

# LFV $\tau$ searches at the Belle and Belle II experiments

[Alberto Martini - DESY \(Deutsches Elektronen-Synchrotron\)](#)

on behalf of the Belle & Belle II collaborations

Tau2023 conference - 5 December 2023

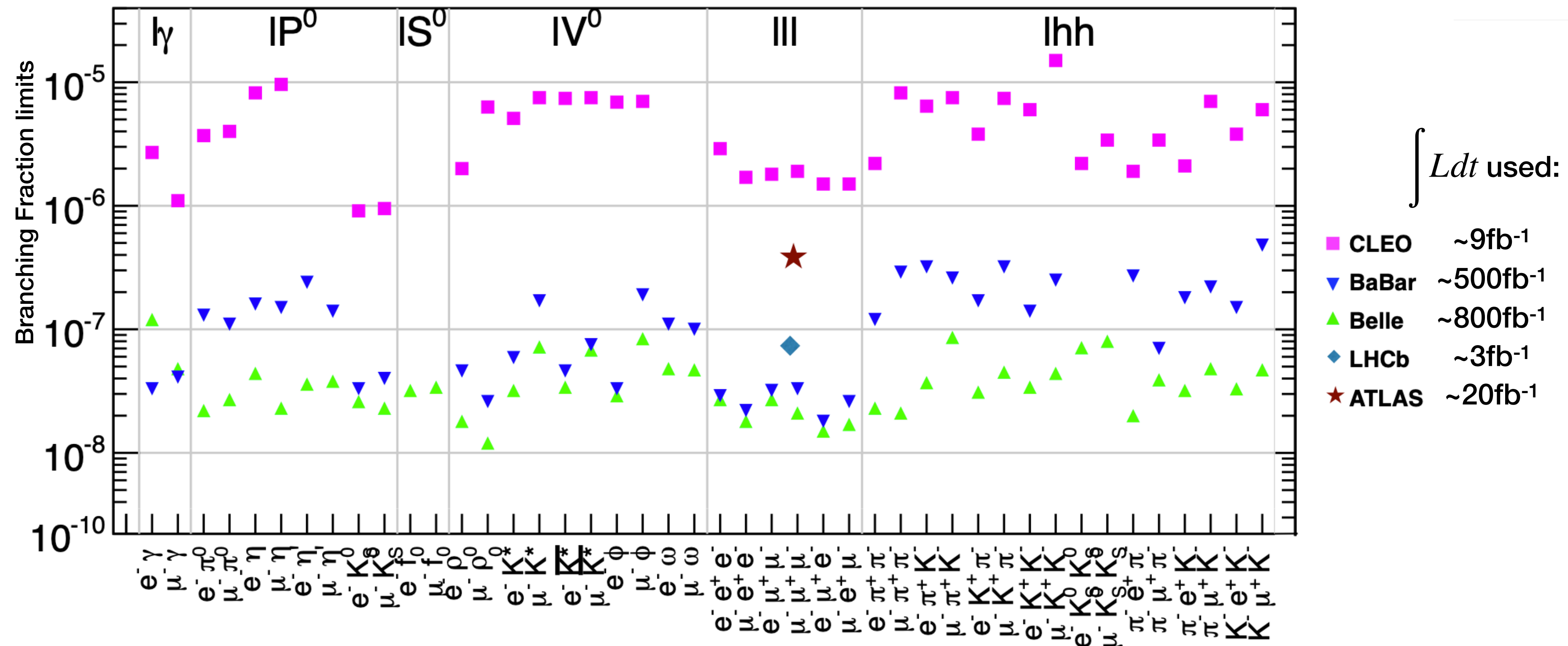


# $\tau$ LFV searches at B-factories

Lepton Flavor Violation (LFV) is allowed in various extensions of the Standard Model (SM) but it **has never been observed**



**See talks by:**  
 Kiyoshi Hayasaka  
 Pankaj Munbodh  
 Innes Bigaran

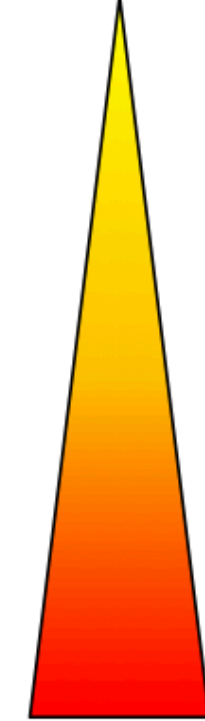


# $\tau$ LFV channels

Search various decay modes:

- $\tau \rightarrow \ell\ell\ell$
- $\tau \rightarrow \ell K_s, \Lambda h$
- $\tau \rightarrow \ell V^0 (\rightarrow hh')$
- $\tau \rightarrow \ell P^0 (\rightarrow \gamma\gamma)$
- $\tau \rightarrow \ell hh'$
- $\tau \rightarrow \ell\gamma$

Simple



Hard

Difficulty of  
background  
reduction

Good determination of  $\tau$  mass and  
energy + few SM background sources

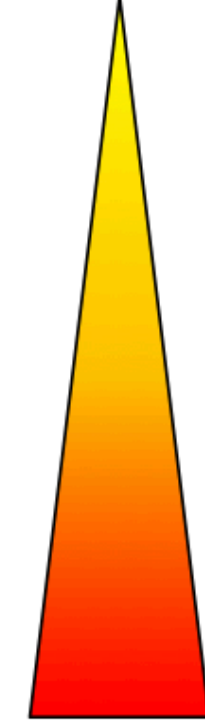
Tough determination of  $\tau$  mass and  
energy + irreducible SM backgrounds

# $\tau$ LFV channels

Search various decay modes:

- $\tau \rightarrow \ell\ell\ell$
- $\tau \rightarrow \ell K_s, \Lambda h$
- $\tau \rightarrow \ell V^0 (\rightarrow hh')$
- $\tau \rightarrow \ell P^0 (\rightarrow \gamma\gamma)$
- $\tau \rightarrow \ell hh'$
- $\tau \rightarrow \ell\gamma$

Simple



Hard

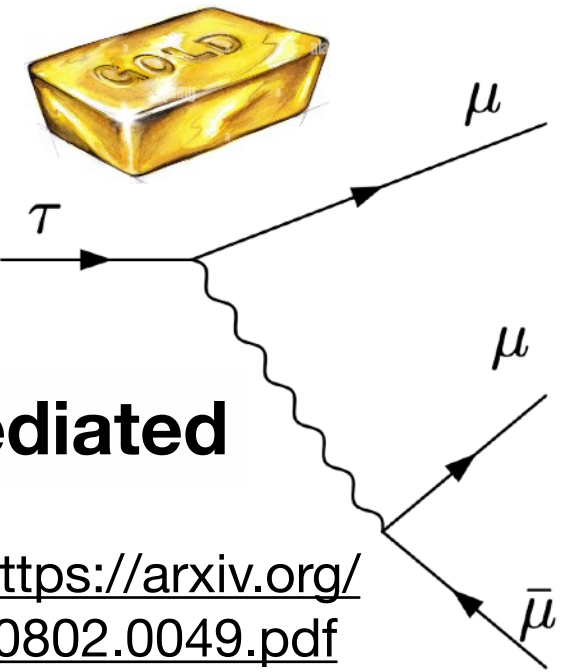
Difficulty of background reduction

Good determination of  $\tau$  mass and energy + few SM background sources

Tough determination of  $\tau$  mass and energy + irreducible SM backgrounds

Golden channel:  $\tau \rightarrow \mu\mu\mu$   
experimentally the most accessible

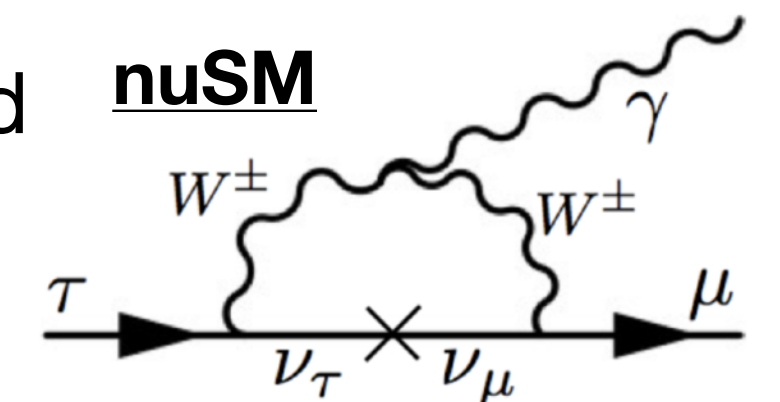
ref: <https://arxiv.org/pdf/1808.10567.pdf>



Z' mediated

ref: <https://arxiv.org/pdf/0802.0049.pdf>

Golden channel:  $\tau \rightarrow \mu\gamma$   
Largest BF in models where a one-loop diagram is involved



nuSM

Ref: <https://arxiv.org/pdf/1301.4652.pdf>

Physics models	$B(\tau \rightarrow \mu\gamma)$	$B(\tau \rightarrow \mu\mu\mu)$
SM + $\nu$ mixing	$10^{-49} \sim 10^{-52}$	$10^{-53} \sim 10^{-56}$
SM+heavy Majorana $\nu_R$	$10^{-9}$	$10^{-10}$
Non-universal Z'	$10^{-9}$	$10^{-8}$
SUSY SO(10)	$10^{-8}$	$10^{-10}$
mSUGRA + seesaw	$10^{-7}$	$10^{-9}$
SUSY Higgs	$10^{-10}$	$10^{-7}$

Ref: <https://arxiv.org/abs/hep-ph/0702136>

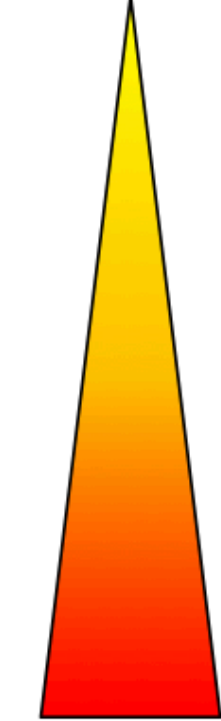
An observation would be a clear signature of NP!

# $\tau$ LFV channels

Search various decay modes:

- ★  $-\tau \rightarrow \ell\ell\ell$
- $-\tau \rightarrow \ell K_s, \Lambda h$
- ★  $-\tau \rightarrow \ell V^0 (\rightarrow hh')$
- $-\tau \rightarrow \ell P^0 (\rightarrow \gamma\gamma)$
- $-\tau \rightarrow \ell hh'$
- $-\tau \rightarrow \ell\gamma$
- ★  $-\tau \rightarrow \ell\alpha$

Simple



Hard

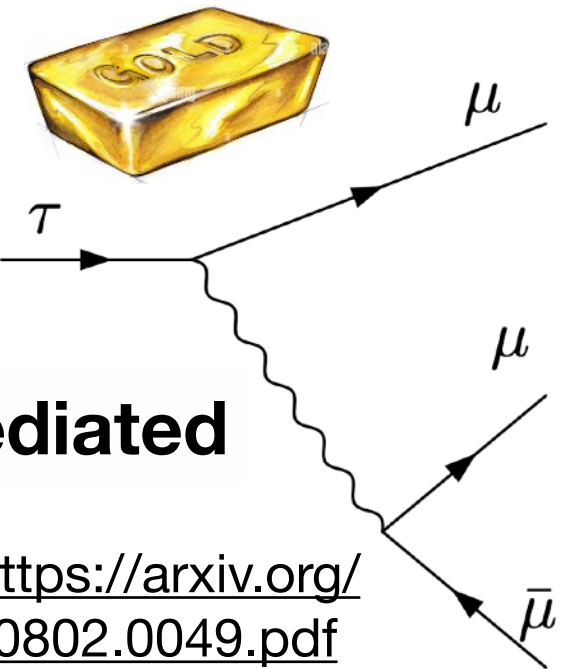
Difficulty of background reduction

Good determination of  $\tau$  mass and energy + few SM background sources

Tough determination of  $\tau$  mass and energy + irreducible SM backgrounds

Golden channel:  $\tau \rightarrow \mu\mu\mu$   
experimentally the most accessible

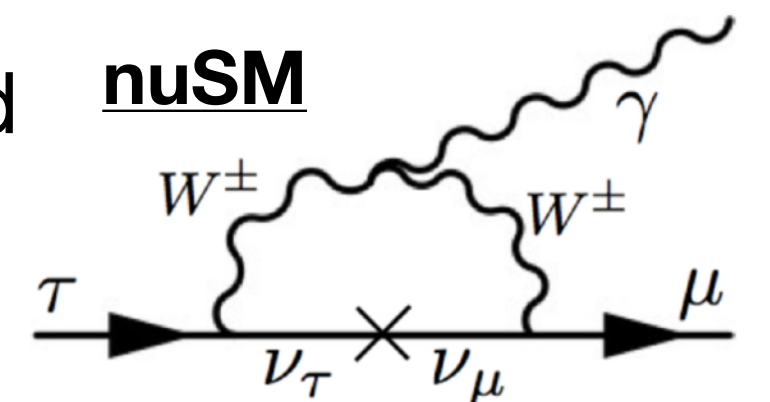
ref: <https://arxiv.org/pdf/1808.10567.pdf>



Z' mediated

ref: <https://arxiv.org/pdf/0802.0049.pdf>

Golden channel:  $\tau \rightarrow \mu\gamma$   
Largest BF in models where a one-loop diagram is involved



nuSM

Ref: <https://arxiv.org/pdf/1301.4652.pdf>

See talk from Sourav Dey later today

Ref: <https://arxiv.org/abs/hep-ph/0702136>

Physics models	$B(\tau \rightarrow \mu\gamma)$	$B(\tau \rightarrow \mu\mu\mu)$
SM + $\nu$ mixing	$10^{-49} \sim 10^{-52}$	$10^{-53} \sim 10^{-56}$
SM+heavy Majorana $\nu_R$	$10^{-9}$	$10^{-10}$
Non-universal Z'	$10^{-9}$	$10^{-8}$
SUSY SO(10)	$10^{-8}$	$10^{-10}$
mSUGRA + seesaw	$10^{-7}$	$10^{-9}$
SUSY Higgs	$10^{-10}$	$10^{-7}$

An observation would be a clear signature of NP!

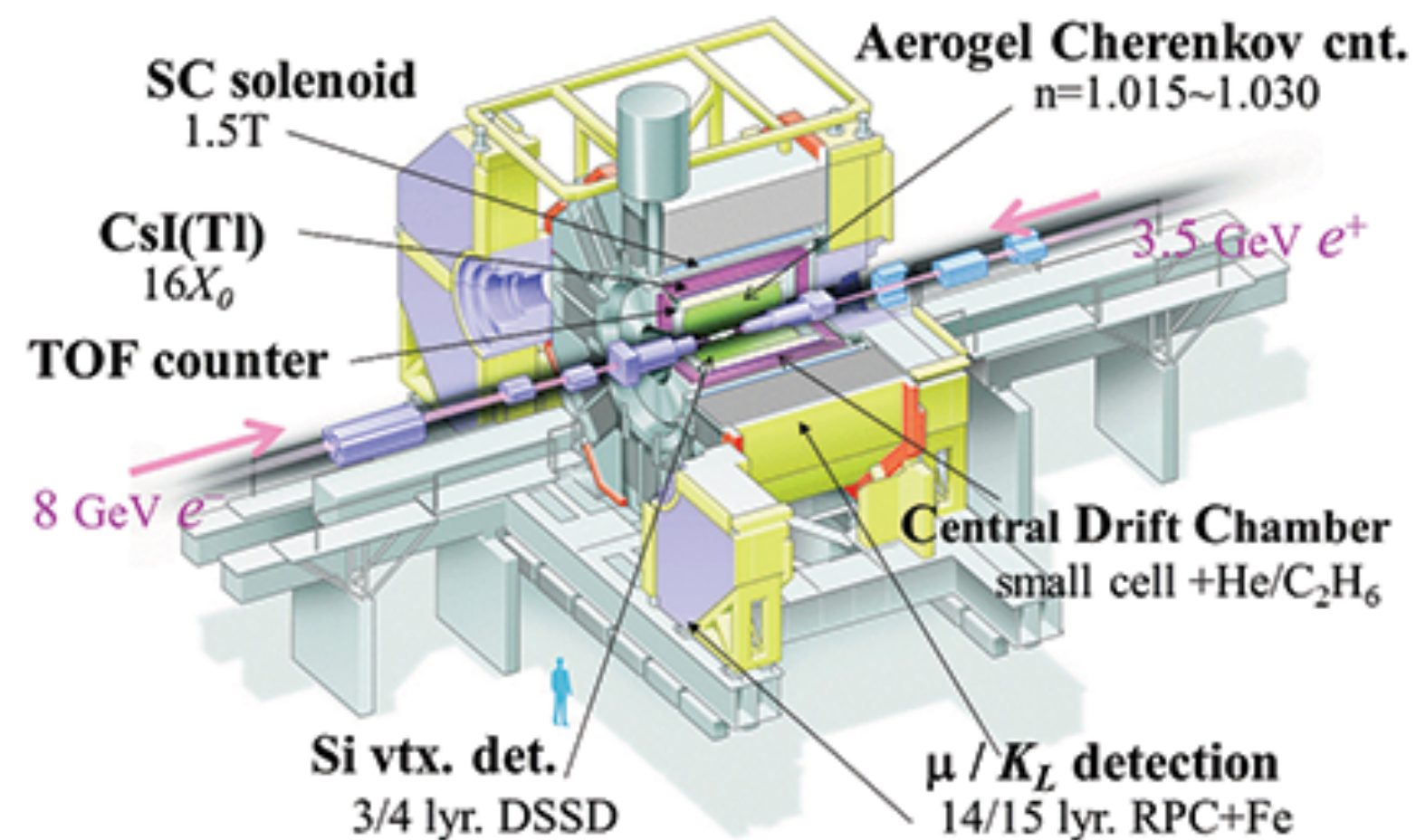
# Introduction to the B-factories: Belle & Belle II

The **Belle experiment (1999 - 2010)** and the **Belle II experiment (2018 - )** operate at B-factories KEKB and SuperKEKB → collisions of  $e^+ e^-$  at  $\Upsilon(4S)$  resonance: 10.58 GeV



Belle recorded  $L_{int} \sim 1000 \text{ fb}^{-1}$

## Belle Detector



Belle II recorded  $L_{int} = 424 \text{ fb}^{-1}$

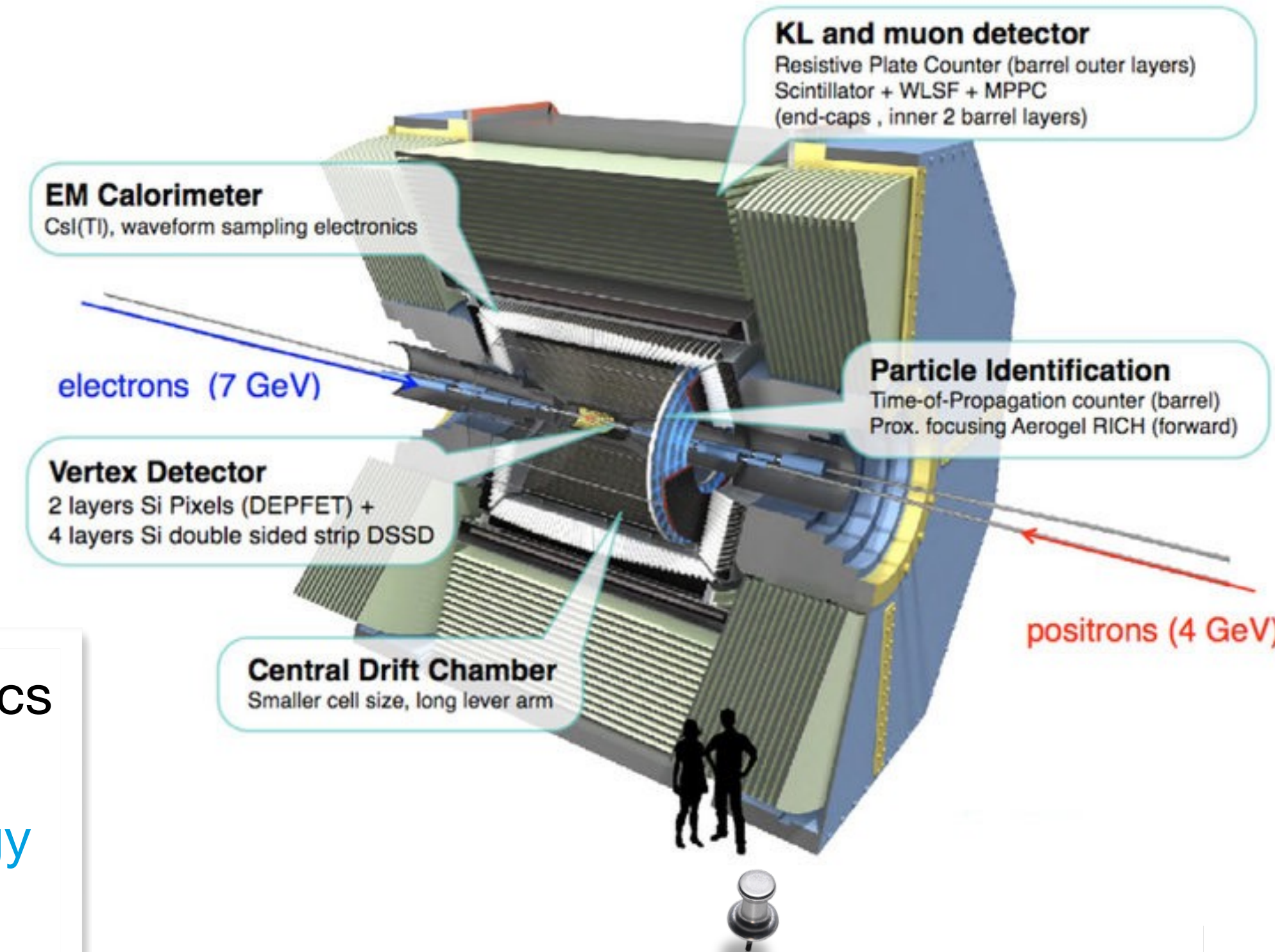
$$\sigma(ee \rightarrow bb) \simeq 1.1 \text{ nb}$$

$$\sigma(ee \rightarrow \tau\tau) \simeq 0.9 \text{ nb}$$

$N_{\tau\tau} \sim 4 \times 10^8$  @ Belle II  
→  $\tau$  factory!

Advantages of studying  $\tau$  physics at B-factories:

- Well defined initial state energy
- Clean environment
- High hermeticity of the detector



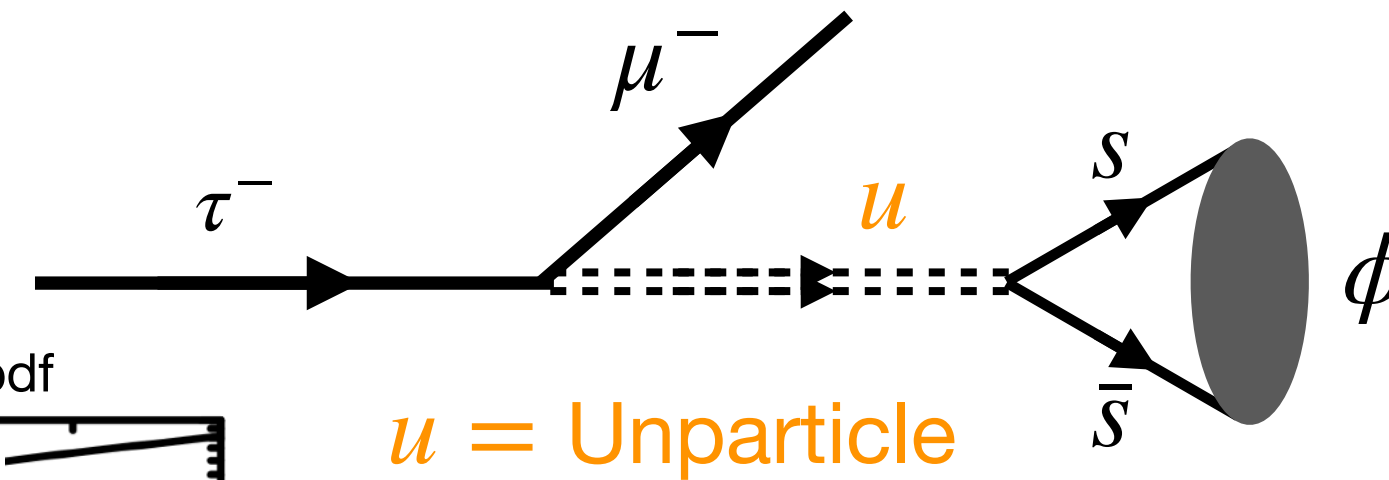
Luminosity world record  
@SuperKEKB:  $4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

# Analysis motivations: $\tau \rightarrow IV^0$

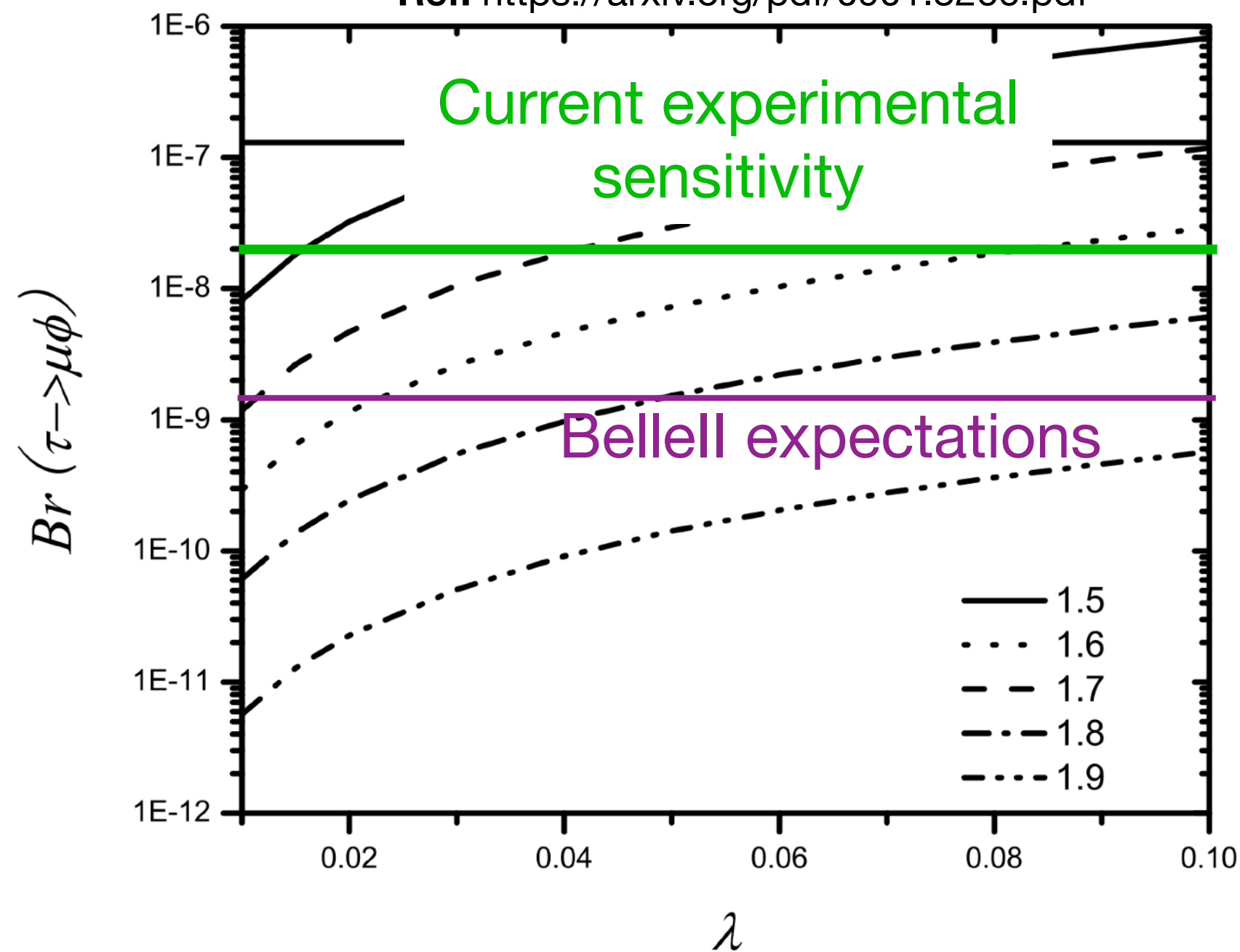
Decay channel forbidden in the SM but allowed in several new physics scenarios

## Unparticle model

Ref: <https://arxiv.org/pdf/hep-ph/0703260.pdf>



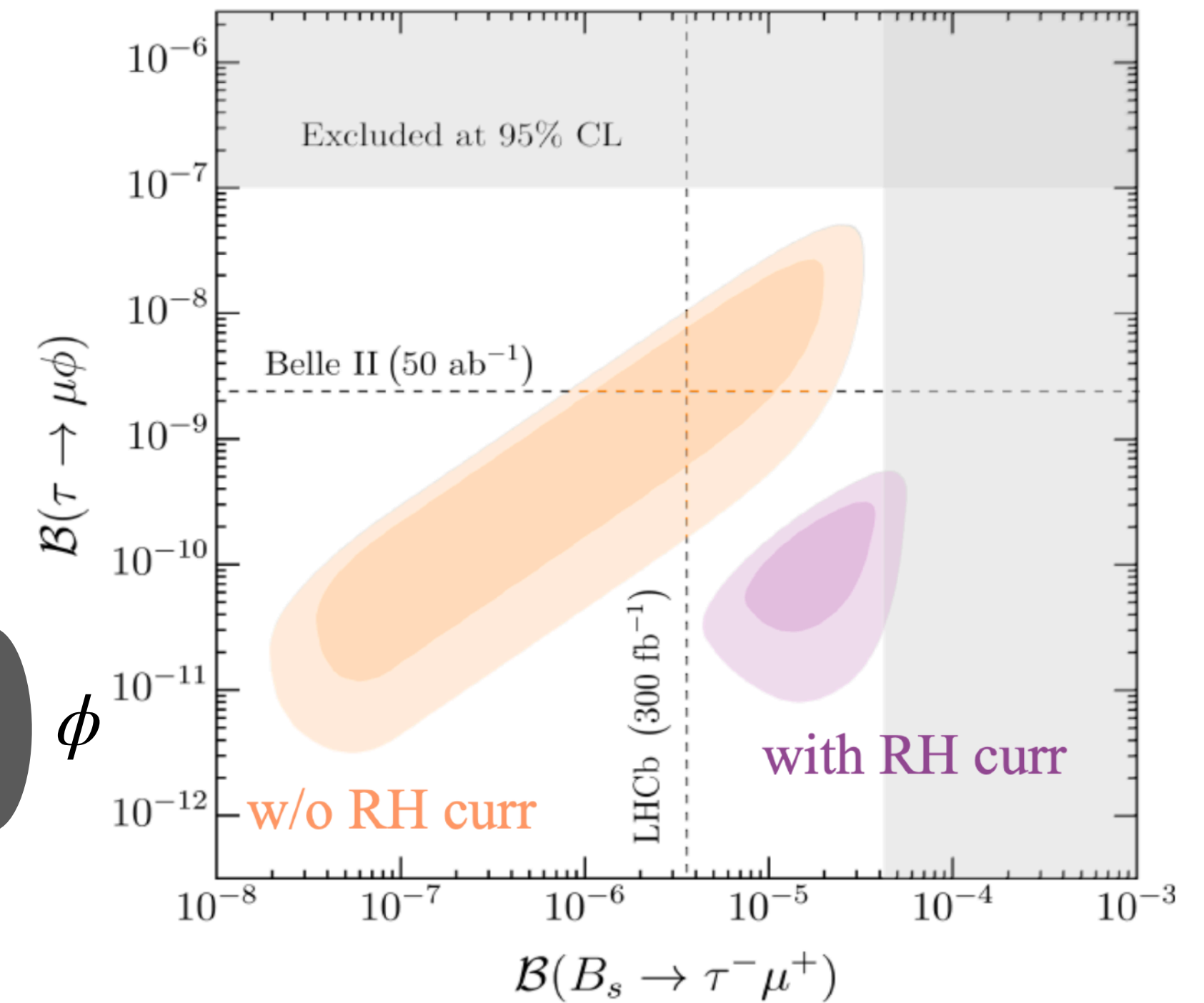
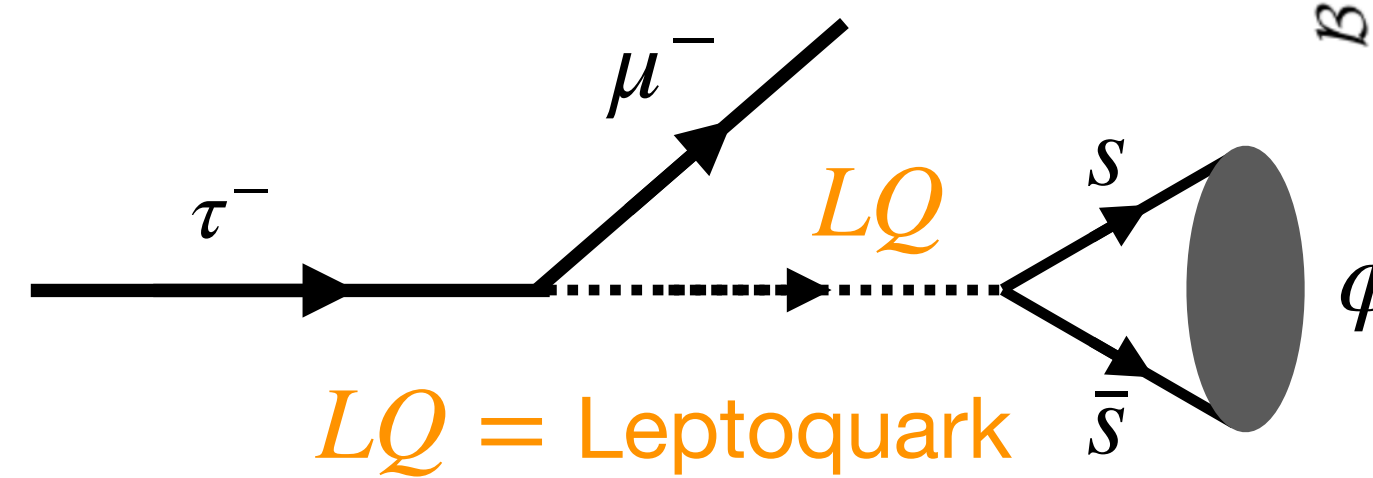
Ref: <https://arxiv.org/pdf/0901.3266.pdf>



One of the golden channels for this model

## Leptoquark model

Ref: <https://arxiv.org/pdf/2103.16558.pdf>



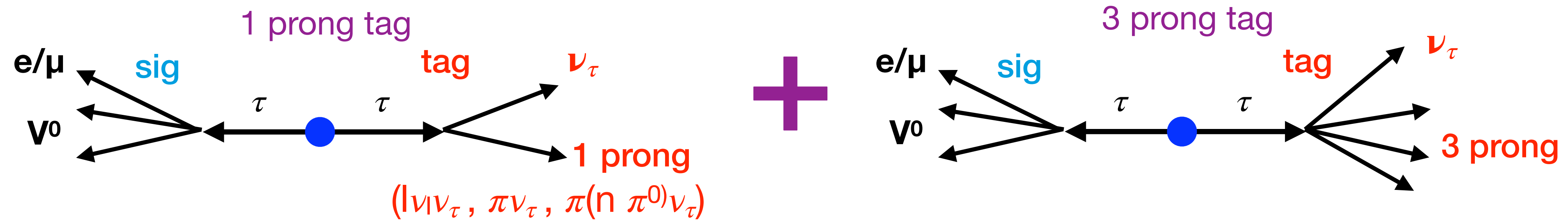
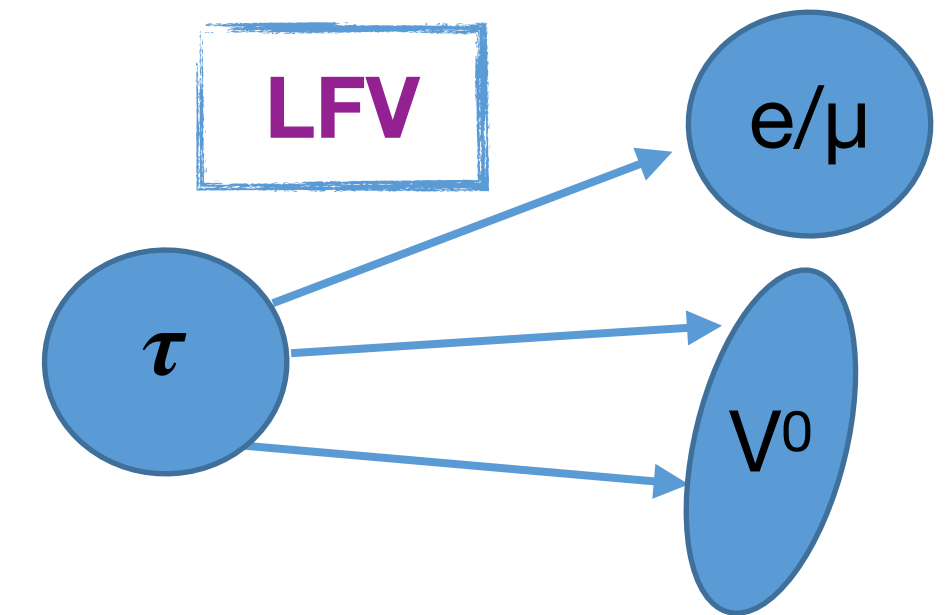
Nice interplay between B and  $\tau$  physics!

# Analysis steps for $\tau \rightarrow lV^0$ @Belle

Belle analysis on  $V^0 = (\rho^0, \phi, \omega, K^*)$

ref: <https://arxiv.org/pdf/2301.03768.pdf>

Analysis including 3-prong decay for  $\tau_{\text{tag}}$  with  $\sim 850 \text{ fb}^{-1}$



## Analysis steps:

- Event selection and background suppression via **BDT**
- Prepare BDT classifier **for each LFV mode**
  - For all modes:  $V^0$  mass; event tag side & decay modes; event shape and kinematics
    - Additional for the  $\omega$  modes: momentum of  $\pi^0$  from  $\omega$  and lower energy of the two photons from  $\pi^0$

Dominant syst. from tracking efficiency and particle identification  
Negligible impact on the limit





# Analysis results for $\tau \rightarrow IV^0$ @Belle

No significant excess found  $\rightarrow$  set ULs at 90% CL by counting approach

Mode	$\varepsilon$ (%)	$N_{\text{BG}}$	$\sigma_{\text{syst}}$ (%)	$N_{\text{obs}}$	$\mathcal{B}_{\text{obs}} (\times 10^{-8})$
$\tau^\pm \rightarrow \mu^\pm \rho^0$	7.78	$0.95 \pm 0.20(\text{stat.}) \pm 0.15(\text{syst.})$	4.6	0	$< 1.7$
$\tau^\pm \rightarrow e^\pm \rho^0$	8.49	$0.80 \pm 0.27(\text{stat.}) \pm 0.04(\text{syst.})$	4.4	1	$< 2.2$
$\tau^\pm \rightarrow \mu^\pm \phi$	5.59	$0.47 \pm 0.15(\text{stat.}) \pm 0.05(\text{syst.})$	4.8	0	$< 2.3$ ●
$\tau^\pm \rightarrow e^\pm \phi$	6.45	$0.38 \pm 0.21(\text{stat.}) \pm 0.00(\text{syst.})$	4.5	0	$< 2.0$ ●
$\tau^\pm \rightarrow \mu^\pm \omega$	3.27	$0.32 \pm 0.23(\text{stat.}) \pm 0.19(\text{syst.})$	4.8	0	$< 3.9$ ●
$\tau^\pm \rightarrow e^\pm \omega$	5.41	$0.74 \pm 0.43(\text{stat.}) \pm 0.06(\text{syst.})$	4.5	0	$< 2.4$ ●
$\tau^\pm \rightarrow \mu^\pm K^{*0}$	4.52	$0.84 \pm 0.25(\text{stat.}) \pm 0.31(\text{syst.})$	4.3	0	$< 2.9$ ●
$\tau^\pm \rightarrow e^\pm K^{*0}$	6.94	$0.54 \pm 0.21(\text{stat.}) \pm 0.16(\text{syst.})$	4.1	0	$< 1.9$ ●
$\tau^\pm \rightarrow \mu^\pm \bar{K}^{*0}$	4.58	$0.58 \pm 0.17(\text{stat.}) \pm 0.12(\text{syst.})$	4.3	1	$< 4.3$ ●
$\tau^\pm \rightarrow e^\pm \bar{K}^{*0}$	7.45	$0.25 \pm 0.11(\text{stat.}) \pm 0.02(\text{syst.})$	4.1	0	$< 1.7$ ●

$$\mathbf{B}(\tau \rightarrow eV^0) < (1.7 - 2.4) \times 10^{-8}$$

$$\mathbf{B}(\tau \rightarrow \mu V^0) < (1.7 - 4.3) \times 10^{-8}$$

**World best results!**

~30% improvement wrt previous results done @Belle with 543 fb<sup>-1</sup>!

ref: <https://arxiv.org/pdf/0801.2475.pdf>



# Analysis steps for $\tau \rightarrow l\phi$ @Belle II

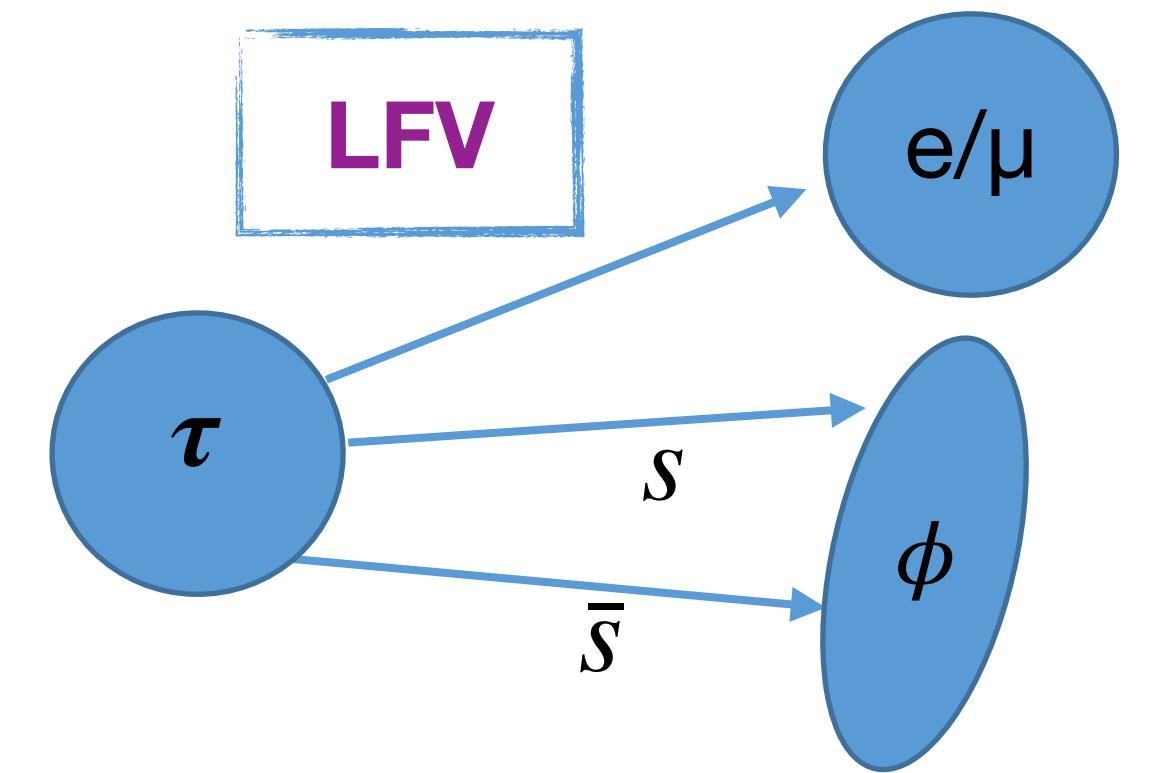
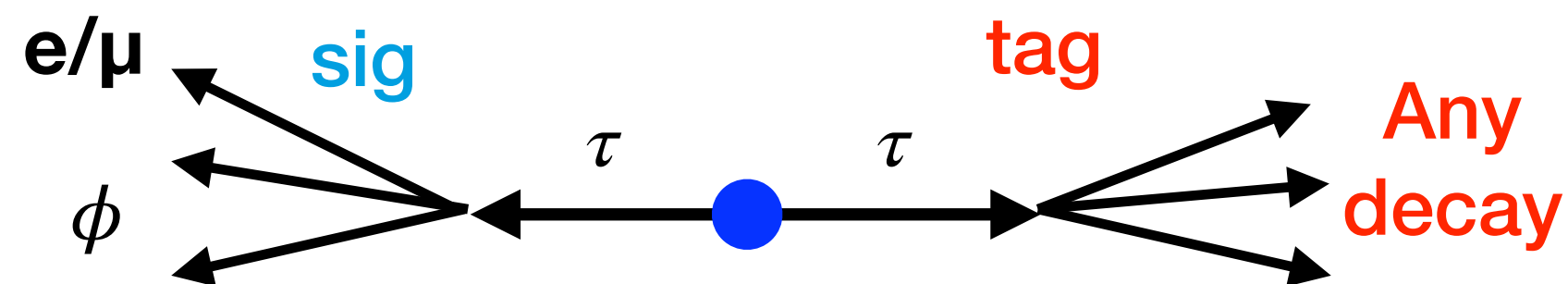
Belle II analysis where  $V^0 = \phi$

ref: <https://arxiv.org/pdf/2305.04759.pdf>



First application of untagged approach with  $190 \text{ fb}^{-1}$

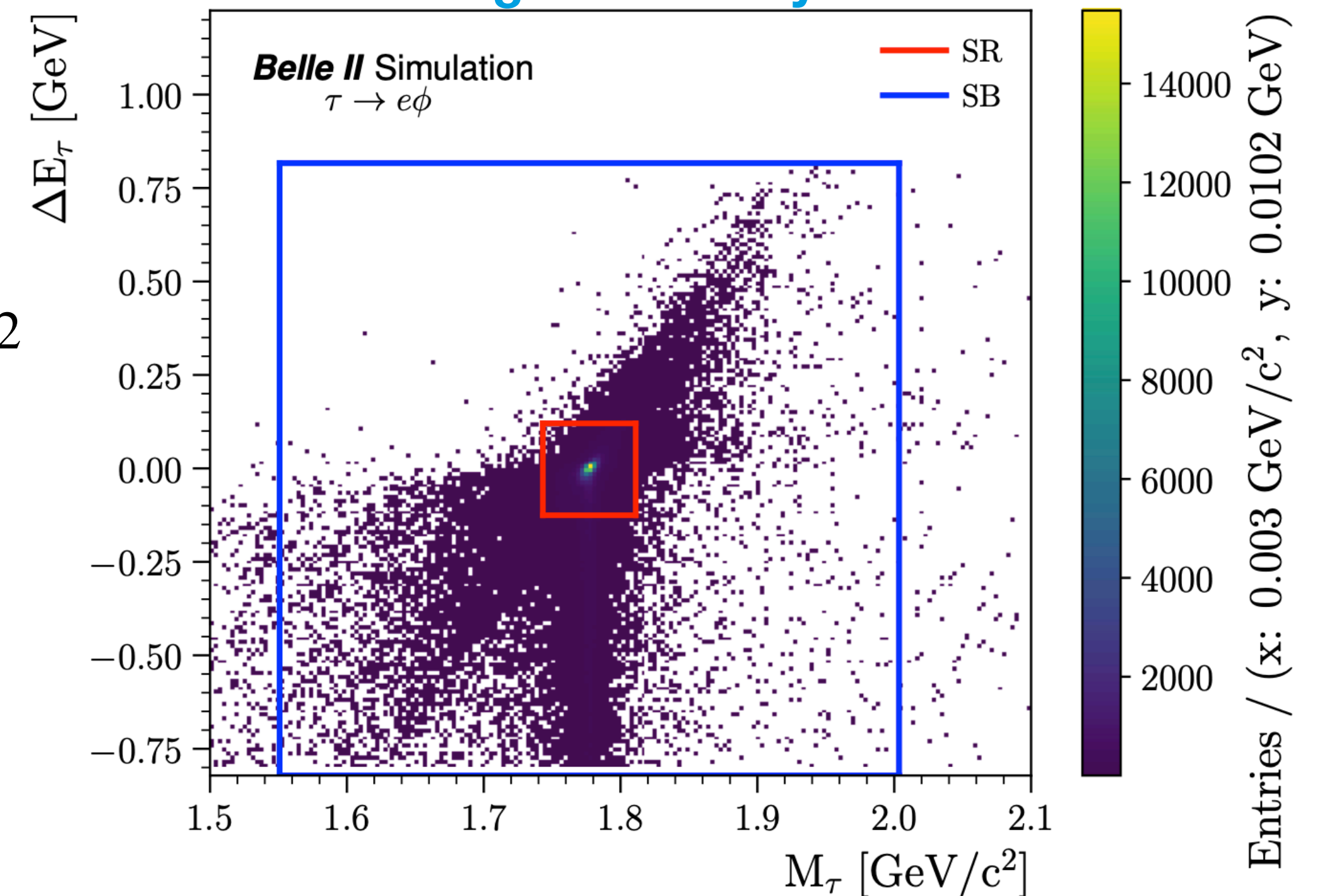
Untagged reconstruction approach



Analysis steps

- Definition of a Signal Region (SR) via the  $M_{l\phi}$  and  $\Delta E_{l\phi} = E_{l\phi}^* - \sqrt{s}/2$
- Event selection and background rejection using via BDT

Signal MC only



# Analysis steps for $\tau \rightarrow l\phi$ @Belle II

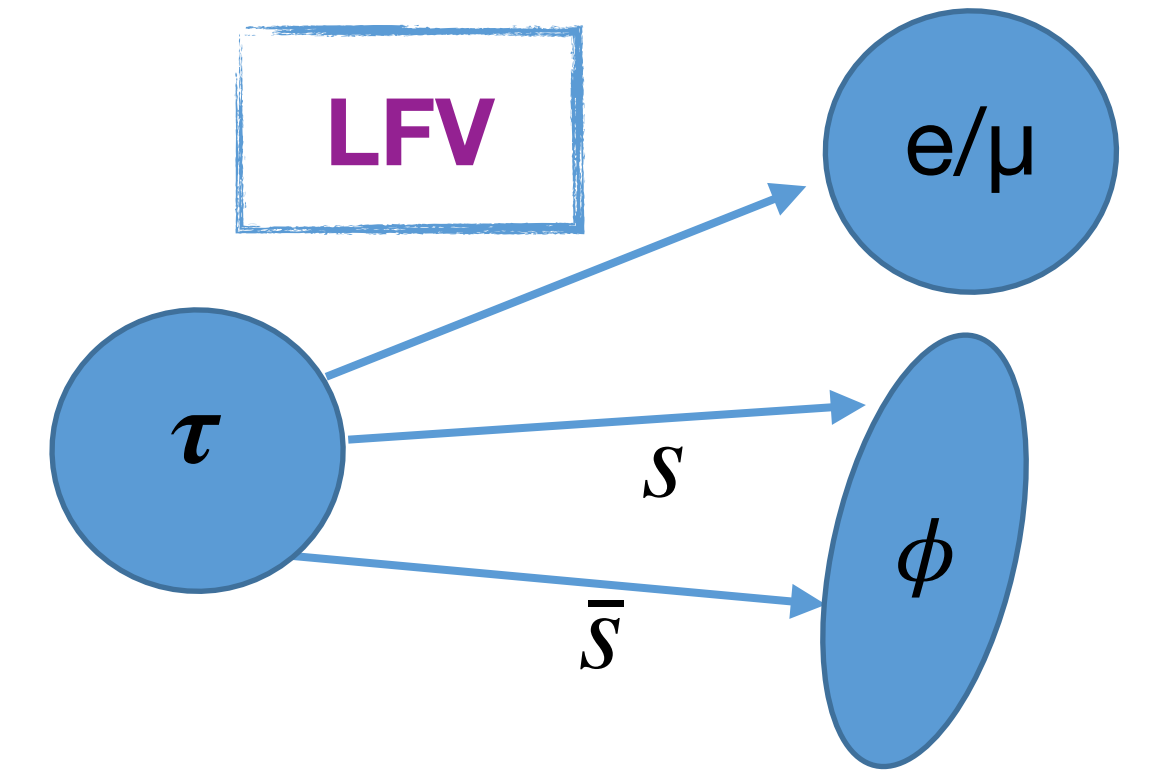
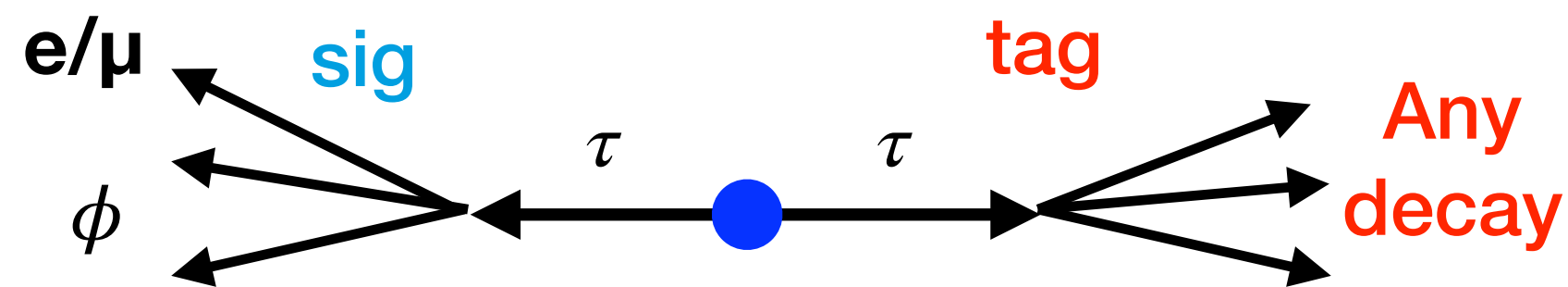
Belle II analysis where  $V^0 = \phi$

ref: <https://arxiv.org/pdf/2305.04759.pdf>



First application of untagged approach with  $190 \text{ fb}^{-1}$

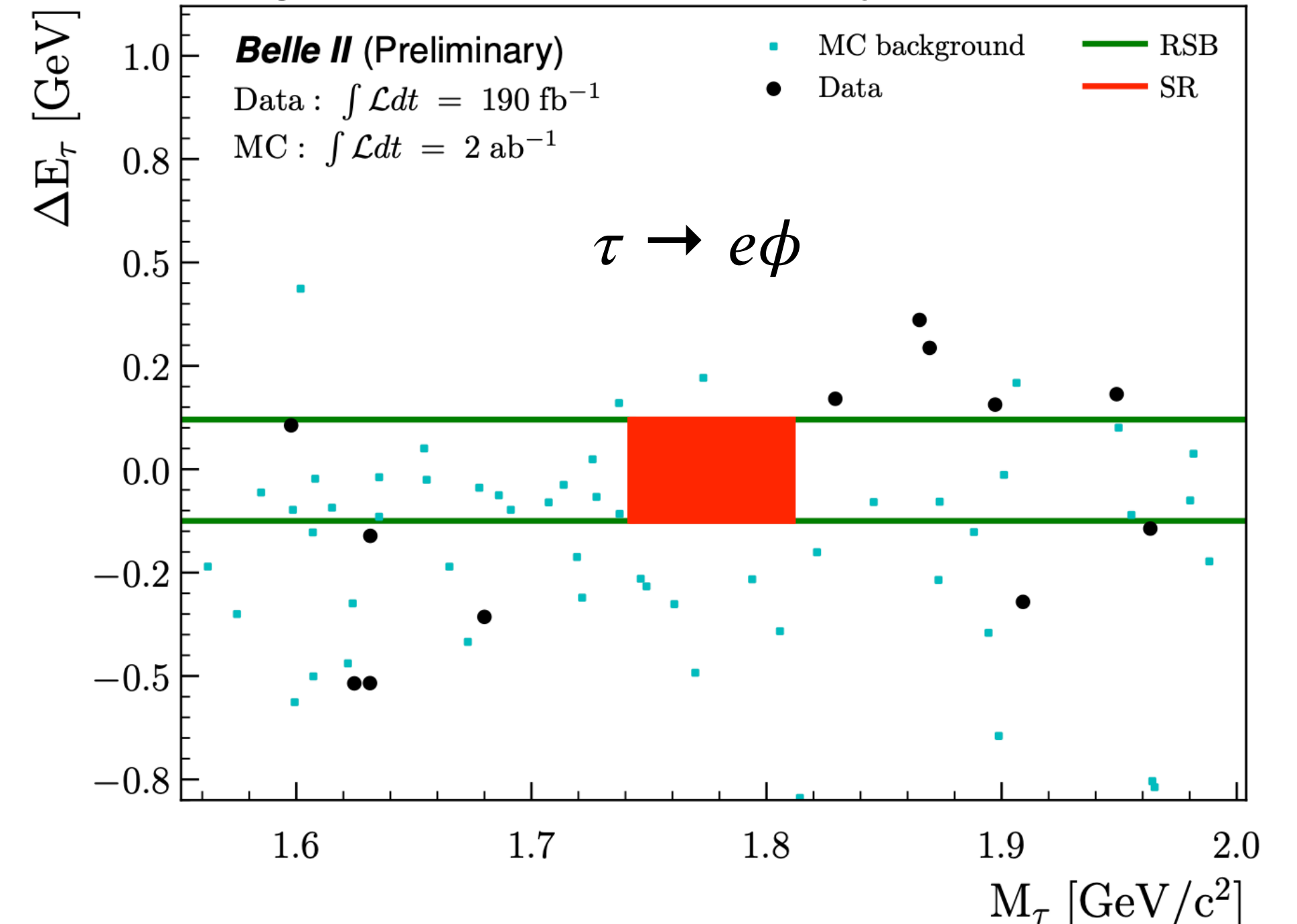
Untagged reconstruction approach



Analysis steps

- Definition of a Signal Region (SR) via the  $M_{l\phi}$  and  $\Delta E_{l\phi} = E_{l\phi}^* - \sqrt{s}/2$
- Event selection and background rejection using via BDT
- Background events evaluated from data in the sideband

Signal detection efficiency  $\sim 2 \times$  Belle



# Analysis steps for $\tau \rightarrow l\phi$ @Belle II

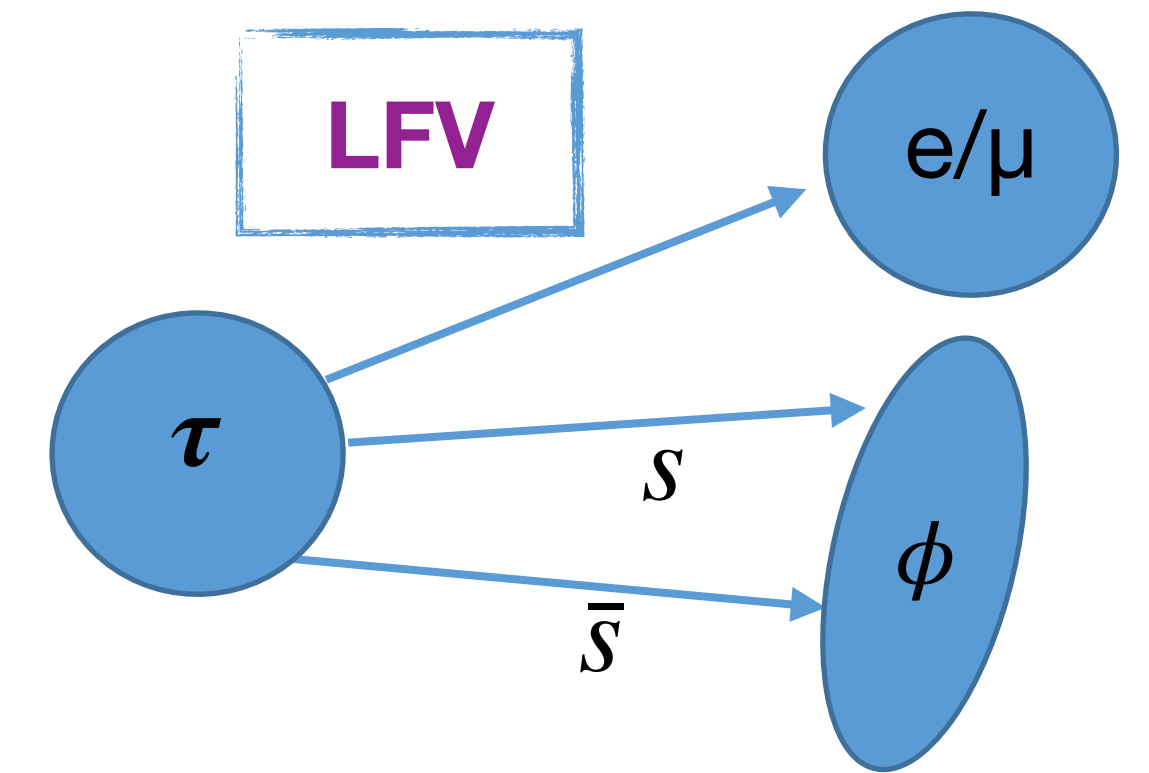
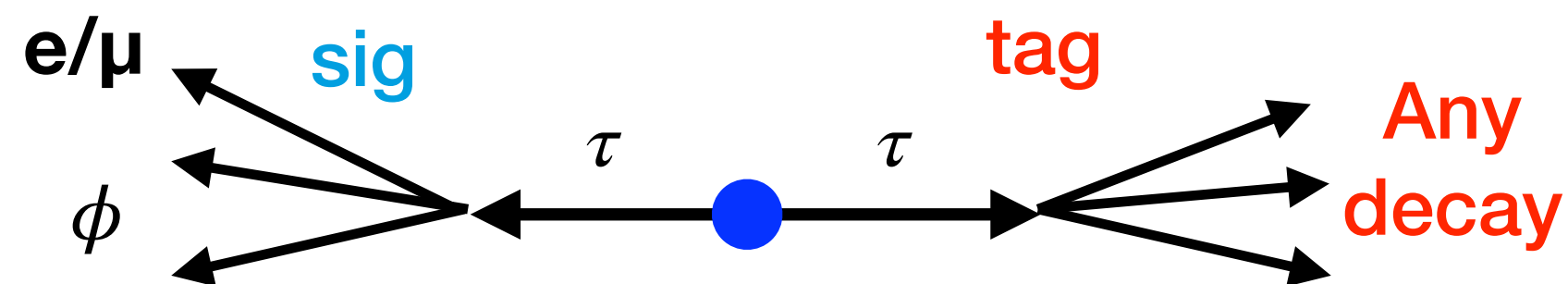
Belle II analysis where  $V^0 = \phi$

ref: <https://arxiv.org/pdf/2305.04759.pdf>



First application of untagged approach with  $190 \text{ fb}^{-1}$

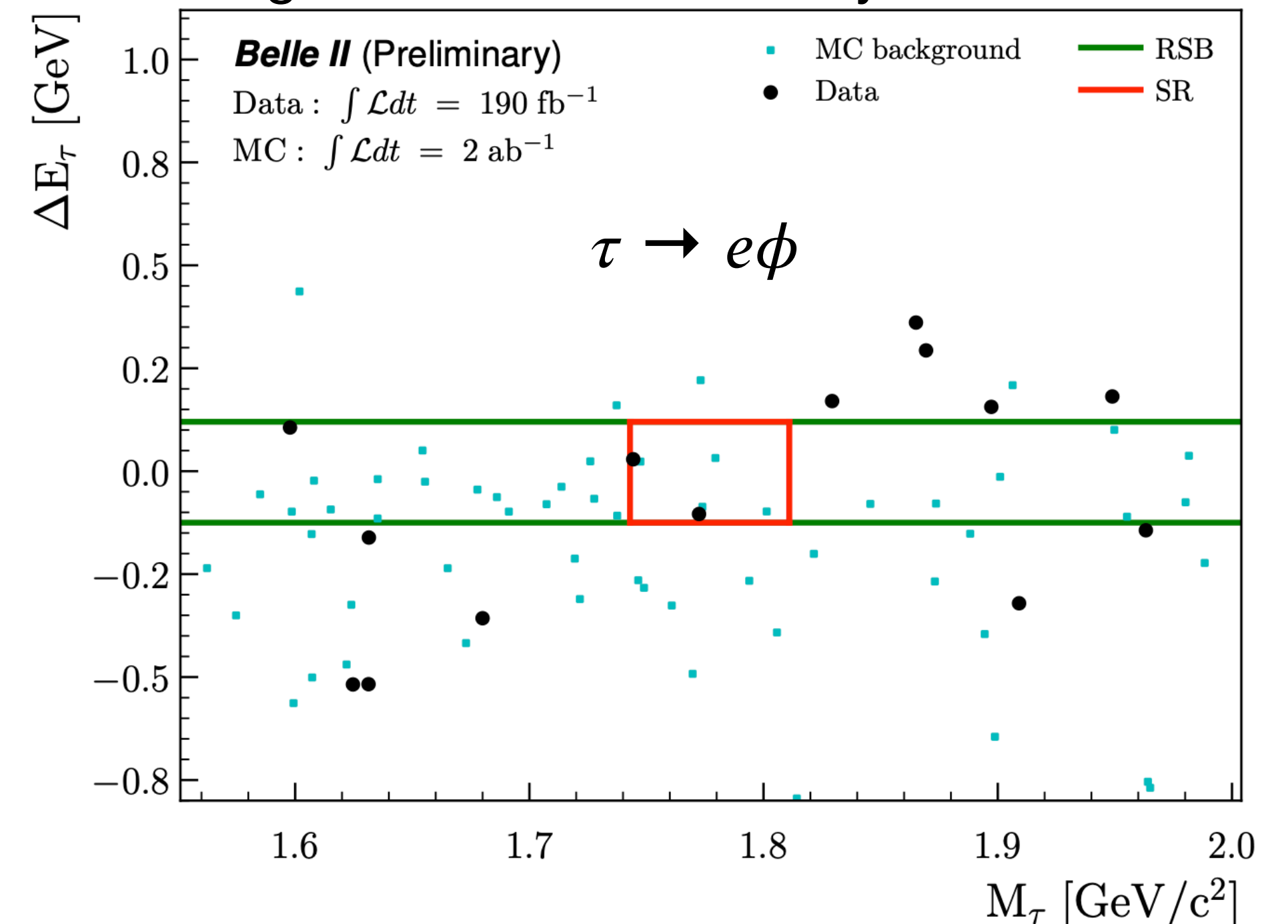
Untagged reconstruction approach



Analysis steps

- Definition of a Signal Region (SR) via the  $M_{l\phi}$  and  $\Delta E_{l\phi} = E_{l\phi}^* - \sqrt{s}/2$
- Event selection and background rejection using via BDT
- Background events evaluated from data in the sideband
- Poisson counting experiment approach in SR

Signal detection efficiency  $\sim 2 \times$  Belle

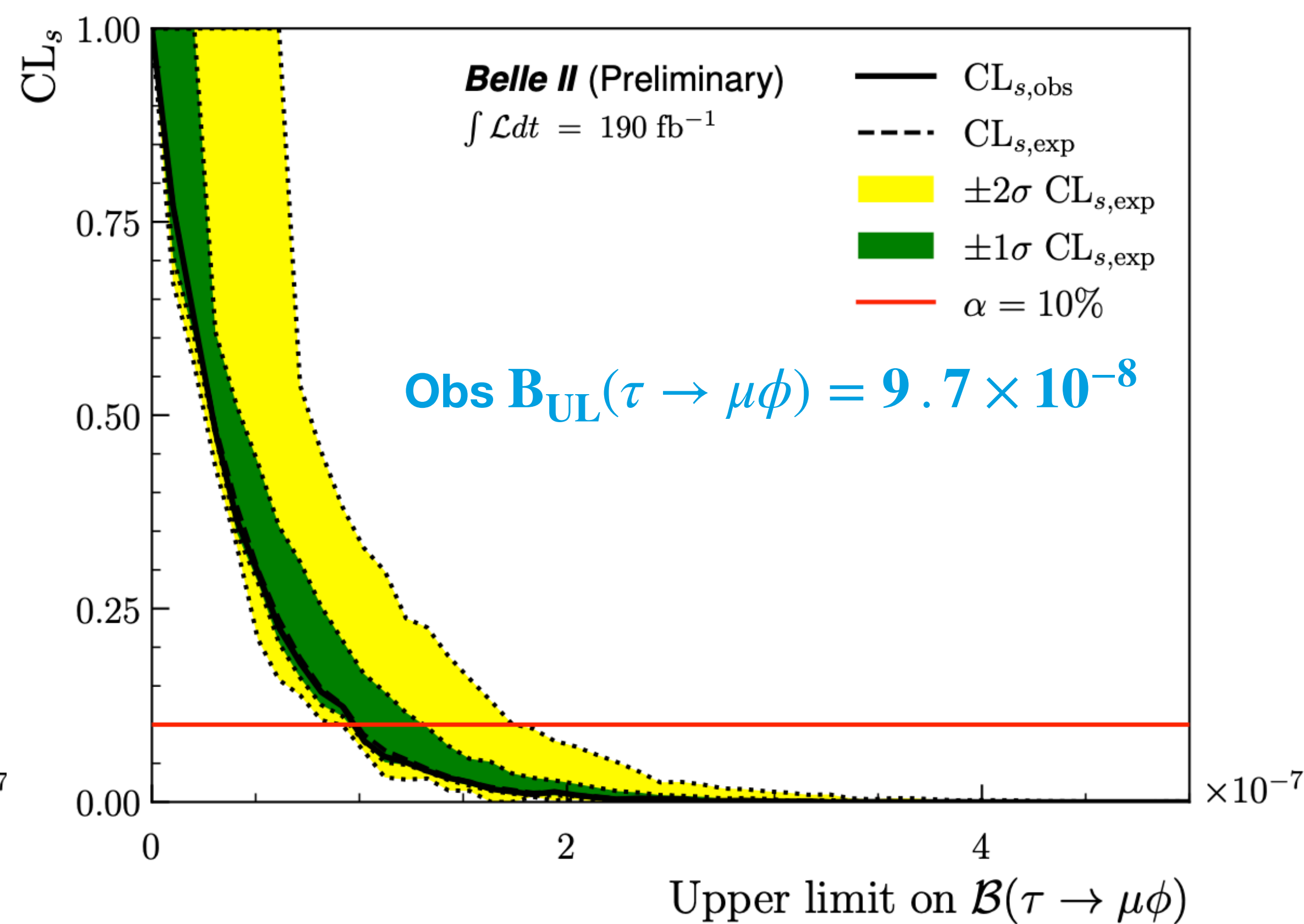
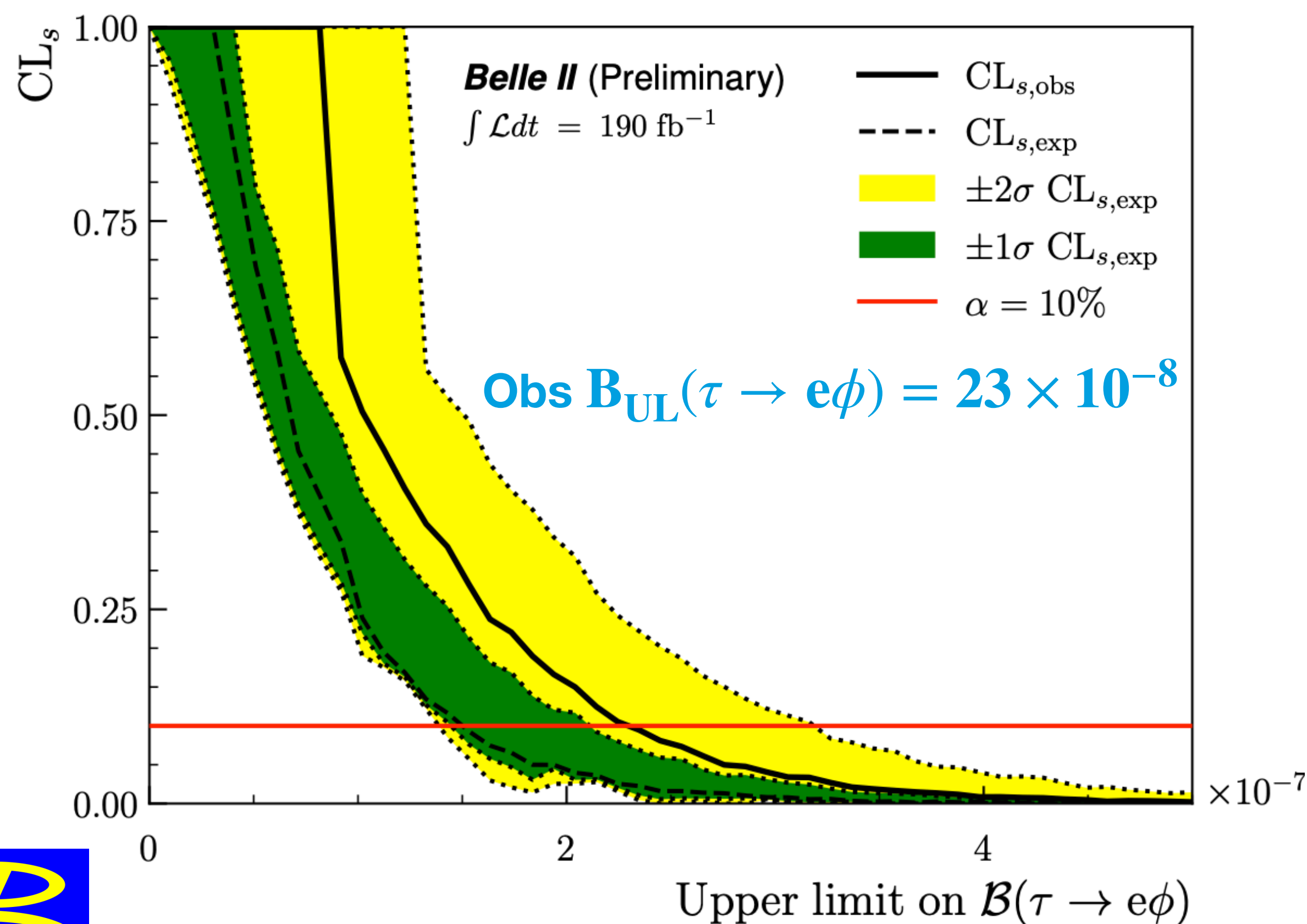


# Results for $\tau \rightarrow l\phi$ @Belle II

No signal evidence  $\rightarrow$  set ULs at 90% CL

Quantity	Region	Mode	
		$e\phi$	$\mu\phi$
$N_{\text{exp}}$	SR	$0.23^{+0.55}_{-0.21}$ (stat)	$0.36^{+0.39}_{-0.23}$ (stat)
$N_{\text{obs}}$	SR	$2.0^{+2.6}_{-1.3}$ (stat)	$0.0^{+1.8}_{-0.0}$ (stat)

Dominant syst. from signal variable mismodeling  
Negligible impact on the limit



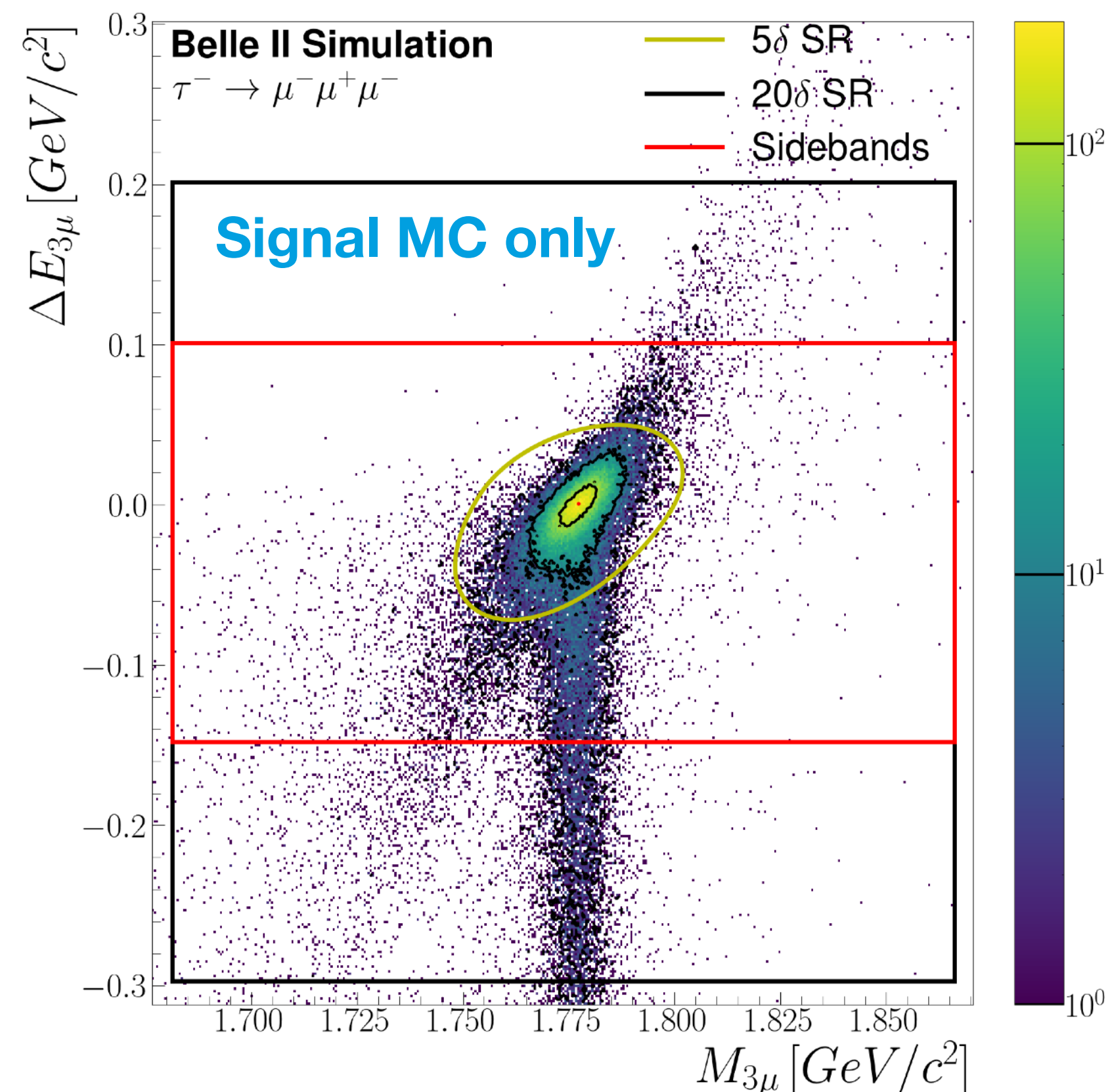
# Analysis of $\tau \rightarrow 3\mu$ @ Belle II

Best upper limits on  $\tau \rightarrow 3\mu$  from Belle:  $2.1 \times 10^{-8}$  @90% CL with 782 fb<sup>-1</sup> but Belle II is already competitive with 424 fb<sup>-1</sup>

Fully reconstructed decay of the signal tau

- No backgrounds from SM processes
- Tight signal region  $\rightarrow$  large background reduction

using  $\Delta E_{3\mu} \equiv E_{\tau\text{sig}} - E_{\text{beam}}$  and  $M_{3\mu}$

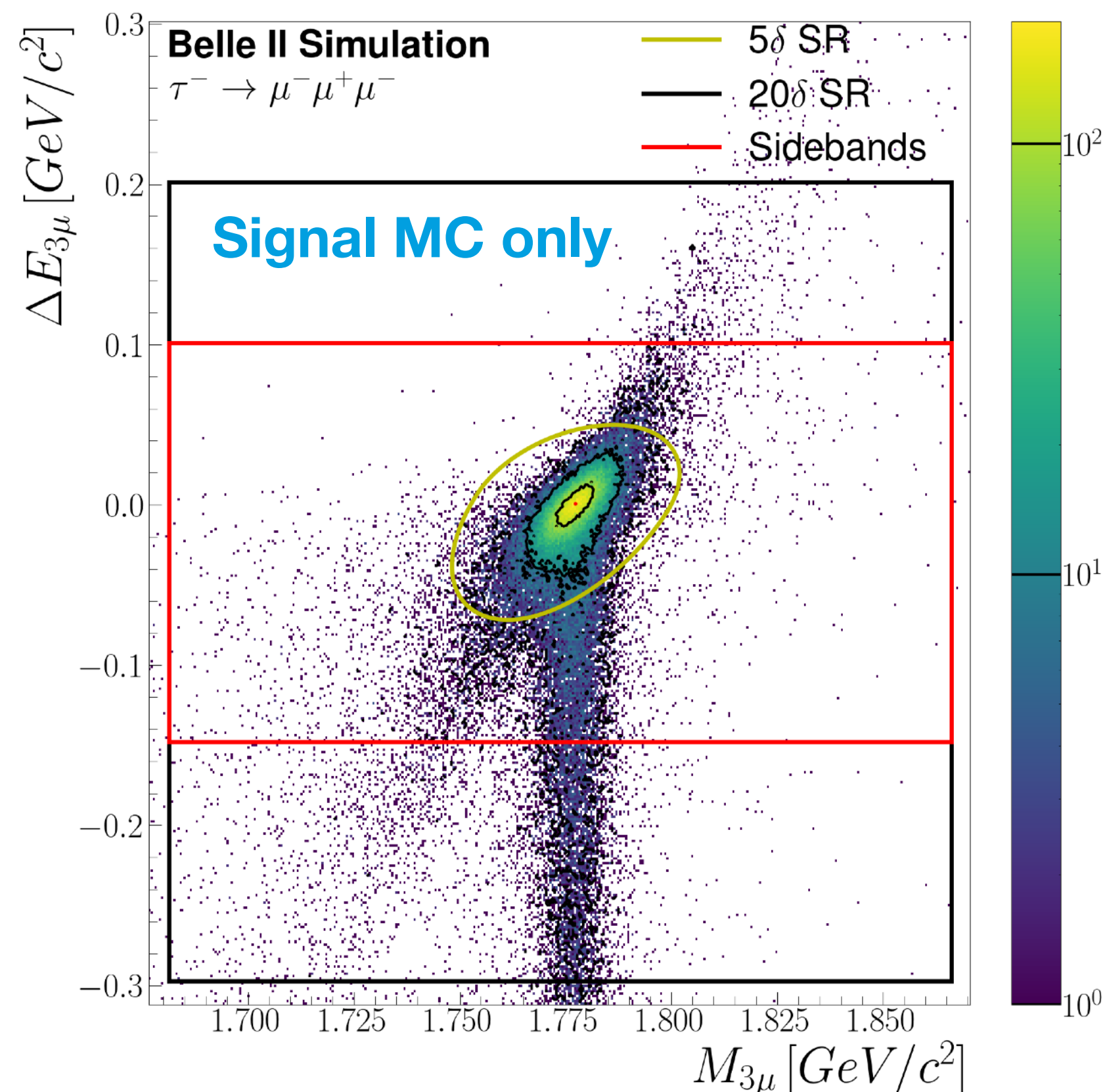


# Analysis of $\tau \rightarrow 3\mu$ @ Belle II

Best upper limits on  $\tau \rightarrow 3\mu$  from Belle:  $2.1 \times 10^{-8}$  @90% CL with 782 fb<sup>-1</sup> but Belle II is already competitive with 424 fb<sup>-1</sup>

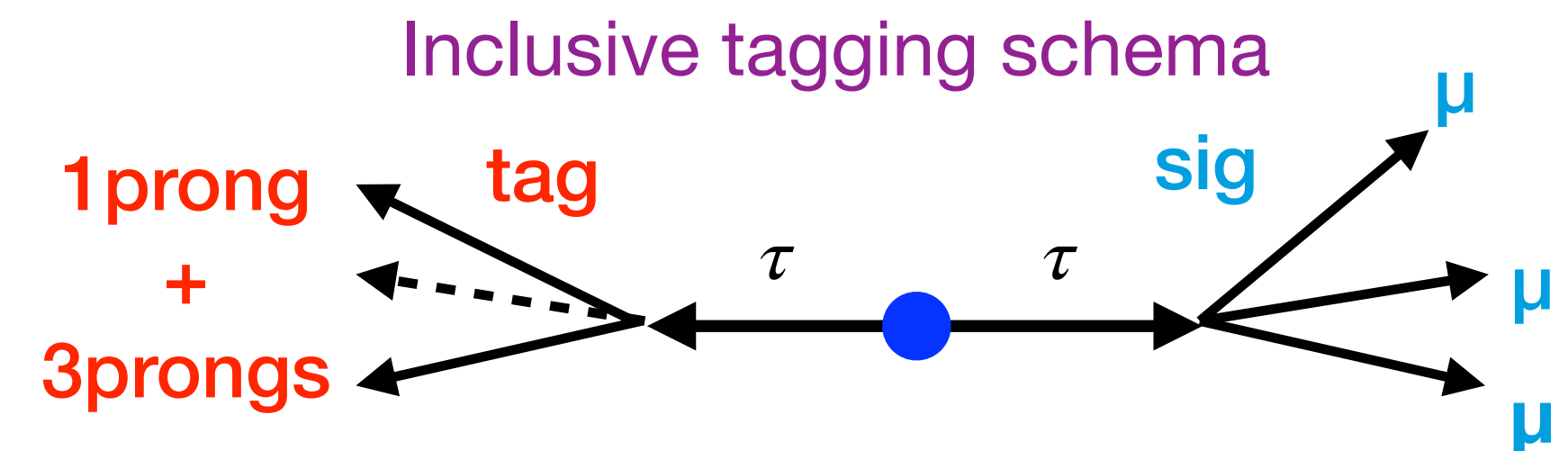
Fully reconstructed decay of the signal tau

- No backgrounds from SM processes
- Tight signal region  $\rightarrow$  large background reduction using  $\Delta E_{3\mu} \equiv E_{\tau\text{sig}} - E_{\text{beam}}$  and  $M_{3\mu}$



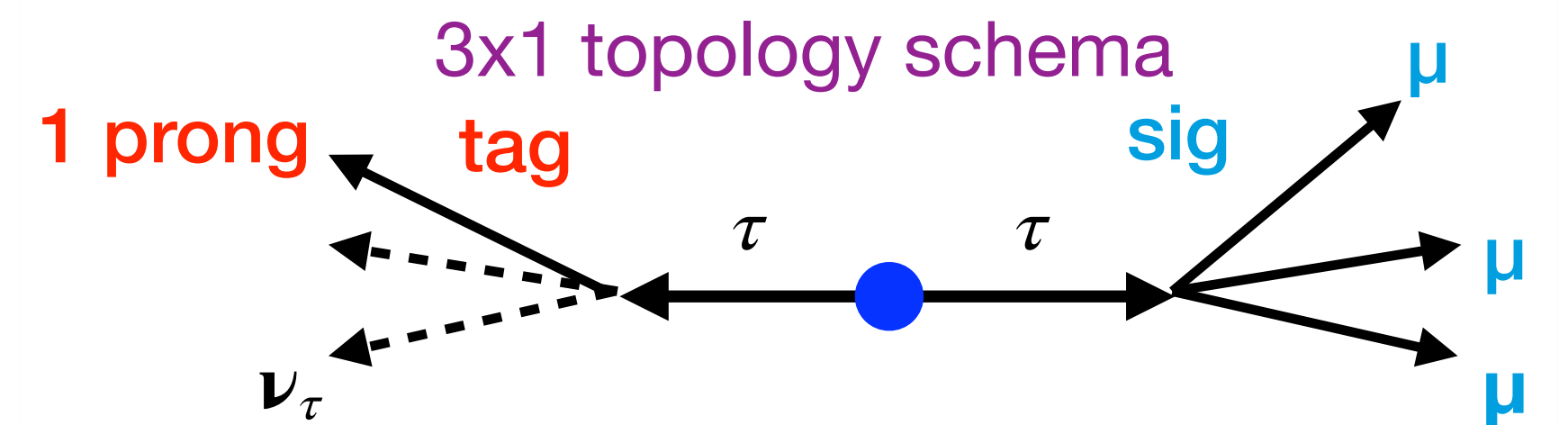
## Main analysis approach:

- Inclusive approach:
  - Selection and background rejection based on BDT
  - Inclusion of 3x1 and 1x1 topologies



## Conventional 3x1 tagging approach:

- muon identification cuts optimised as a function of the track momentum



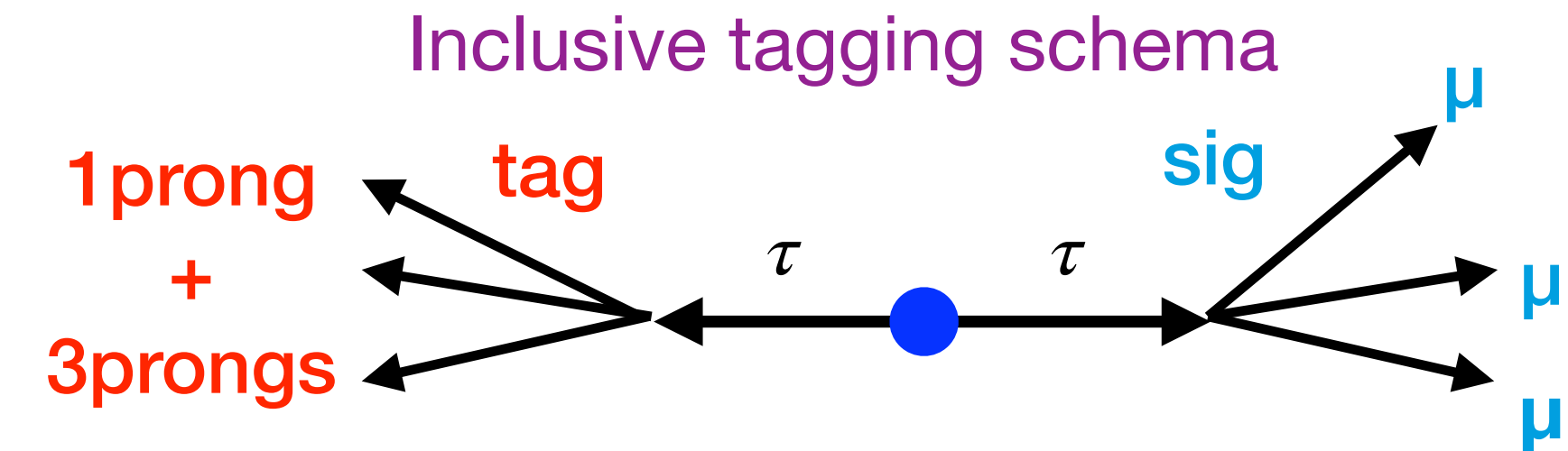
# Results for $\tau \rightarrow 3\mu$ @Belle II: inclusive approach

## Analysis selection and results: inclusive approach

GBoost BDT trained on 32 variables:

- Inputs from: signal  $\tau$ ; event tag side; event shape and kinematics

$\epsilon_{\text{sig}} = 20.42 \pm 0.06\%$  ~3x larger than Belle & Expected BKG:  $0.5^{+1.4}_{-0.5}$  events





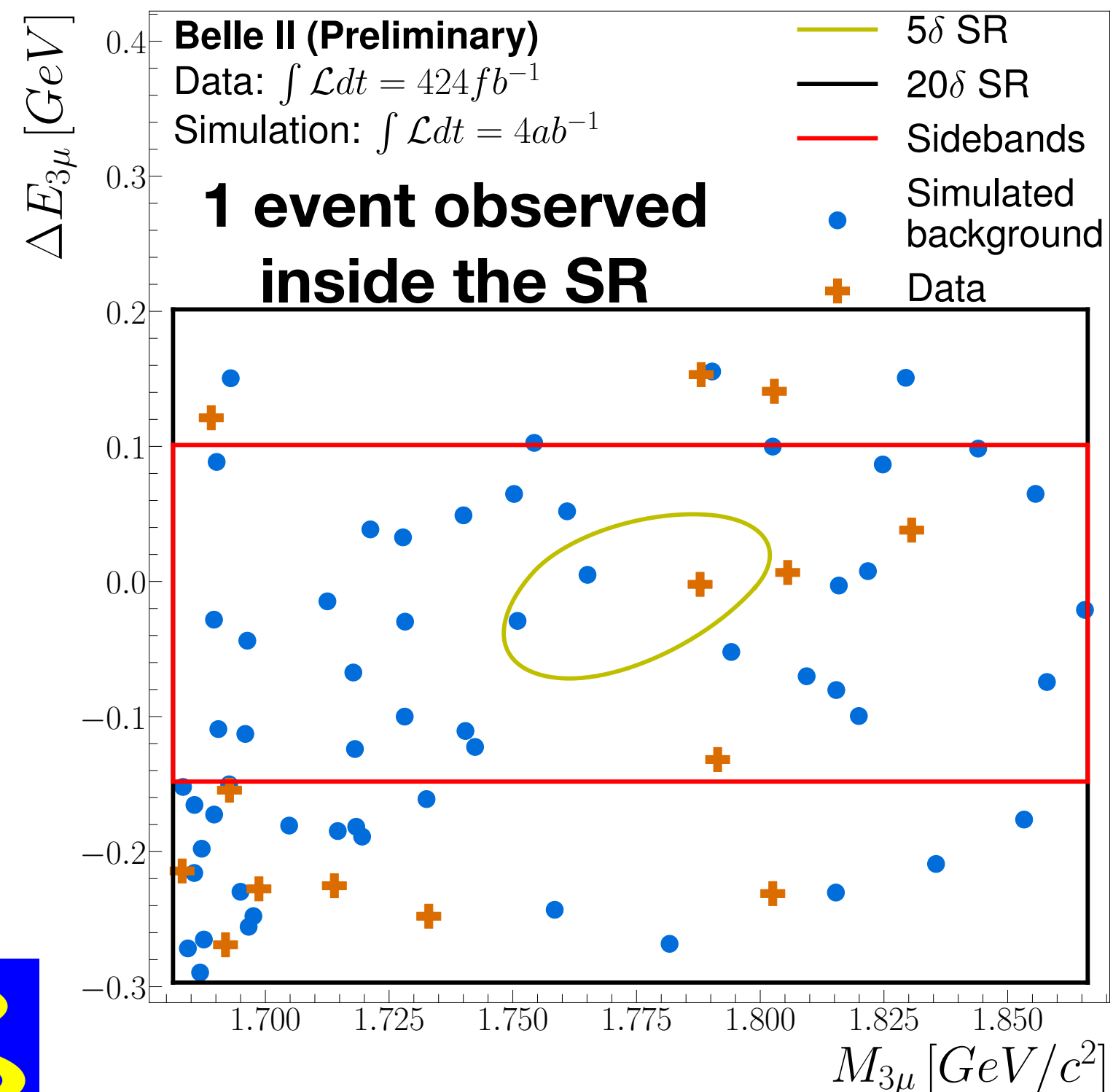
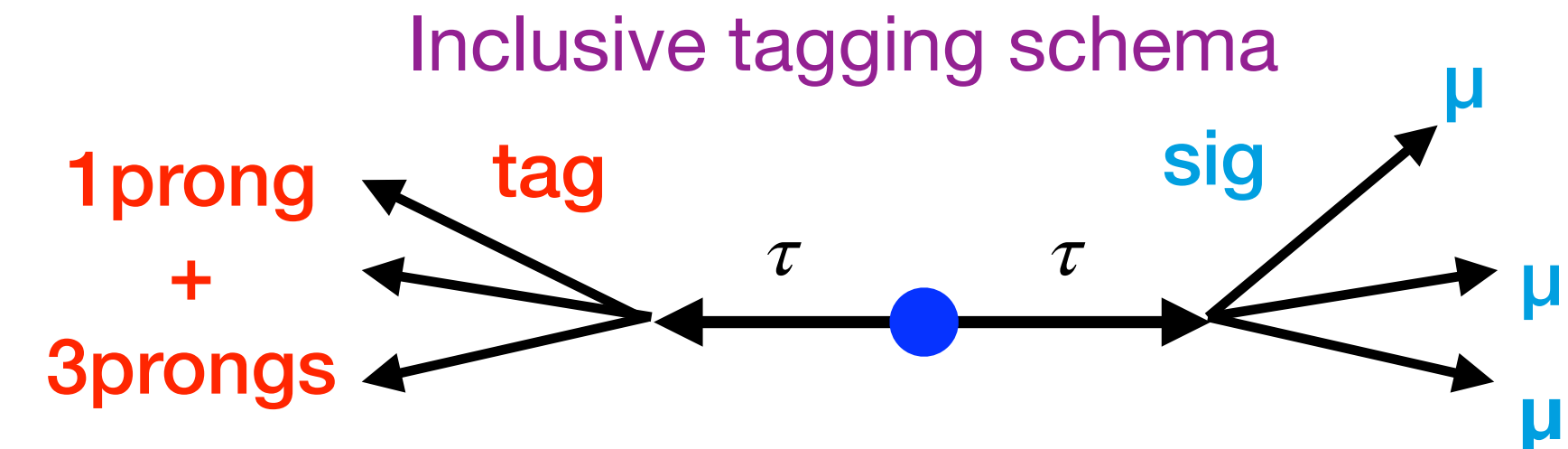
# Results for $\tau \rightarrow 3\mu$ @Belle II: inclusive approach

## Analysis selection and results: inclusive approach

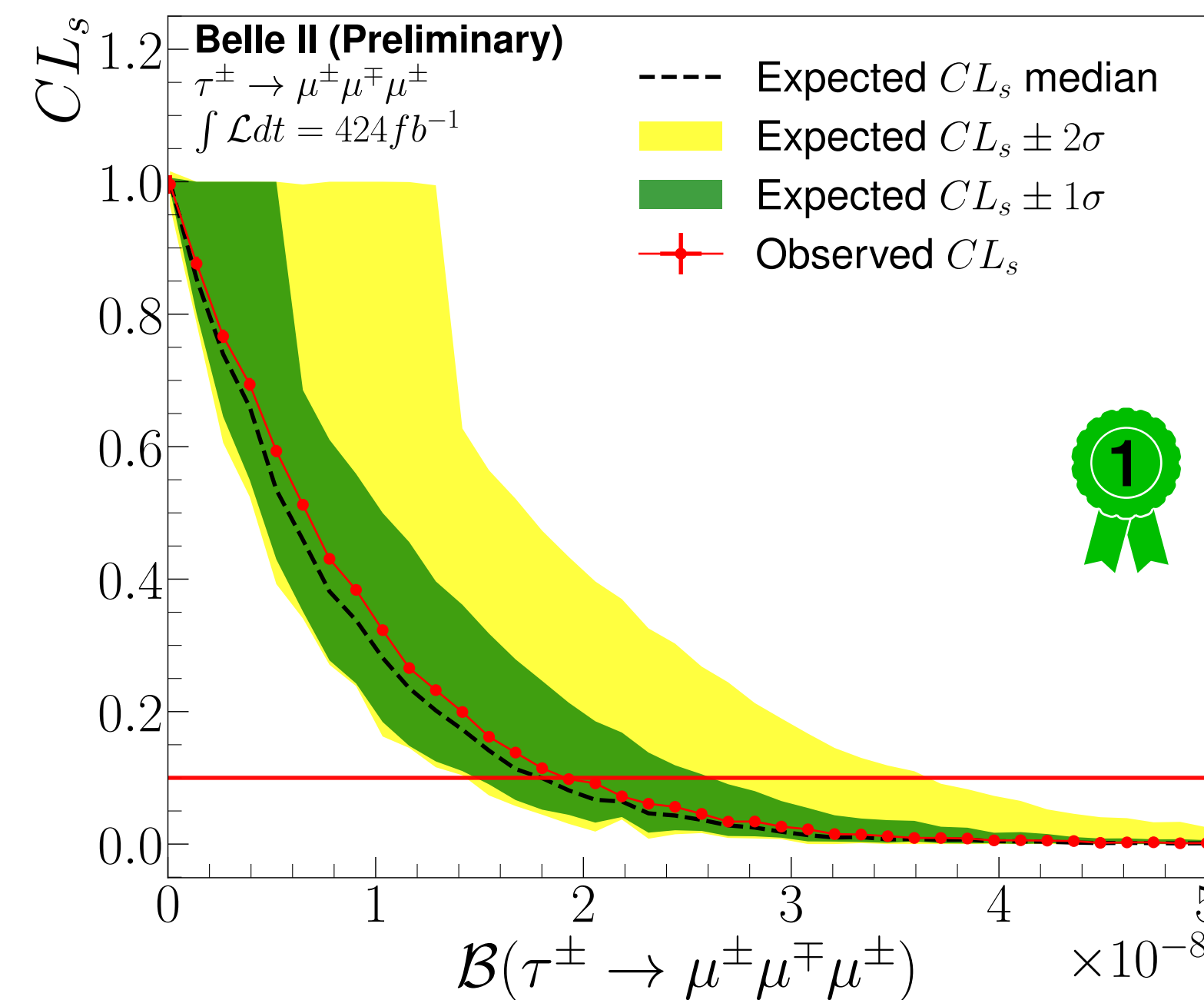
GBoost BDT trained on 32 variables:

- Inputs from: signal  $\tau$ ; event tag side; event shape and kinematics

$\epsilon_{\text{sig}} = 20.42 \pm 0.06\%$  ~3x larger than Belle & Expected BKG:  $0.5^{+1.4}_{-0.5}$  events



No significant excess in  $424 \text{ fb}^{-1}$  of data  $\rightarrow$  90% C.L. upper limits using the CLs method



Dominant syst. from lepton ID efficiency  
Negligible impact on the limit

**Obtained most stringent limit**

$1.9 \times 10^{-8}$





# Summary



- B-factories are a perfect environment for LFV searches on  $\tau$  sector
  - Belle and Belle II are also a  $\tau$ -factories!

★ World best result!

- New high profile searches:

- $\tau \rightarrow IV^0$  @Belle & Belle II and  $\tau \rightarrow 3\mu$  @Belle II



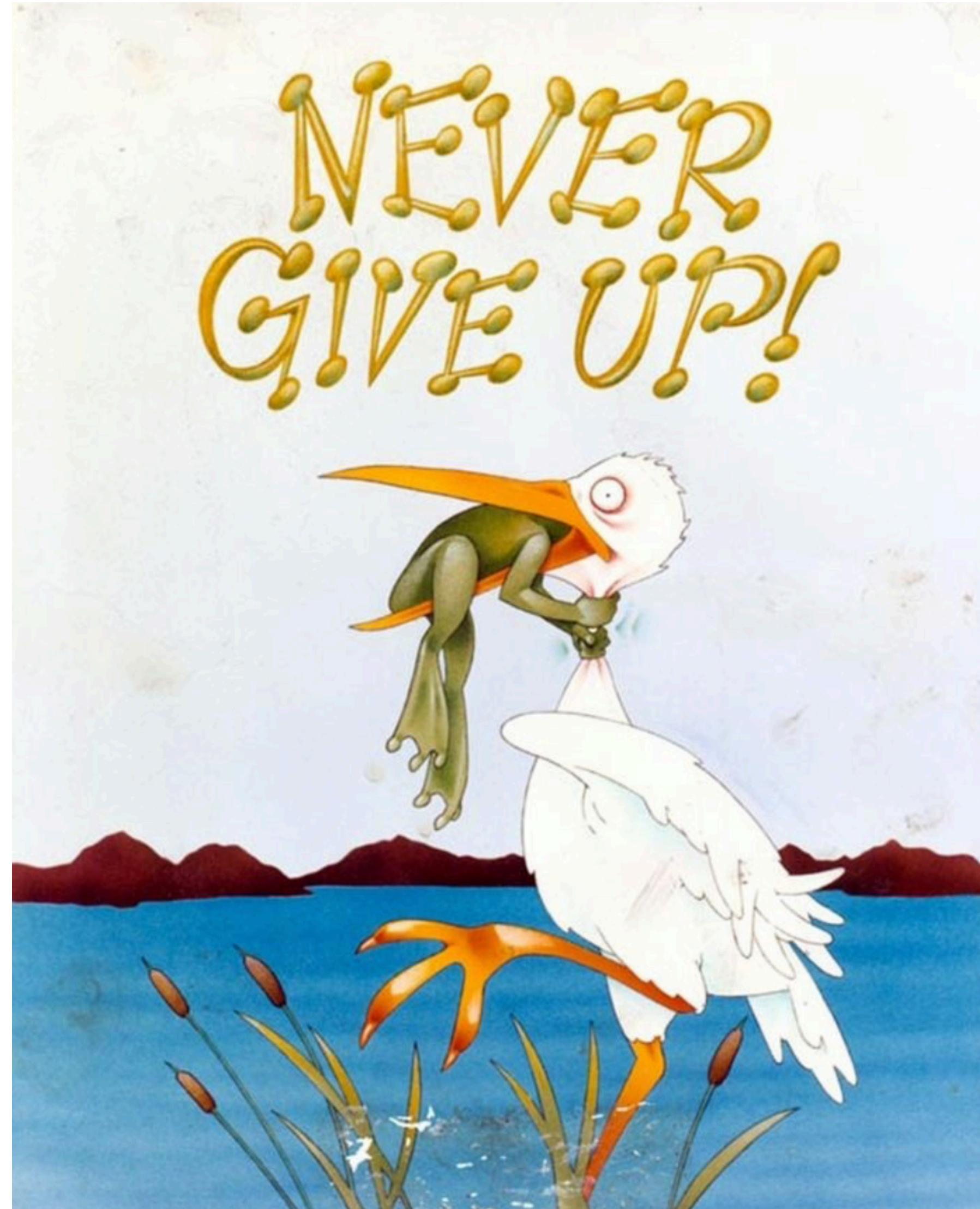
$\tau \rightarrow l\alpha$  search @Belle II  
in Sourav Dey's talk

- Belle II worked hard to overcome the larger samples from Belle/BABAR to produce competitive limits
- More results to come with a larger dataset so stay tuned!

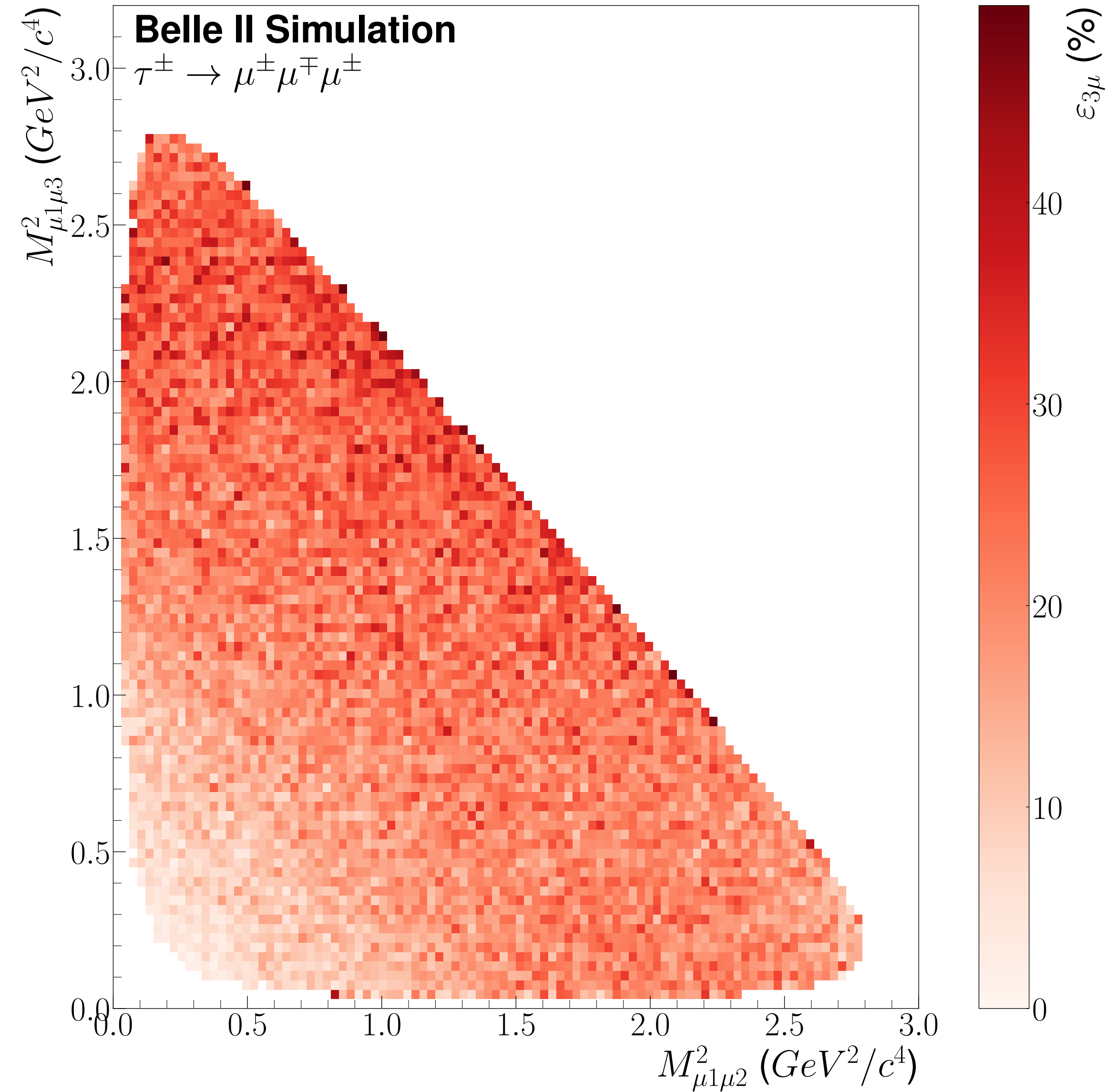
*Thank  
you*



# Emergency slides!!



# Phase space for the $\tau \rightarrow 3\mu$ search



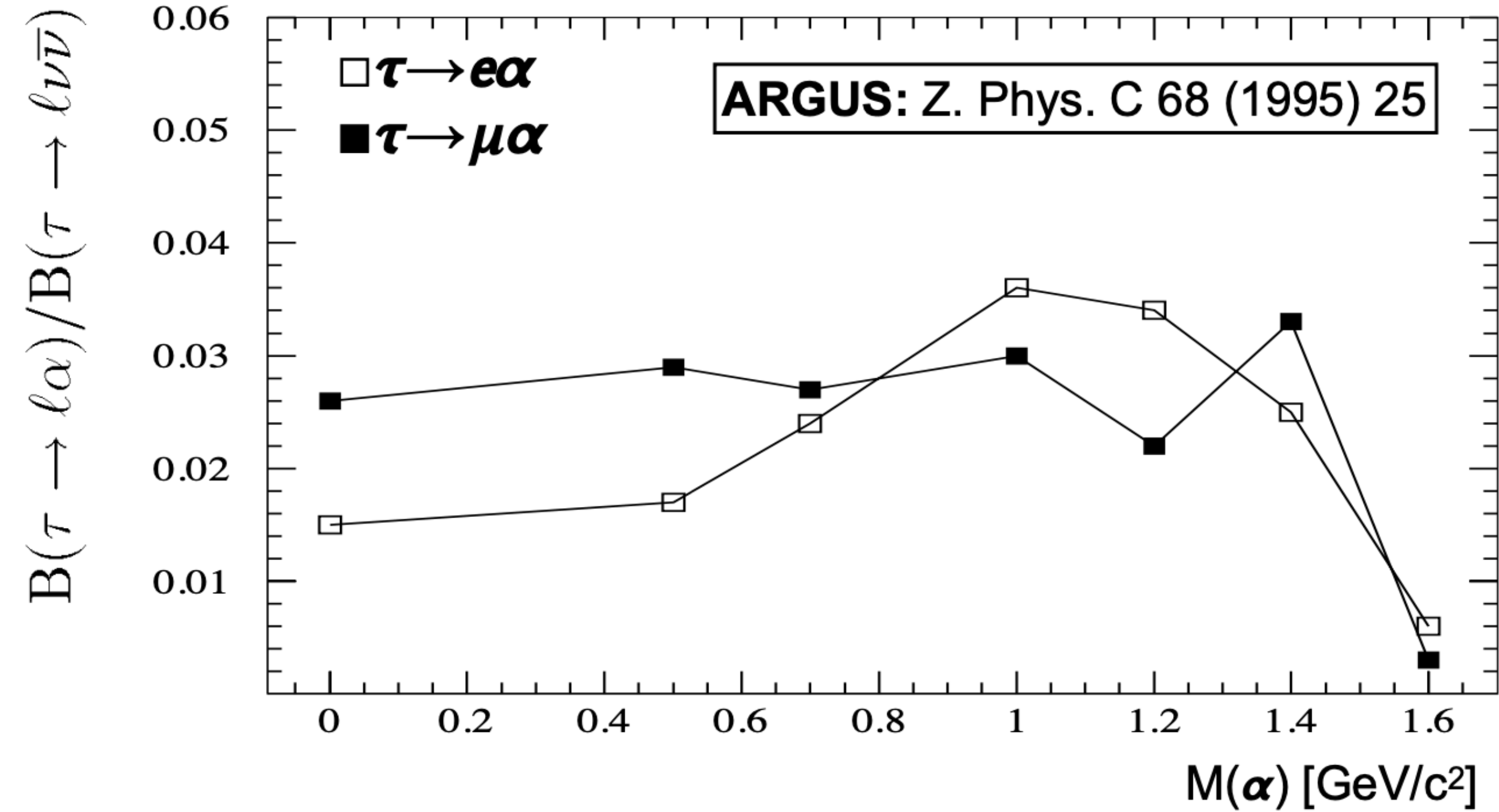
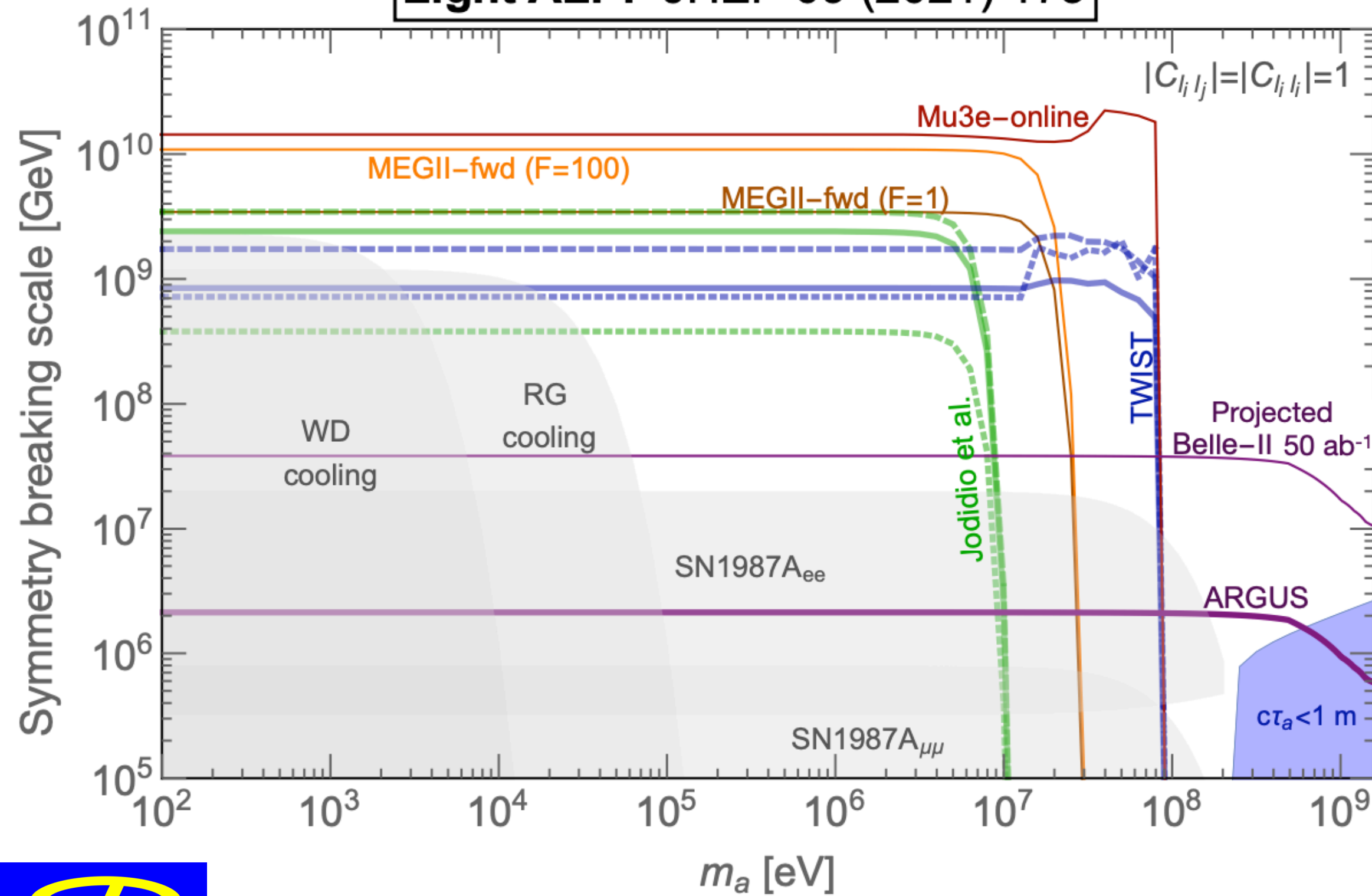
Quite uniform  
distribution, a part for  
low masses

# $\tau \rightarrow l\alpha$ motivation

Search for LFV two-body decay  $\tau \rightarrow l + \alpha$  ( $l = e, \mu$ )  
 $\alpha$  is an invisible gauge boson that can be predicted by several NP models  $\rightarrow$  LFV  $Z'$ , **light ALP candidate**, more..

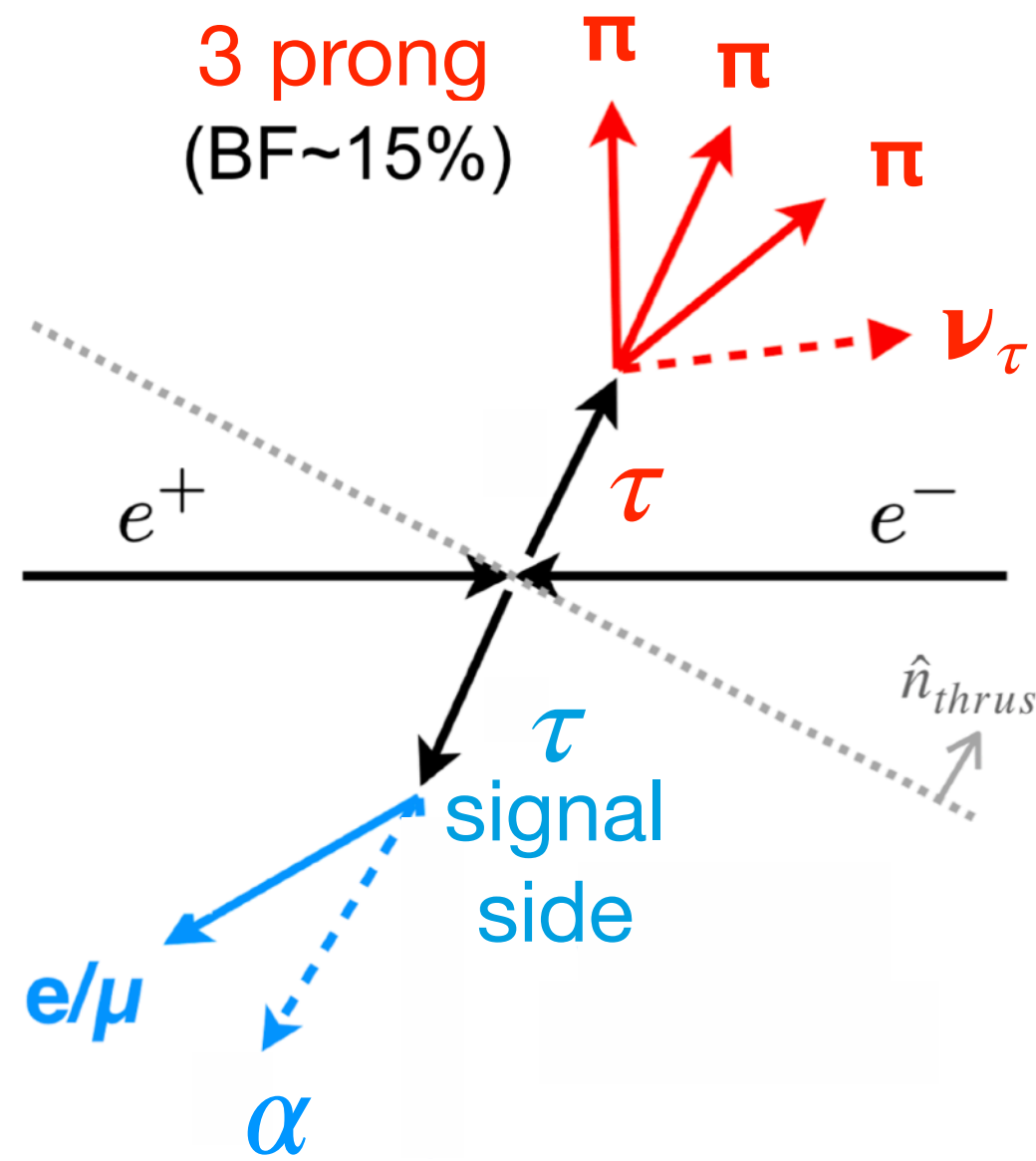
Best upper limits on  $B(\tau \rightarrow l\alpha)/B(\tau \rightarrow l\nu\bar{\nu})$   
 from ARGUS (1995, 476 pb<sup>-1</sup>)

**Light ALP: JHEP 09 (2021) 173**

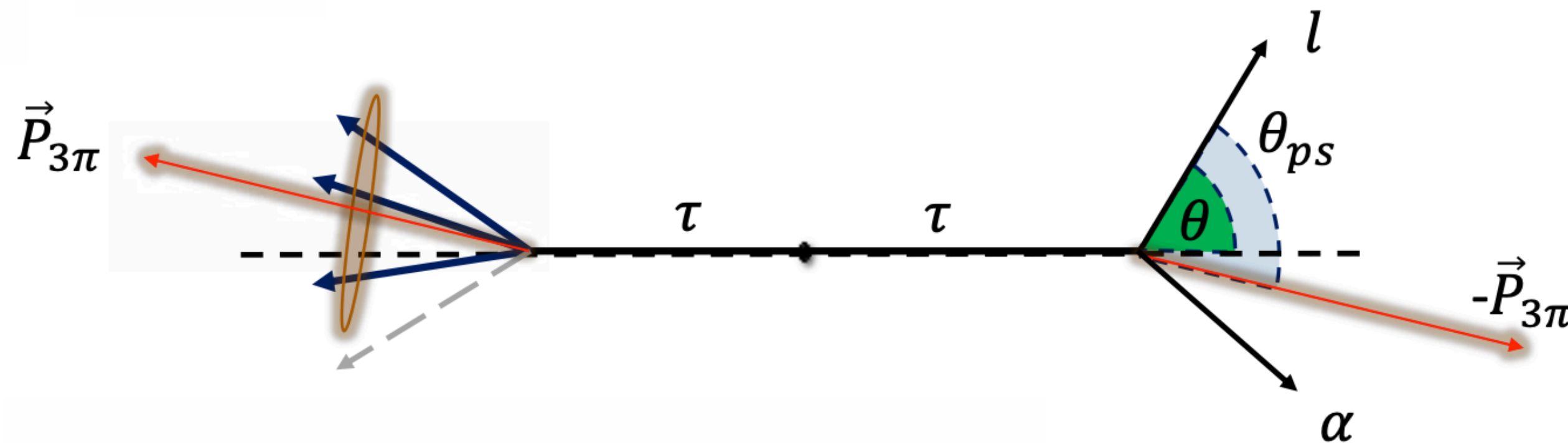


# $\tau \rightarrow l\alpha$ analysis @Belle II

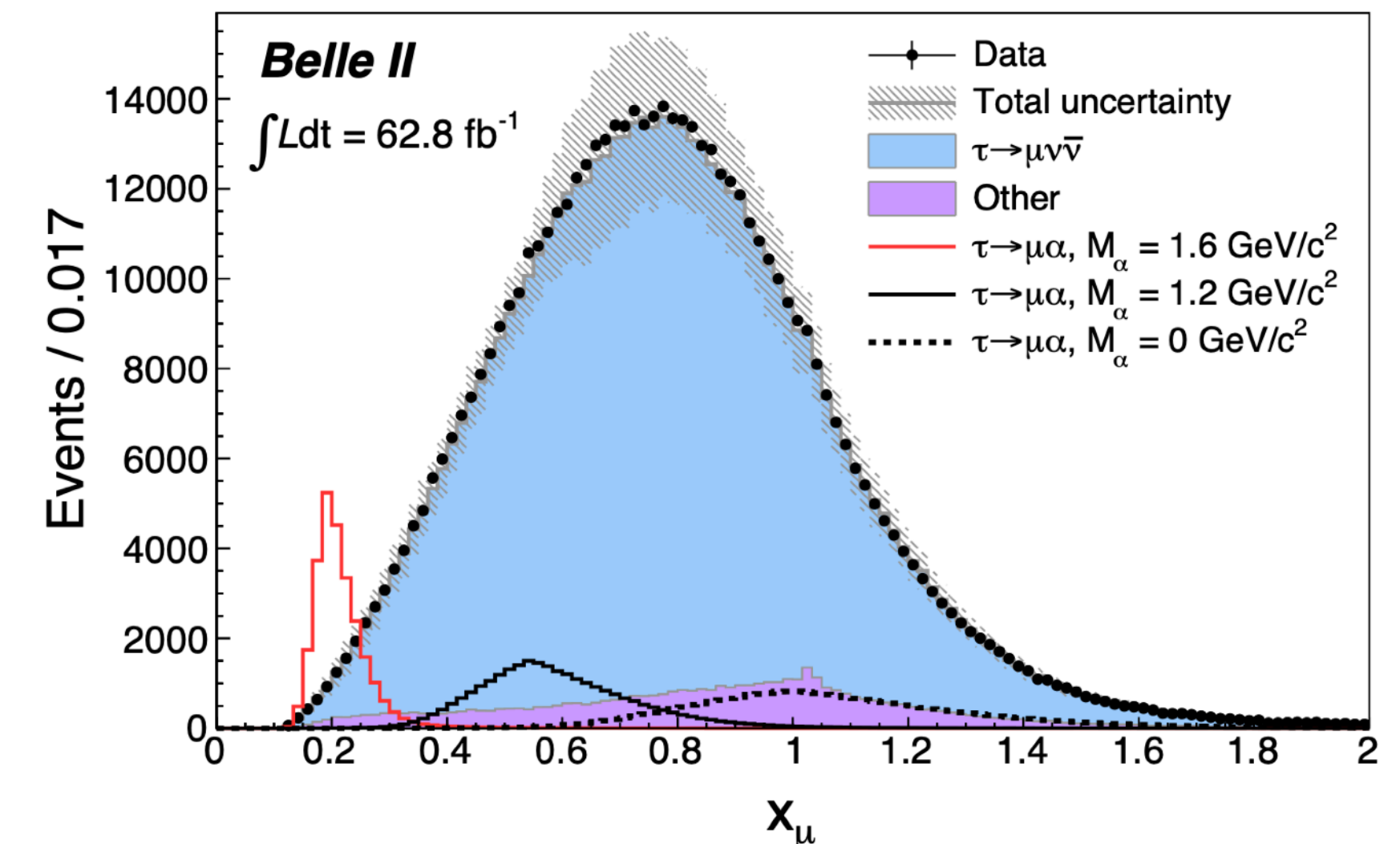
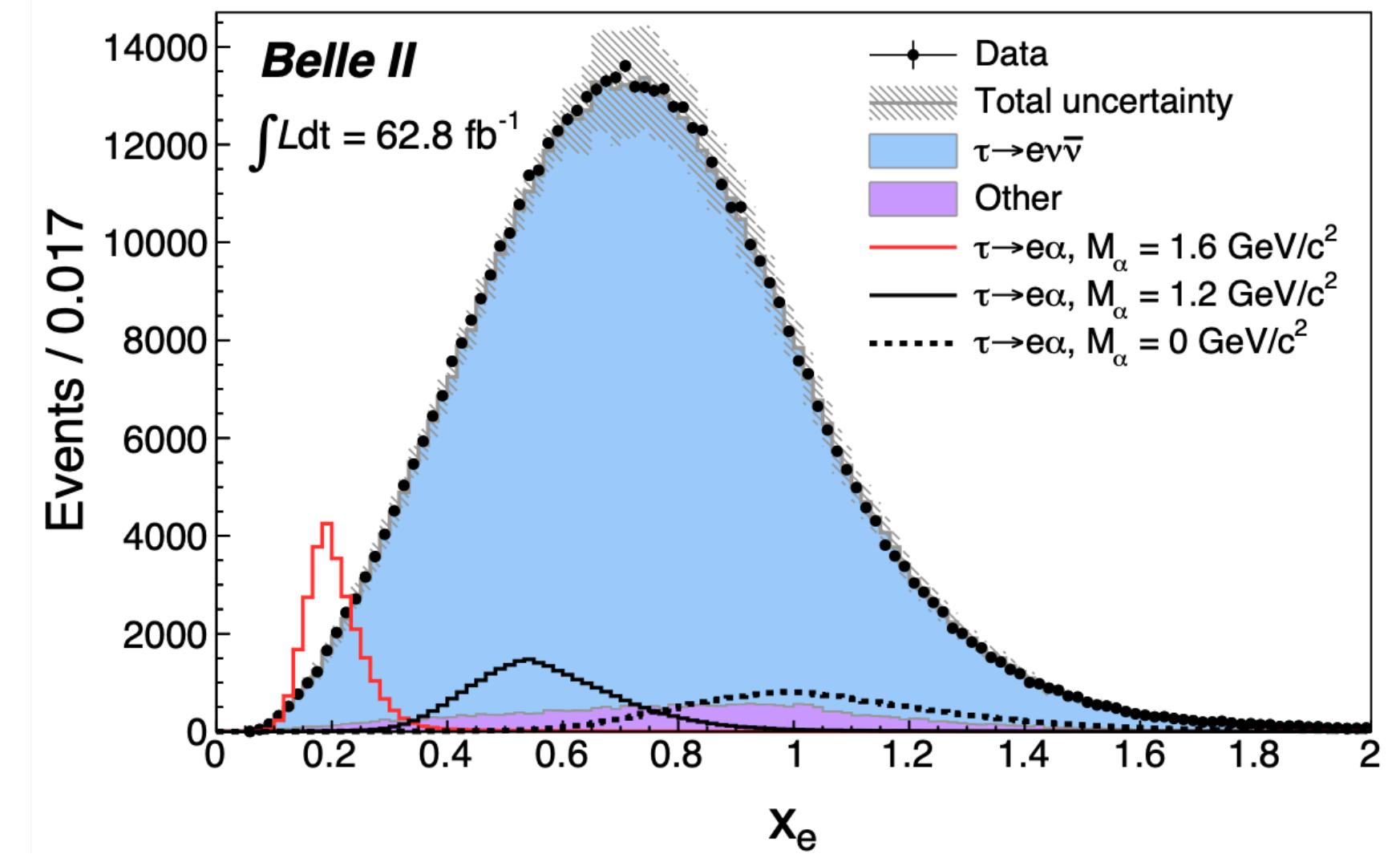
ARGUS analysis approach is adopted  $\rightarrow$  definition of pseudo-rest (ps) frame



- Tag side:  $\tau \rightarrow 3\pi\nu_\tau$
- Pseudo-rest frame implies:
  - $\vec{p}_\tau \sim -\vec{p}_{3\pi}$
  - $E_\tau \sim \sqrt{s}/2$
- Veto neutrals:  $\pi^0, \gamma$
- Selection optimised on  $\tau \rightarrow l\nu\bar{\nu}_\tau$  as irreducible background



Signal signature: bump in the  $x_l \equiv \frac{E_l^*}{m_\tau c^2/2}$  distribution



# Results for $\tau \rightarrow l\alpha$ @ Belle II

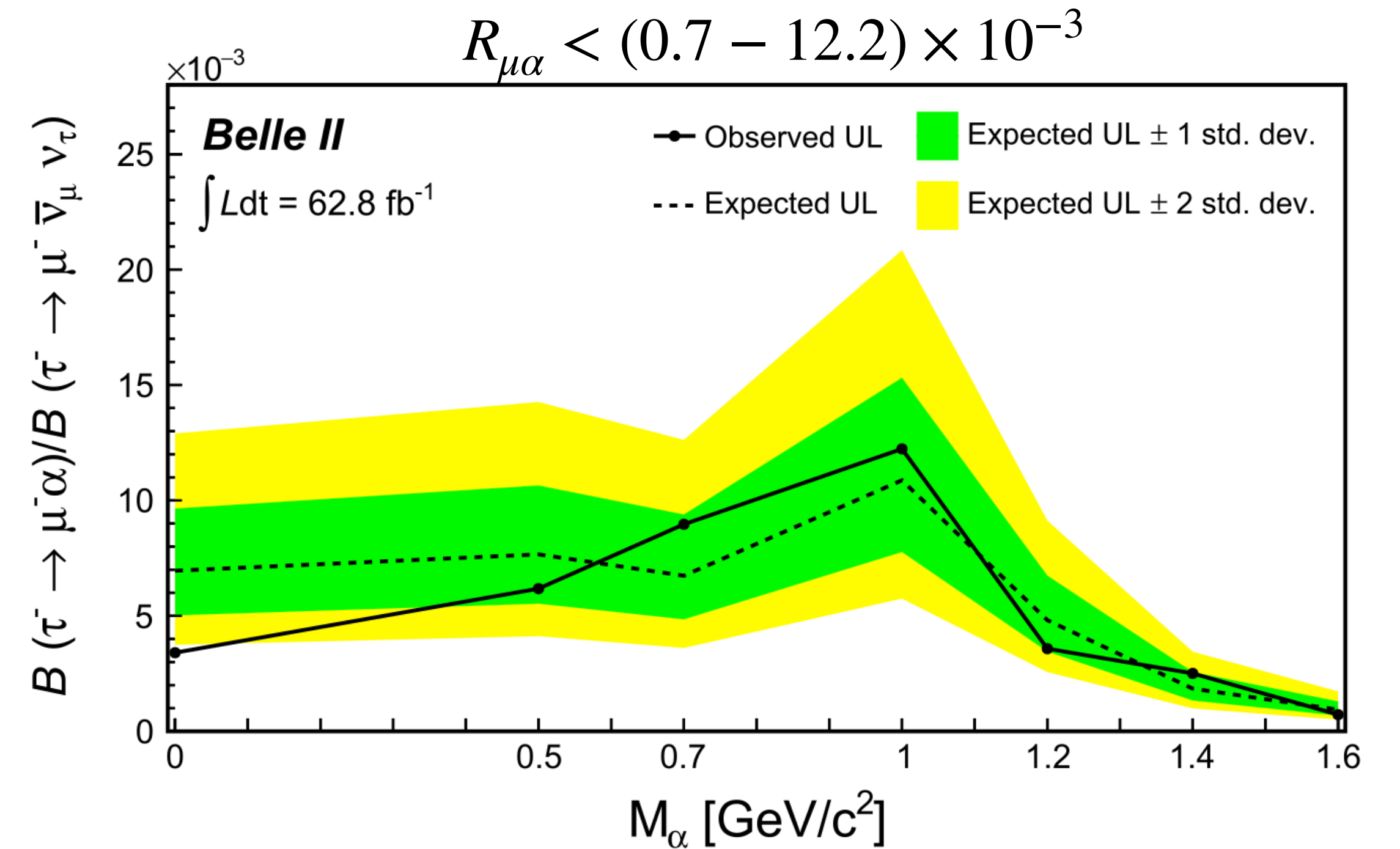
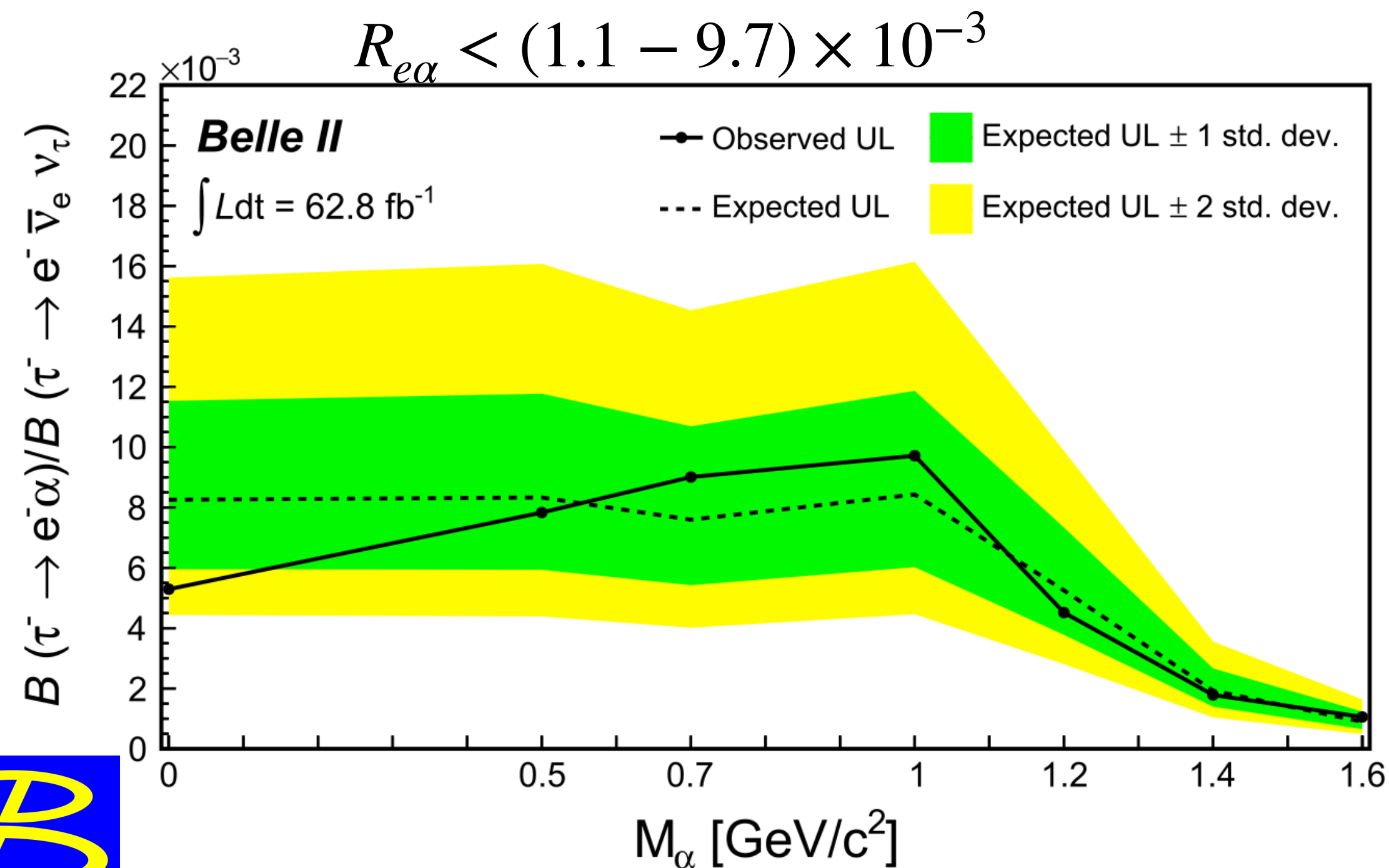
95% C.L. upper limits using the CLs method → **no significant excess in 62.8 fb<sup>-1</sup> of data (2019-20)**

Ref: <https://journals.aps.org/prl/pdf/10.1103/PhysRevLett.130.181803>

Maximum likelihood fit on  $x_l$  distributions → UL on the branching fractions

**Best measurement today: 2.2–14 times more stringent than previous best limits** depending on the value of the  $\alpha$  mass

Dominant syst. from lepton ID efficiency  
Negligible impact on the limit



# Physics: $\tau$ analyses

