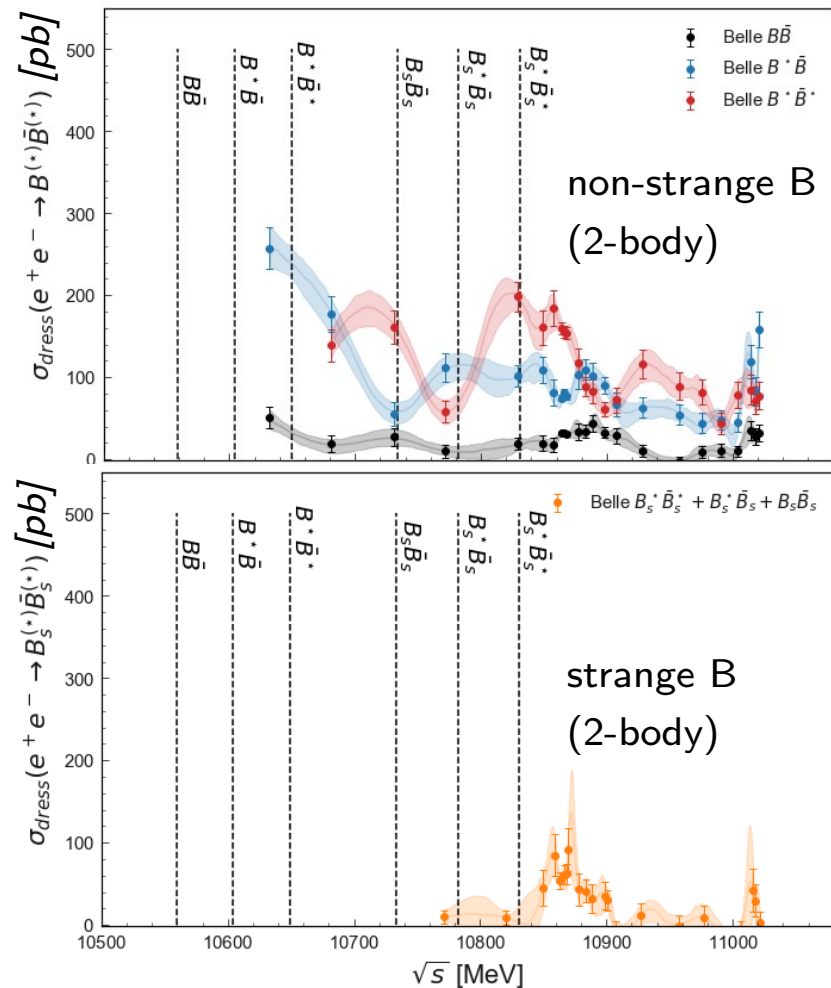
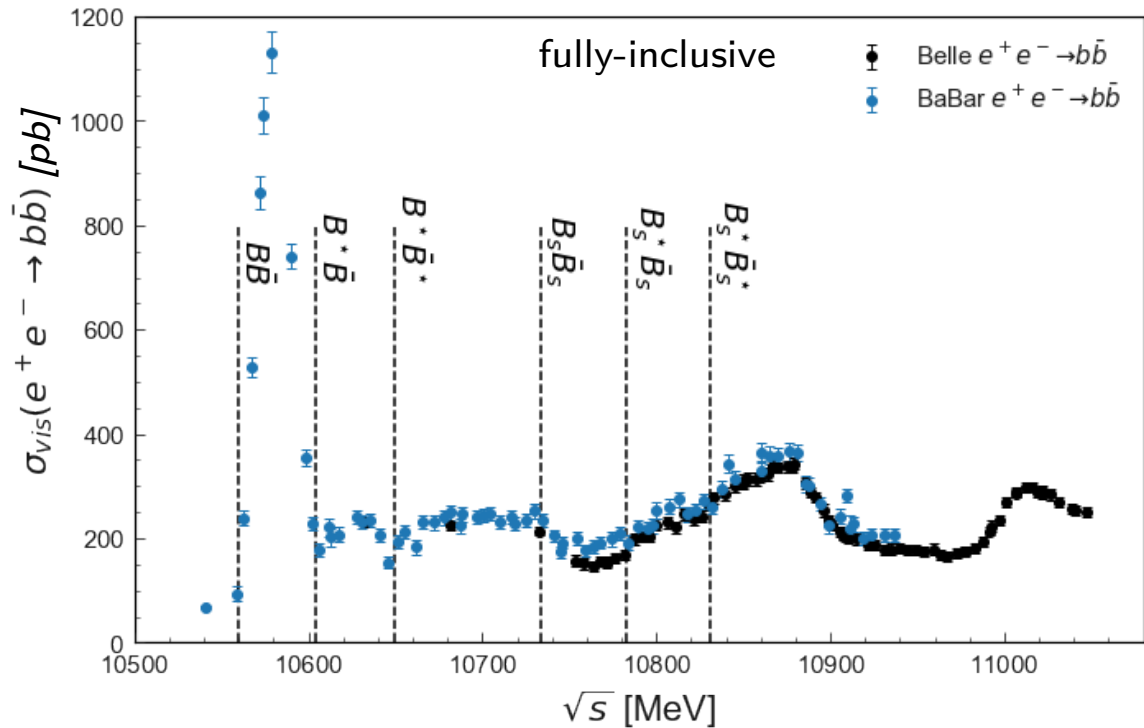
# Belle (II) relevant datasets



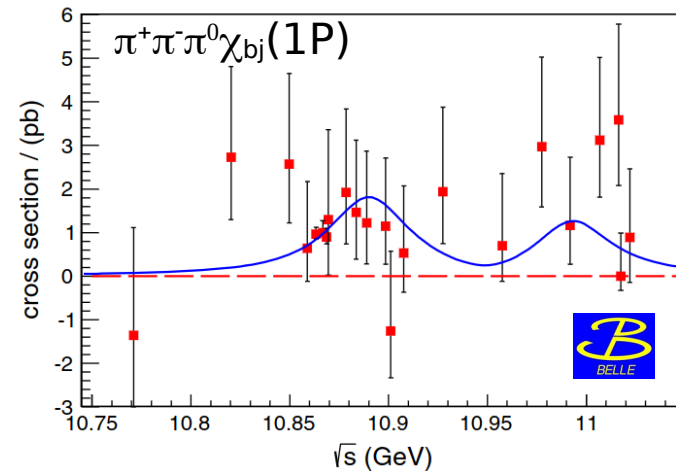
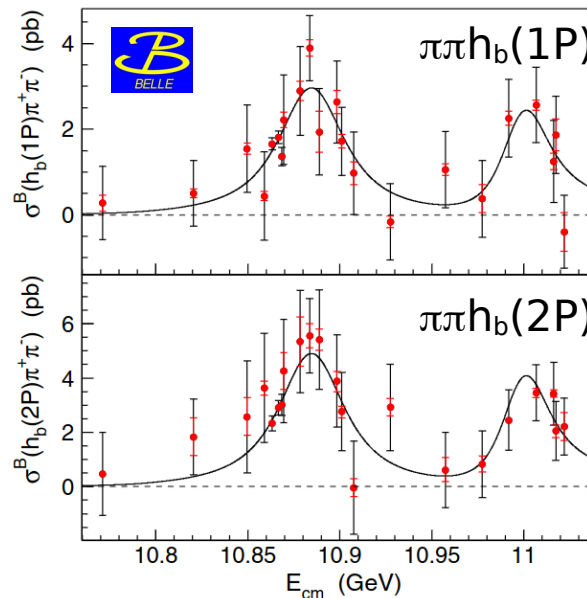
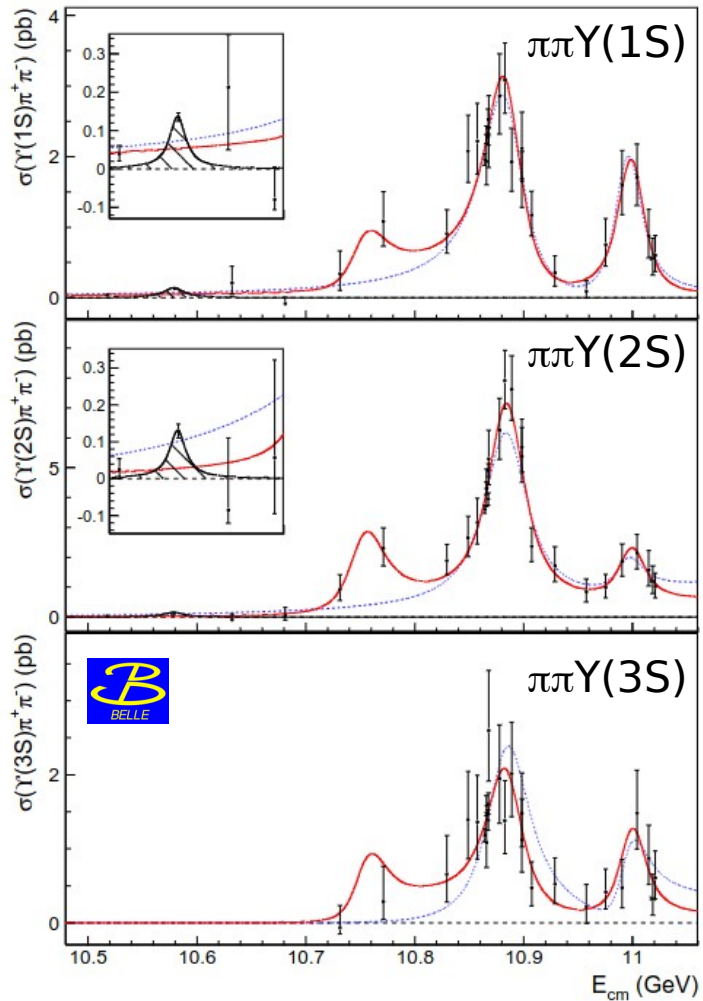
# The threshold region



# The threshold region: open flavour



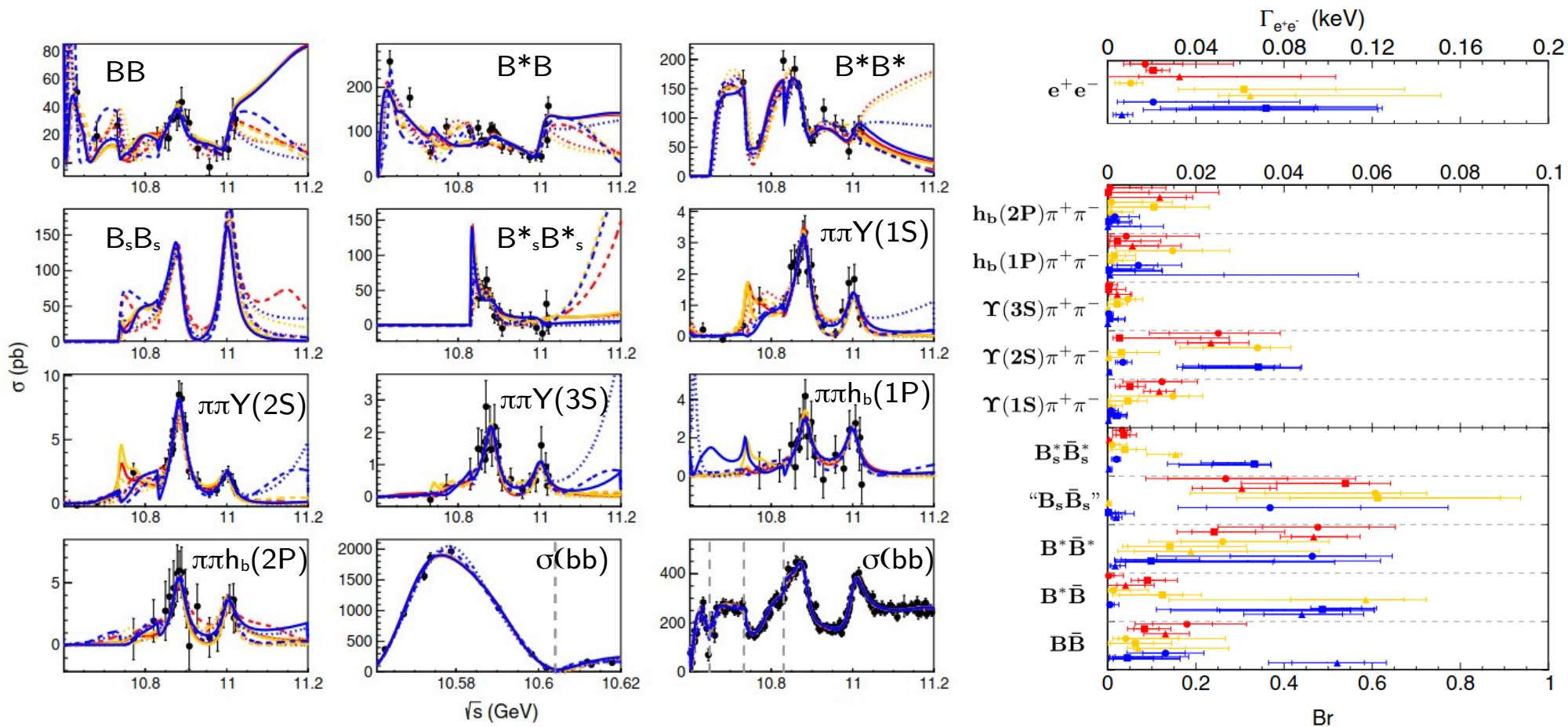
# The threshold region: hidden flavour



## New structure in $\pi\pi\Upsilon(nS)$ , the $\Upsilon(10750)$

	$\Upsilon(10860)$	$\Upsilon(11020)$	New structure
M (MeV/c <sup>2</sup> )	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0+1.0}_{-4.5-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
$\Gamma$ (MeV)	$36.6^{+4.5+0.5}_{-3.9-1.1}$	$23.8^{+8.0+0.7}_{-6.8-1.8}$	$35.5^{+17.6+3.9}_{-11.3-3.3}$

[Hüsken et al. PRD 106 094013 (2022)]





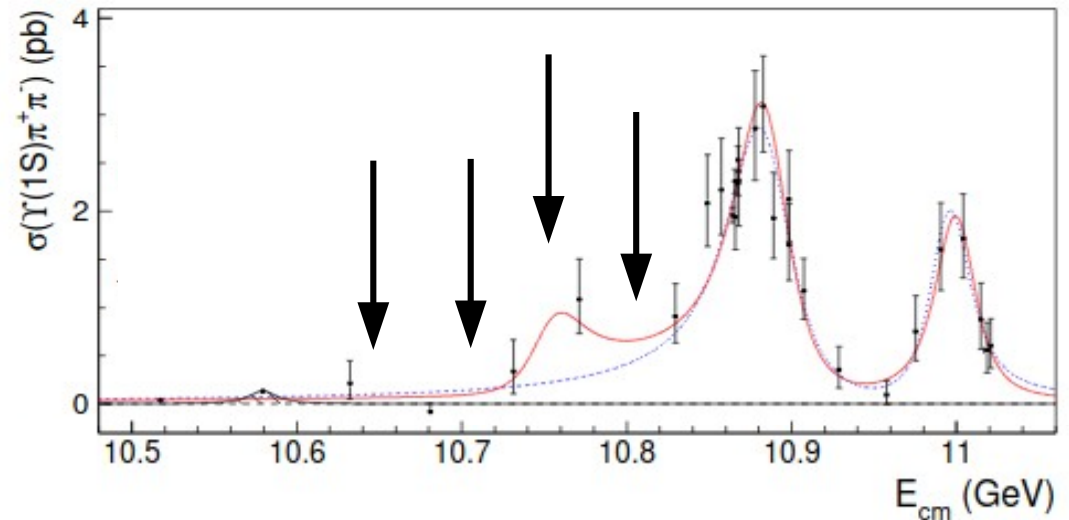
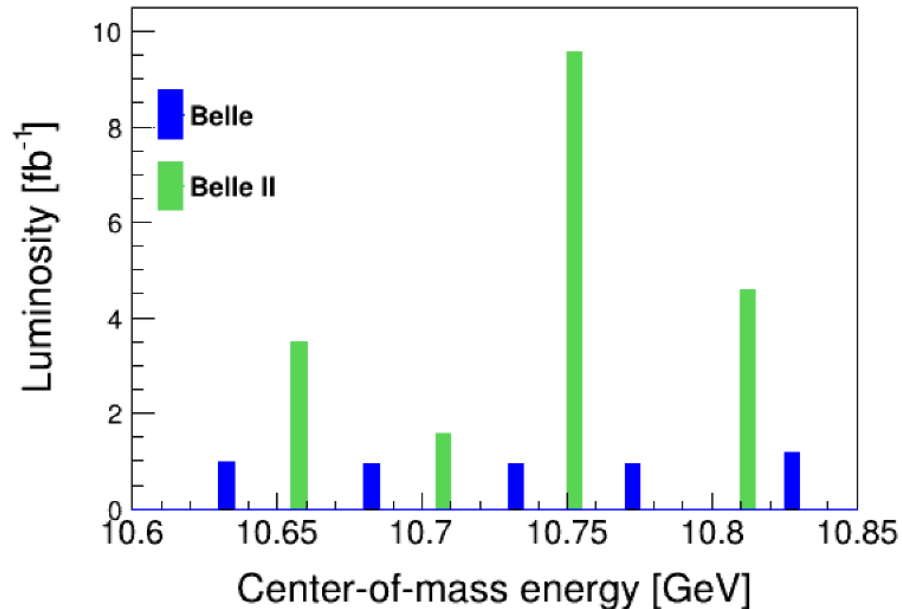
# The new Belle II dataset

In fall 2021 Belle II took data above the  $Y(4S)$

→ Goal: study the golden channels to characterize the  $Y(10750)$

→ Special data taking, lots of discussions and preparation

→ If you have an idea and you like it, don't give up ;)



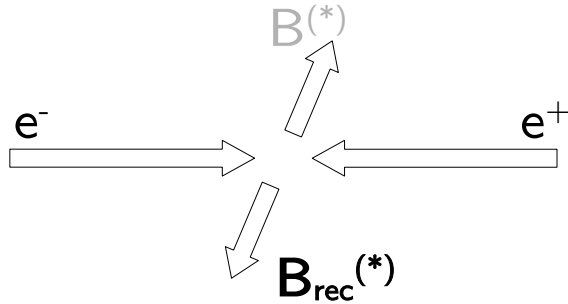
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*News: open flavour cross sections*

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# BB decomposition updated

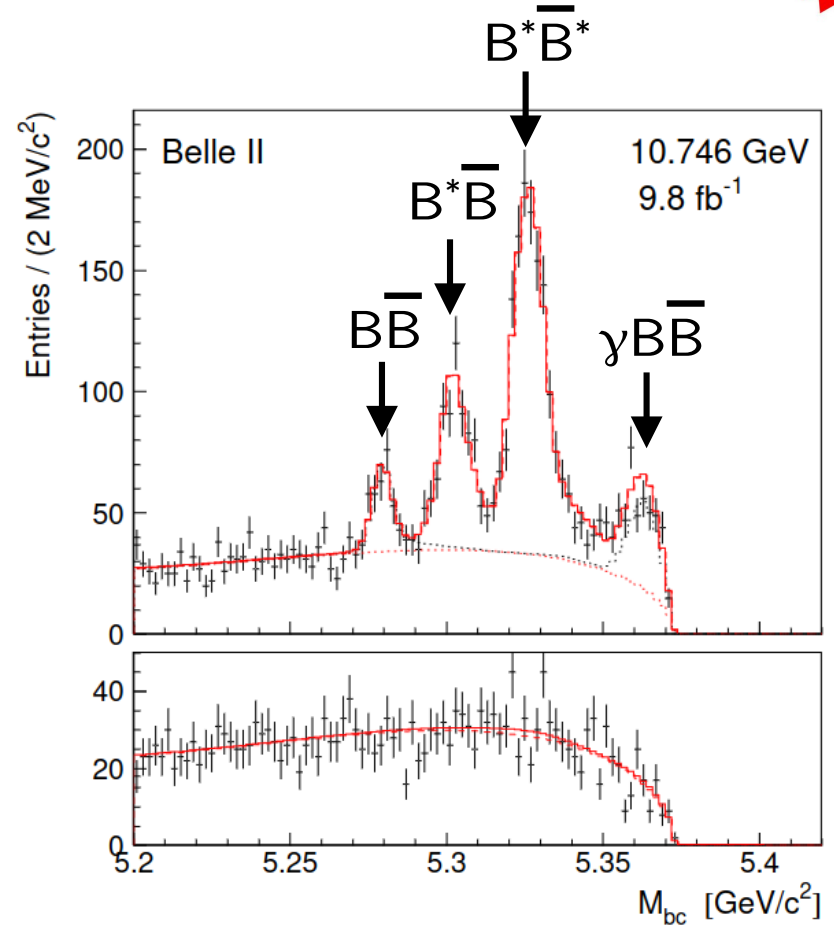
[Belle II Preliminary]



Semi-inclusive reconstruction:

- Reconstruct one  $B^{(*)}$  in 16 modes with  $D_{(s)}^{(*)}$  or  $J/\psi$
- Ignore  $\gamma$  from  $B^*$  to  $B$
- Separate processes by momentum ( $M_{bc}$ )

$$M_{bc} = \sqrt{(E_{cm}/2)^2 - p_B^2}$$



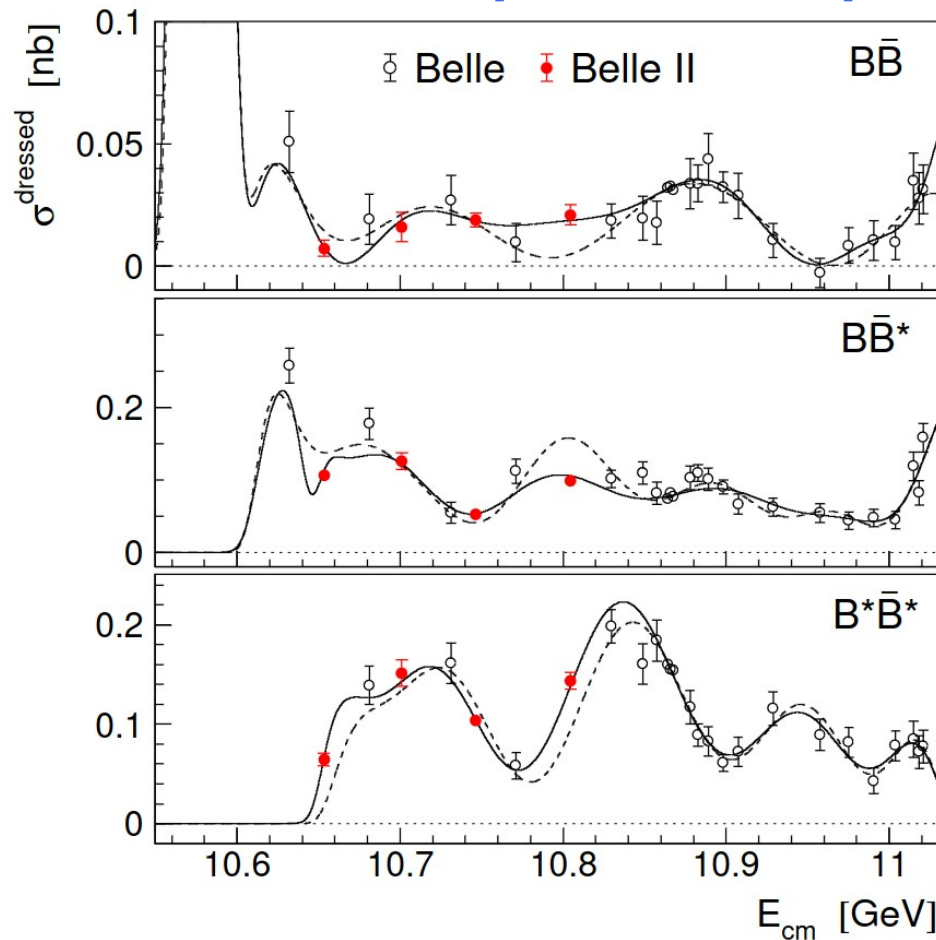
# BB decomposition updated

[Belle II Preliminary]



Prominent features:

- Sharp rise in  $B^*B^*$ 
  - first point only  $\sim 2$  MeV above  $B^{0*}B^{0*}$  threshold
  - Indication of bound state?
- Dip in  $B^*B$  at the  $B^*B^*$  threshold



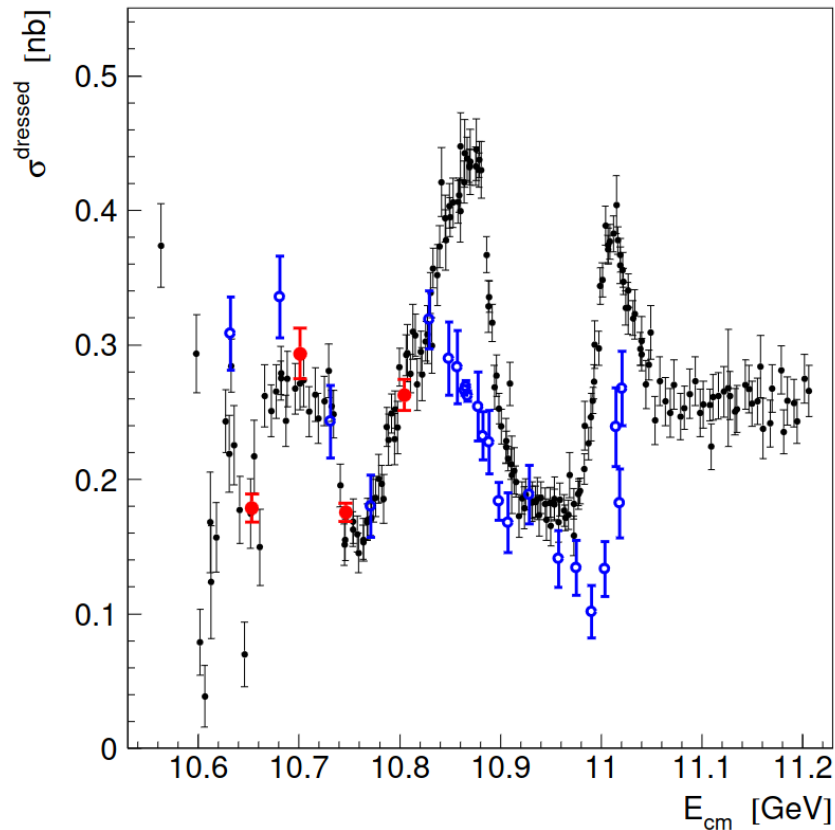
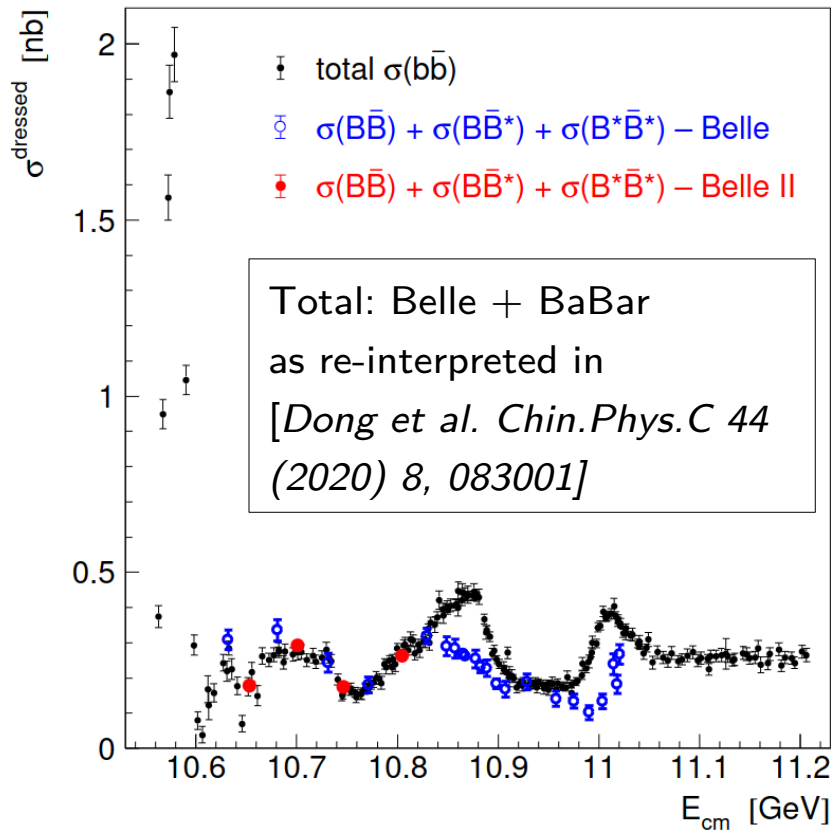
# BB decomposition updated

[Belle II Preliminary]



Do we saturate the total cross section?

→ not yet!



$$e^+e^- \rightarrow B^{(*)}B^{(*)}+X \text{ and } B_s^{(*)}B_s^{(*)}+X$$

[JHEP 08 2023, 131 (2023)]



Measure the fully-inclusive  $e^+e^- \rightarrow B_{(s)}^{(*)}B_{(s)}^{(*)}+X$

→ Use  $D^0$  as proxy for a  $B^0$

→ Use  $D_s^-$  as proxy for  $B_s^0$

→ Use D momentum to identify the quark-level process

$$e^+e^- \rightarrow b\bar{b} \rightarrow D_{(s)} + X$$

$$e^+e^- \rightarrow u\bar{u}, d\bar{d}, s\bar{s}, c\bar{c} \rightarrow D_{(s)} + X$$

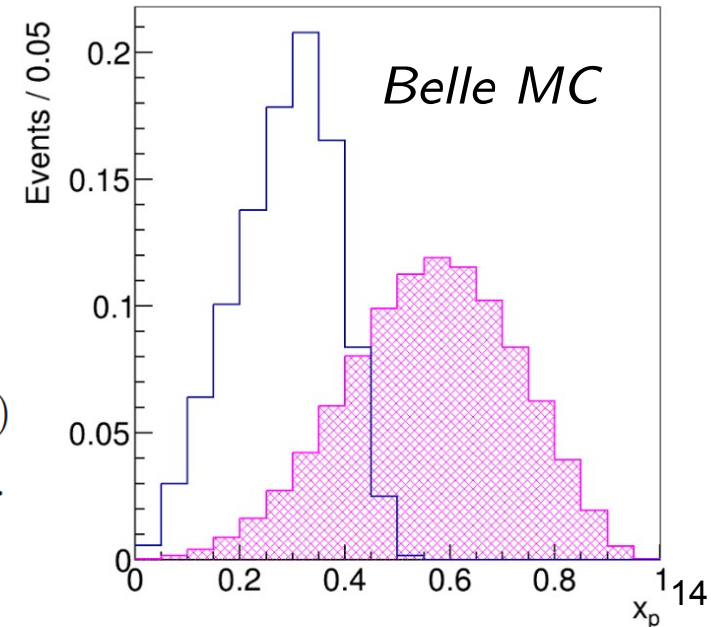
→ Solve the equation system:

$$\begin{aligned} \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^\pm X) &= 2\sigma(e^+e^- \rightarrow B_s^0\bar{B}_s^0 X)\mathcal{B}(B_s^0 \rightarrow D_s^\pm X) \\ &\quad + 2\sigma(e^+e^- \rightarrow B\bar{B} X)\mathcal{B}(B \rightarrow D_s^\pm X), \end{aligned}$$

$$\begin{aligned} \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0/\bar{D}^0 X) &= 2\sigma(e^+e^- \rightarrow B_s^0\bar{B}_s^0 X)\mathcal{B}(B_s^0 \rightarrow D^0/\bar{D}^0 X) \\ &\quad + 2\sigma(e^+e^- \rightarrow B\bar{B} X)\mathcal{B}(B \rightarrow D^0/\bar{D}^0 X). \end{aligned}$$

$$BF[B^0 \rightarrow D^0 + X] \sim 67\%$$

$$BF[B_s^0 \rightarrow D_s^- + X] \sim 60\%$$



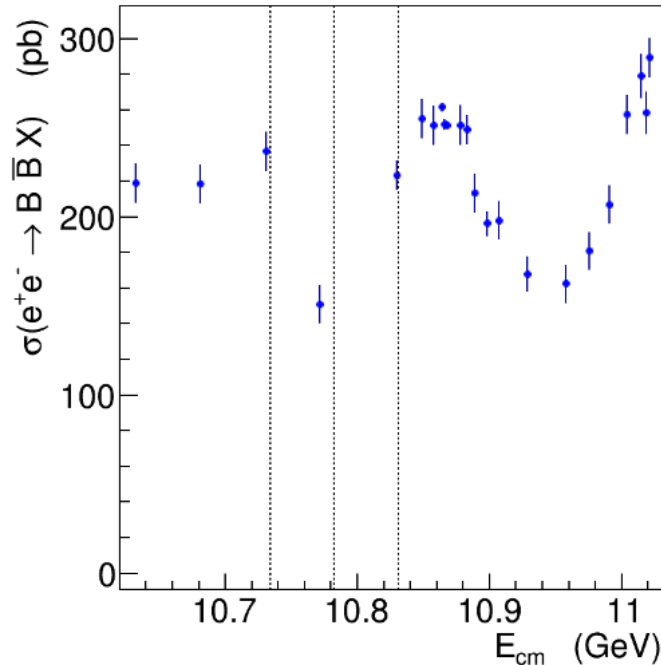
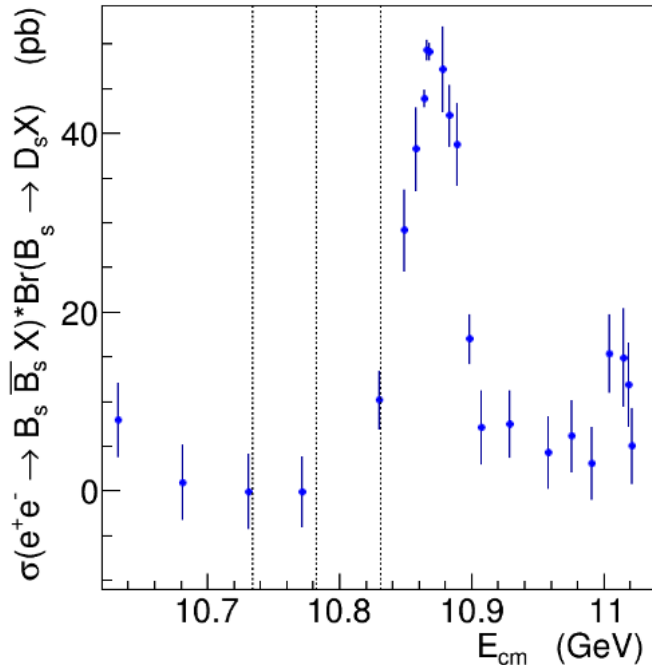


$$e^+e^- \rightarrow B^{(*)}B^{(*)}+X \text{ and } B_{(s)}^{(*)}B_{(s)}^{(*)}+X$$

Measure the fully-inclusive  $e^+e^- \rightarrow B_{(s)}^{(*)}B_{(s)}^{(*)}+X$

→ Use  $D^0$  as proxy for a  $B^0$

→ Use  $D_s^-$  as proxy for  $B_s^0$



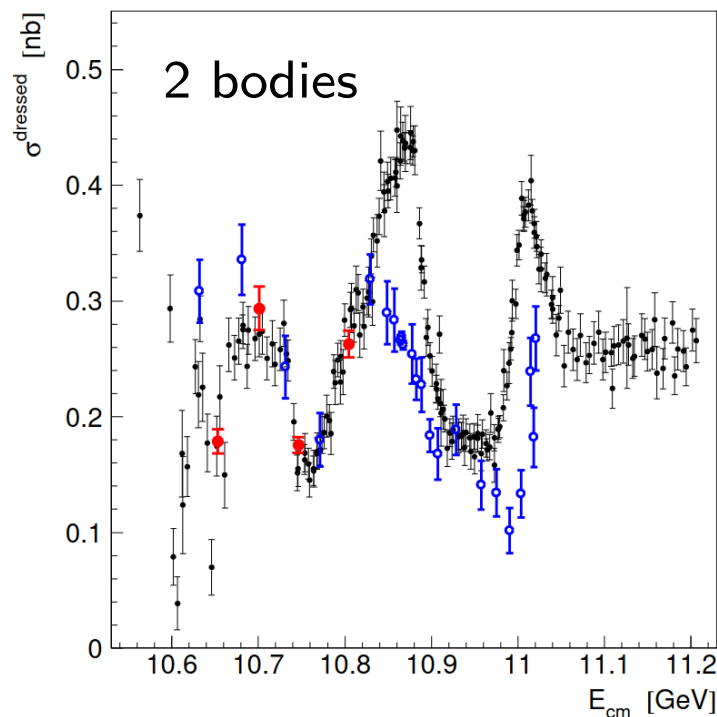
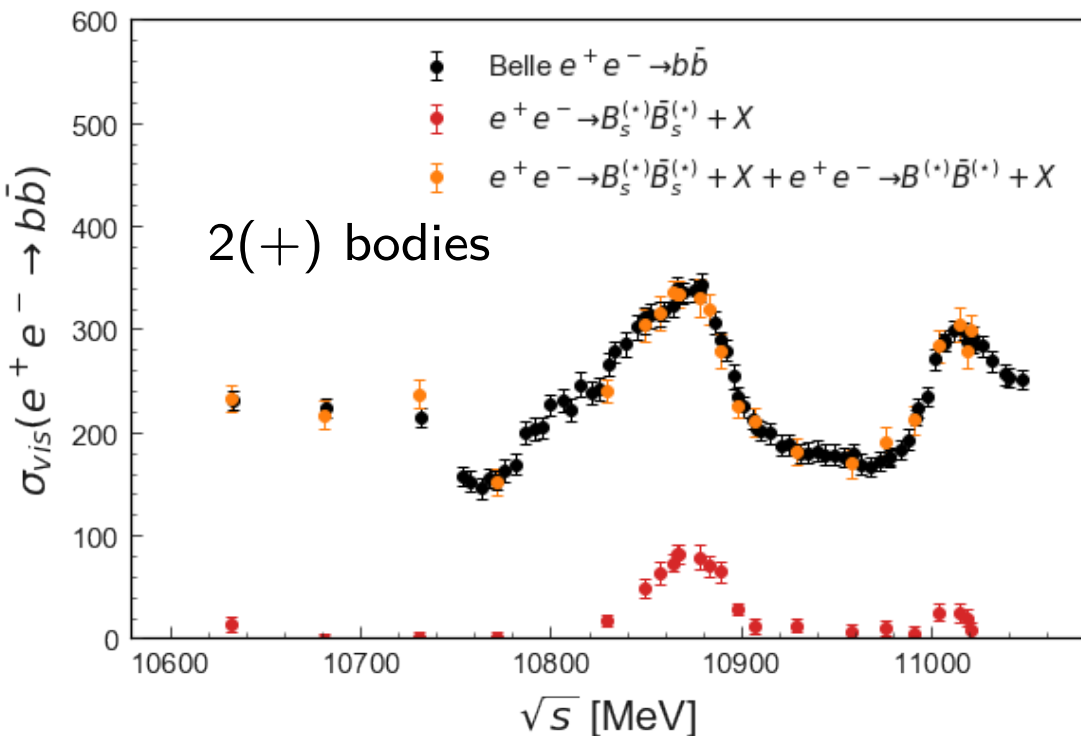


$$e^+e^- \rightarrow B^{(*)}B^{(*)} + X \text{ and } B_s^{(*)}B_s^{(*)} + X$$

Measure the fully-inclusive  $e^+e^- \rightarrow B_{(s)}^{(*)}B_{(s)}^{(*)} + X$

→ Use  $D^0$  as proxy for a  $B^0$

→ Use  $D_s^-$  as proxy for  $B_s^0$





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*News: hidden flavour cross sections*

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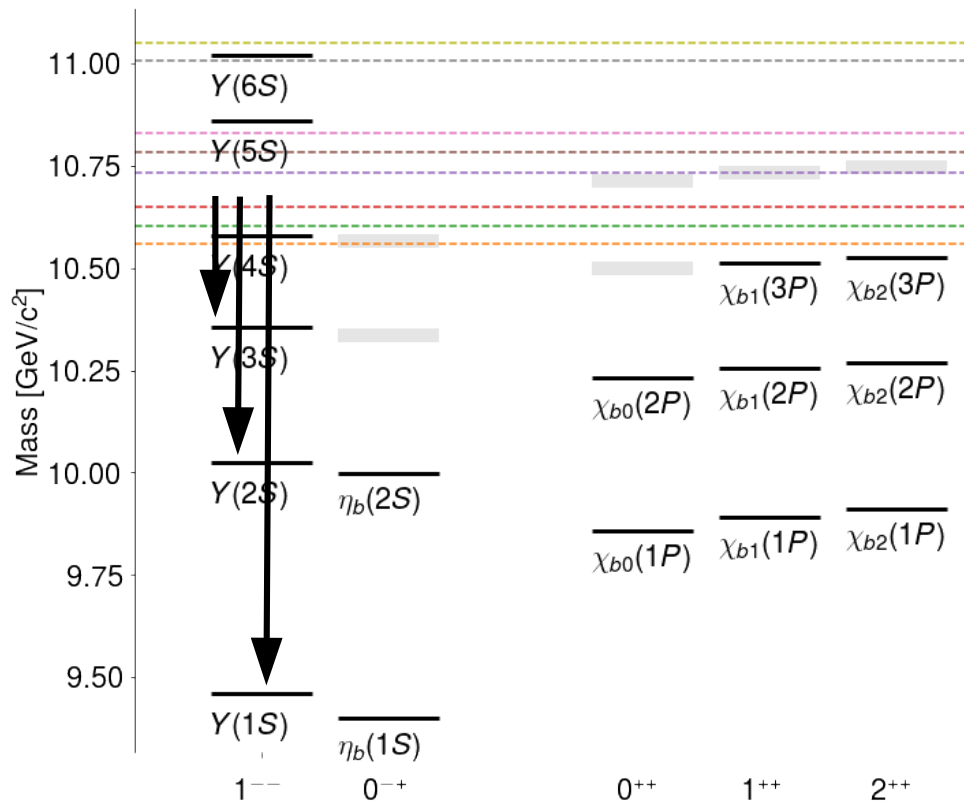
$$e^+e^- \rightarrow Y(nS) \pi^+\pi^-$$

Discovery mode of the  $Y(10750)$

→ Confirm its existence

→ Measure the di-pion spectrum

→ look for  $Z_b$  contributions



$$e^+e^- \rightarrow Y(nS) \pi^+\pi^-$$

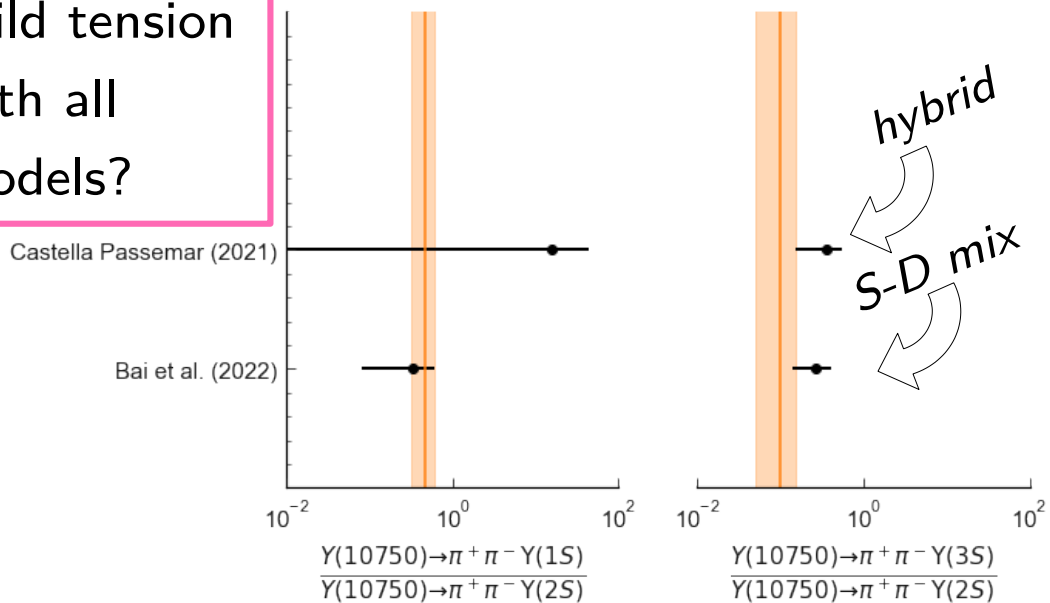
Discovery mode of the  $Y(10750)$

→ Confirm its existence

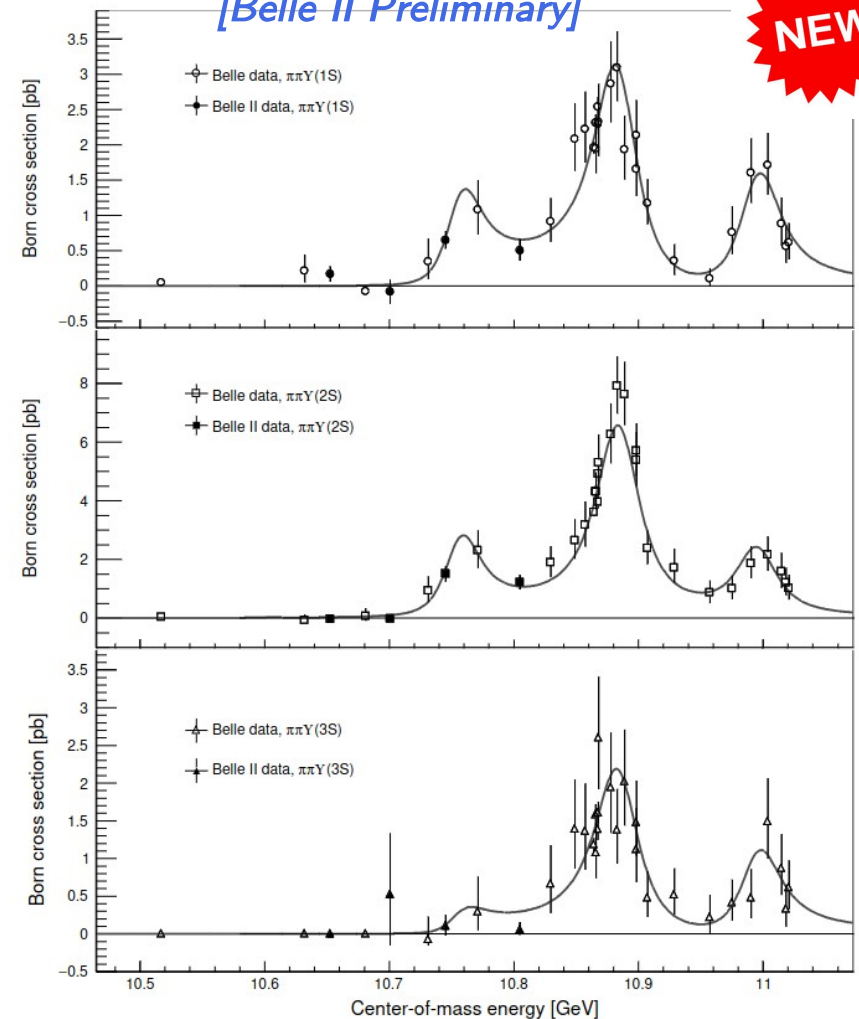
→  $>8 \sigma$  combined significance (B+BII)

	$\mathcal{R}_{\sigma(1S/2S)}^{Y(10753)}$	$\mathcal{R}_{\sigma(3S/2S)}^{Y(10753)}$	$\mathcal{R}_{\sigma(1S/2S)}^{Y(5S)}$	$\mathcal{R}_{\sigma(3S/2S)}^{Y(5S)}$	$\mathcal{R}_{\sigma(1S/2S)}^{Y(6S)}$	$\mathcal{R}_{\sigma(3S/2S)}^{Y(6S)}$
Ratio	$0.46^{+0.15}_{-0.12}$	$0.10^{+0.05}_{-0.04}$	$0.45^{+0.04}_{-0.04}$	$0.32^{+0.04}_{-0.03}$	$0.64^{+0.23}_{-0.13}$	$0.41^{+0.16}_{-0.12}$

Mild tension with all models?



[Belle II Preliminary]



$$e^+e^- \rightarrow Y(nS) \pi^+\pi^-$$

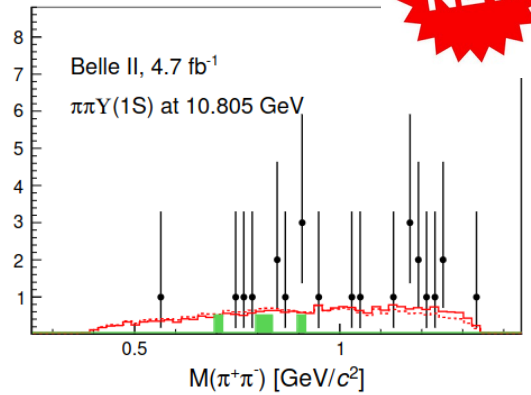
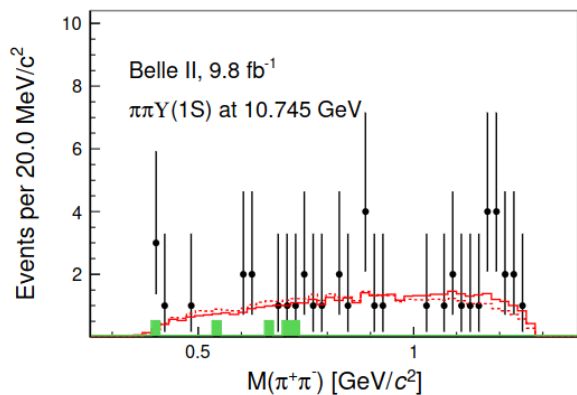
Discovery mode of the  $Y(10750)$

→ Confirm its existence

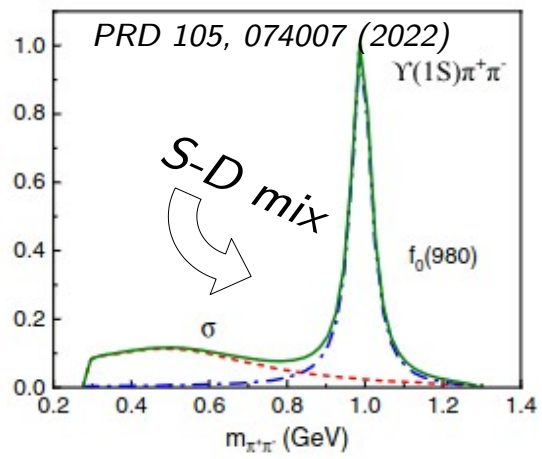
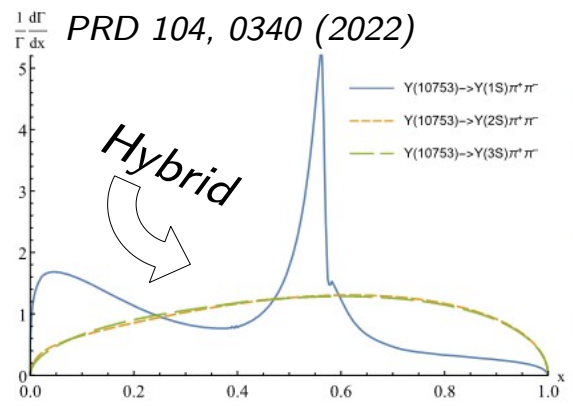
→ Measure the di-pion spectrum

→ **No sign of  $f_0$  in  $\pi\pi Y(1S)$**

[Belle II Preliminary]



Disagreement with all available predictions



$$e^+e^- \rightarrow Y(nS) \pi^+\pi^-$$

Discovery mode of the  $Y(10750)$

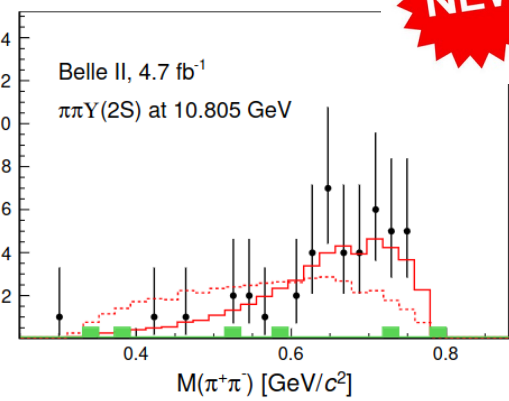
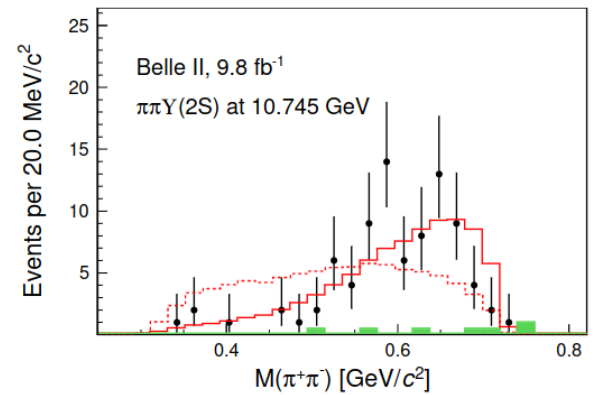
→ Confirm its existence

→ Measure the di-pion spectrum

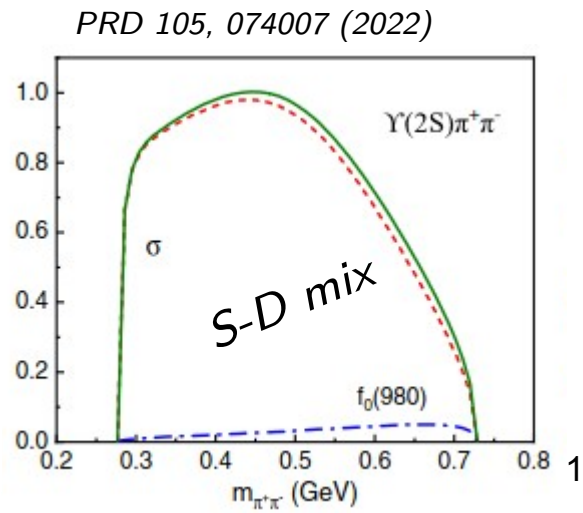
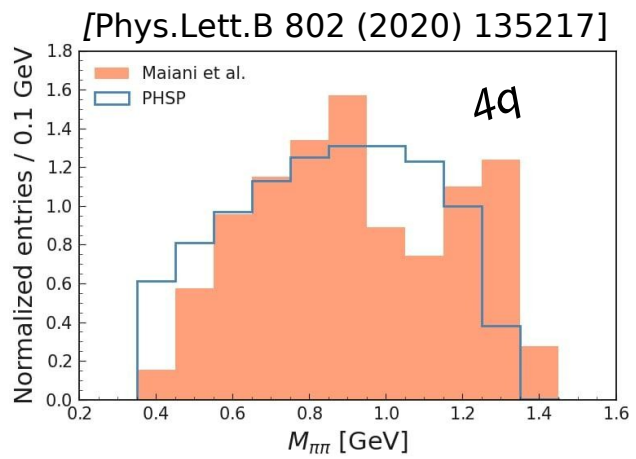
→ No sign of  $f_0$  in  $\pi\pi Y(1S)$

→  $M(\pi\pi)$  similar to what's seen  
 $Y(2S) \rightarrow \pi\pi Y(1S)$

[Belle II Preliminary]



Disagreement with S-D model. Compatible with  $4q$ ?



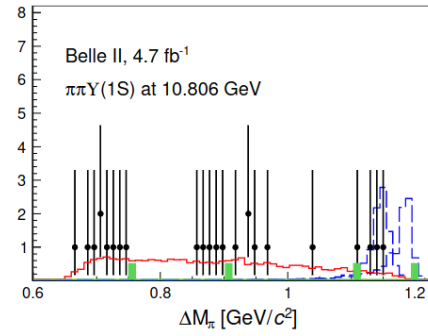
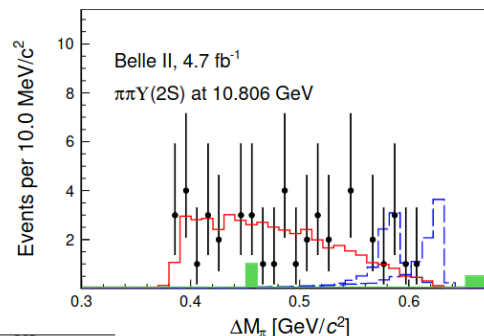
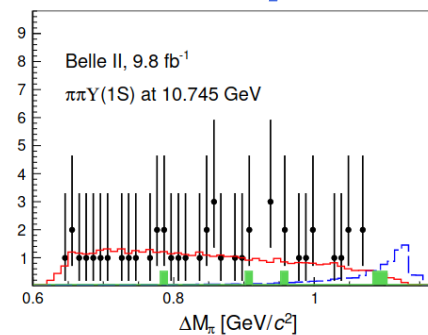
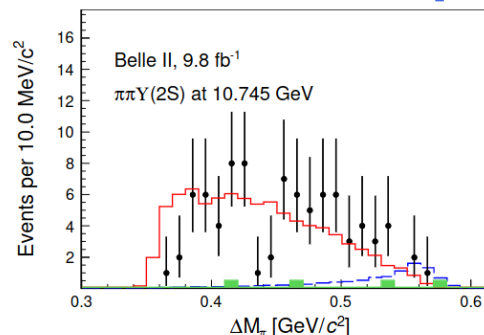


[Belle II Preliminary]

$$e^+e^- \rightarrow Y(nS) \pi^+\pi^-$$

Discovery mode of the  $Y(10750)$

- Confirm its existence
- Measure the di-pion spectrum
- look for  $Z_b$  contributions
- **No indication of  $Z_b$**



Mode	$N_{Z_{b1}}$	$N_{Z_{b1}}^{UL}$	$\sigma_{Z_{b1}}$ (pb)	$\sigma_{Z_{b1}}^{UL}$ (pb)	$N_{Z_{b2}}^{UL}$	$N_{Z_{b2}}$	$\sigma_{Z_{b2}}$ (pb)	$\sigma_{Z_{b2}}^{UL}$ (pb)
10.745 GeV								
$\pi\mathcal{T}(1S)$	$0.0_{-0.0}^{+1.6}$	< 4.9	$0.00_{-0.00}^{+0.04}$	< 0.13	—	—	—	—
$\pi\mathcal{T}(2S)$	$5.8_{-4.6}^{+5.9}$	< 13.8	$0.06_{-0.05}^{+0.06}$	< 0.14	—	—	—	—
10.805 GeV								
$\pi\mathcal{T}(1S)$	$2.5_{-1.6}^{+2.4}$	< 5.2	$0.21_{-0.13}^{+0.20}$	< 0.43	$0.0_{-0.0}^{+0.7}$	< 5.8	$0.00_{-0.00}^{+0.03}$	< 0.28
$\pi\mathcal{T}(2S)$	$5.2_{-3.0}^{+3.8}$	< 12.3	$0.15_{-0.09}^{+0.11}$	< 0.35	$0.0_{-0.0}^{+0.8}$	< 6.0	$0.00_{-0.00}^{+0.04}$	< 0.30

$$e^+e^- \rightarrow \chi_{b1,2}(1P) \omega$$

$Y(10750) \rightarrow \omega \chi_b$  in the conventional quarkonium model (S-D mixing state)

[Y.S. Li, et al., PRD 104, 034036 (2021)]

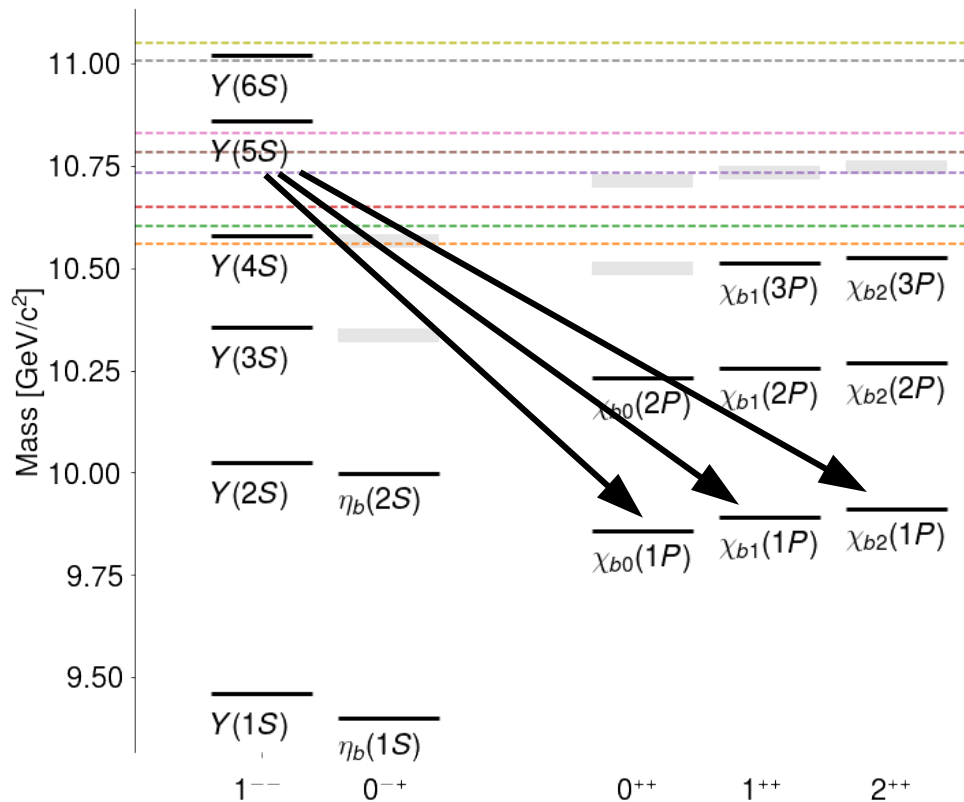
$$\mathcal{B}[Y(10753) \rightarrow \chi_{b0}\omega] = (0.73-6.94) \times 10^{-3},$$

$$\mathcal{B}[Y(10753) \rightarrow \chi_{b1}\omega] = (0.25-2.16) \times 10^{-3},$$

$$\mathcal{B}[Y(10753) \rightarrow \chi_{b2}\omega] = (1.08-11.5) \times 10^{-3}.$$

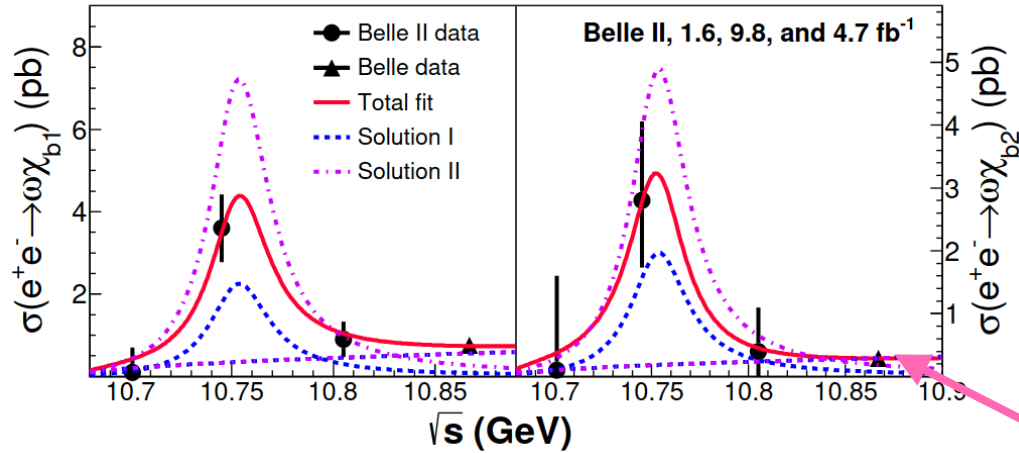
$$R_{12} = \frac{\mathcal{B}[Y(10753) \rightarrow \chi_{b1}\omega]}{\mathcal{B}[Y(10753) \rightarrow \chi_{b2}\omega]} = (0.18-0.22)$$

$$R_{02} = \frac{\mathcal{B}[Y(10753) \rightarrow \chi_{b0}\omega]}{\mathcal{B}[Y(10753) \rightarrow \chi_{b2}\omega]} = (0.55-0.63)$$



$$e^+e^- \rightarrow \chi_{b1,2}(1P) \omega$$

[PRL 130, 091902 (2023)]



$$\sigma[ee \rightarrow \omega \chi_{b0}(1P)] < 11.3 \text{ pb} @ 10.750 \text{ GeV}$$

Two solutions (constr. or destr. interference):

$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega \chi_{b1}(1P)] = \begin{pmatrix} 0.63 \pm 0.39 \pm 0.20 \\ 2.01 \pm 0.38 \pm 0.76 \end{pmatrix} eV$$

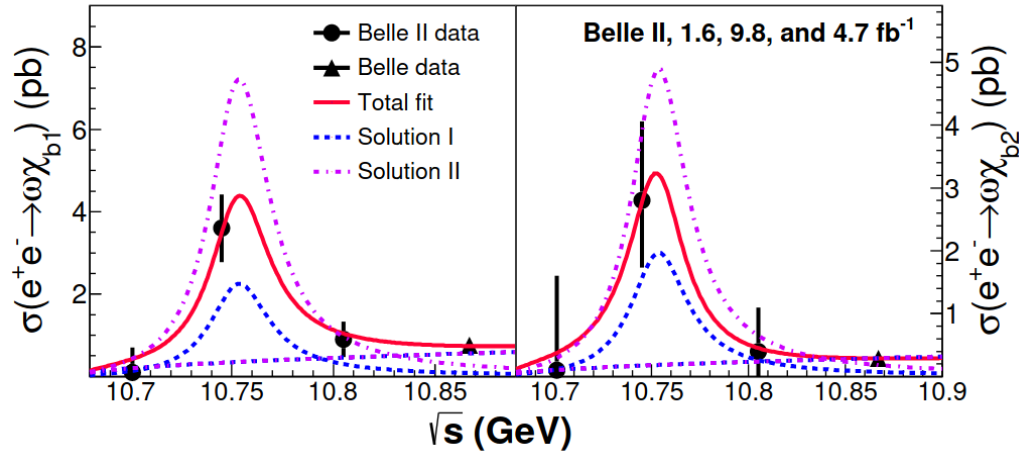
$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega \chi_{b2}(1P)] = \begin{pmatrix} 0.53 \pm 0.40 \pm 0.15 \\ 1.32 \pm 0.44 \pm 0.53 \end{pmatrix} eV$$

What we thought was  $Y(5S) \rightarrow \omega \chi_{bj}(1P)$  is probably just the tail of the  $Y(10750)$ !



$$e^+e^- \rightarrow \chi_{b1,2}(1P) \omega$$

[PRL 130, 091902 (2023)]



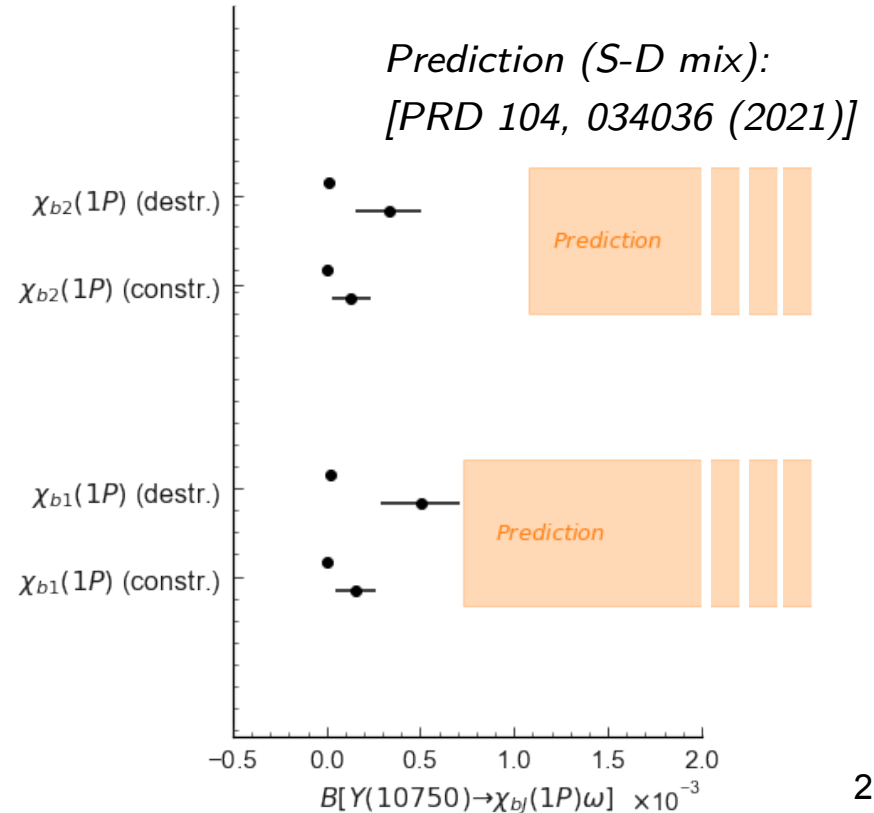
Disagreement with S-D model

$$\sigma[ee \rightarrow \omega \chi_{b0}(1P)] < 11.3 \text{ pb @ } 10.750 \text{ GeV}$$

Two solutions (constr. or destr. interference):

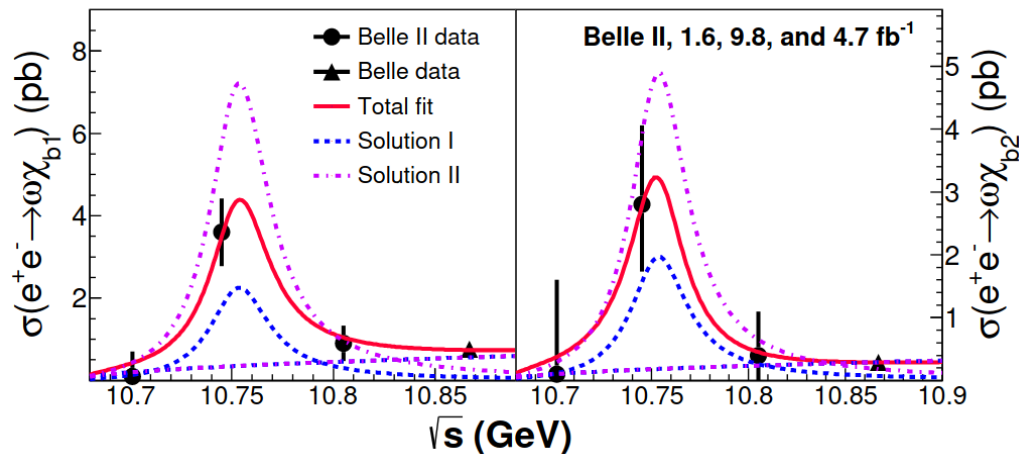
$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega \chi_{b1}(1P)] = \begin{matrix} (0.63 \pm 0.39 \pm 0.20) \text{ eV} \\ (2.01 \pm 0.38 \pm 0.76) \text{ eV} \end{matrix}$$

$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega \chi_{b2}(1P)] = \begin{matrix} (0.53 \pm 0.40 \pm 0.15) \text{ eV} \\ (1.32 \pm 0.44 \pm 0.53) \text{ eV} \end{matrix}$$



$$e^+e^- \rightarrow \chi_{b1,2}(1P) \omega$$

[PRL 130, 091902 (2023)]

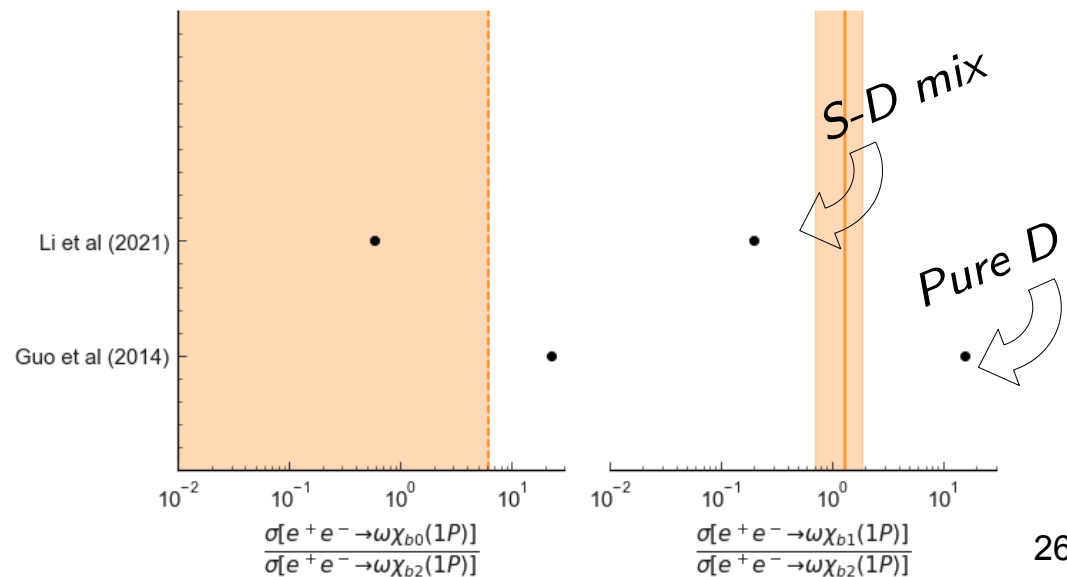


Disagreement with both pure D and S-D mixed predictions

Measured ratios:

$$\frac{B[Y(10750) \rightarrow \omega \chi_{b1}(1P)]}{B[Y(10750) \rightarrow \omega \chi_{b2}(1P)]} = 1.3 \pm 0.6$$

$$\frac{B[Y(10750) \rightarrow \omega \chi_{b0}(1P)]}{B[Y(10750) \rightarrow \omega \chi_{b2}(1P)]} < 7 \quad (\text{private extrapolation})$$



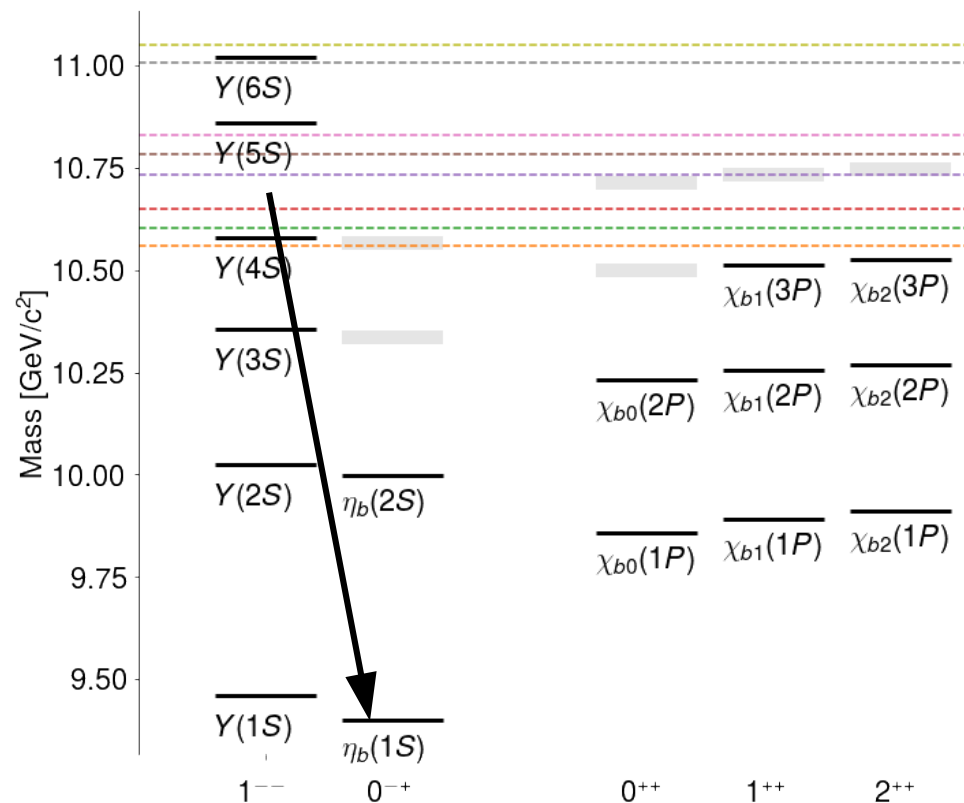
$$e^+e^- \rightarrow \eta_b(1S) \omega$$

[Wang, Chin. Phys. C 43, 123102 (2019)]

Mode	$\mathcal{B}(4q)$ (%)	$\mathcal{B}(b\bar{b})$ (%)
$B\bar{B}$	$39.3^{+38.7}_{-22.9}$	21.3
$B\bar{B}^*$	$\sim 0.2$	14.3
$B^*\bar{B}^*$	$52.3^{+54.9}_{-31.7}$	64.1
$B_s\bar{B}_s$	-	0.3
$\omega\eta_b$	$7.9^{+14.0}_{-5.0}$	-
$f_0(1370)\Upsilon$	$0.2^{+0.6}_{-0.2}$	-
$\omega\Upsilon$	$\sim 0$	-

Strategy:

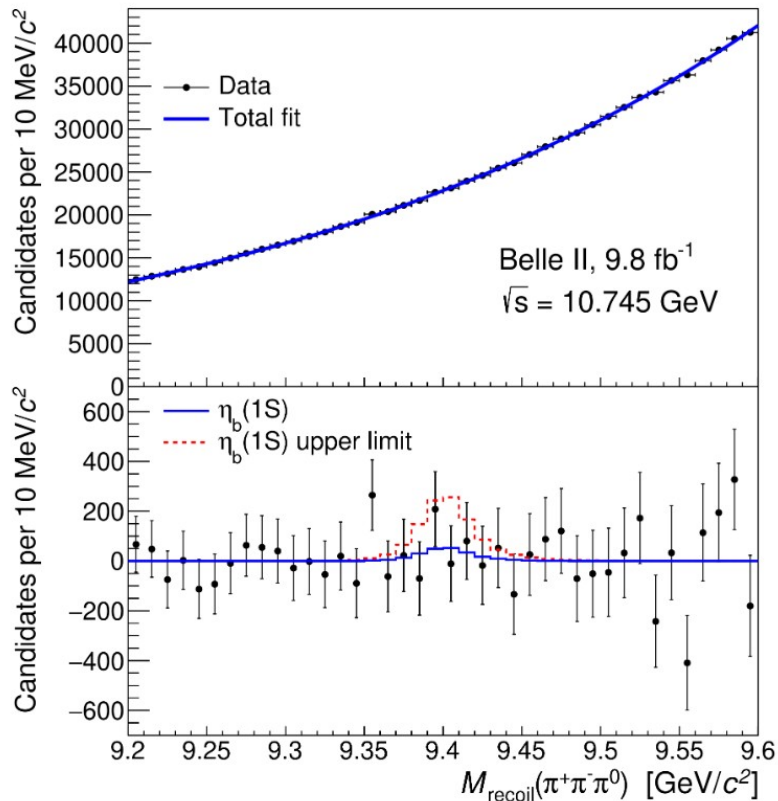
- Reconstruct  $\omega$
- Measure its recoil mass





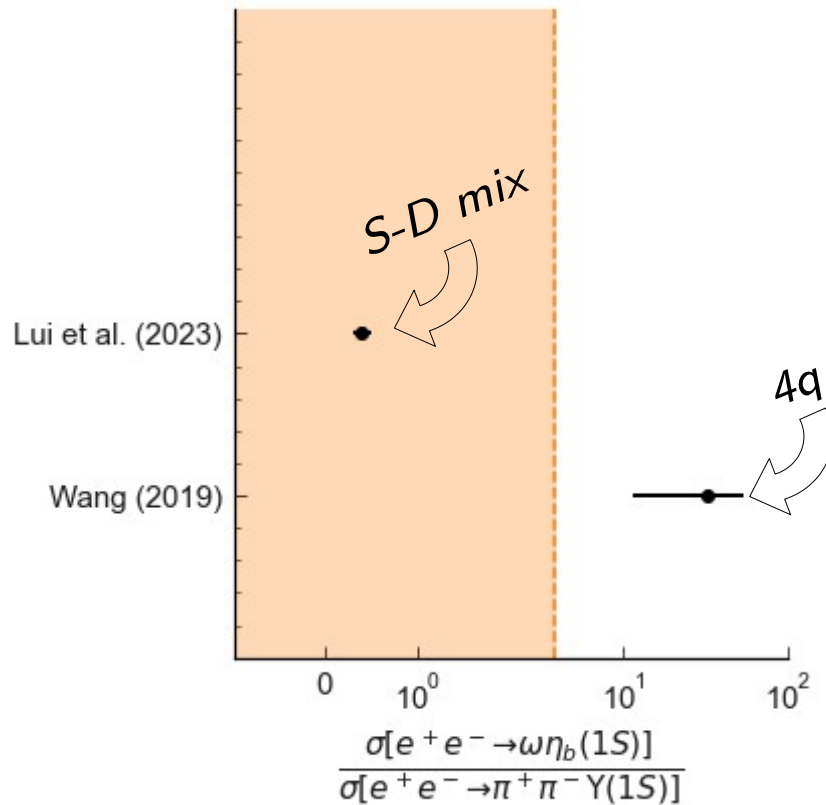
[arxiv:2312.13043]

Compatible with S-D mixed



No evidence of  $\omega$  transition to  $\eta_b(1S)$ !

$$\sigma_B(e^+e^- \rightarrow \eta_b(1S)\omega) < 2.5 \text{ pb}$$



We don't have yet clear indications on the nature of the  $Y(10750)$

→ S-D mixed state model compatible with  $\omega\eta_b(1S)$ , but not with  $\omega\chi_{bj}(1P)$

→ No enhancement of  $\omega\eta_b(1S)$  predicted by tetraquark model.

→ No indication of  $f_0$  in  $M(\pi\pi)$  in  $Y(10750) \rightarrow \pi\pi Y(nS)$

→ New precise data on inclusive and exclusive  $e^+e^- \rightarrow B^{(*)}_{(s)}\bar{B}^{(*)}_{(s)}$  cross sections

→ Can be used to get  $G[Y(10750) \rightarrow B^{(*)}\bar{B}^{(*)}]$

→ Data are waiting to be fitted ;)

We don't have yet clear indications on the nature of the  $Y(10750)$

→ S-D mixed state model compatible with  $\omega\eta_b(1S)$ , but not with  $\omega\chi_{bj}(1P)$

→ No enhancement of  $\omega\eta_b(1S)$  predicted by tetraquark model.

→ No indication of  $f_0$  in  $M(\pi\pi)$  in  $Y(10750) \rightarrow \pi\pi Y(nS)$

→ New precise data on inclusive and exclusive  $e^+e^- \rightarrow B^{(*)}_{(s)}\bar{B}^{(*)}_{(s)}$  cross sections

→ Can be used to get  $G[Y(10750) \rightarrow B^{(*)}\bar{B}^{(*)}]$

→ Data are waiting to be fitted ;)

What's next:  $\pi\pi h_b(1P)$ ,  $\eta h_b(1P)$ ,  $\eta Y(1D)$ ,  $\eta^{(\prime\prime)} Y(nS)$ ,  $Y(1S)$  inclusive, radiative transitions...

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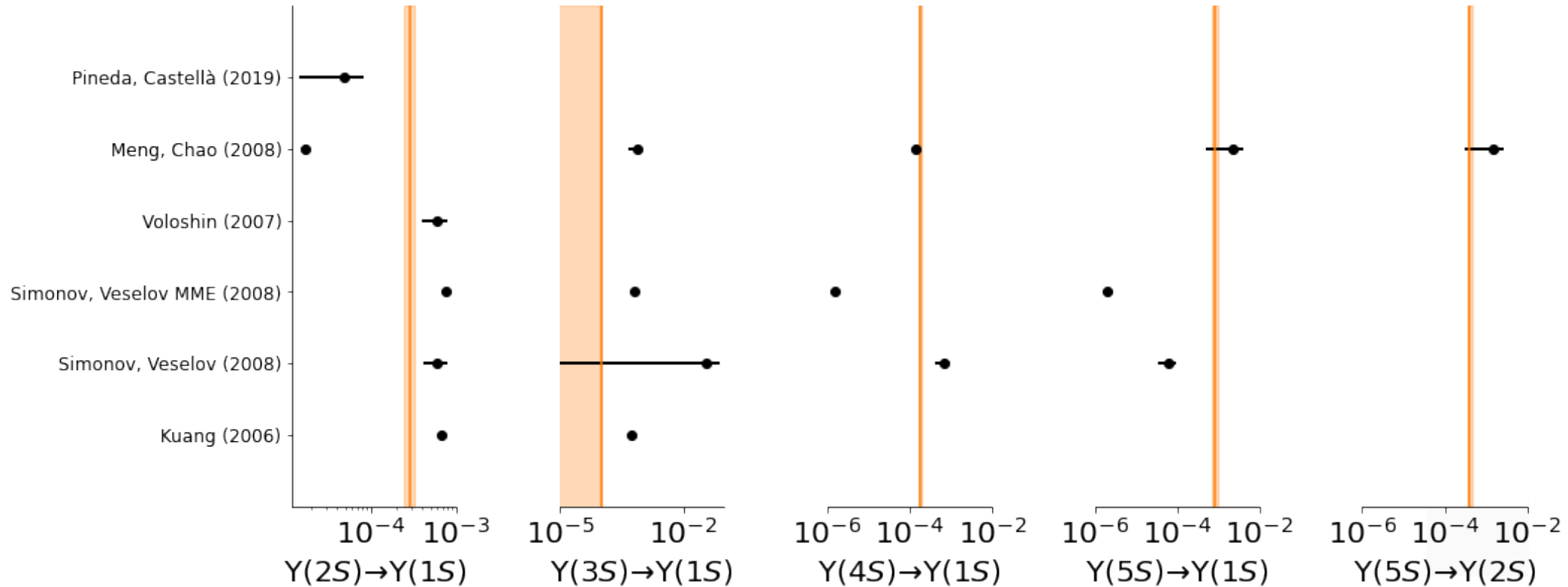
*Backup*

---

# $\eta$ transitions updated

$$\mathcal{B}(\Upsilon(5S) \rightarrow \Upsilon(1S)\eta) = (0.85 \pm 0.15 \pm 0.08) \times 10^{-3},$$

$$\mathcal{B}(\Upsilon(5S) \rightarrow \Upsilon(2S)\eta) = (4.13 \pm 0.41 \pm 0.37) \times 10^{-3},$$





*arXiv:1808.10567*

## Tracking and vertexing

→ More precise

## Particle identification

→ Much more powerful

## Calorimetry

→ ~Unchanged (Better reconstruction, but more backgrounds)

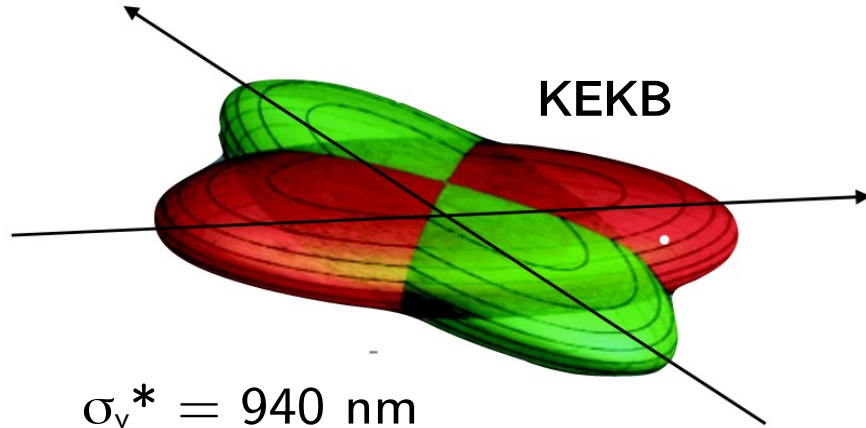
# Super-KEKB: the nano-beam scheme

$$L = \frac{\gamma_{\pm}}{2er_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \left( \frac{I_{\pm} \xi_{y\pm}}{\beta_y^*} \right) \left( \frac{R_L}{R_{\xi_{y\pm}}} \right)$$

Lorentz factor  $\rightarrow$   $\frac{\gamma_{\pm}}{2er_e}$   
 Beam current  $\rightarrow$   $I_{\pm}$   
 Beam-beam factor  $\rightarrow$   $\left( \frac{R_L}{R_{\xi_{y\pm}}} \right)$   
 Beam aspect ratio (flat beam  $\sim$  1-2%)  $\rightarrow$   $\frac{\sigma_y^*}{\sigma_x^*}$   
 Vertical beta function at IP  $\rightarrow$   $\beta_y^*$   
 Geometrical corrections (Hourglass effect...)  $\rightarrow$   $R_{\xi_{y\pm}}$

**Brute force:** Increase the current (x2)

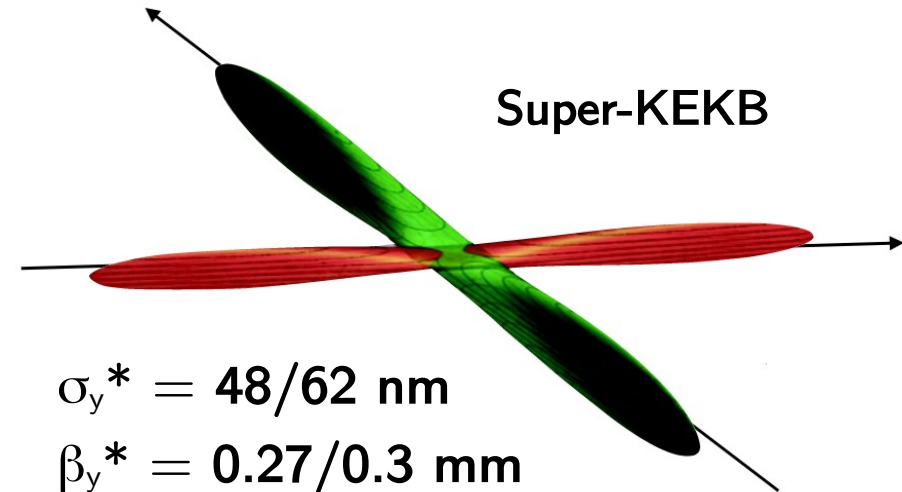
**Precision:** denser beams, smaller  $\beta^*$  (x20)



$$\sigma_y^* = 940 \text{ nm}$$

$$\beta_y^* = 5.9 \text{ mm}$$

$$\sigma_x^* = 147/170 \text{ } \mu\text{m}$$



$$\sigma_y^* = 48/62 \text{ nm}$$

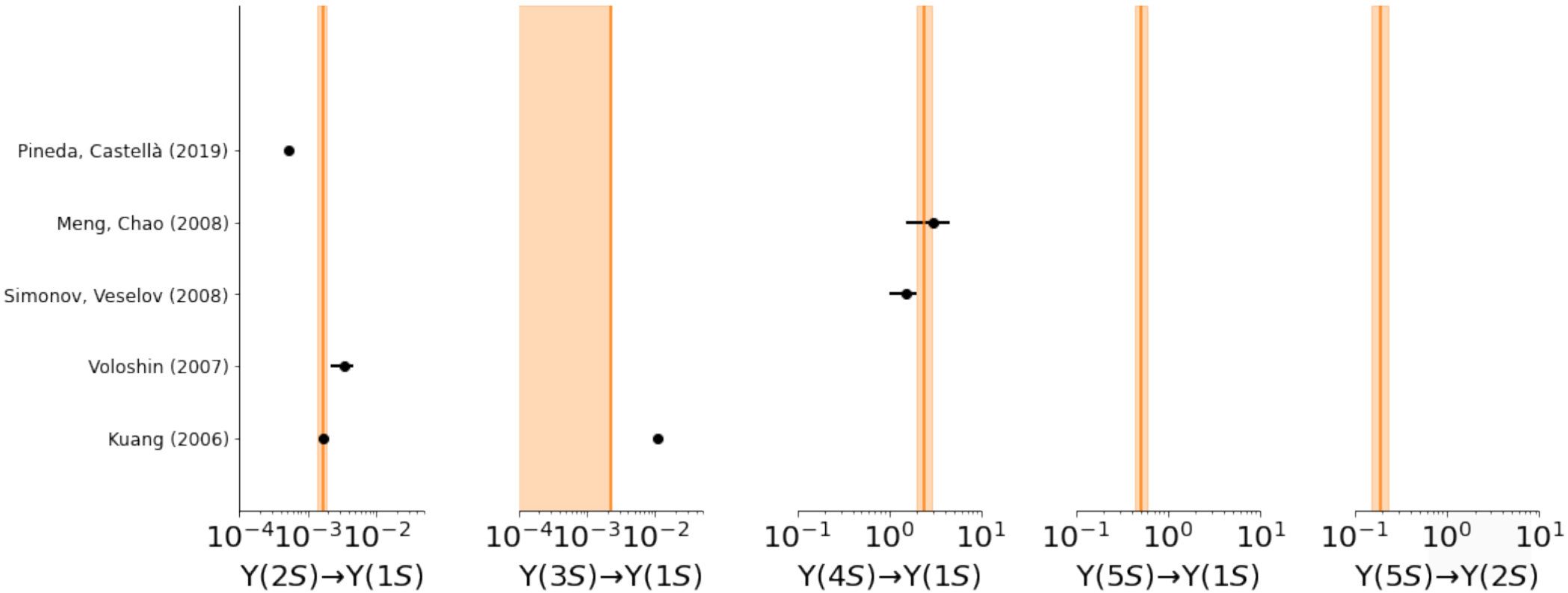
$$\beta_y^* = 0.27/0.3 \text{ mm}$$

$$\sigma_x^* = 10.1/10.7 \text{ } \mu\text{m}$$

# $\eta/\pi\pi$ Ratio updated

$$\frac{\Gamma(\Upsilon(5S) \rightarrow \Upsilon(2S)\eta)}{\Gamma(\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-)} = 0.51 \pm 0.06 \pm 0.04$$

$$\frac{\Gamma(\Upsilon(5S) \rightarrow \Upsilon(1S)\eta)}{\Gamma(\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-)} = 0.19 \pm 0.04 \pm 0.01$$



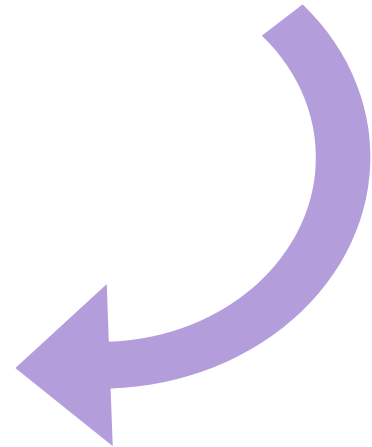
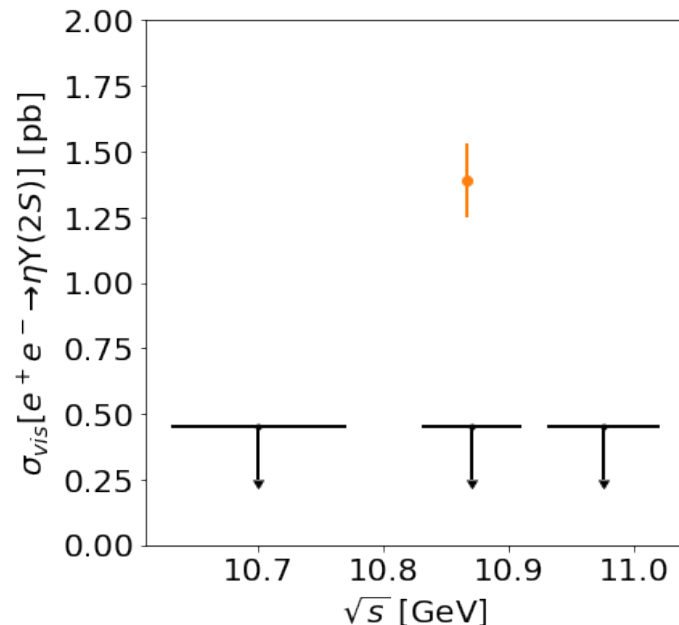
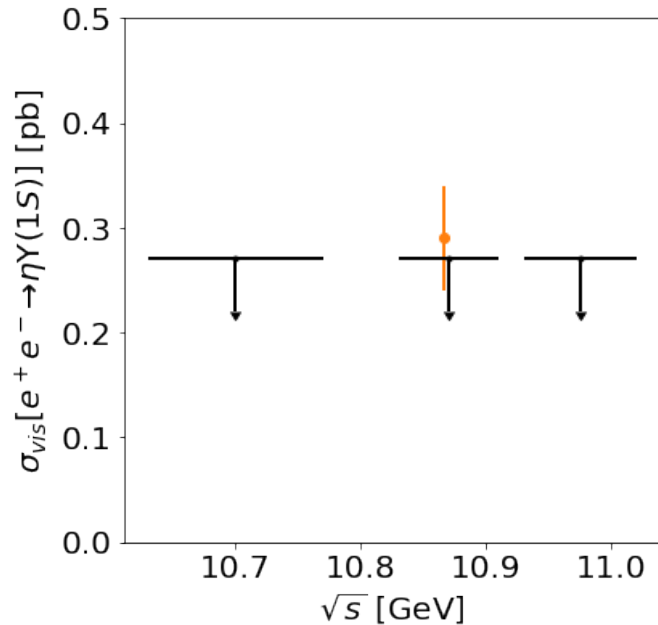
# $Y(5S) \rightarrow \eta Y(1S, 2S)$

Results of the combined decays modes:

$$\sigma_B(e^+e^- \rightarrow \Upsilon(2S)\eta) = 2.07 \pm 0.21 \pm 0.19 \text{ pb,}$$

$$\sigma_B(e^+e^- \rightarrow \Upsilon(1S)\eta) = 0.42 \pm 0.08 \pm 0.04 \text{ pb,}$$

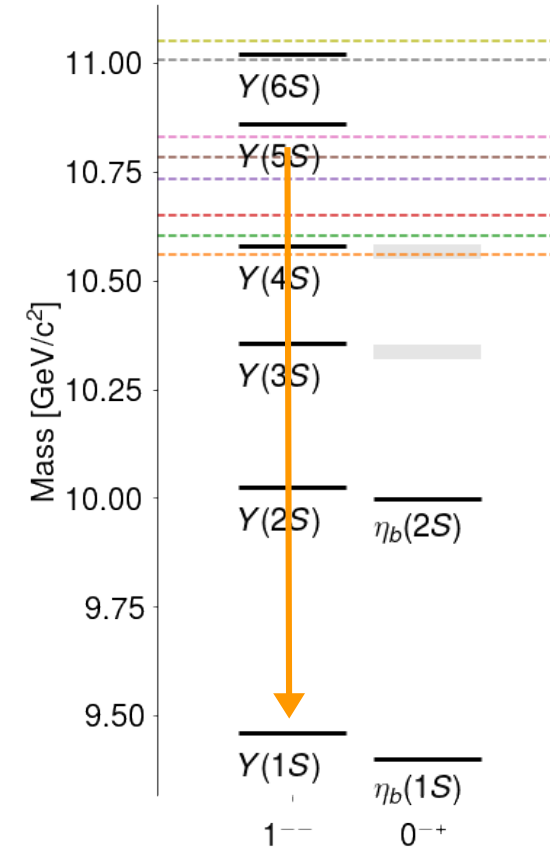
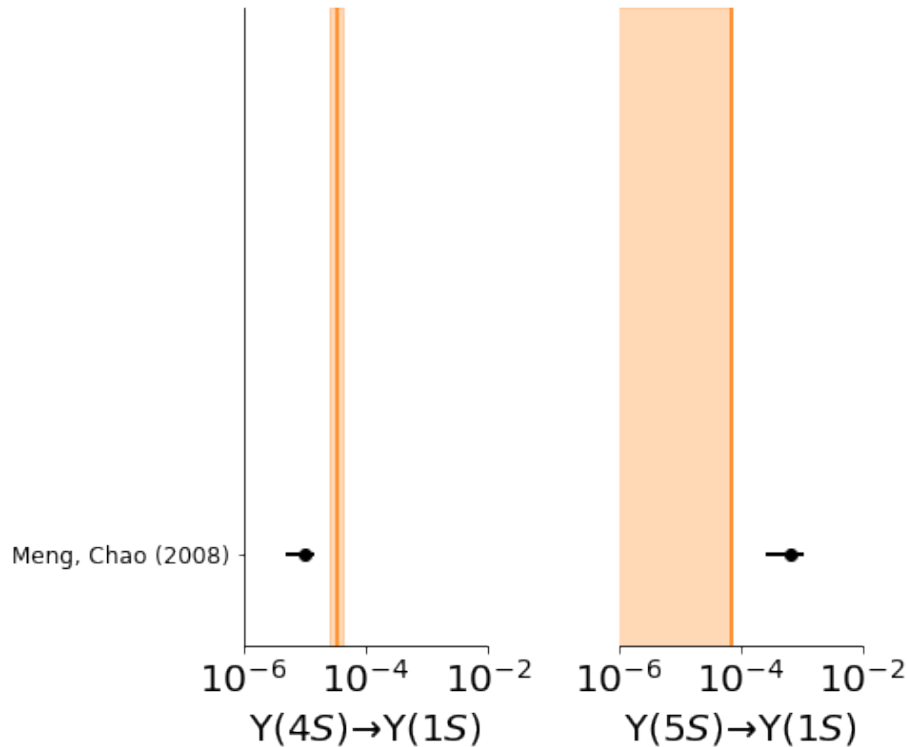
No Significant yield in the Belle scan  
data outside the  $Y(5S)$



$$Y(5S) \rightarrow \eta' Y(1S)$$

Combining the two decay modes:

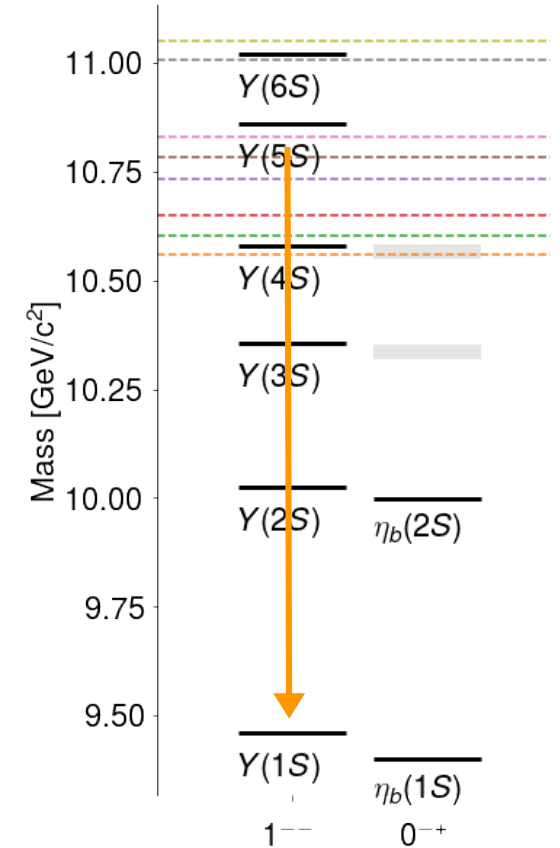
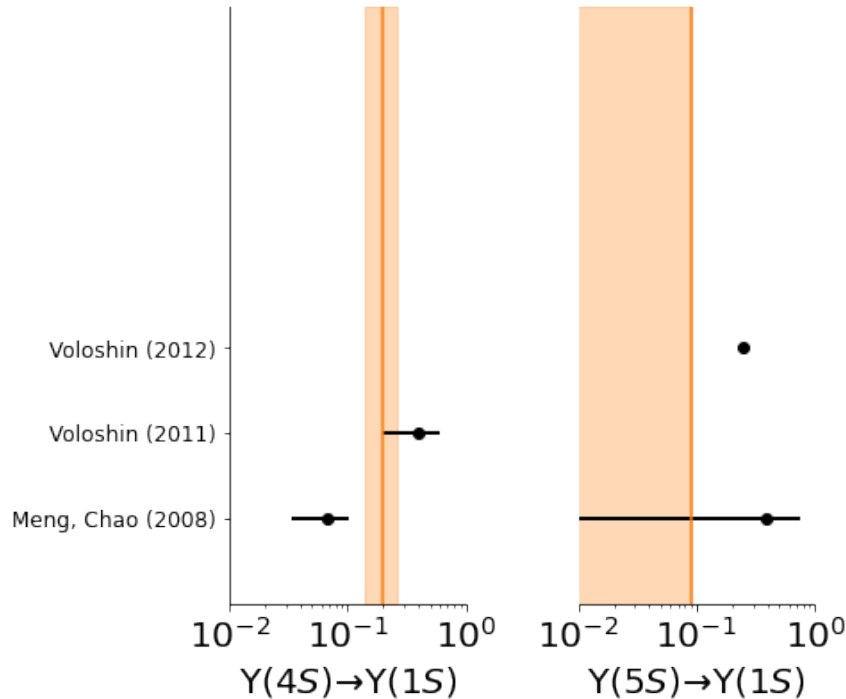
$$\mathcal{B}(Y(5S) \rightarrow Y(1S)\eta') < 6.9 \times 10^{-5}, CL = 90\%.$$



$$Y(5S) \rightarrow \eta' Y(1S)$$

Combining the two decay modes:

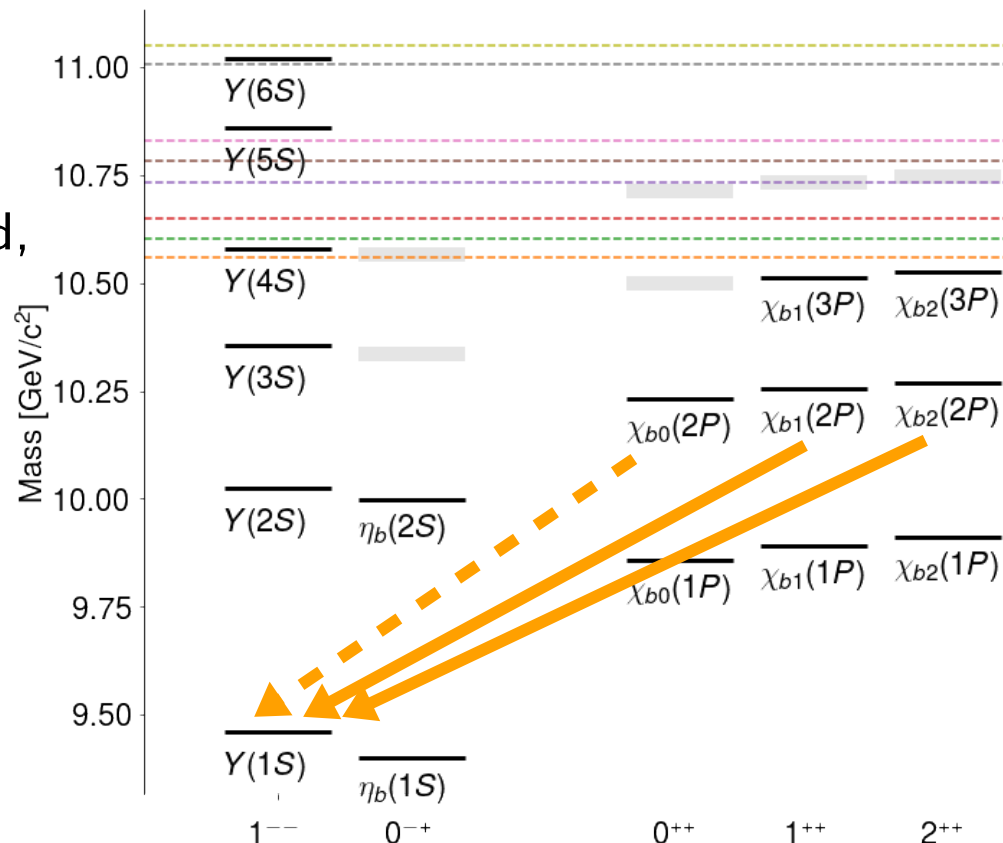
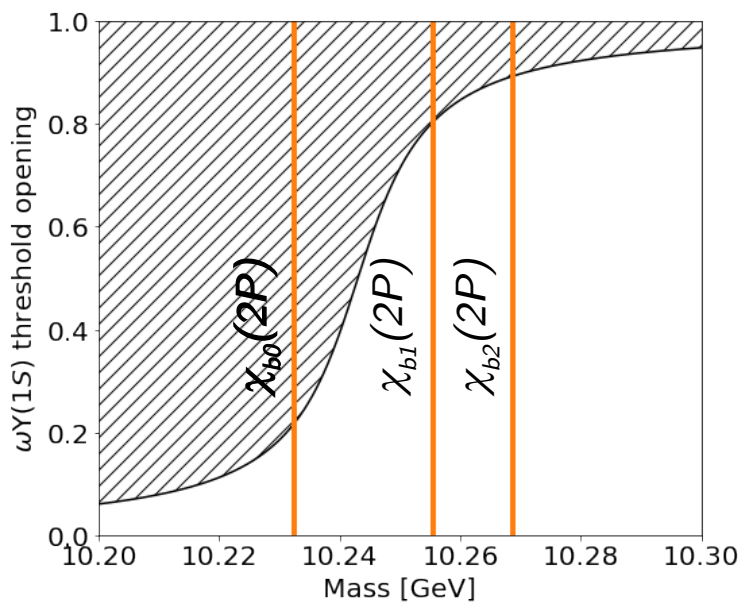
$$\frac{\Gamma(Y(5S) \rightarrow Y(1S)\eta')}{\Gamma(Y(5S) \rightarrow Y(1S)\eta)} < 0.09 \quad (CL = 90\%)$$



$$\chi_{b0}(2P) \rightarrow \omega Y(1S)$$

## Peculiar features

- $\omega$   $Y(1S)$  threshold between  $\chi_{b0}$  and  $\chi_{b1}$
- $\chi_{b0}(2P)$  decay still possible sub-threshold, like in  $X(3872) \rightarrow \omega J/\psi$





$$\chi_{b0}(2P) \rightarrow \omega Y(1S)$$

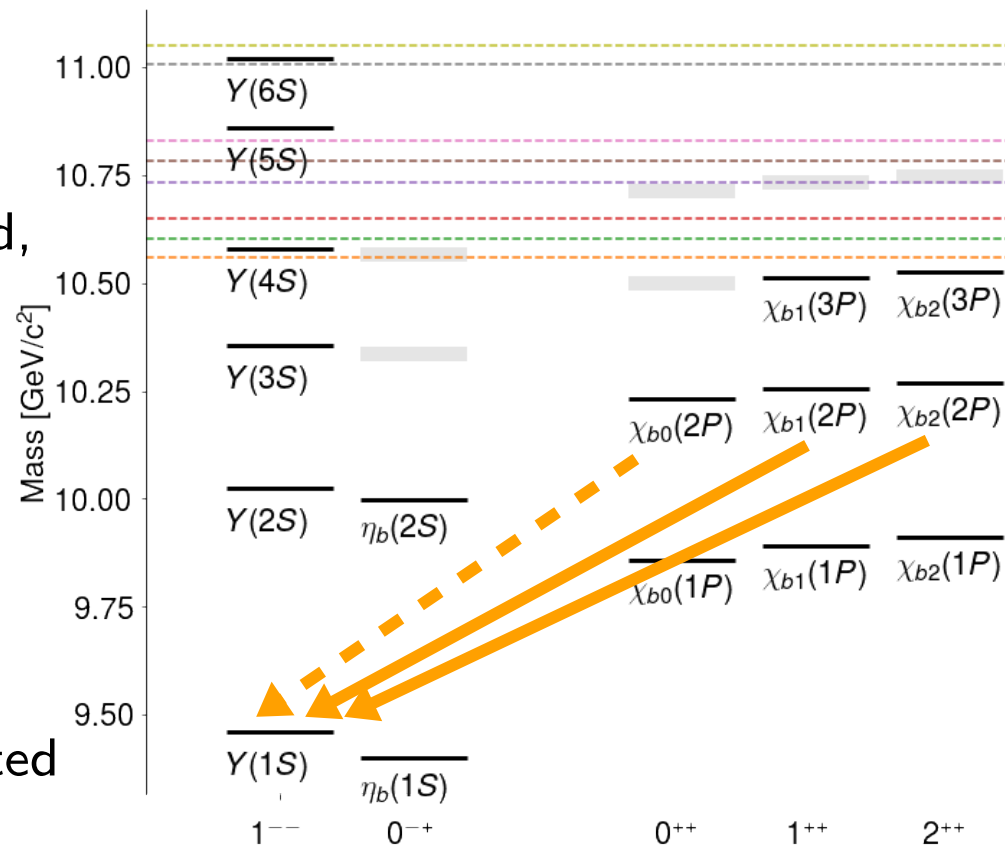
## Peculiar features

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## Reconstruction strategy:

Mass of  $\omega + \mu\mu$  pair

- $\chi_b(2P)$  produced by non-reconstructed radiative decay of  $Y(3S)$

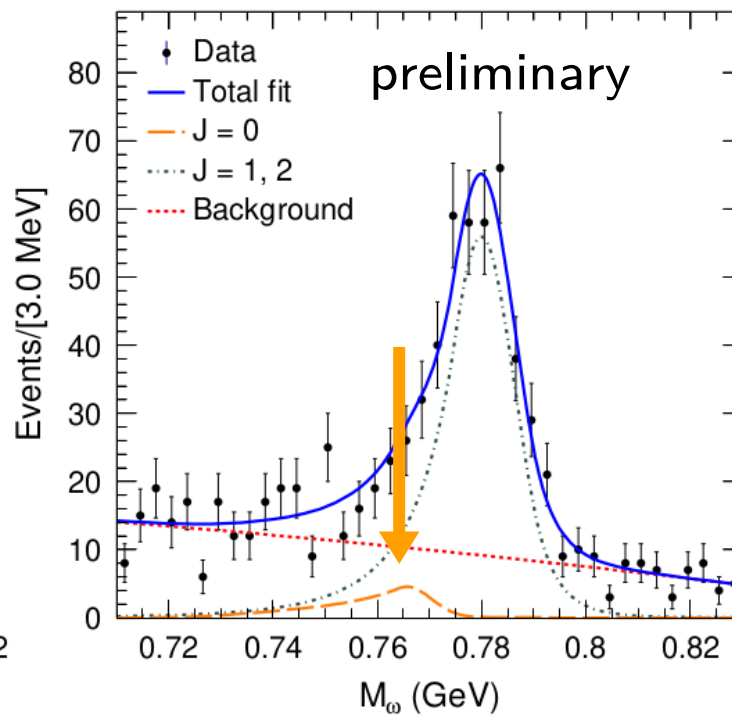
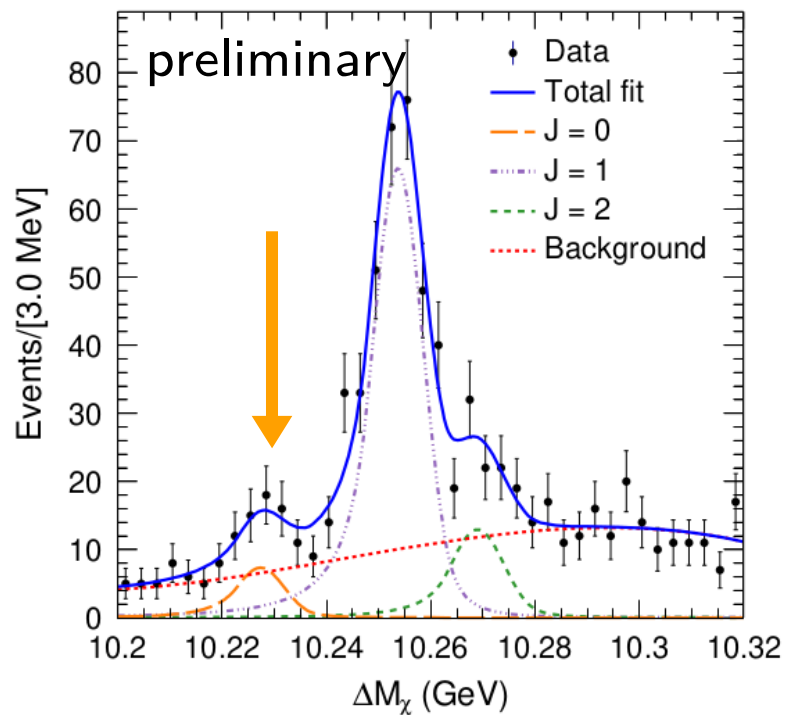


$$\chi_{b0}(2P) \rightarrow \omega Y(1S)$$

First evidence of  $\chi_{b0} \rightarrow \omega Y(1S)$  ( $3.6 \sigma$ ) preliminary

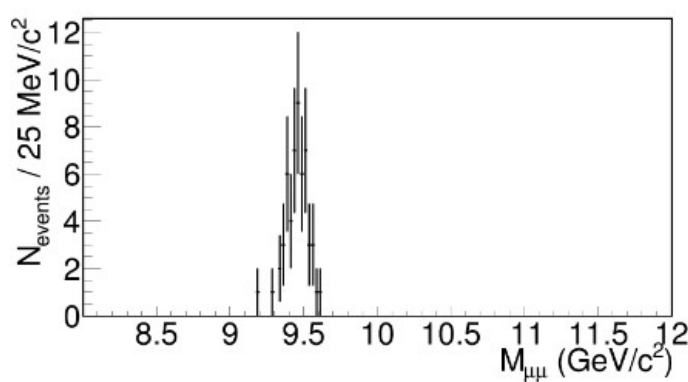
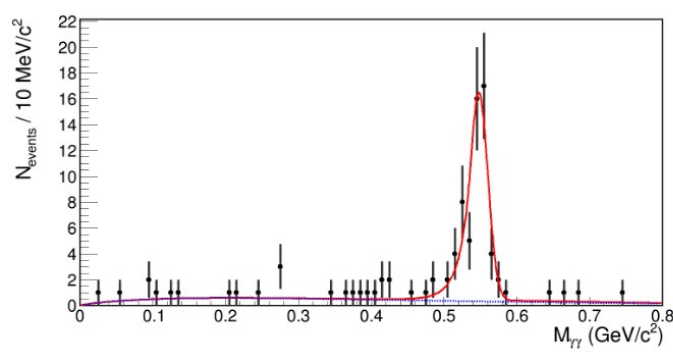
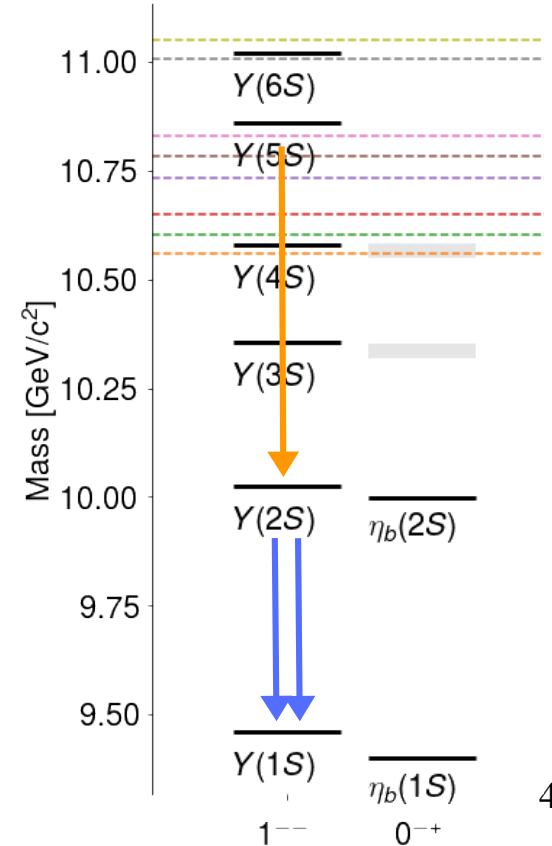
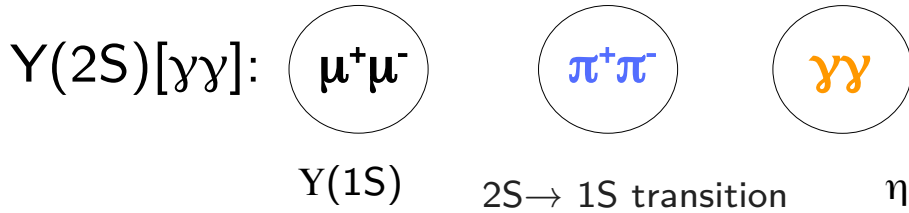
$$\mathcal{B}(\chi_{b0}(2P) \rightarrow \omega Y(1S)) = (0.54_{-0.18}^{+0.19} \pm 0.07)\%$$

NEW



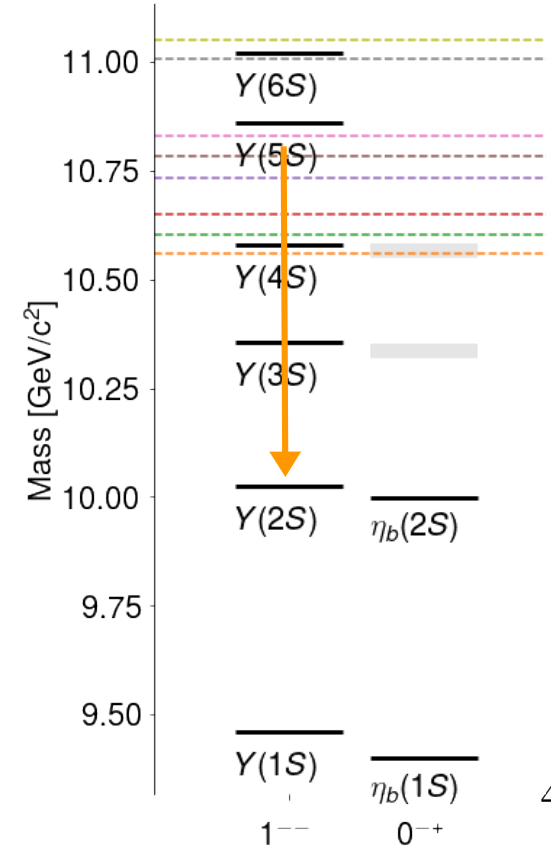
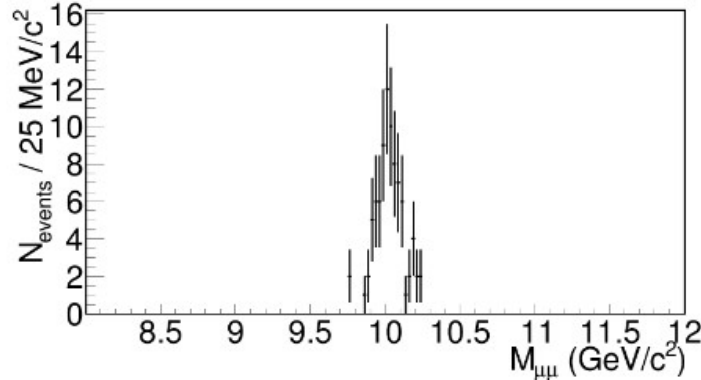
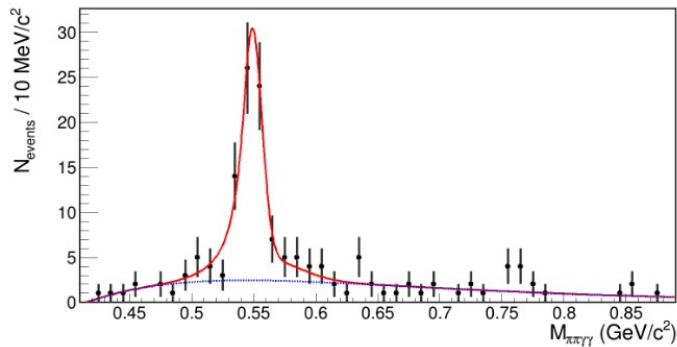
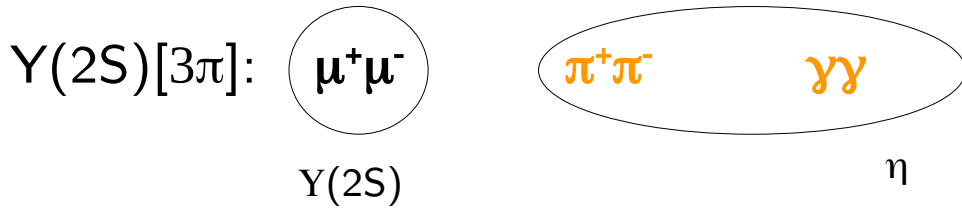
# $Y(5S) \rightarrow \eta Y(1S, 2S)$

New analysis of  $\eta$  and  $\eta'$  transitions from the  $Y(5S)$  region.  
 One final state, several decays:  $\mu^+\mu^- \pi^+\pi^- \gamma\gamma$



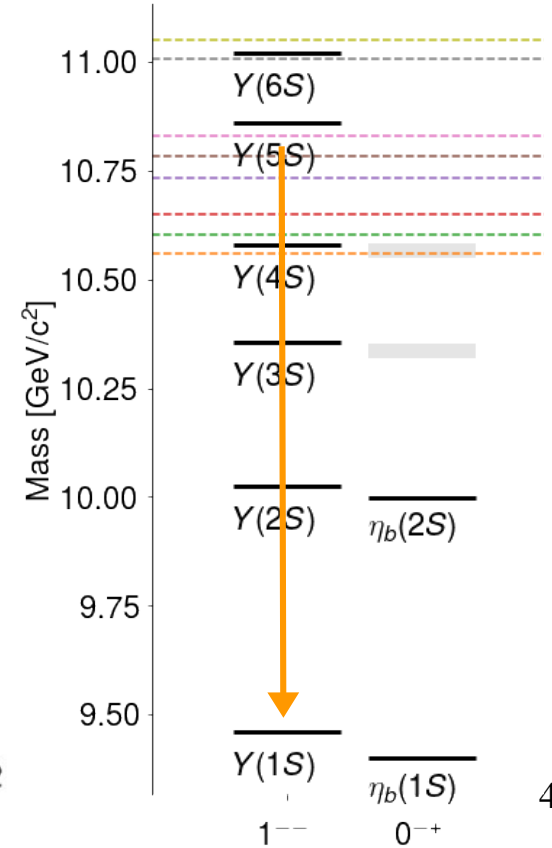
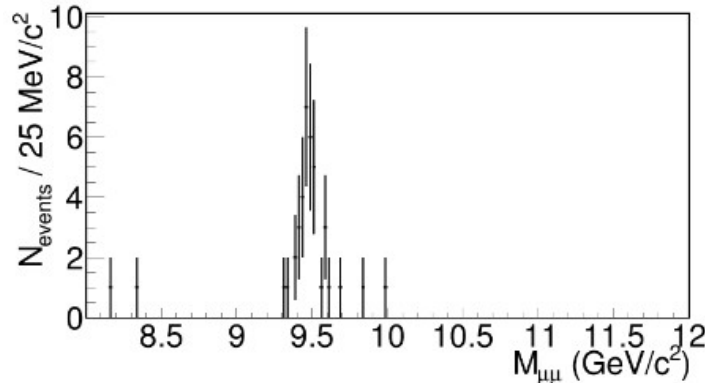
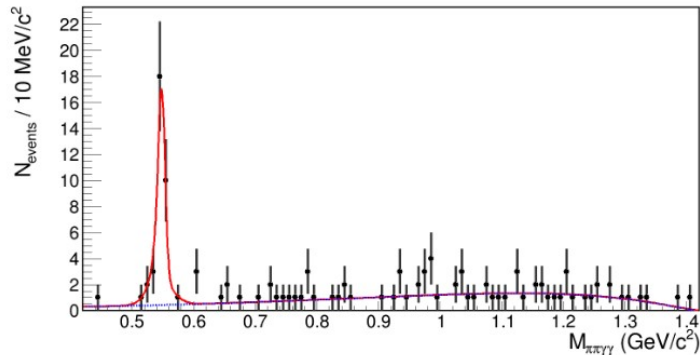
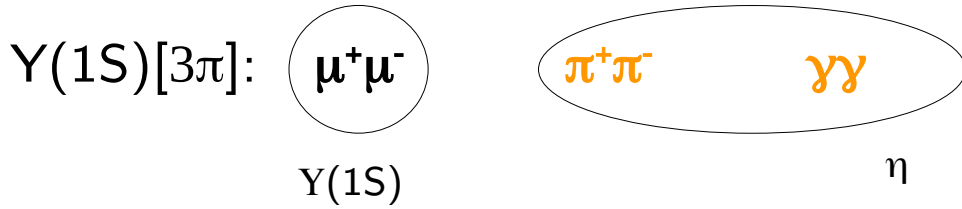
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