

Aspen Winter Conference
New Methods and Ideas at the Frontiers of Particle Physics
March 2022

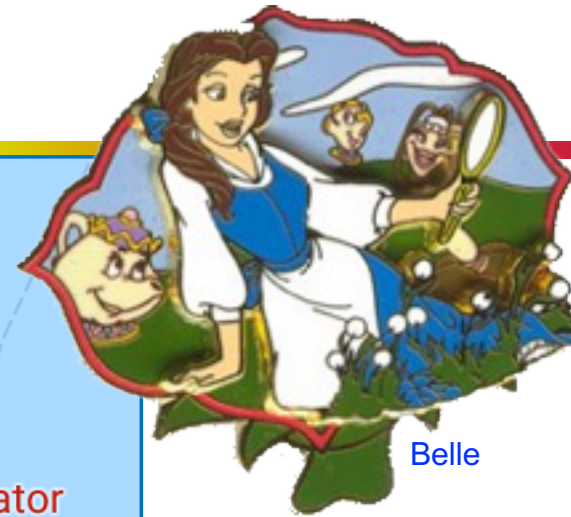


Belle II: Recent Results, Status, and Prospects



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Belle II/SuperKEKB



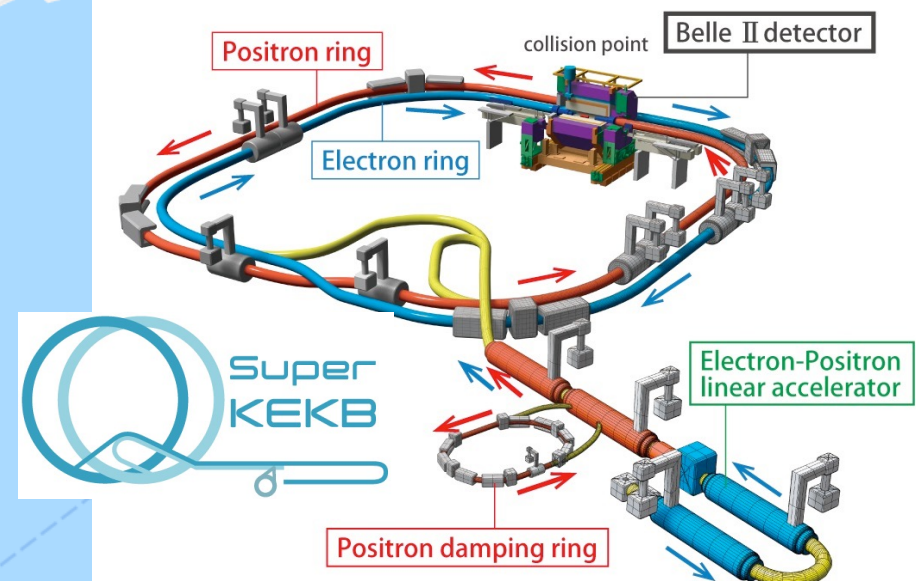
Belle

Belle II Collaboration

≈1100 researchers

>123 institutions

≈26 nations



Motivation

Big Questions

- Origin of generations & role of flavor
- CP violation & baryon asymmetry



Not addressed by Standard Model; need "New Physics" (NP)

Both Questions necessarily involve 3 generations → heavy quarks

Where to look for NP?

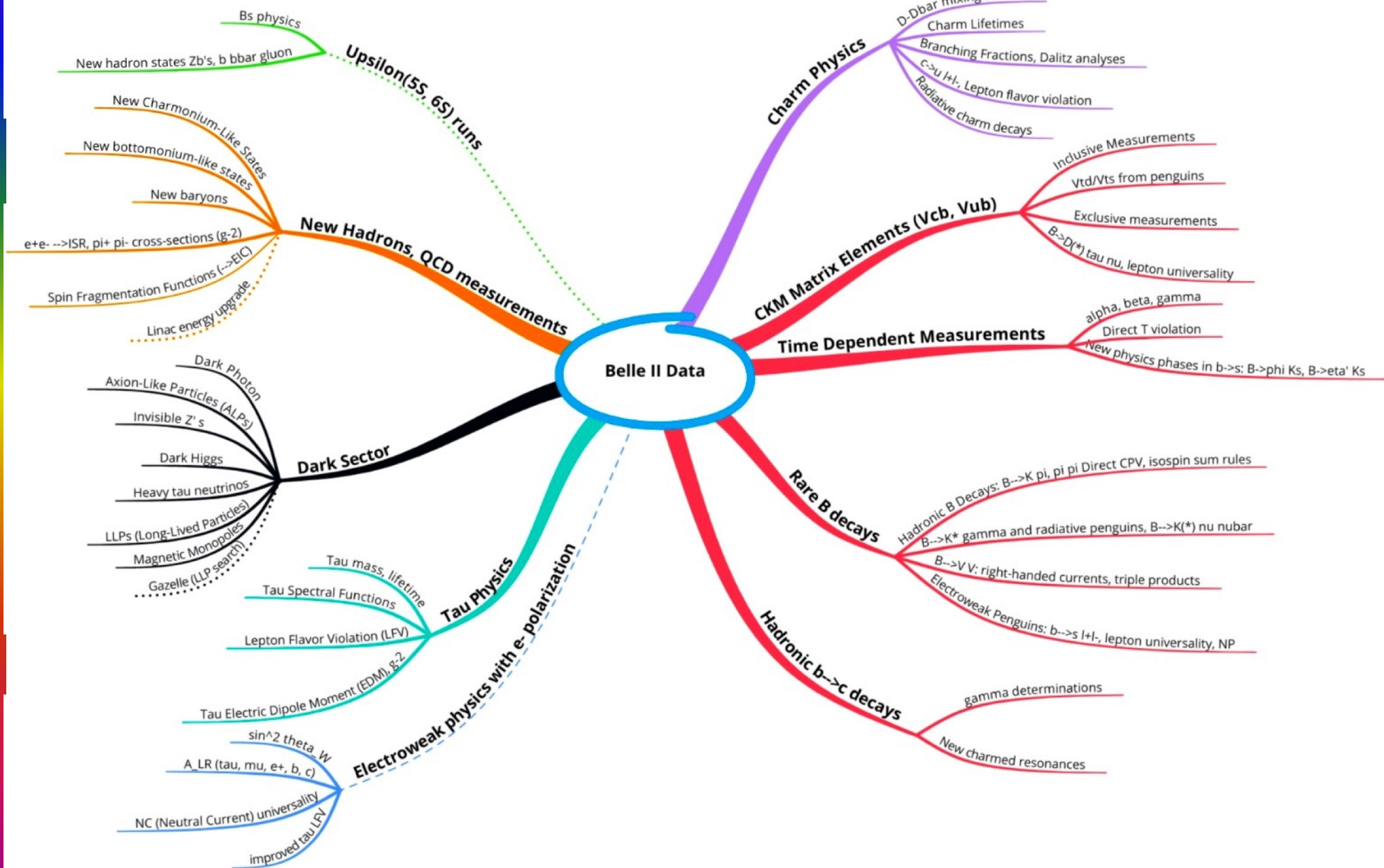
- Direct searches at Energy Frontier → stringent limits
- Indirect: SM anomalies, *hints* in B decay
 - e.g. lepton universality: tension

$$\mathcal{R}(D^{(*)}) \equiv \frac{\mathcal{B}(B \rightarrow \bar{D}^{(*)} \tau^+ \nu)}{\mathcal{B}(B \rightarrow \bar{D}^{(*)} \ell^+ \nu)} (\approx 3.9 \sigma); R(K^{(*)}) \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)} (1.5-3.1 \sigma)$$

Belle II will probe New Physics (NP) at the multi-TeV scale: B, c, τ

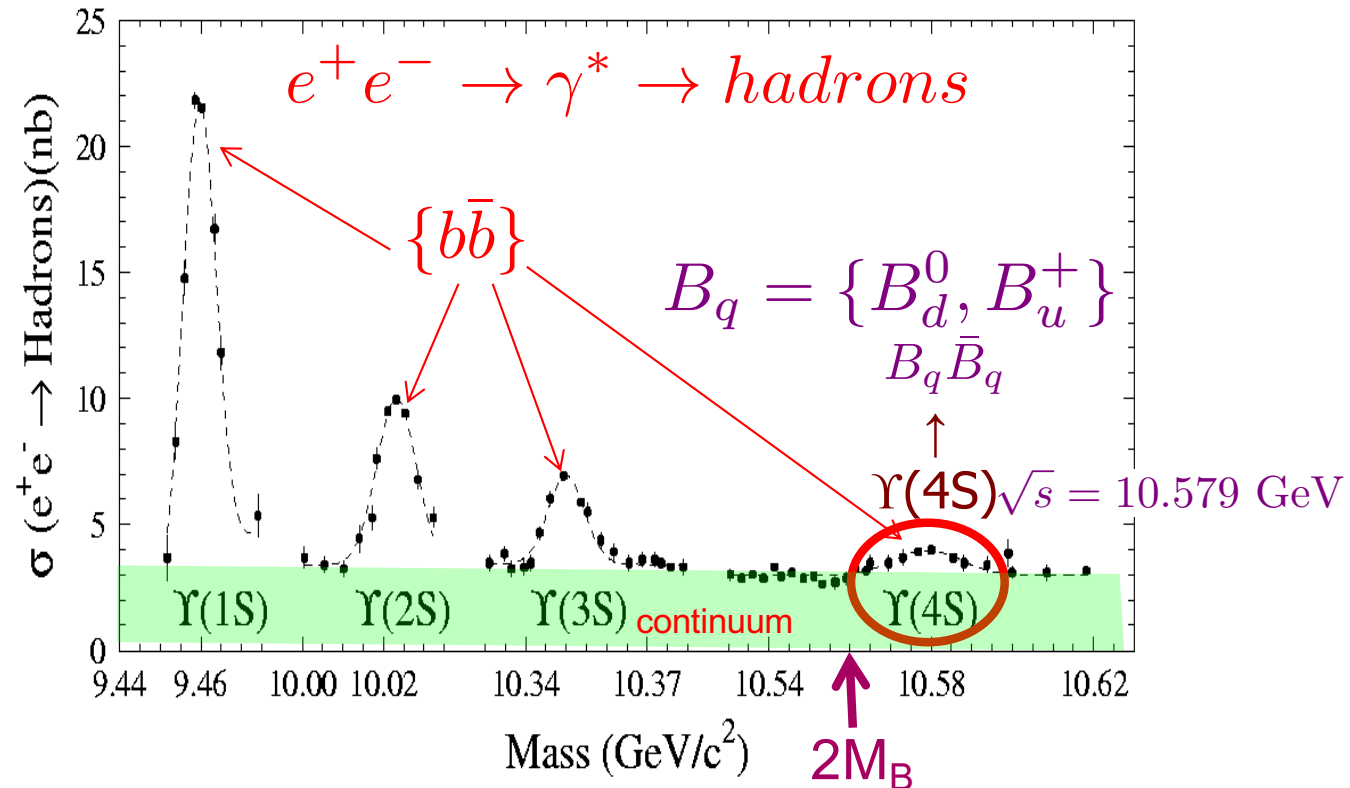
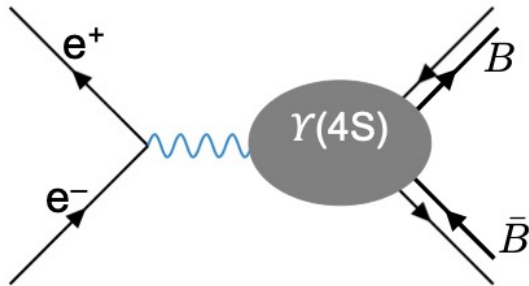
- Precision Standard Model measurements & challenges (multiprong)
 - Unitarity of CKM matrix → CP asymmetries, rare decays
 - lepton universality
- dark particles via missing energy

Belle II: rich Physics program (not only NP)



Belle II @ SuperKEKB: $e^+e^- \rightarrow \Upsilon(4S)$ (primarily)

Upsilon region
9-12 GeV



- Complete annihilation \Rightarrow event CMS = e^+e^- CMS
- Near-threshold @ $\Upsilon(4S)$: exclusive B-pair events
- “Hermetic” detector captures (almost) every detectable particle
 \Rightarrow “neutrals reconstruction” $\{K_L, n, \nu, \text{dark matter}\}$
- Average multiplicity (chg+neutral) $\sim 15\text{-}20$

Event environment



$$\sqrt{s} = 10.579 \text{ GeV}$$

7.0 GeV e^-

4.0 GeV e^+



SuperKEKB beams are **asymmetric** (7 GeV e^- /4 GeV e^+):
produces $\Upsilon(4S) \approx 1 \text{ nb}$



$$v \approx 0.27 c$$

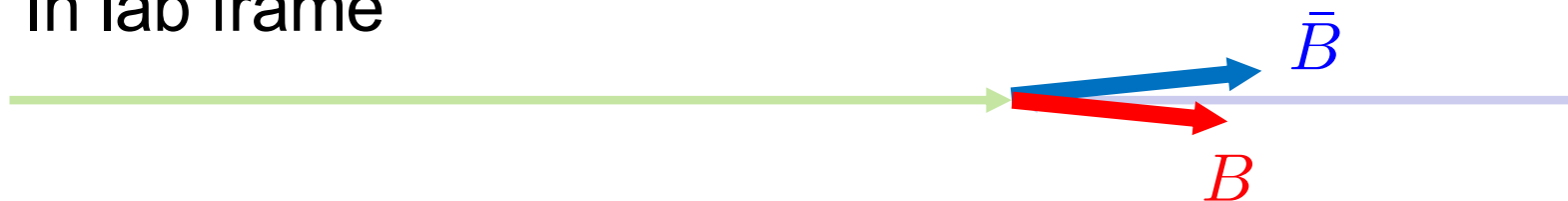
Event environment

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

$$\sqrt{s} = 10.579 \text{ GeV}$$

Slow: $p_B \approx 0.33 \text{ GeV}/c$ in CMS

In lab frame



In lab frame each B travels $\langle\beta\gamma c\tau\rangle \approx 130 \mu\text{m}$ in direction of CMS

Event environment



$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

→ many channels

→ light “stable” particles

$$\rightarrow \pi^\pm / K^\pm / p / \bar{p}$$

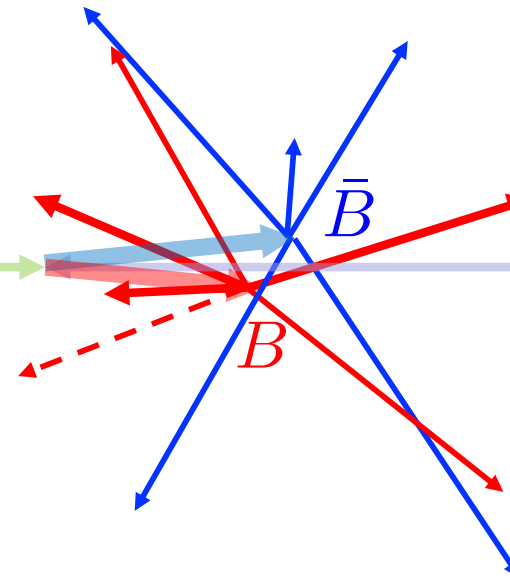
$$e^\pm / \mu^\pm$$

$$K_S^0 \rightarrow \pi^+ \pi^-$$

$$\pi^0 \rightarrow \gamma\gamma$$

$$K_L^0 / n / \bar{n}$$

$$\nu_e / \bar{\nu}_e$$



B^+ modes	B^0 modes
$B^+ \rightarrow \bar{D}^0 \pi^+$	$B^0 \rightarrow D^- \pi^+$
$B^+ \rightarrow \bar{D}^0 \pi^+ \pi^0$	$B^0 \rightarrow D^- \pi^+ \pi^0$
$B^+ \rightarrow \bar{D}^0 \pi^+ \pi^0 \pi^0$	$B^0 \rightarrow D^- \pi^+ \pi^+ \pi^-$
$B^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^-$	$B^0 \rightarrow D_s^+ D^-$
$B^+ \rightarrow D_s^+ \bar{D}^0$	$B^0 \rightarrow D^{*-} \pi^+$
$B^+ \rightarrow \bar{D}^{*0} \pi^+$	$B^0 \rightarrow D^{*-} \pi^+ \pi^0$
$B^+ \rightarrow \bar{D}^{*0} \pi^+ \pi^0$	$B^0 \rightarrow D^{*-} \pi^+ \pi^+ \pi^-$
$B^+ \rightarrow \bar{D}^{*0} \pi^+ \pi^+ \pi^-$	$B^0 \rightarrow D^{*-} \pi^+ \pi^+ \pi^- \pi^0$
$B^+ \rightarrow \bar{D}^{*0} \pi^+ \pi^+ \pi^- \pi^0$	$B^0 \rightarrow D_s^{*+} D^-$
$B^+ \rightarrow D_s^{*+} \bar{D}^0$	$B^0 \rightarrow D_s^+ D^{*-}$
$B^+ \rightarrow D_s^+ \bar{D}^{*0}$	$B^0 \rightarrow D_s^{*+} D^{*-}$
$B^+ \rightarrow \bar{D}^0 K^+$	$B^0 \rightarrow J/\psi K_S^0$
$B^+ \rightarrow D^- \pi^+ \pi^+$	$B^0 \rightarrow J/\psi K^+ \pi^+$
$B^+ \rightarrow J/\psi K^+$	$B^0 \rightarrow J/\psi K_S^0 \pi^+ \pi^-$
$B^+ \rightarrow J/\psi K^+ \pi^+ \pi^-$	
$B^+ \rightarrow J/\psi K^+ \pi^0$	
	D^+, D^{*+}, D_s^+ modes
	D^0, D^{*0} modes
	$D^+ \rightarrow K^- \pi^+ \pi^+$
	$D^0 \rightarrow K^- \pi^+$
	$D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0$
	$D^0 \rightarrow K^- \pi^+ \pi^0$
	$D^+ \rightarrow K^- K^+ \pi^+$
	$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$
	$D^+ \rightarrow K^- K^+ \pi^+ \pi^0$
	$D^0 \rightarrow \pi^- \pi^+$
	$D^+ \rightarrow K_S^0 \pi^+$
	$D^0 \rightarrow \pi^- \pi^+ \pi^0$
	$D^+ \rightarrow K_S^0 \pi^+ \pi^0$
	$D^0 \rightarrow K_S^0 \pi^0$
	$D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$
	$D^0 \rightarrow K_S^0 \pi^+ \pi^-$
	$D^{*+} \rightarrow D^0 \pi^+$
	$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$
	$D^{*+} \rightarrow D^+ \pi^0$
	$D^0 \rightarrow K^- K^+$
	$D_s^+ \rightarrow K^+ K_S^0$
	$D^0 \rightarrow K^- K^+ K_S^0$
	$D_s^+ \rightarrow K^+ \pi^+ \pi^-$
	$D^{*0} \rightarrow D^0 \pi^0$
	$D_s^+ \rightarrow K^+ K^- \pi^+$
	$D^{*0} \rightarrow D^0 \gamma$
	$D_s^+ \rightarrow K^+ K^- \pi^+ \pi^0$
	$D_s^+ \rightarrow K^+ K_S^0 \pi^+ \pi^-$
	$D_s^+ \rightarrow K^- K_S^0 \pi^+ \pi^+$
	$D_s^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$
	$D_s^+ \rightarrow \pi^+ \pi^+ \pi^-$
	$D_s^{*+} \rightarrow D_s^+ \pi^0$

B reconstruction

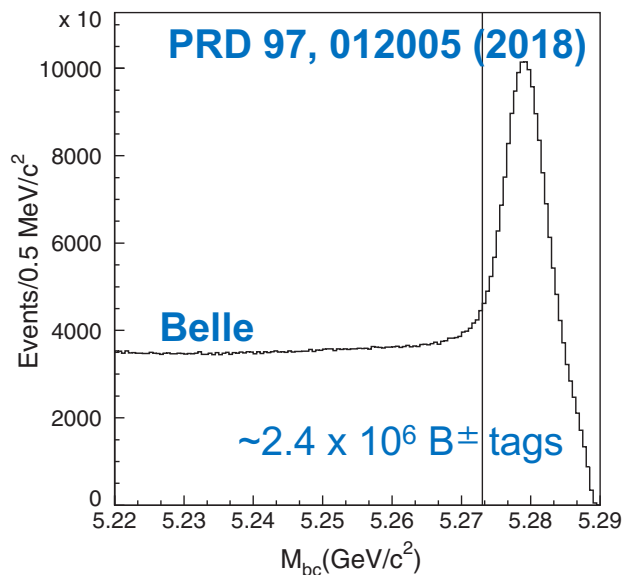
Full reconstruction (>1000 modes)

$$E_{\text{tag}} = \sum_{i,\text{tag}} E_i = E_{\text{beam}} \quad (\text{CMS frame})$$

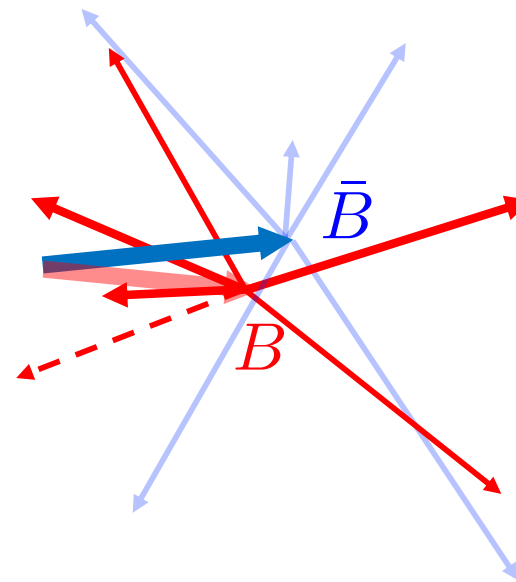
$$\vec{p}_{\text{tag}} = \sum_{i,\text{tag}} \vec{p}_i$$

→ Beam-constrained mass

$$M_{\text{bc}} = \sqrt{E_{\text{beam}}^2 - \vec{p}_{\text{tag}}^2}$$



Remainder
(detected & undetected)
= other B



- absolute branching fractions
- inclusive rates
- detailed angular, kinematic distributions
- invisible particles (neutrinos, dark matter)
- low systematics

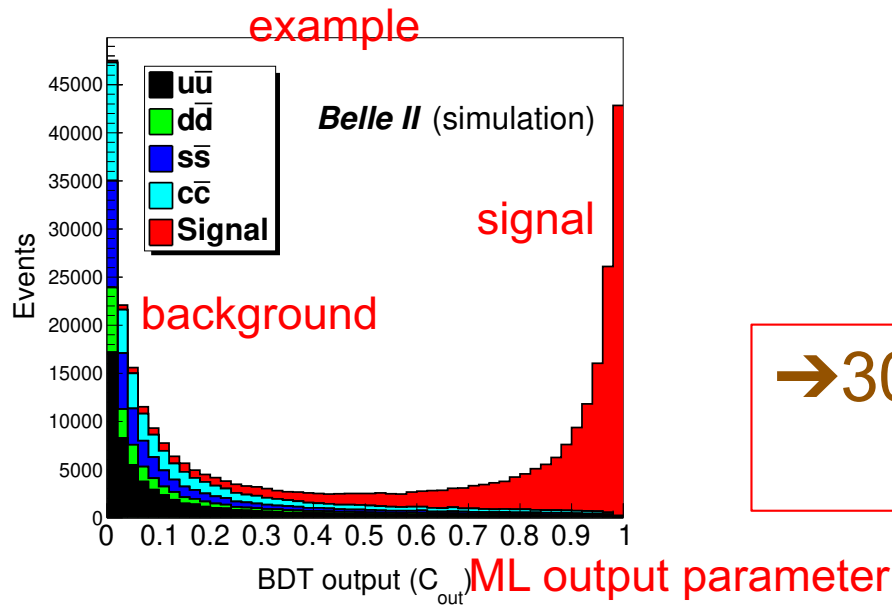
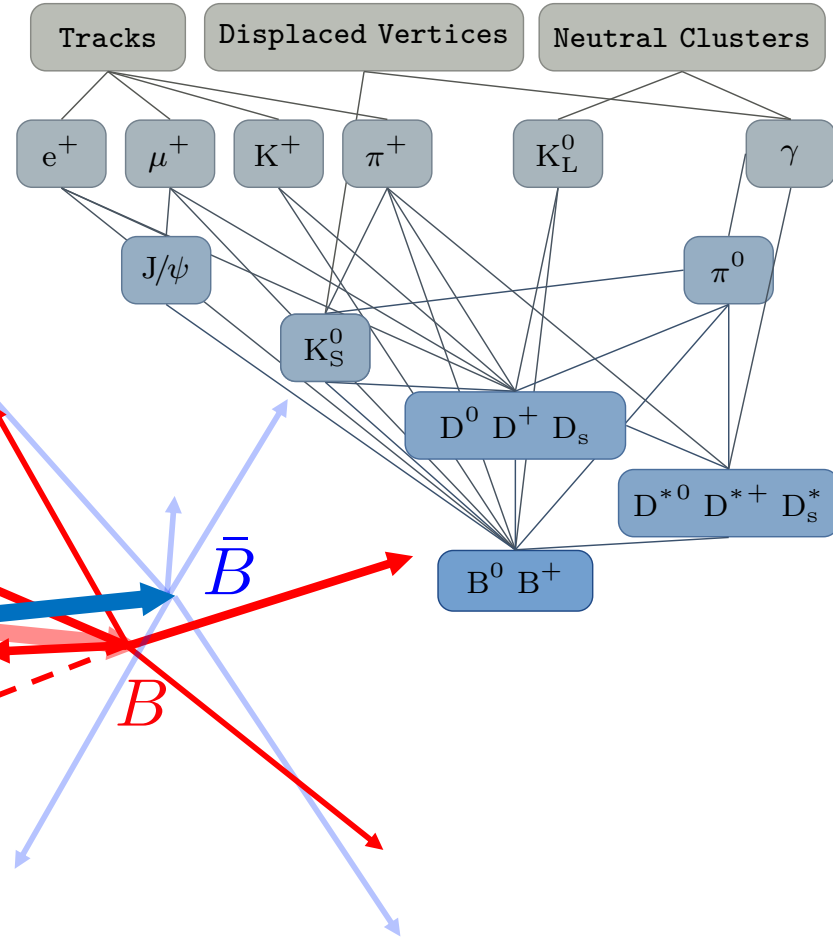
Belle II: Full Event Interpretation



Machine Learning

To differentiate “signal,” background events

- Input information
 - Tags: full, partial (e.g. semileptonic)
 - rest-of-event
 - event shape
 - vertexing
- ML Training: signal / background MC



→ 30%-50% efficiency improvement vs Belle full reconstruction

Belle II: improve through resolution, (much) better statistics



Brief history & status

e^+e^- B-factories (\approx equal #'s $B\bar{B}$, $c\bar{c}$, $\tau^+\tau^-$)

- Belle (1999-2010) 772M events, each; \approx 600 papers published
- Babar (1999-2008) 465M; \approx 600 published
- Belle II (2019-)
 - 189.3 fb $^{-1}$ \approx 190M: results reported here
 - to date: \approx 290 M collected; ultimate goal = 50G (>100X)
 - published /submitted physics results so far
 - Integrated luminosity [Chinese Physics C 44, 021001 (2020)]
 - search for invisible Z' [PRL 124, 141801 (2020)]
 - search for Axion-like [PRL 125, 161806 (2020)]
 - search for $K\nu\bar{\nu}$ [PRL 127, 181802 (2021)]
 - D^0 and D^+ lifetimes [PRL 127, 211801 (2021)]
 - Belle+Belle II, CKM angle φ_3 [JHEP 02 2022, 063 (2022)]

Belle II NEW results

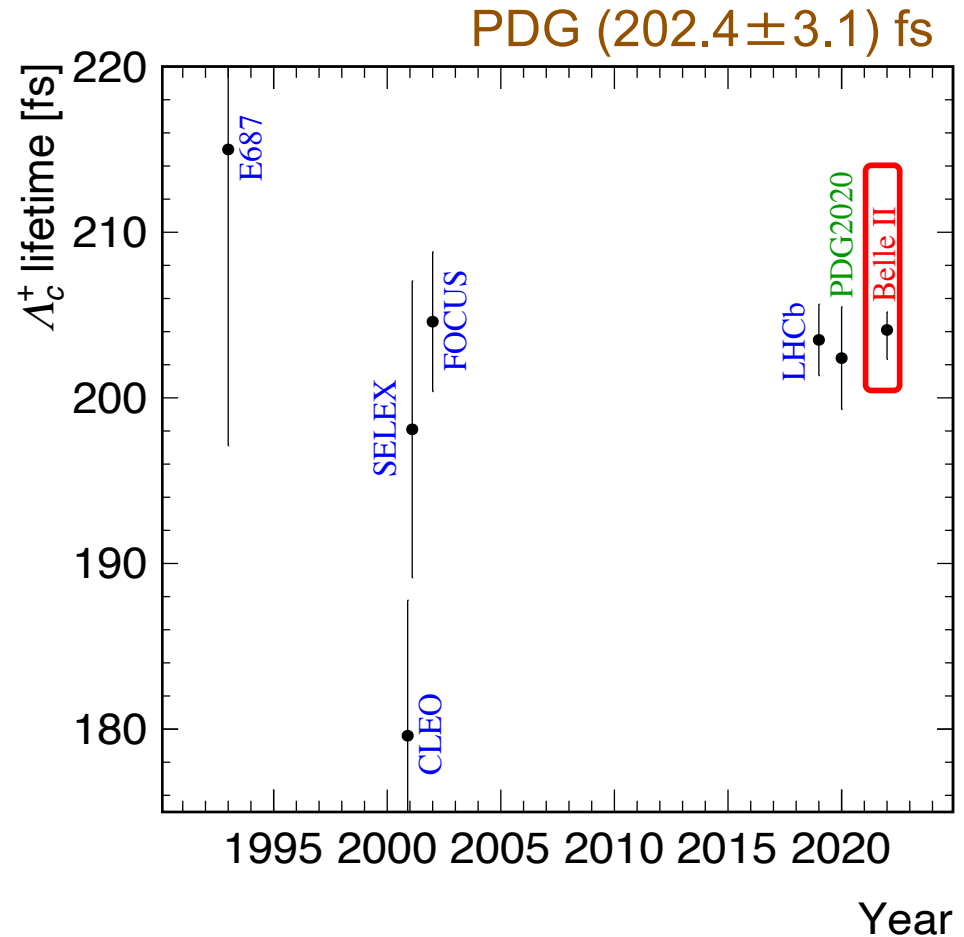
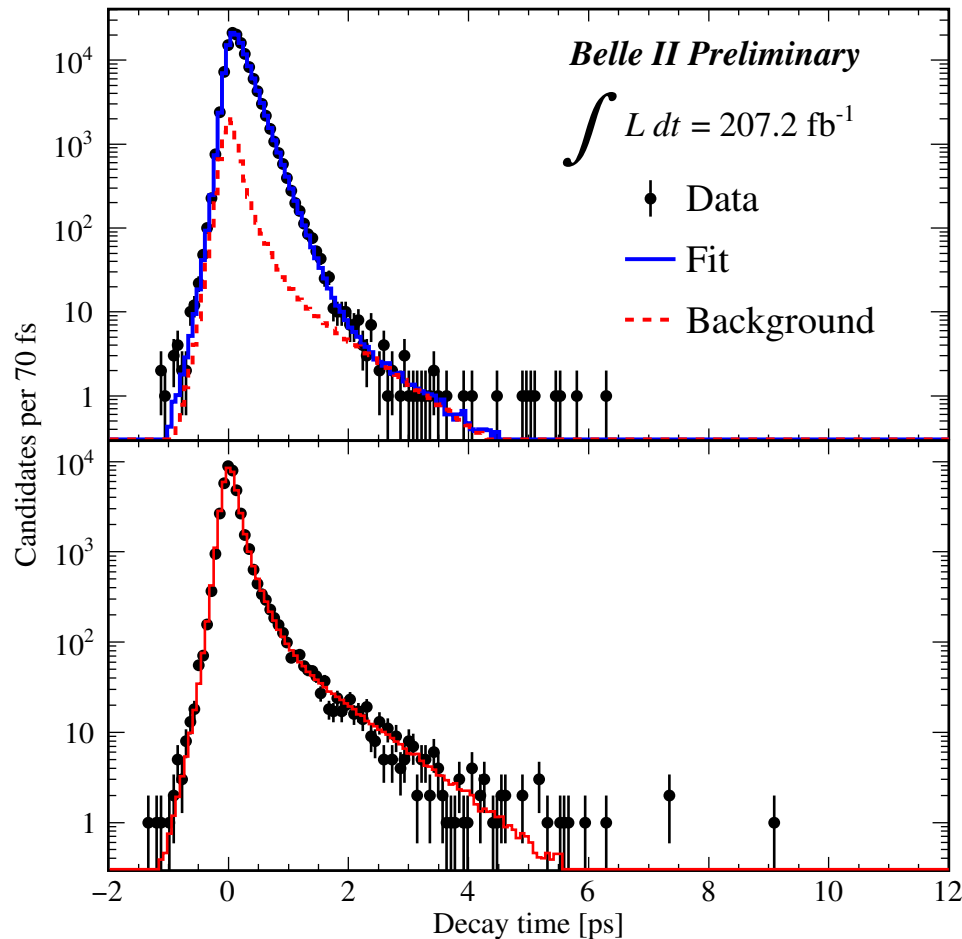
charm lifetimes

experimental: partial widths require full; $\Gamma_{\text{partial}} = \mathcal{B} \times \Gamma = \mathcal{B}/\tau$

Belle II 72 fb⁻¹: $\tau(D^0) = (410.5 \pm 1.1_{\text{stat}} \pm 0.8_{\text{sys}}) \text{ fs}$ PDG (410.1 ± 1.5) fs
 PRL 127, 211801 (2021) $\tau(D^+) = (1030.4 \pm 4.7_{\text{stat}} \pm 3.1_{\text{sys}}) \text{ fs}$ (1040 ± 7) fs
BEST

NEW Λ_c 207 fb⁻¹

$\tau(\Lambda_c) = (204.12 \pm 0.84_{\text{stat}} \pm 0.69_{\text{sys}}) \text{ fs}$



Search for Darkhiggstrahlung



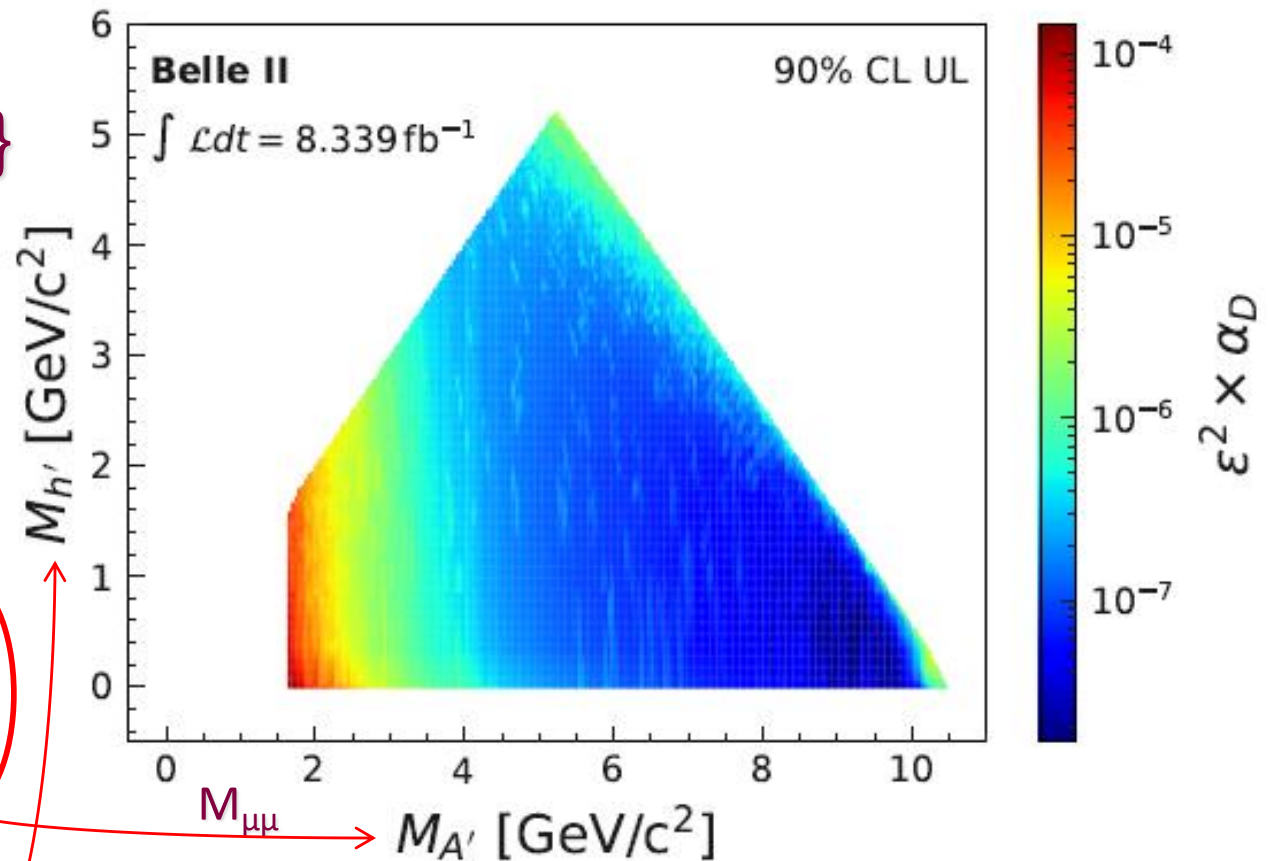
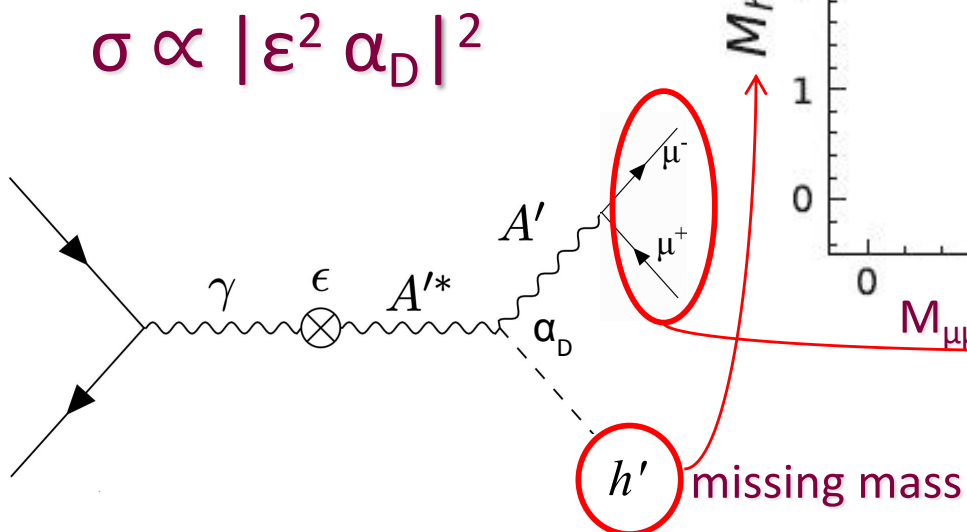
non-SM

2-track trigger: 8.34 fb^{-1}

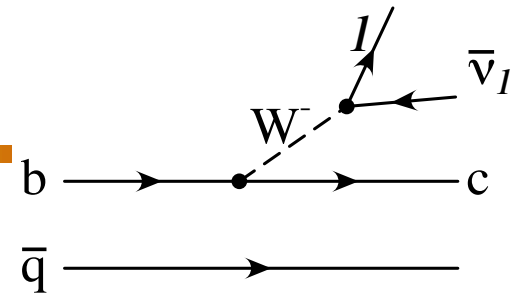
dark Higgs+dark photon
 $e^+e^- \rightarrow h' A' \{ \rightarrow \mu^+\mu^- \}$

Belle II preliminary

90% CL upper limits on $\epsilon^2 \times \alpha_D$



$$B^0 \rightarrow D^{*-} \ell^+ \nu$$



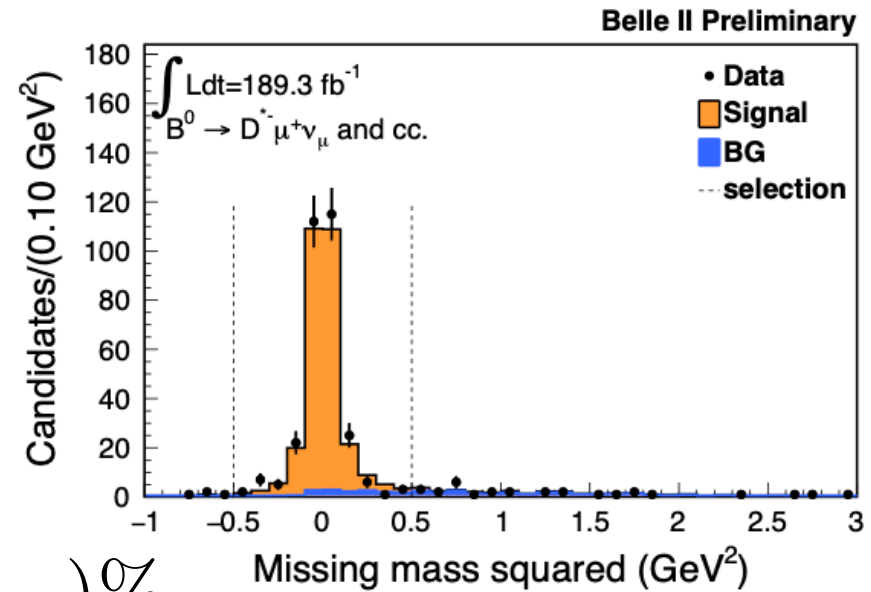
SM: spectator $\rightarrow |V_{cb}|$

- experimental considerations
 - FEI, ν via missing mass
 - \rightarrow clean exclusive reconstruction

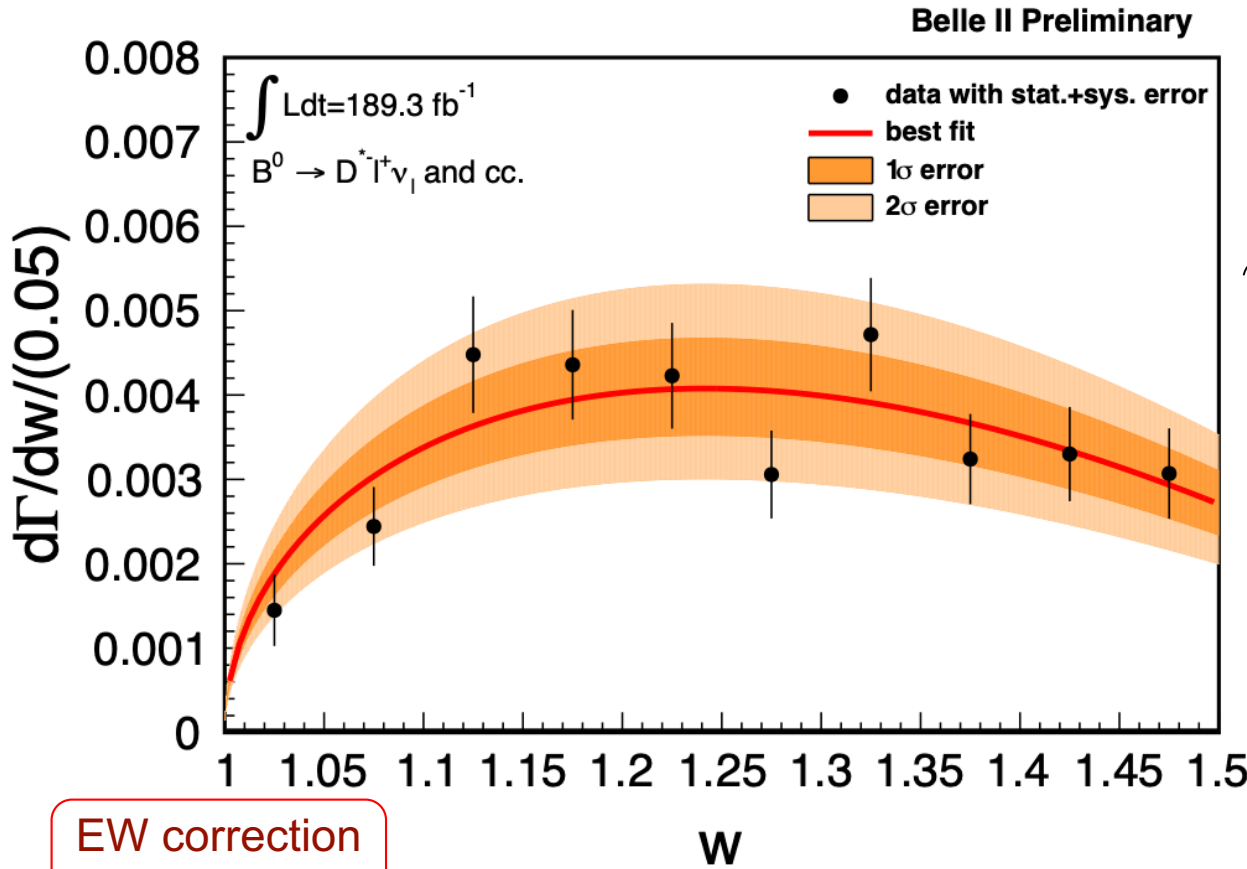
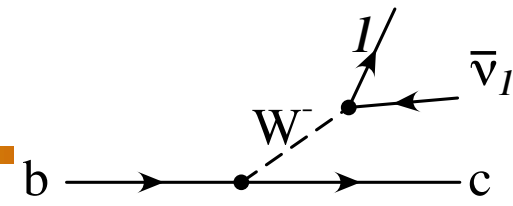
$$\mathcal{B}(B^0 \rightarrow D^{*-} \ell^+ \nu)$$

$$= (5.27 \pm 0.22_{stat} \pm 0.38_{sys})\%$$

[PDG: $(5.06 \pm 0.12)\%$]



- \mathcal{B} to $|V_{cb}|$: Heavy Quark Effective Theory (HQET)
 - $\rightarrow q^2$ distribution/form factor



$$w = \frac{m_B^2 - m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

= 1 at q^2_{\max}

EW correction (theory)

phase space

form factor (theory)
Parametrized shape
lattice eval at $w=1$

$$\frac{d\Gamma}{dw} = \frac{\eta_{EW}^2 G_F^2}{48\pi^3} m_{D^*}^3 (m_B - m_{D^*})^2 g(w) F^2(w) |V_{cb}|^2$$

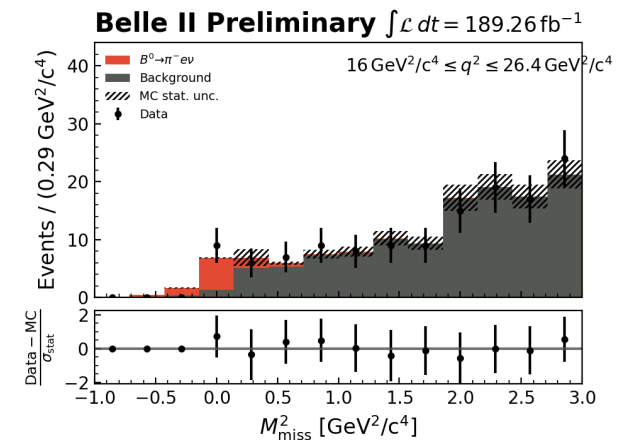
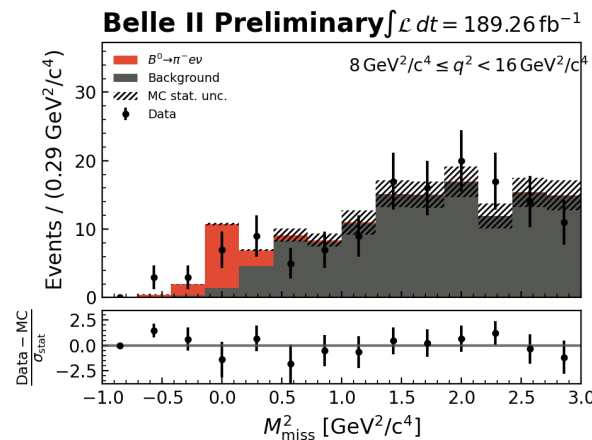
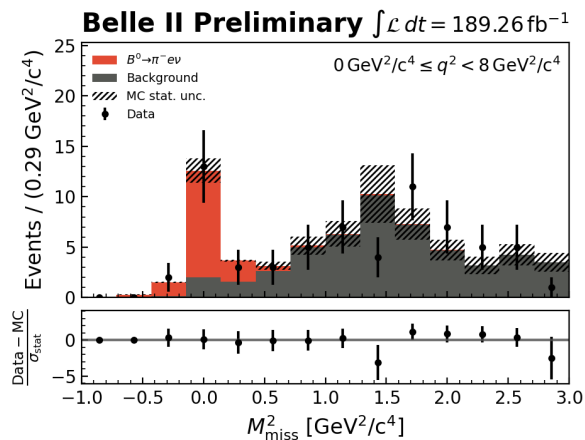
$\rightarrow |V_{cb}| = 0.0379 \pm 0.0027$

$$B \rightarrow \pi e^+ \nu$$

SM: spectator $\rightarrow |V_{ub}|$

- experimental & theoretical (similar to $|V_{cb}|$)
similar experimental/theoretical approach
3 bins of q^2 ; fit for form factor; evaluate at $w=1$

$$B^0 \rightarrow \pi^- e^+ \nu$$



$$B \rightarrow \pi e^+ \nu$$



$|V_{ub}|$: q^2 distribution

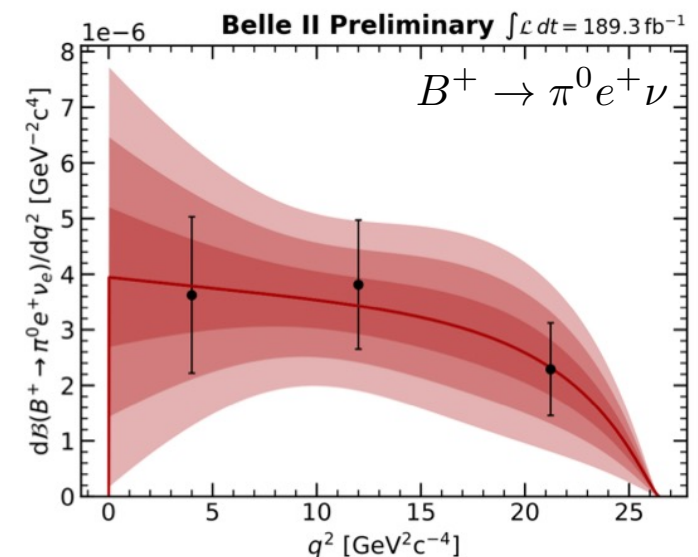
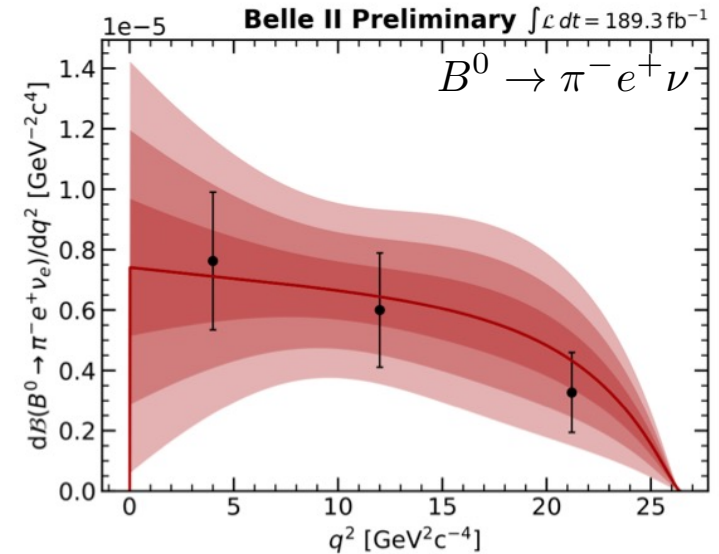
$$B^0 \rightarrow \pi^- e^+ \nu$$

$$\mathcal{B} = (1.43 \pm 0.27_{\text{stat}} \pm 0.07_{\text{sys}}) \times 10^{-4}$$

$$B^+ \rightarrow \pi^0 e^+ \nu$$

$$\mathcal{B} = (8.33 \pm 1.67_{\text{stat}} \pm 0.55_{\text{sys}}) \times 10^{-5}$$

$$\frac{d\mathcal{B}}{dq^2}(B \rightarrow \pi \ell \nu) \propto |\mathcal{M}|^2 \propto |V_{ub}|^2 f_+^2(q^2)$$

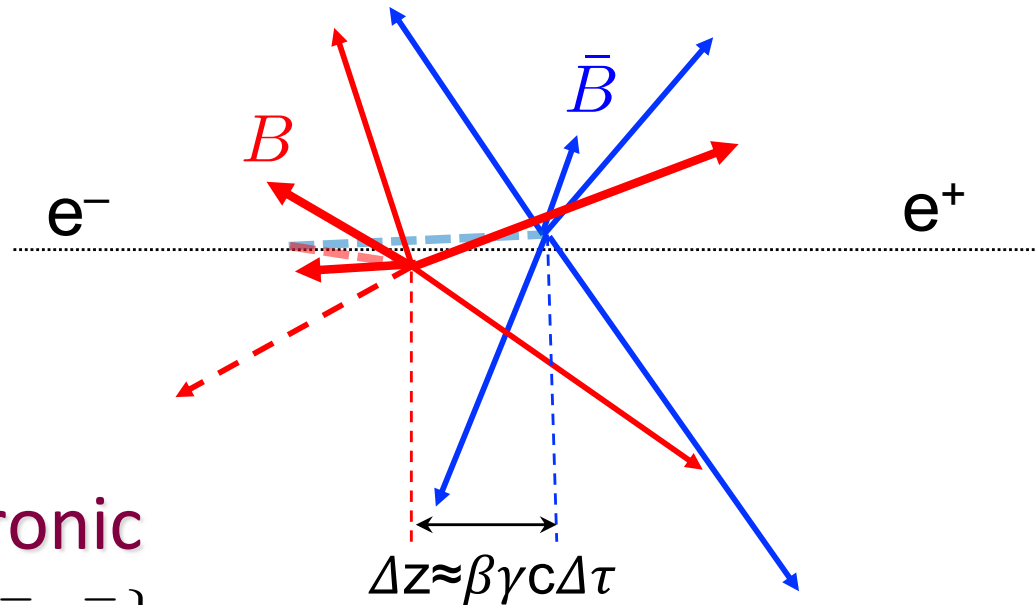


Decay mode	Fitted $ V_{ub} $
$B^0 \rightarrow \pi^- e^+ \nu_e$	$(3.71 \pm 0.55) \times 10^{-3}$
$B^+ \rightarrow \pi^0 e^+ \nu_e$	$(4.21 \pm 0.63) \times 10^{-3}$
Combined fit	$(3.88 \pm 0.45) \times 10^{-3}$

B^0 lifetime and mixing Δm_d

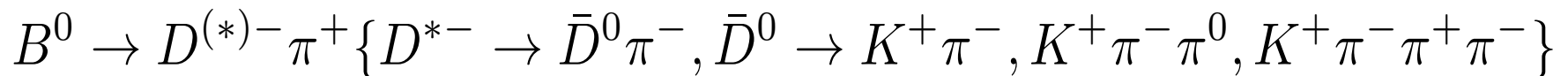
SM: benchmark for CP asymmetry measurements

CMS in lab frame: $\beta\gamma \approx 0.27$
 \rightarrow mean vertex separation
 $\Delta z \approx 130 \mu\text{m}$



Vertex reconstruction

- fully reconstructed hadronic



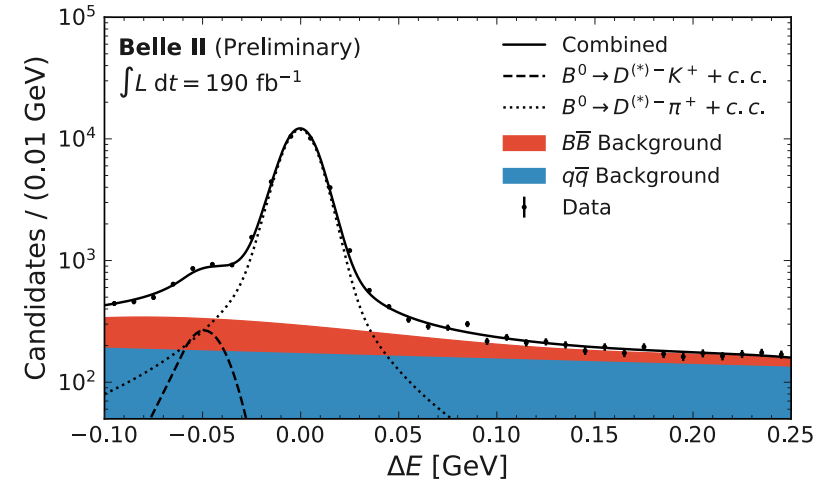
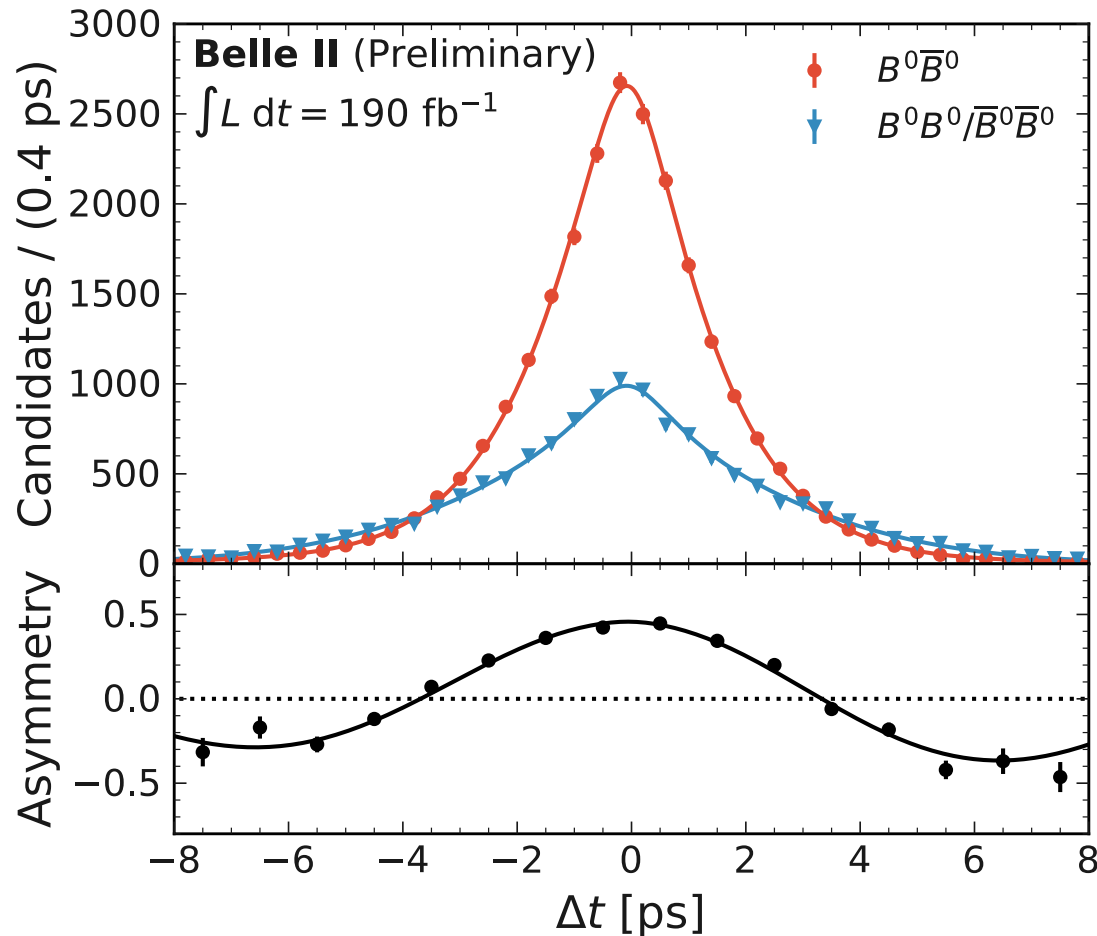
- + Belle flavor tag – 7 quality bins, dilution factors \underline{w}_i

Time distributions: same/opposite flavor

$$f(\Delta t') = \frac{e^{-|\Delta t'|/\tau_{B^0}}}{4\tau_{B^0}} (1 + q\mathcal{D} \cos \Delta m_d \Delta t')$$

$q = 1$ opp flavor
 $q = -1$ same flavor
 $\mathcal{D} = 1 - 2w$

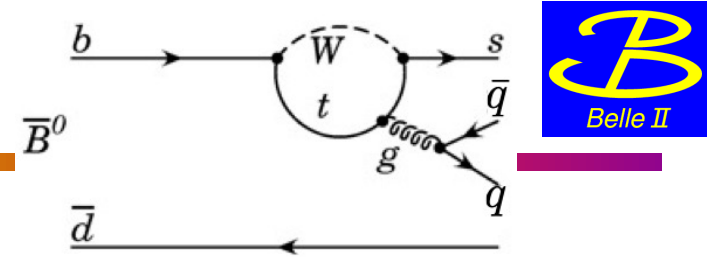
B^0 lifetime and mixing Δm_d



$$\tau_{B^0} = 1.499 \pm 0.013 \text{ (stat.)} \pm 0.008 \text{ (syst.) ps}$$

$$\Delta m_d = 0.516 \pm 0.008 \text{ (stat.)} \pm 0.005 \text{ (syst.) ps}^{-1}$$

$$B^0 \rightarrow K^0 \pi^0$$



SM: time-dependent CP asymmetry

$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q \{ \mathcal{A}_{CP} \cos(\Delta m_d \Delta t) + \overset{\sin 2\varphi_1}{\mathcal{S}_{CP}} \sin(\Delta m_d \Delta t) \}],$$

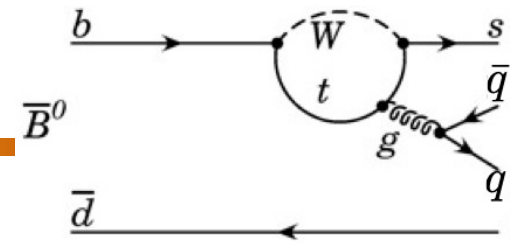
\mathcal{A}_{CP} : $K\pi$ isospin sum rule

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)} = 0$$

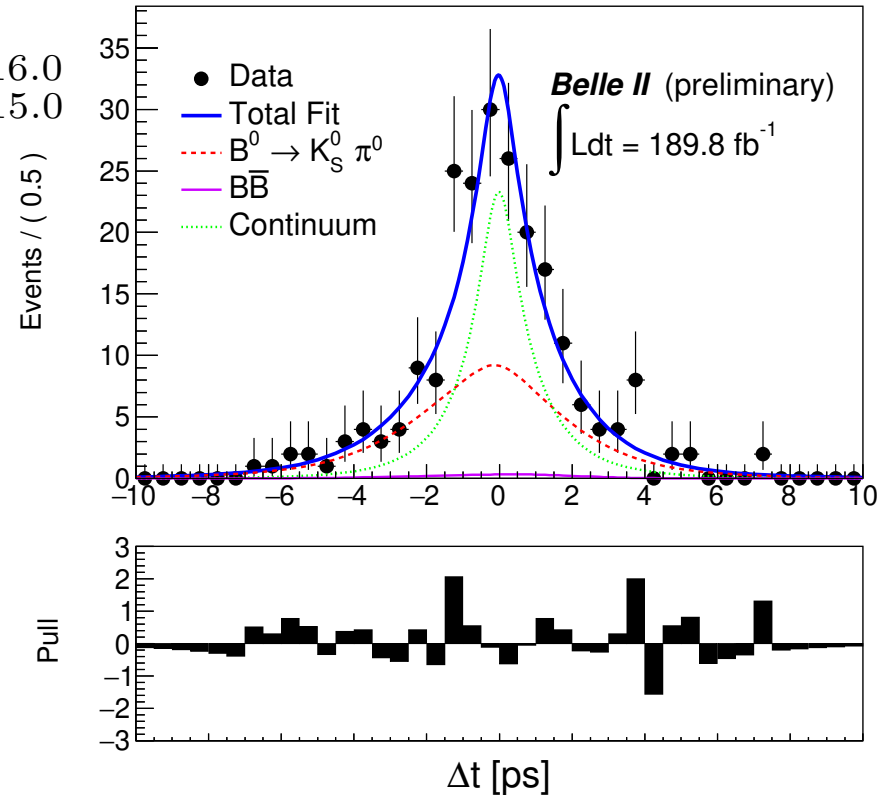
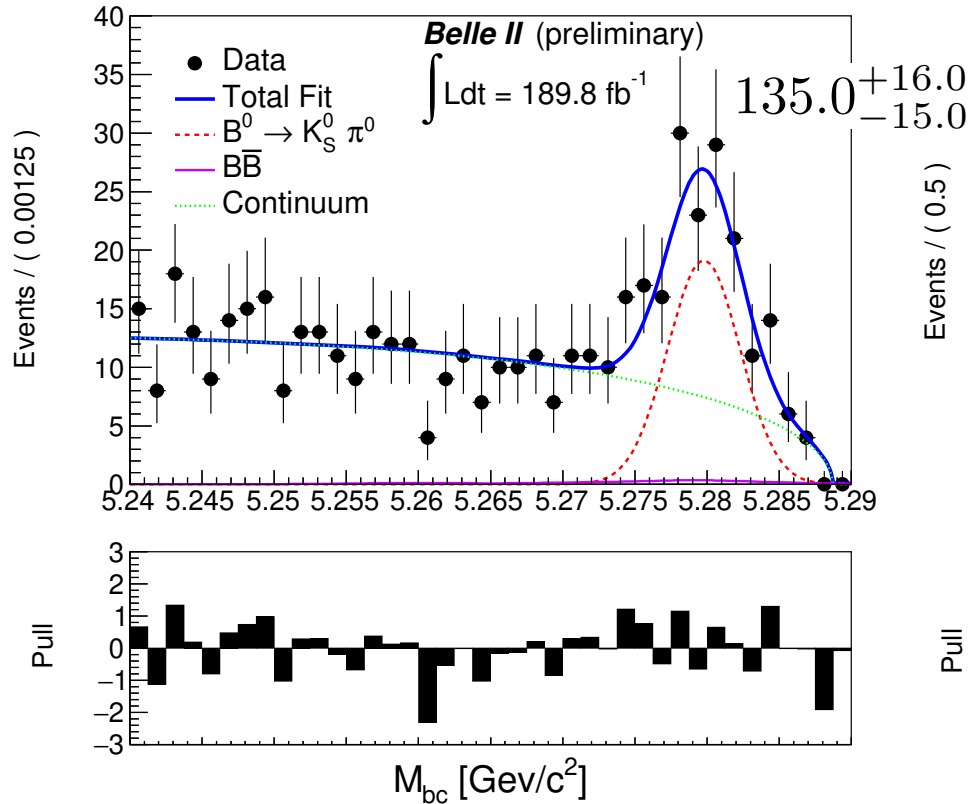
$K^0\pi^0$: only at e^+e^- B-factory, most challenging

NP: may appear as $\mathcal{A}_{CP} \neq 0$

$$B^0 \rightarrow K^0 \pi^0$$



Branching fraction, \mathcal{A}_{CP}



Observable	Fitted value	WA[1] value
$\mathcal{B}(B^0 \rightarrow K^0 \pi^0) \times 10^{-6}$	$11.0 \pm 1.2(stat) \pm 1.0(syst)$	9.9 ± 0.5
\mathcal{A}_{CP}	$-0.41^{+0.30}_{-0.32}(stat) \pm 0.09(syst)$	-0.01 ± 0.10

$$B^0 \rightarrow K_S^0 \pi^0 \gamma$$

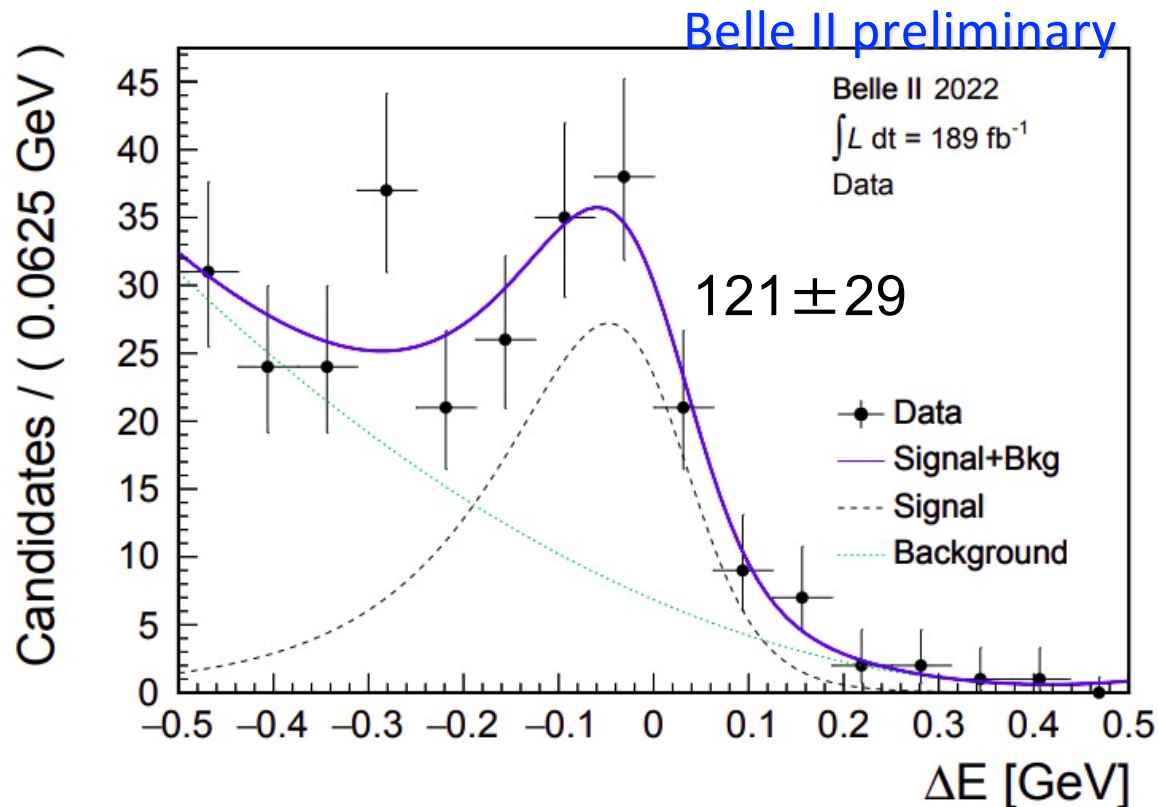


SM $b \rightarrow s \gamma$: γ polarization is flavor-specific due to V-A

→ CP asymmetry suppressed

NP may appear as time-dependent CP asymmetry

Branching fraction

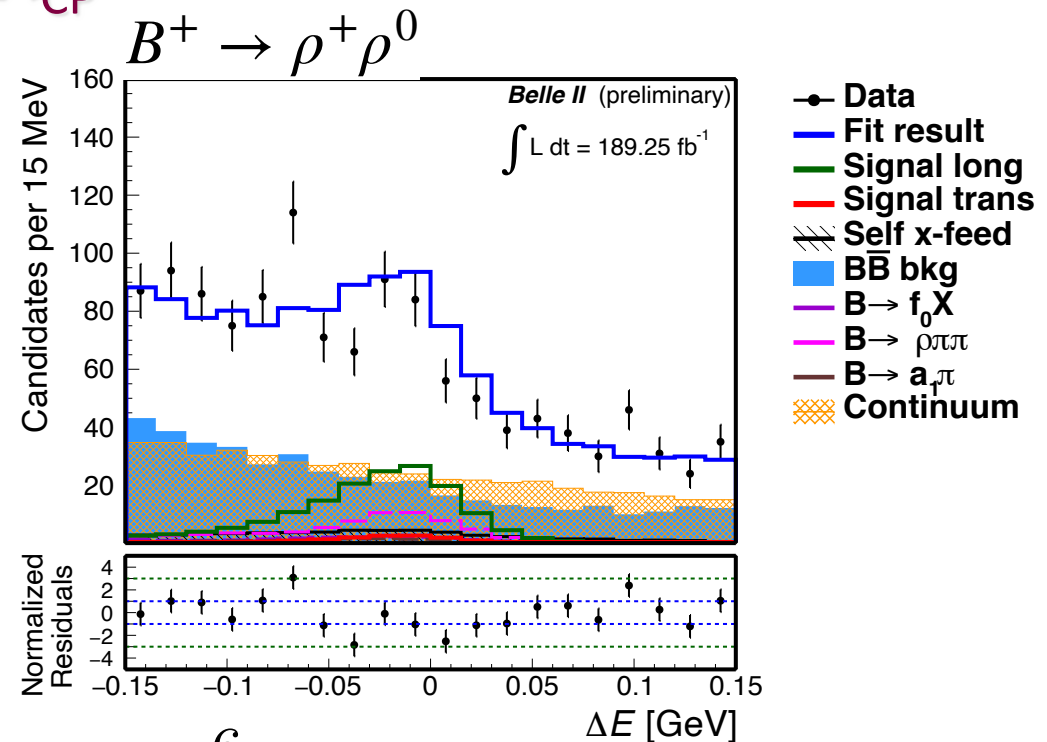
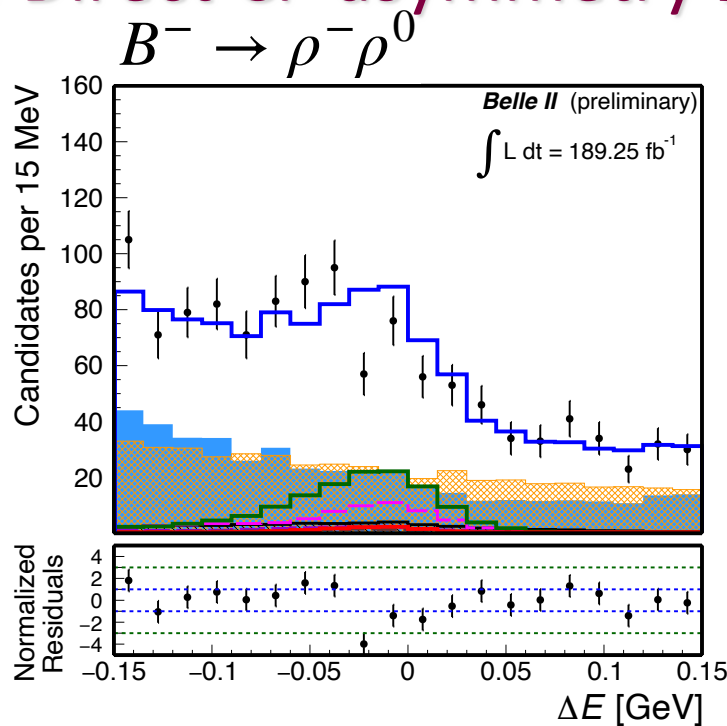
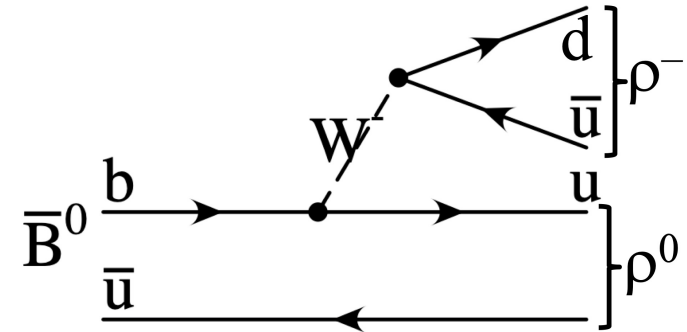


$$\mathcal{B}(B^0 \rightarrow K_S^0 \pi^0 \gamma) = (7.3 \pm 1.8 \text{ (stat)} \pm 1.0 \text{ (syst)}) \times 10^{-6}$$

$$B^\pm \rightarrow \rho^\pm \rho^0$$

SM: $b \rightarrow u$

- φ_2 via BF/isospin relations
 - polarization-dependent
- NP: Direct CP asymmetry \mathcal{A}_{CP}



$$\mathcal{B} = (23.2_{-2.1}^{+2.2} \pm 2.7) \times 10^{-6}$$

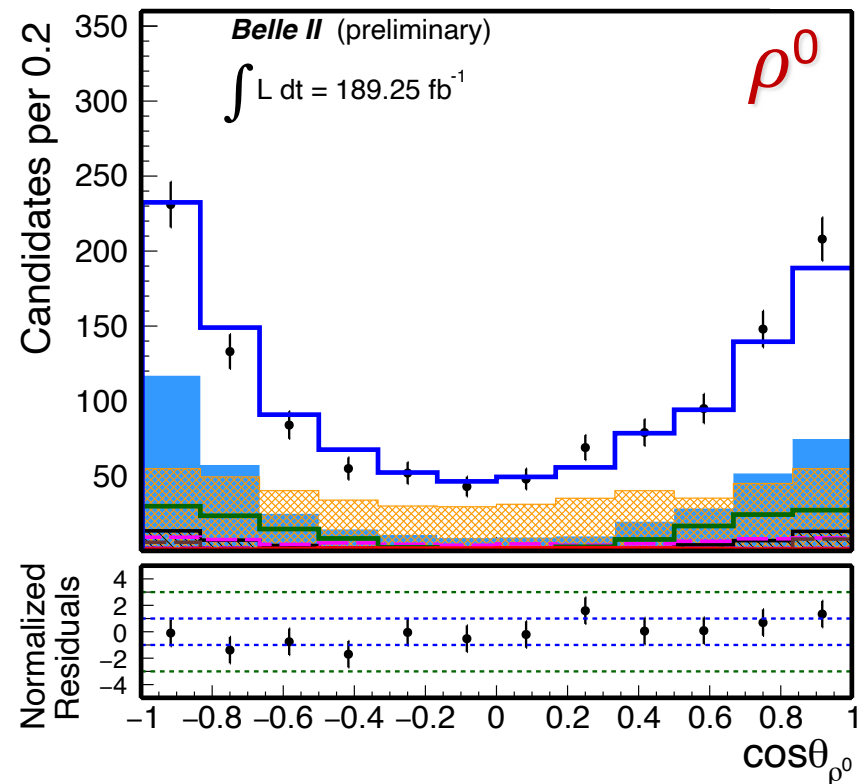
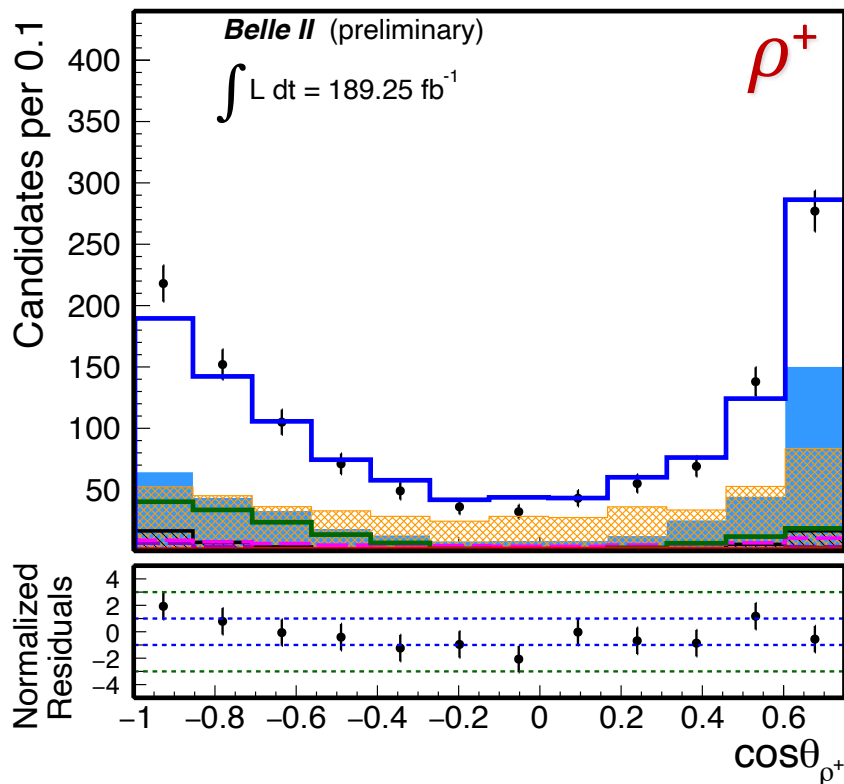
$$\mathcal{A}_{CP} \equiv \frac{\Gamma_{B^-} - \Gamma_{B^+}}{\Gamma_{B^-} + \Gamma_{B^+}} = -0.069 \pm 0.068 \pm 0.039$$

$$B^{\pm} \rightarrow \rho^{\pm} \rho^0$$

longitudinal polarization fraction f_L

$\cos(\text{helicity angle})$

- Data
- Fit result
- Signal long
- Signal trans
- ▨ Self x-feed
- BB bkg
- $B \rightarrow f_0 X$
- $B \rightarrow \rho\pi\pi$
- $B \rightarrow a_1\pi$
- ▨ Continuum



$$f_L = 0.943_{-0.033}^{+0.035} \pm 0.027$$

$$B \rightarrow K^{*0} \ell^+ \ell^-$$

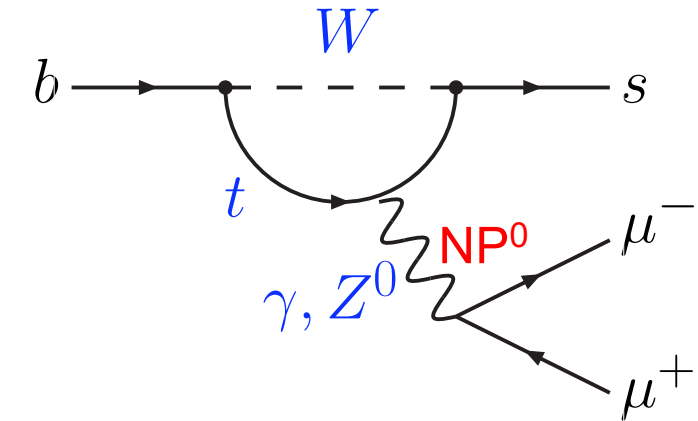
SM: suppressed (CKM unitarity)

NP may appear in anomalies of

- branching fraction(s)
 - lepton universality μ/e

$$R(K^{(*)}) = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}$$

$$= 1 \pm \mathcal{O}(10^{-2})$$

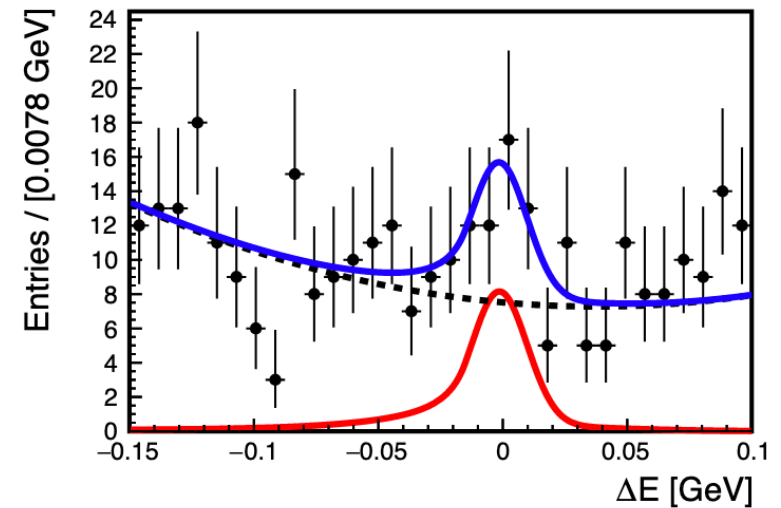
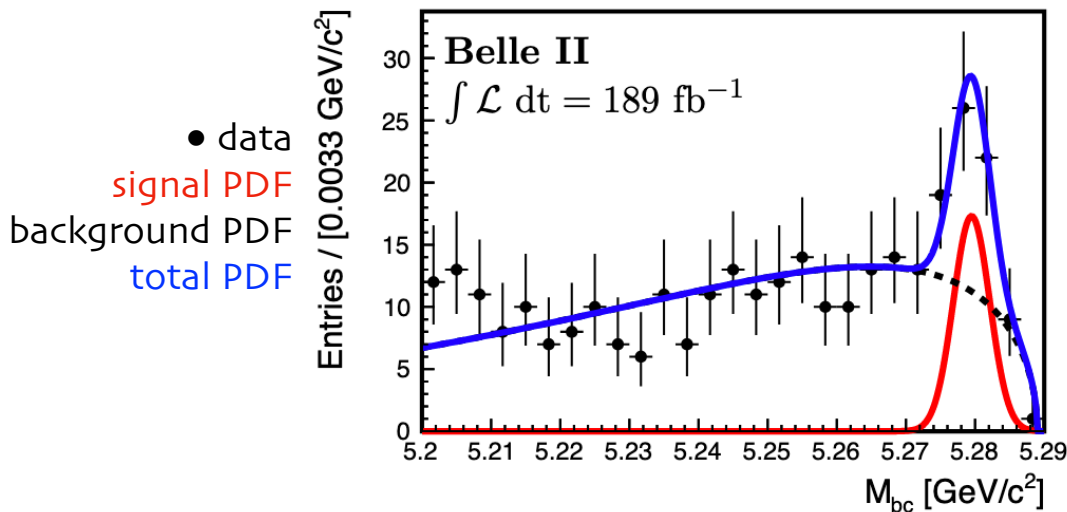


1.5-3.1 σ tension [LHCb]

- Angular distributions

$$B \rightarrow K^{*0} \ell^+ \ell^-$$


Belle II preliminary

 $B \rightarrow K^* \ell \ell$ fit projections
PDG $\mathcal{B} \times 10^6$

$$\mathcal{B}(B \rightarrow K^* \mu^+ \mu^-) = (1.19 \pm 0.31_{-0.07}^{+0.08}) \times 10^{-6}$$

 0.94 ± 0.05

$$\mathcal{B}(B \rightarrow K^* e^+ e^-) = (1.42 \pm 0.48 \pm 0.09) \times 10^{-6}$$

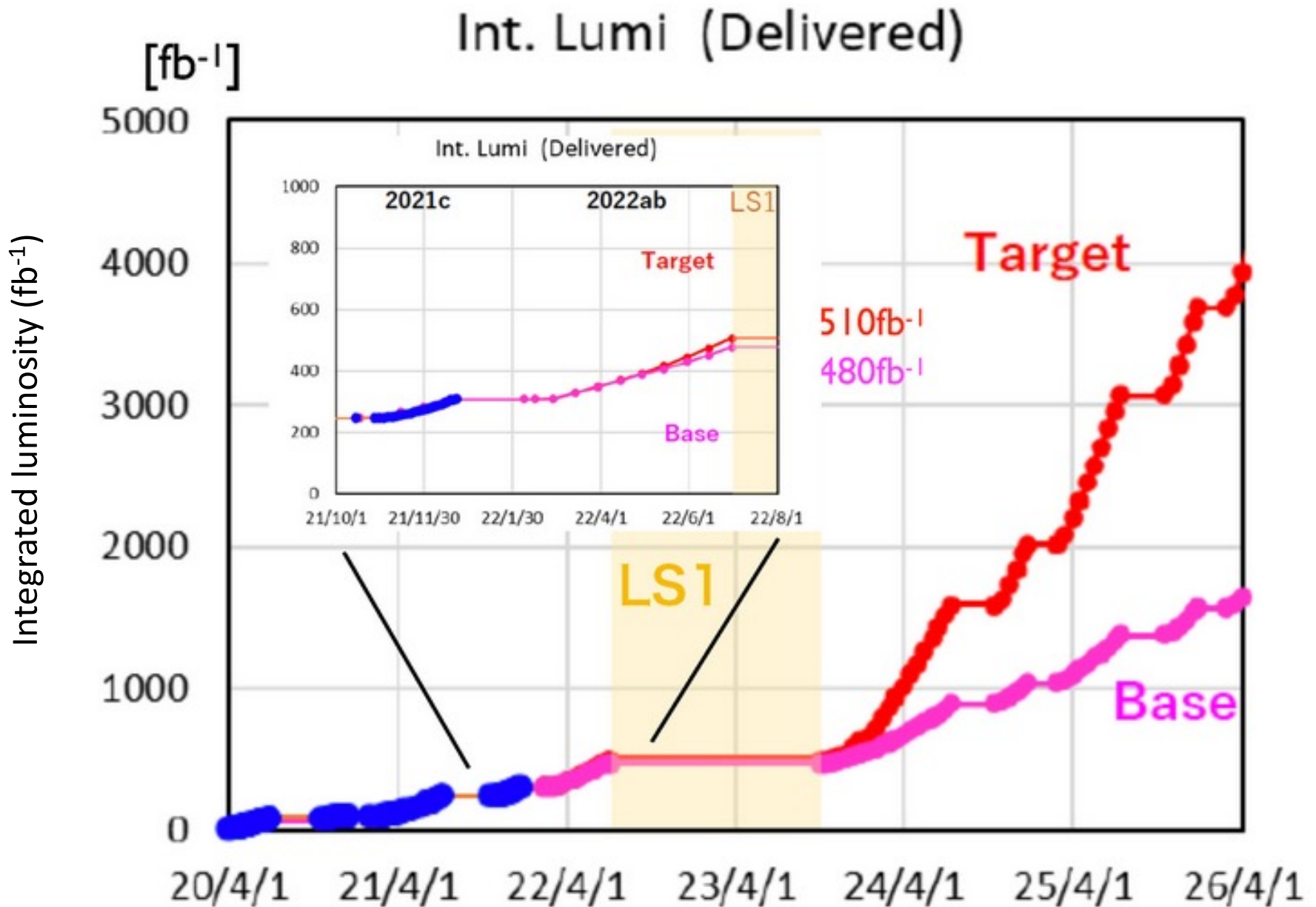
 $1.03 \pm .19$

$$\mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = (1.25 \pm 0.30_{-0.07}^{+0.08}) \times 10^{-6}$$

 0.99 ± 0.12

$K^* ee$ is dominated by B-factories

SuperKEKB/Belle II Luminosity Profile



Summary



$e^+e^-@Y$ region: powerful event environment, rich physics

- Belle II/SuperKEKB: hermetic detector, nano-beams
 - 189.3 fb⁻¹ analyzed, new results
 - time-dependent measurements
 - world-leading charm lifetimes: D^0 , D^+ , Λ_c
 - B mixing, lifetime – ready for time-dependent CP
 - A_{CP} for $B^0 \rightarrow K^0 \pi^0$ (single K_S vertex!)
 - time-independent
 - $|V_{xb}|$ via exclusive semileptonic/form factors
 - B decays: $\rho^\pm \rho^0$, $K_S^0 \pi^0 \gamma$, $K^* \ell^+ \ell^-$
 - darkhiggsstrahlung search
 - (Much) more to come – probe multi-TeV mass scale at the Intensity Frontier ...

with better statistics & resolution...



... be prepared for surprises





Backup Slides

Belle II Detector

STATISTICS
 VERTEXING
 PARTICLE ID (π/K)
 "HERMETICITY"

K_L and muon detector:
 Resistive Plate Chambers (barrel outer layers)
 Scintillator + WLSF + SiPM's (end-caps, inner 2 barrel layers)

EM Calorimeter:
 CsI(Tl), waveform sampling (barrel+endcap)

e^- (7 GeV)

Particle Identification
 iTOP detector system (barrel)
 Prox. focusing Aerogel RICH (fwd)
 dE/dx in CDC

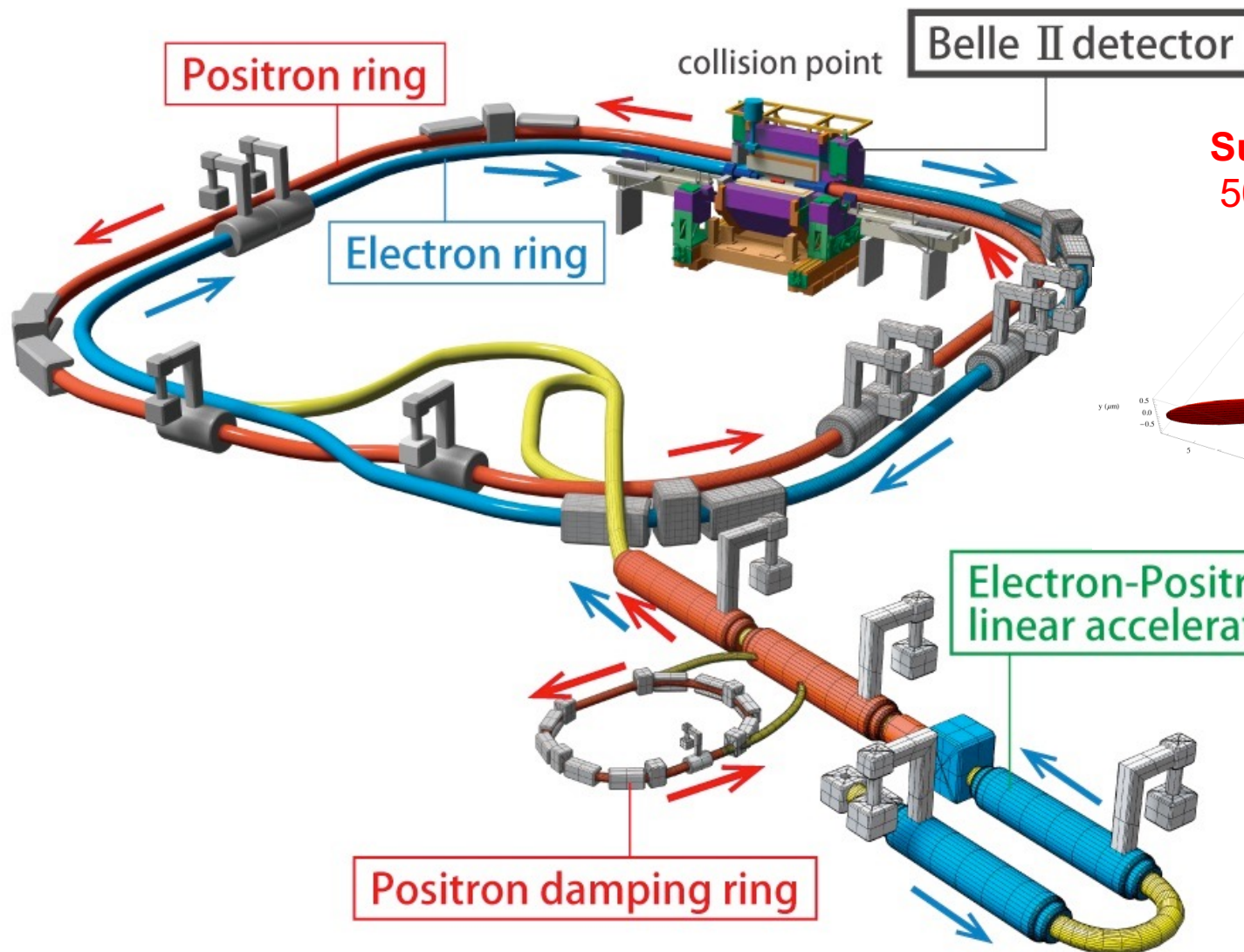
Beryllium beam pipe
 2cm diameter

e^+ (4 GeV)

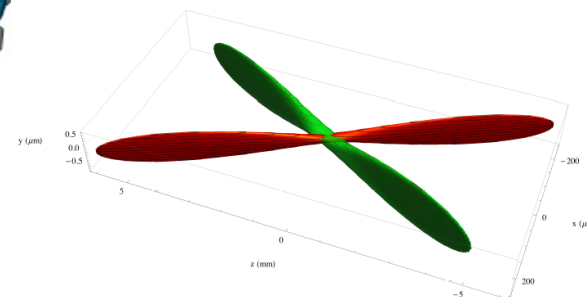
Vertex Detector
 2 layers DEPFET + 4 layers DSSD

Central Drift Chamber
 He(50%):C₂H₆(50%), small cells,
 long lever arm, fast electronics





SuperKEKB nano-beam
50 nm x 10 μ m x 0.5 mm
41 mr crossing angle



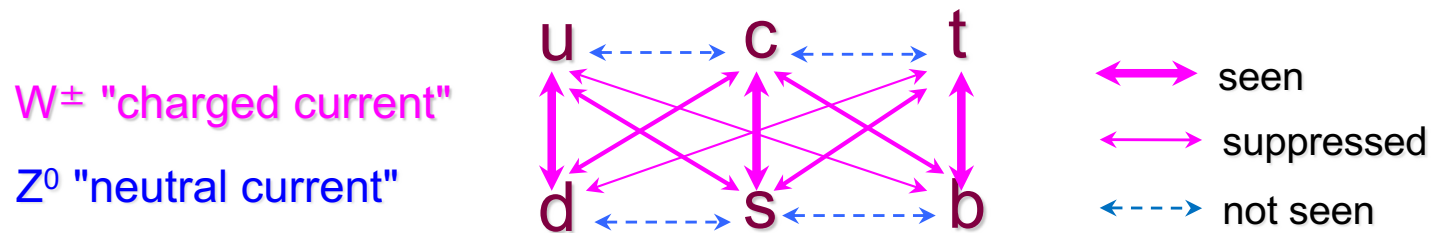
CKM Matrix

Standard Model: 12 fermion flavors (+antifermion)

Flavors interact only via the Weak force, mediated by W^\pm , Z^0

quark couplings:

- neutral current – \approx universal, no generation x-ing
- charged current – all different, \approx generation-conserving



All observations explained if matrix of couplings is unitary

GIM

(Glashow-Iliopoulos-Maiani)

$$g_F \times \begin{pmatrix} d & s & b \\ u & V_{ud} & V_{us} & V_{ub} \\ c & V_{cd} & V_{cs} & V_{cb} \\ t & V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

9 complex couplings
 \rightarrow 18 free parameters

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \mathcal{M} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

unitary transformation
 mass \leftrightarrow weak
 eigenstates

Kobayashi-Maskawa

explicit parametrization (Wolfenstein):

$$\begin{pmatrix} 1-\lambda^2/2 & \lambda & \lambda^3 A(\rho-i\eta) \\ -\lambda & 1-\lambda^2/2 & \lambda^2 A \\ \lambda^3 A(1-\rho-i\eta) & -\lambda^2 A & 1 \end{pmatrix}$$

For 3 generations, 4 free
 parameters, including
 1 irreducible **imaginary** part

Unitarity of CKM matrix

Decay rates $\propto |\text{Amplitude}|^2$

$$\begin{bmatrix} 1 - \frac{\lambda^2}{2} & \lambda & \lambda^3 A(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & \lambda^2 A \\ \lambda^3 A(1 - \rho - i\eta) & -\lambda^2 A & 1 \end{bmatrix}$$

Unitarity: $\sum_k V_{ik} V_{jk}^* = \delta_{ij}$

Explicitly for $i=1, j=3$:

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

$$= \lambda^3 A \underbrace{[(\rho + i\eta) - 1 + (1 - \rho - i\eta)]}$$

3 terms form “Unitarity triangle” in ρ - η complex plane

