

Measurements of CKM Parameters at Belle II

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(On behalf of the Belle II Collaboration)

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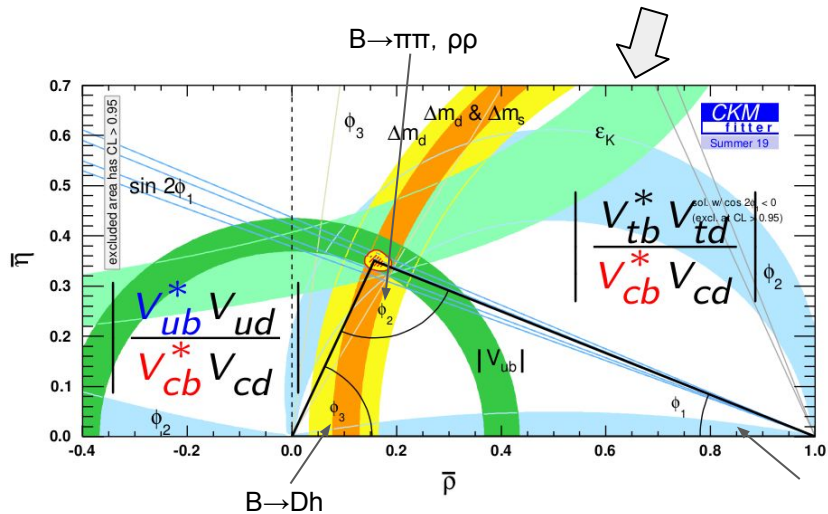


CKM matrix and unitarity triangle

Complex phase cause CP violation

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A^2\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

$$V^\dagger V = 1 \quad \Rightarrow \quad \begin{matrix} V_{ub}^* V_{ud} & + & V_{cb}^* V_{cd} & + & V_{tb}^* V_{td} & = & 0 \\ \lambda^3 \cdot 1 & & \lambda^2 \cdot \lambda & & 1 \cdot \lambda^3 & & \end{matrix}$$



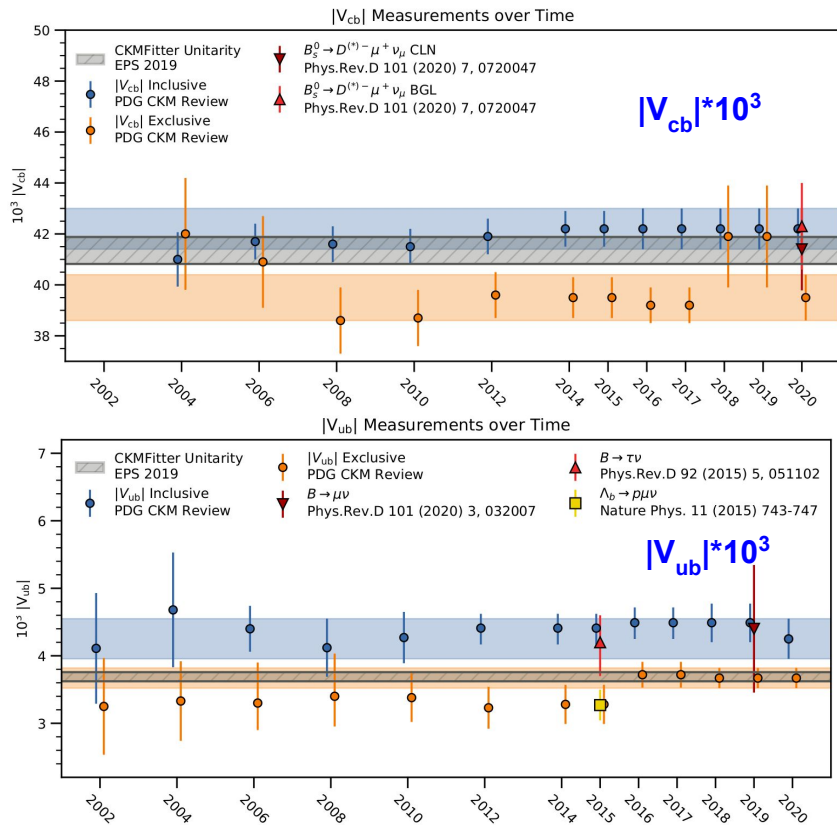
The Belle II Physics Book

[arXiv:1808.10567](https://arxiv.org/abs/1808.10567)

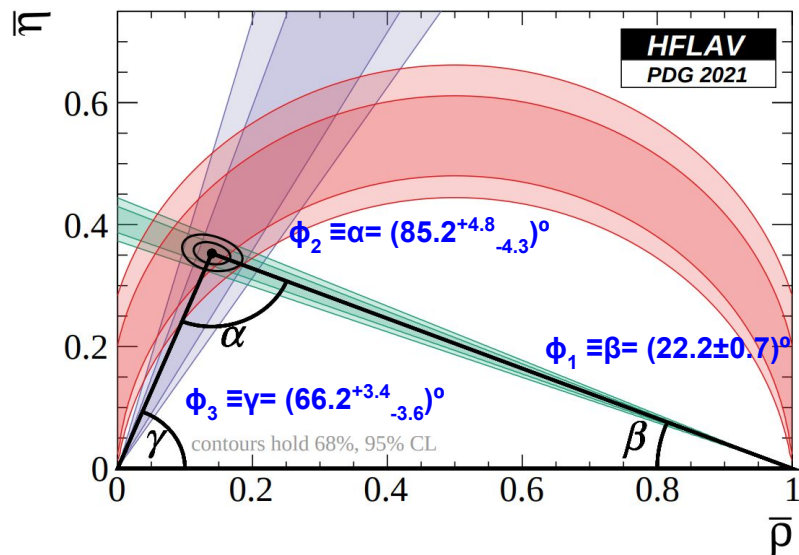
Observables	Expected the. accuracy	Expected exp. uncertainty	Facility (2025)
UT angles & sides			
ϕ_1 [°]	***	0.4	Belle II
ϕ_2 [°]	**	1.0	Belle II
ϕ_3 [°]	***	1.0	LHCb/Belle II
$ V_{cb} $ incl.	***	1%	Belle II
$ V_{cb} $ excl.	***	1.5%	Belle II
$ V_{ub} $ incl.	**	3%	Belle II
$ V_{ub} $ excl.	**	2%	Belle II/LHCb

Golden modes and time-dependent CPV

✳ Tension of $|V_{cb}|$ and $|V_{ub}|$ measurements between inclusive and exclusive processes.



✳ Status of $\sin(2\phi_1)$, ϕ_2 and ϕ_3 measurement



Precision of angles and sides of the unitarity triangle is an important test for the standard model.

The Belle II detector

Vertex detector (VXD)

Inner 2 layers: pixel detector (PXD)
Outer 4 layers: strip sensor (SVD)
Vertex resolution : $15 \mu\text{m}$

Central Drift Chamber (CDC)

Track efficiency $\sim 99\%$
 dE/dx resolution : 5%
 p_T resolution : 0.4%

ElectroMagnetic Calorimeter (ECL)

Barrel: CsI(Tl) + waveform sampling
Endcap: waveform sampling
Energy resolution : $1.6 - 4\%$

Features:

Energy-asymmetric e^+e^- collider \rightarrow low background.
Highest luminosity ($3.1 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$) in the world.

Particle Identification

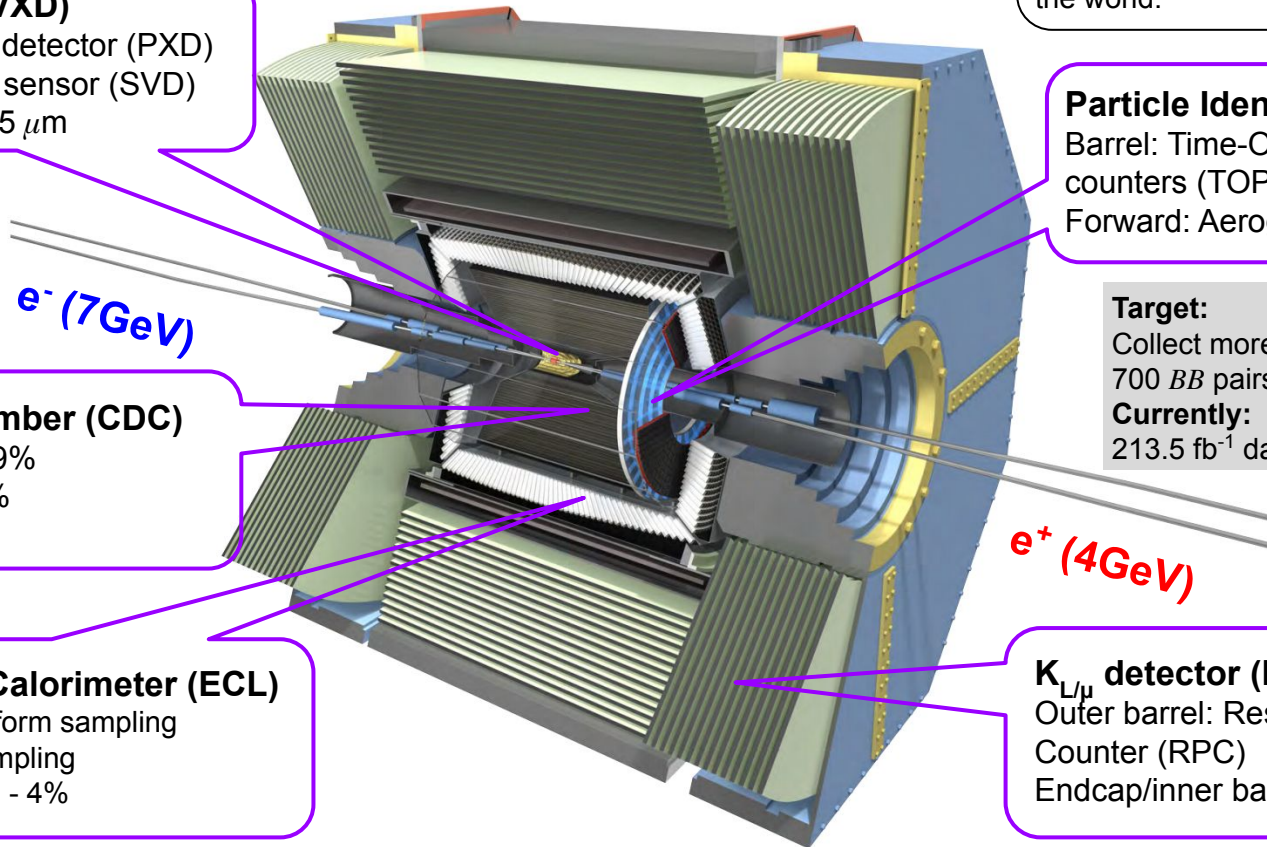
Barrel: Time-Of-Propagation counters (TOP)
Forward: Aerogel RICH (ARICH)

Target:

Collect more than 50ab^{-1} data;
700 BB pairs/second
Currently:
 213.5fb^{-1} data are collected.

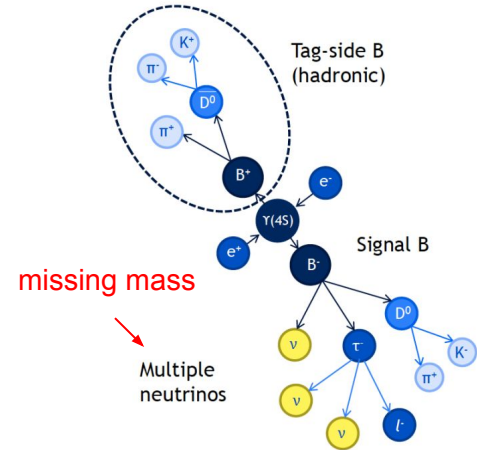
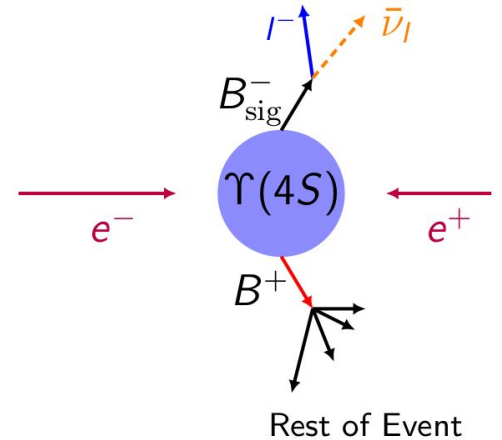
$K_{L/\mu}$ detector (KLM)

Outer barrel: Resistive Plate Counter (RPC)
Endcap/inner barrel: Scintillator



B decay reconstruction

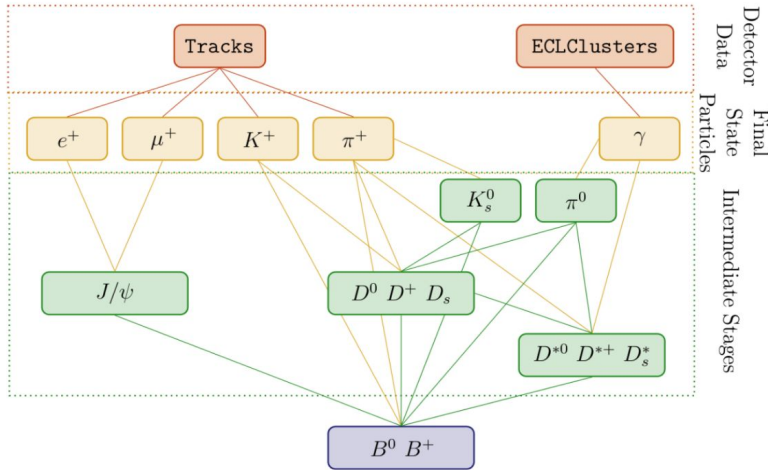
- Collide e^+ and e^- at the threshold energy (10.58 GeV) to make $\Upsilon(4S)$ particles
- $\Upsilon(4S)$ decays to B^+B^- and B^0B^0 >96% of the time.
- **Untagged** approach:
 - Reconstruct signal first.
 - Inclusively sum over all tracks and clusters in remaining event or use only signal side information
 - High efficiency but large background
- **Tagged** approach:
 - Reconstruct one B meson as tag-side (B_{tag})
 - Study remaining B meson as signal (B_{sig})
 - Flavour and kinematic constraints: $B_{\text{tag}} \Rightarrow B_{\text{sig}}$



Full Event Interpretation (FEI)

Advanced tagging technique

The FEI uses a **multivariate technique** to reconstruct the B-tag side (hadronic or semileptonic) through $O(10^3)$ decay modes in a $Y(4S)$ decay.



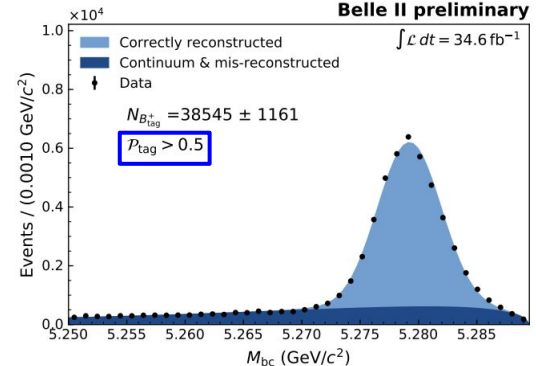
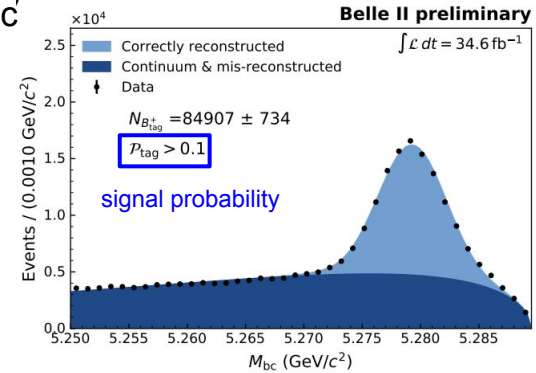
Tagging efficiency of FEI (evaluated on Belle MC)

ϵ_{tag} for had.: 0.78%(B^+), 0.46%(B^0)
 ϵ_{tag} for SL: 1.80%(B^+), 2.04%(B^0)

[Comput Softw Big Sci \(2019\) 3: 6](#)

Had. tagging with Belle II data

[arXiv:2008.06096](#)



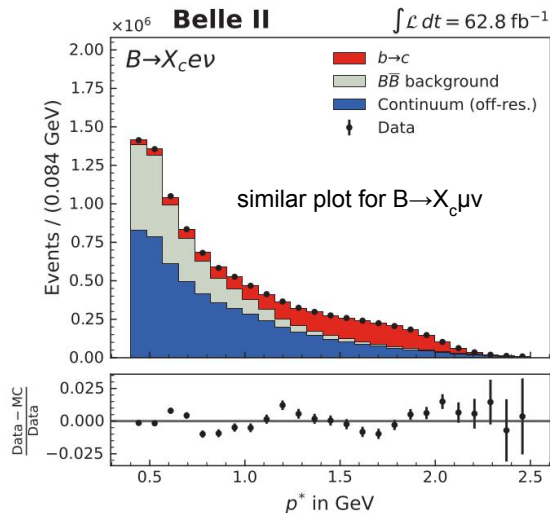
Determine the correctly reconstructed tag-side yield by fitting $m_{bc} = \sqrt{E_{\text{beam}}^2/4 - p_{B_{\text{tag}}}^{*2}}$.

Inclusive $|V_{cb}|$ measurement

- Measure the **spectral moments** (moments of lepton energy or hadronic mass) in order to simultaneously determine the non-perturbative elements and $|V_{cb}|$. Details about this approach: [JHEP02\(2019\)177](https://arxiv.org/abs/1902.02629)

Untagged $B \rightarrow X_c \ell \nu$

[arXiv:2103.02629](https://arxiv.org/abs/2103.02629)



Demand one well-identified lepton.

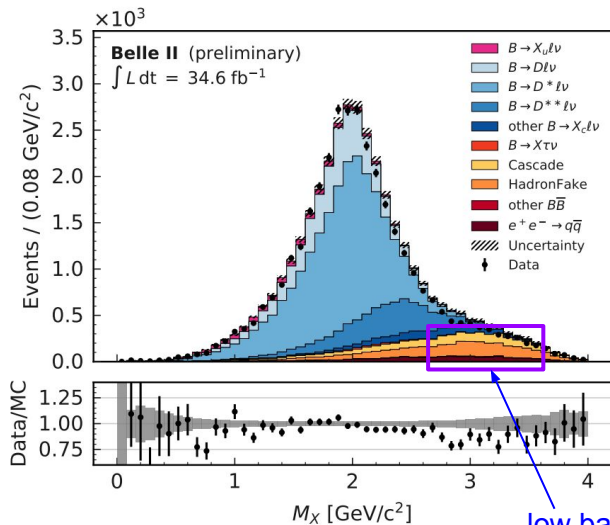
Exploit missing mass and momentum to reject backgrounds.

Obtained $BF(B \rightarrow X_c \ell \nu)$: $(9.75 \pm 0.03_{\text{stat}} \pm 0.47_{\text{sys}})\%$

Main source: the knowledge of $B \rightarrow X_c \ell \nu$ composition.

Had. Tagged $B \rightarrow X_c \ell \nu$

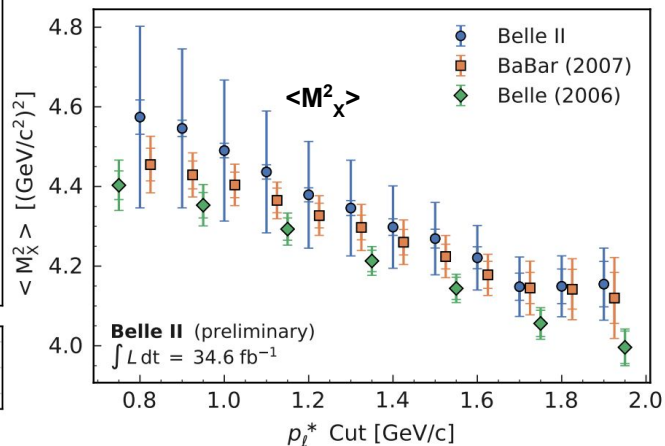
[arXiv:2009.04493](https://arxiv.org/abs/2009.04493)



low background

Measure the first six **hadronic mass moments**.

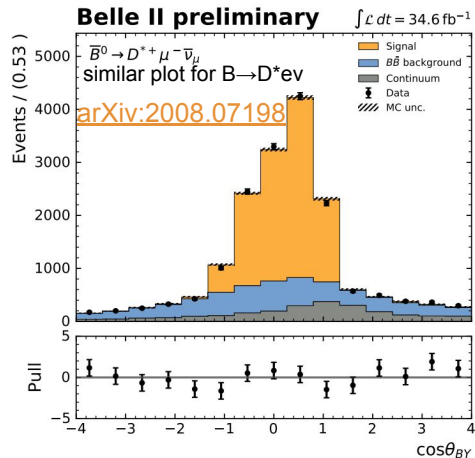
Measured $\langle M^2_X \rangle$ moments as a function of different p_t^* cuts



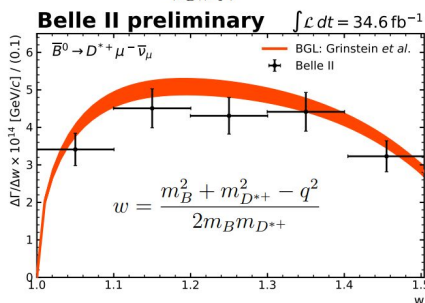
Next: $|V_{cb}|$ extraction from $q^2 = (p_B - p_X)^2$ moments.

Exclusive $|V_{cb}|$ measurement

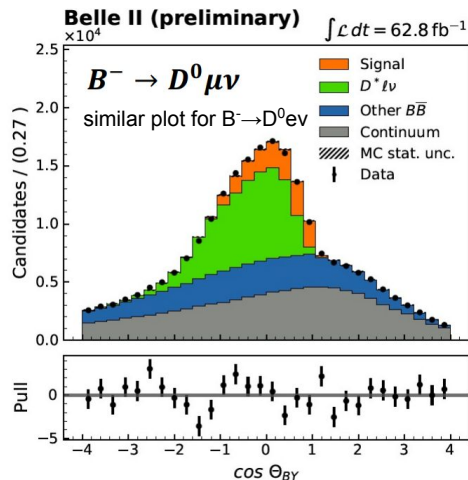
Untagged $B^0 \rightarrow D^{*-} \ell^+ \nu$



$$\cos \theta_{BY} = \frac{2 E_B^+ E_Y^+ - m_B^2 - m_Y^2}{2 |p_B^+| |p_Y^+|} \quad Y: D^* \ell \text{ system}$$



Untagged $B^- \rightarrow D^0 \ell^+ \nu$



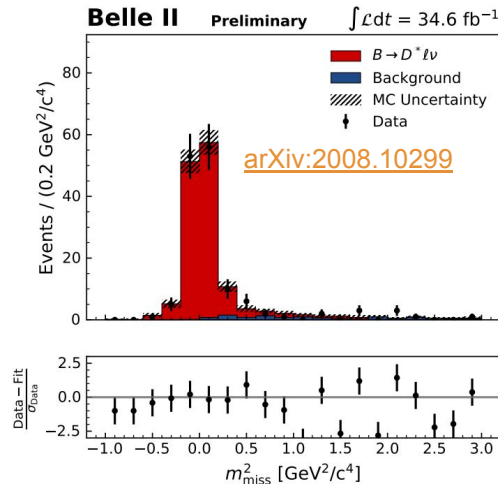
Measured $\text{BR}(B^- \rightarrow D^0 \ell^+ \nu)$:

$$(2.29 \pm 0.05_{\text{stat}} \pm 0.08_{\text{sys}})\%$$

PDG value:

$$(2.35 \pm 0.09)\%$$

Hadronically tagged $B^0 \rightarrow D^{*-} \ell^+ \nu$



$$m_{\text{miss}}^2 = (p_{e^+ e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_\ell)^2$$

Measured $\text{BR}(B^0 \rightarrow D^{*-} \ell^+ \nu)$:

Untagged: $(4.60 \pm 0.05_{\text{stat}} \pm 0.17_{\text{sys}} \pm 0.45_{\pi_s})\%$

Tagged: $(4.51 \pm 0.41_{\text{stat}} \pm 0.27_{\text{sys}} \pm 0.45_{\pi_s})\%$

$\text{BR}(B^0 \rightarrow D^{*-} \ell^+ \nu)$ PDG value:

$$(5.05 \pm 0.14)\%$$

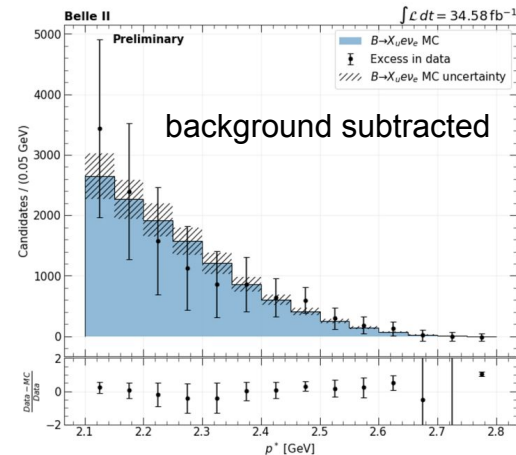
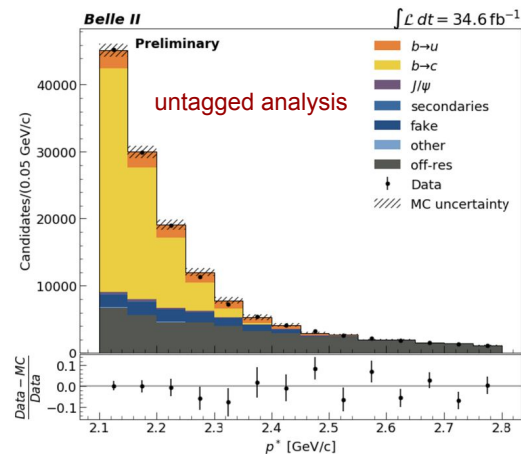
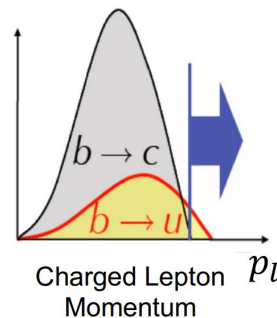
Plan: $|V_{cb}|$ measurement, analysis of angular observables, e.g., A_{FB}

Unfolded w spectrum agrees with previous analysis well.

Inclusive $|V_{ub}|$ measurement

BELLE2-NOTE-PL-2020-026

- Challenge in the measurement of $B \rightarrow X_u \ell \nu$:
 - large background from $b \rightarrow c$ events
- To suppress charm decay, exploit the lepton momentum endpoint, where $b \rightarrow c$ component is relatively small
- Analysis strategy:
 - select one well-identified electron
 - extract signal yield by fitting electron momentum in the center-of-mass frame
- Background subtracted distribution is consistent with $B \rightarrow X_u \ell \nu$ prediction. The significance of the yield is 3σ .



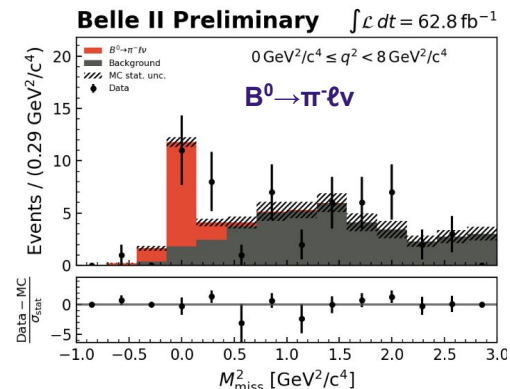
Capable of measuring $|V_{ub}|$ with more data.

Exclusive $|V_{ub}|$ measurement

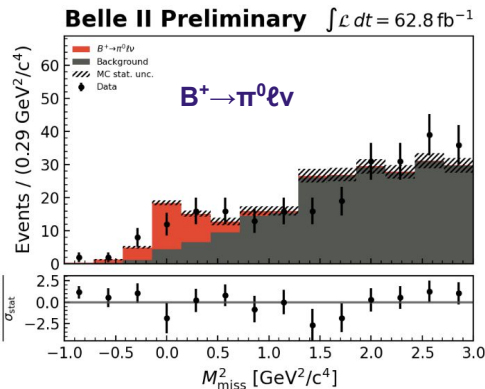
BELLE2-CONF-PH-2021-013

Hadronically tagged $B \rightarrow \pi \ell \nu$

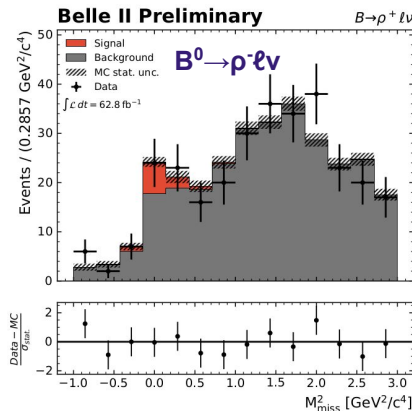
Hadronically tagged $B \rightarrow \rho \ell \nu$



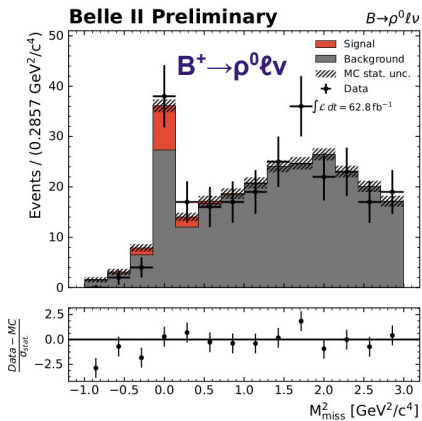
$B \rightarrow \pi^+ \ell \nu$ in first q^2 bin



$\mathcal{B}(B^+ \rightarrow \pi^0 \ell \nu) = (8.29 \pm 1.99_{\text{stat}} \pm 0.46_{\text{sys}})\%$



$\mathcal{B}(B^0 \rightarrow \rho^+ \ell \nu) = (1.51 \pm 1.13_{\text{stat}} \pm 0.09_{\text{sys}})\%$



$\mathcal{B}(B^+ \rightarrow \rho^0 \ell \nu) = (9.26 \pm 6.33_{\text{stat}} \pm 0.38_{\text{sys}})\%$

relatively lower statistical uncertainty \rightarrow promising for precise $|V_{ub}|$ measurement

Calculate the sum of the partial branching fractions in three bins of q^2 .

- Extract signal yield for each channel by fitting m^2_{miss} .
- All branching ratios are in agreement with PDG values.
- Untagged exclusive $|V_{ub}|$ measurement is also on-going.

Measurement of $\sin(2\phi_1)$

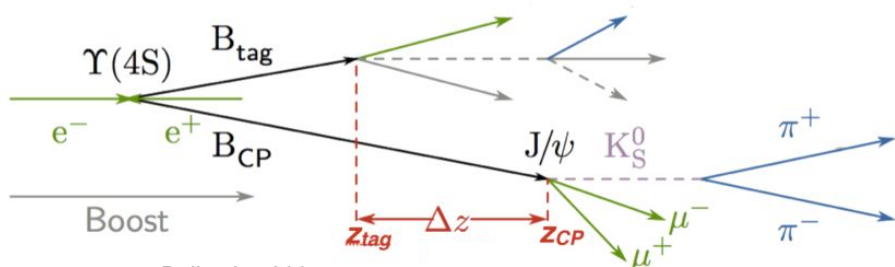
BELLE2-NOTE-PL-2020-11

$$A_f(\Delta t) = \frac{\Gamma(\bar{B}^0 \rightarrow J/\psi K_S^0) - \Gamma(B^0 \rightarrow J/\psi K_S^0)}{\Gamma(\bar{B}^0 \rightarrow J/\psi K_S^0) + \Gamma(B^0 \rightarrow J/\psi K_S^0)}$$

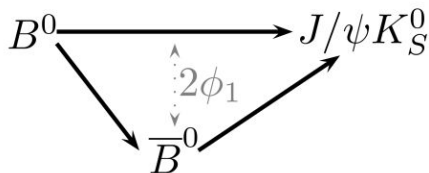
$$= S_f \sin(\Delta m_B \Delta t) + A_f \cos(\Delta m_B \Delta t)$$

Δm_B is measured by $B^0\bar{B}^0$ mixing

Assume no direct CPV: $A_f \approx 0$



Belle: $\Delta z \approx 200 \mu\text{m}$
 Belle II: $\Delta z \approx 130 \mu\text{m}$
 with better Δz resolution

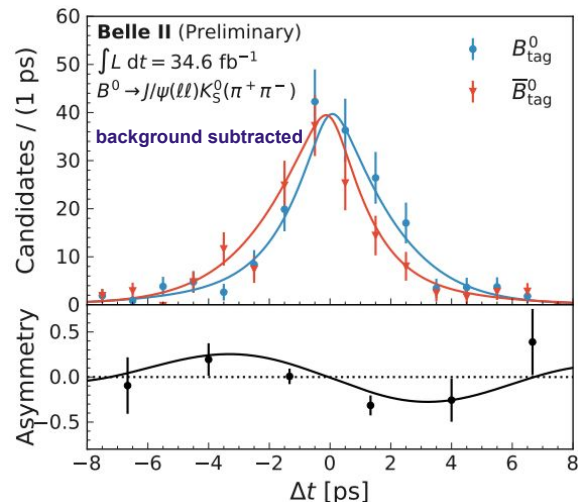
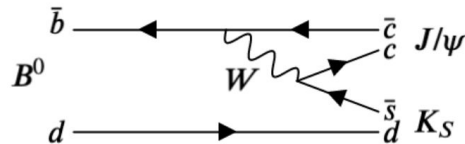


distance measurement

$$\Delta t = \Delta z / (\beta\gamma c)$$

time measurement

Golden mode: $B^0 \rightarrow J/\psi K^0$
 (tree-level decay)



$$\sin(2\phi_1) \approx S_f = 0.55 \pm 0.21_{\text{stat}} \pm 0.04_{\text{sys}}$$

world average: 0.699 ± 0.017

Toward ϕ_2

Unique Belle II capability to study all the $B \rightarrow \pi\pi, \rho\rho$ partner decays to determine ϕ_2

$B^0 \rightarrow \pi^0 \pi^0$: very challenging because four γ 's.

Train BDT to suppress background photons.

3D fit of ΔE -Mbc-continuum suppression BDT.

Unique Belle II reach.

$$\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = (0.98^{+0.48}_{-0.39}(\text{stat}) \pm 0.27(\text{syst})) \times 10^{-6}$$

[arXiv:2107.02373](https://arxiv.org/abs/2107.02373)

$B^+ \rightarrow \rho^+ \rho^0$: π -only final state, large background because of ρ mass width. Additional challenge of angular analysis \rightarrow 6D fit including helicity angles.

longitudinal polarization fraction

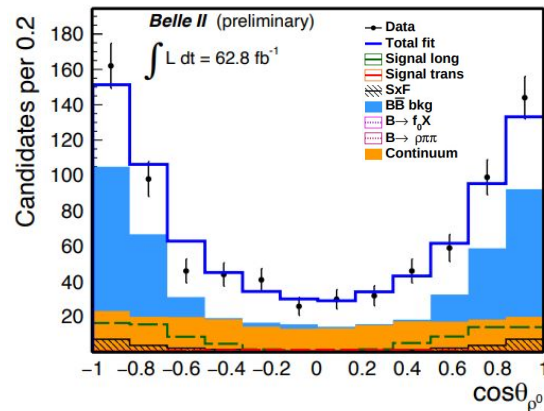
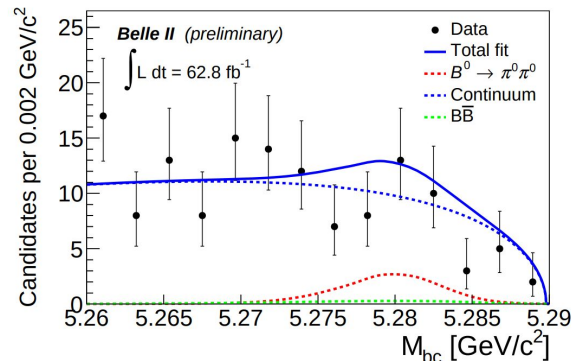
$$f_L(B^+ \rightarrow \rho^+ \rho^0) = (0.936^{+0.049}_{-0.041}(\text{stat}) \pm 0.021(\text{syst}))$$

$$\mathcal{B}(B^+ \rightarrow \rho^+ \rho^0) = (20.6 \pm 3.2(\text{stat}) \pm 4.0(\text{syst})) \times 10^{-6}$$

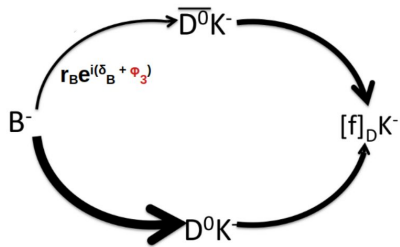
[arXiv:2109.11456](https://arxiv.org/abs/2109.11456)

20% precision improvement wrt Belle on the same lumi!

On track to measure the CKM angle ϕ_2 at Belle II



Toward ϕ_3



important set of observables:

$$R^{(*)0} = \frac{\Gamma(B^- \rightarrow D^{(*)0} K^-)}{\Gamma(B^- \rightarrow D^{(*)0} \pi^-)}$$

$$R^{(*)+} = \frac{\Gamma(\bar{B}^0 \rightarrow D^{(*)+} K^-)}{\Gamma(\bar{B}^0 \rightarrow D^{(*)+} \pi^-)}$$

$$\frac{\mathcal{A}^{\text{suppr.}}(B^- \rightarrow \bar{D}^0 K^-)}{\mathcal{A}^{\text{favor.}}(B^- \rightarrow D^0 K^-)} = r_B e^{i(\delta_B + \phi_3)}$$

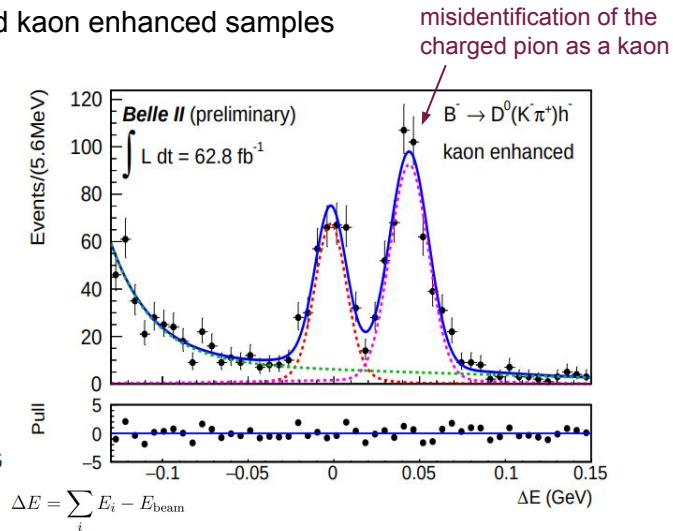
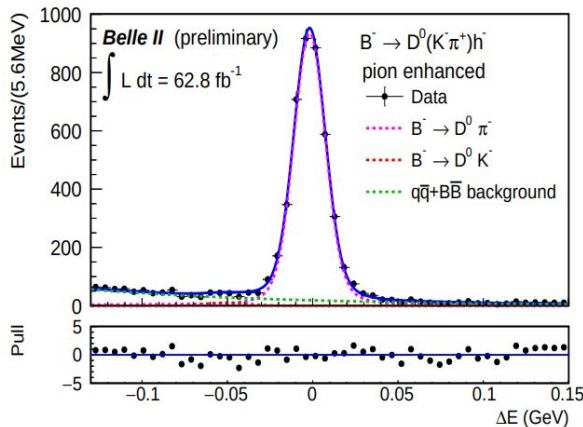
The most sensitive mode to determine ϕ_3

$$B^- \rightarrow D^0(K_S^0 \pi^+ \pi^-) K^-$$

for this mode, fit not only ΔE but also the output from fast boosted decision tree

[arXiv:2104.03628](https://arxiv.org/abs/2104.03628)

simultaneous fit to pion and kaon enhanced samples



results comparison

	$B^- \rightarrow D^0(K^- \pi^+) h^-$	$B^- \rightarrow D^0(K_S^0 \pi^+ \pi^-) h^-$	$\bar{B}^0 \rightarrow D^+ h^-$
Belle II $R^{+ / 0} (\times 10^{-2})$	$7.66 \pm 0.55 \begin{smallmatrix} +0.11 \\ -0.08 \end{smallmatrix}$	$6.32 \pm 0.81 \begin{smallmatrix} +0.09 \\ -0.11 \end{smallmatrix}$	$9.22 \pm 0.58 \pm 0.09$
LHCb $R^{+ / 0} (\times 10^{-2})$	$7.77 \pm 0.04 \pm 0.07$	$7.77 \pm 0.04 \pm 0.07$	$8.22 \pm 0.11 \pm 0.25$

Expect 1.6° precision on ϕ_3 with 50 ab^{-1} dataset.

Summary and prospects

- Precision measurement of CKM parameters is a keystone of Belle II program
- Intensive activity ongoing on early data to prepare measurements of UT angles and sides
- Preliminary results are reported based on 30-60/fb on BF for determining $|V_{cb}|$ and $|V_{ub}|$, $\sin(2\phi_1)$, $B \rightarrow DK$ parameters sensitive to ϕ_3 , and $B \rightarrow \pi^0 \pi^0 / \rho^+ \rho^0$ parameters sensitive to ϕ_2

Backup

Comparison with LHCb

Property	LHCb	Belle II
$\sigma_{b\bar{b}}$ (nb)	~150,000	~1
$\int L dt$ (fb ⁻¹)	~25	~50,000
Background level	High	Low
Typical efficiency	Low	High
π^0, K_S efficiency	Low	High
Initial state	Not well known	Well known
Decay-time resolution	Excellent	Good
Collision spot size	Large	Tiny
Heavy bottom hadrons	B_S, B_C, b -baryons	Partly B_S
τ physics capability	Limited	Excellent
B-flavor tagging efficiency	3.5 - 6%	36%